

Decimal 256

Binary ~~010000000~~ = 01111111

$$\begin{aligned}
 256 - 2^8 &= 128 \quad (1) \\
 128 - 2^6 &= 64 \quad (1) \\
 64 - 2^5 &= 32 \quad (1) \\
 32 - 2^4 &= 16 \quad (1) \\
 16 - 2^3 &= 8 \quad (1) \\
 8 - 2^2 &= 4 \quad (1) \\
 4 - 2^1 &= 2 \quad (1) \\
 2 - 2^0 &= 1 \quad (1)
 \end{aligned}$$

Octal ~~200~~ = 400₈

32%0

8%4

Hex 10%256 = 10000 = 100₁₆

10%16 = 0400

16%1 = 0401

Base-7 1%256 = 36004 = 514₇

7%36 = 5%01

7%1 = 0400

7%5 = 0405

Hex 16%159 = 9%15(F) = 9F₁₆

16%9 = 0409

Base-7 7%159 = 22005 340₇

7%22 = 3%01 315₇

7%3 = 0403

Decimal

Binary 10101010

Decimal

$$\begin{aligned}
 1 \times 2^7 + 0 \times 2^6 + 1 \times 2^5 + 0 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 &= 170_{10}
 \end{aligned}$$

Octal 8%170 = 21%2 = 252₈

8%21 = 2%5

8%2 = 0%2

Hex 16%170 = 104010(A) = AA₁₆

16%10 = 04010(A)

Base-7 7%170 = 24%2 = 332₇

7%24 = 3%3

7%3 = 0403

Octal 237

Decimal $2 \times 8^2 + 3 \times 8 + 7$
 $= 128 + 24 + 7$
 $= 159_{10}$

Binary 2%159 = 79%1 (10011111)₂

2%79 = 39%1 (10011111)₂

2%39 = 19%1

2%19 = 9%1

2%9 = 4%1

2%4 = 2%0

2%2 = 1%0

2%1 = 0%1

Hex 81

Decimal $16 \times 8 + 1$
 $= 129$

Binary $= 2\sqrt{29} = 64901 = (10000001)_{11}$
 $2\sqrt{64} = 32900$
 $2\sqrt{32} = 16900$
 $2\sqrt{16} = 8900$
 $2\sqrt{8} = 4900$
 $2\sqrt{4} = 2900$
 $2\sqrt{2} = 1000$
 $2\sqrt{1} = 0901$

Base Octal $8\sqrt{29} = 16401 = 201_{11}$
 $8\sqrt{16} = 2900$
 $8\sqrt{2} = 0902$

Base 7 $7\sqrt{29} = 18403 = 243_{11}$
 $7\sqrt{18} = 2904$
 $7\sqrt{2} = 0902$

1.2
 1.2.1 1010.10101010

$0 \times 2^0 + 1 \times 2^1 + 0 \times 2^2 + 1 \times 2^3$
 $= 0 + 2 + 0 + 8 = 10$

$0 \times 2^0 + 1 \times 2^1 + 0 \times 2^2 + 1 \times 2^3$
 $+ 0 \times 2^4 + 1 \times 2^5 + 0 \times 2^6 + 1 \times 2^7$

~~$10 \times 2^0 + 1 \times 2^1 + 0 \times 2^2 + 1 \times 2^3$~~
 ~~$+ 0 \times 2^4 + 1 \times 2^5 + 0 \times 2^6 + 1 \times 2^7$~~

$= 0 + 0.5 + 0 + 0.125 + 0 + 0.03125 + 0 + 0.0078125$
 $= 0.6640625$

$1010.10101010 = 10.6640625_{11}$

Base 7 42

Decimal $(4 \times 1) + 2 = 30_{11}$

Binary $2\sqrt{30} = 15400$ ~~(00011110)~~
 $(00011110)_{11}$

$2\sqrt{15} = 7901$

$2\sqrt{7} = 3901$

$2\sqrt{3} = 1901$

$2\sqrt{1} = 0901$

Octal $8\sqrt{30} = 3906 = 36_{11}$

$8\sqrt{3} = 0903$

Hex $16\sqrt{30} = 19014 = 1E_{11}$

$16\sqrt{1} = 0901$

1.2.2

11110011.11001111

$128 + 64 + 32 + 16 + 2 + 1$
 $= 243_{11}$

$0.5 + 0.25 + 0 + 0 + 0.03125 + 0.015625 + 0.0078125$
 $+ 0.00390625$

$= 0.80859375_{11}$

243.80859375

1.3

1.3.1

100↓ 50↓ -50↓
01100100 00110010 11001101 +1
11001110

100-50
01100100
+ 11001110
1 00110010 = 50 11

1.3.2

20↓ 60↓ -60↓
00010100 00111000 11000011 +1
11000100

20-60
00010100
+ 11000100
1 10110000 2's -40
xor 00100111
+
00101000 = 40
Regular Binary

$2\sqrt{100} = 50$
 $2\sqrt{50} = 25$
 $2\sqrt{25} = 12$
 $2\sqrt{12} = 6$
 $2\sqrt{6} = 3$
 $2\sqrt{3} = 1$
 $2\sqrt{1} = 0$

100↓
1100100

$2\sqrt{50} = 25$
 $2\sqrt{25} = 12$
 $2\sqrt{12} = 6$
 $2\sqrt{6} = 3$
 $2\sqrt{3} = 1$
 $2\sqrt{1} = 0$

$2\sqrt{20} = 10$
 $2\sqrt{10} = 5$
 $2\sqrt{5} = 2$
 $2\sqrt{2} = 1$
 $2\sqrt{1} = 0$

20↓
10100

$2\sqrt{60} = 30$
 $2\sqrt{30} = 15$
 $2\sqrt{15} = 7$
 $2\sqrt{7} = 3$
 $2\sqrt{3} = 1$
 $2\sqrt{1} = 0$