Data Mining:

Concepts and Techniques

- Chapter 2 -

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Chapter 2: Getting to Know Your Data

Data Objects and Attribute Types



- Basic Statistical Descriptions of Data
- Data Visualization
- Measuring Data Similarity and Dissimilarity
- Summary

Types of Data Sets

Record

Relational records

 Data matrix, e.g., numerical matrix, crosstabs

 Document data: text documents: termfrequency vector

Transaction data

Graph and network

World Wide Web

Social or information networks

Molecular Structures

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Video data: sequence of images

Temporal data: time-series

Sequential Data: transaction sequences

Genetic sequence data

Spatial, image and multimedia:

Spatial data: maps

Image data:

Video data:

)-	team	coach	pla y	ball	score	game	n Wi.	lost	timeout	season
Document 1	3	0	5	0	2	6	0	2	0	2
Document 2	0	7	0	2	1	0	0	3	0	0
Document 3	0	1	0	0	1	2	2	0	3	0

TID	Items
1	Bread, Coke, Milk
2	Juice, Bread
3	Juice, Coke, Diaper, Milk
4	Juice, Bread, Diaper, Milk
5	Coke, Diaper, Milk

Important Characteristics of Structured Data

- Dimensionality
 - Curse of dimensionality
- Sparsity
 - Only presence counts
- Resolution
 - Patterns depend on the scale
- Distribution
 - Centrality and dispersion

Data Objects

- Data sets are made up of data objects.
- A data object represents an entity.
- Examples:
 - sales database: customers, store items, sales
 - medical database: patients, treatments
 - university database: students, professors, courses
- Also called samples, examples, instances, data points, objects, tuples.
- Data objects are described by attributes.
- Database rows -> data objects; columns ->attributes.

Attributes

- Attribute (or dimensions, features, variables): a data field, representing a characteristic or feature of a data object.
 - E.g., customer _ID, name, address
- Types:
 - Nominal
 - Binary
 - Numeric: quantitative
 - Interval-scaled
 - Ratio-scaled

Attribute Types

- Nominal: categories, states, or "names of things"
 - Hair_color = { auburn, black, blond, brown, grey, red, white}
 - marital status, occupation, ID numbers, zip codes

Binary

- Nominal attribute with only 2 states (0 and 1)
- Symmetric binary: both outcomes equally important
 - e.g., gender
- Asymmetric binary: outcomes not equally important.
 - e.g., medical test (positive vs. negative)
 - Convention: assign 1 to most important outcome (e.g., HIV positive)

Ordinal

- Values have a meaningful order (ranking) but magnitude between successive values is not known.
- Size = {small, medium, large}, grades, army rankings

Numeric Attribute Types

Quantity (integer or real-valued)

Interval

- Measured on a scale of equal-sized units
- Values have order
 - E.g., temperature in C°or F°, calendar dates
- No true zero-point

Ratio

- Inherent zero-point
- We can speak of values as being an order of magnitude larger than the unit of measurement (10 K° is twice as high as 5 K°).
 - e.g., temperature in Kelvin, length, counts, monetary quantities

Discrete vs. Continuous Attributes

Discrete Attribute

- Has only a finite or countably infinite set of values
 - E.g., zip codes, profession, or the set of words in a collection of documents
- Sometimes, represented as integer variables
- Note: Binary attributes are a special case of discrete attributes

Continuous Attribute

- Has real numbers as attribute values
 - E.g., temperature, height, or weight
- Practically, real values can only be measured and represented using a finite number of digits
- Continuous attributes are typically represented as floating-point variables

Chapter 2: Getting to Know Your Data

- Data Objects and Attribute Types
- Basic Statistical Descriptions of Data



- Data Visualization
- Measuring Data Similarity and Dissimilarity
- Summary

Basic Statistical Descriptions of Data

Motivation

- To better understand the data: central tendency, variation and spread
- Data dispersion characteristics
 - median, max, min, quantiles, outliers, variance, etc.
- Numerical dimensions correspond to sorted intervals
 - Data dispersion: analyzed with multiple granularities of precision
 - Boxplot or quantile analysis on sorted intervals
- Dispersion analysis on computed measures
 - Folding measures into numerical dimensions
 - Boxplot or quantile analysis on the transformed cube

Measuring the Central Tendency

- $\overline{x} = \frac{1}{n} \sum_{i=1}^{n} x_i \qquad \mu = \frac{\sum x}{N}$ Mean (algebraic measure) (sample vs. population): Note: *n* is sample size and *N* is population size.
 - Weighted arithmetic mean:
 - Trimmed mean: chopping extreme values

$$\overline{x} = \frac{\sum_{i=1}^{n} w_i x_i}{\sum_{i=1}^{n} w_i x_i}$$

age

81 - 110

Median:

- Middle value if odd number of values, or average of the middle two values otherwise
- Estimated by

	1 0	200
ed by interpolation (for <i>grouped data</i>):	6 - 15	450
$n/2-(\sum frea)l$	16-20	300
$median = L_1 + (\frac{n/2 - (\sum freq)l}{c}) width$	21 - 50	1500
$freq_{median}$	51 - 80	700
	01 110	4.4

Mode

- Value that occurs most frequently in the data
- Unimodal, bimodal, trimodal
- Empirical formula: $mean-mode=3\times(mean-median)$

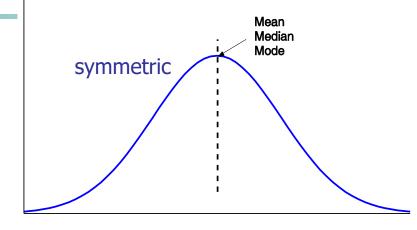
frequency

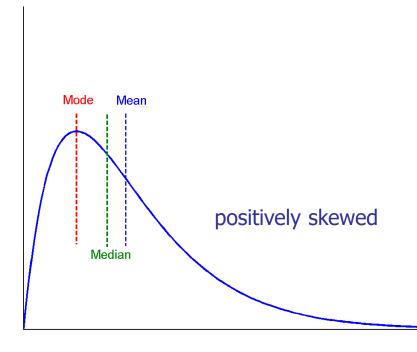
200

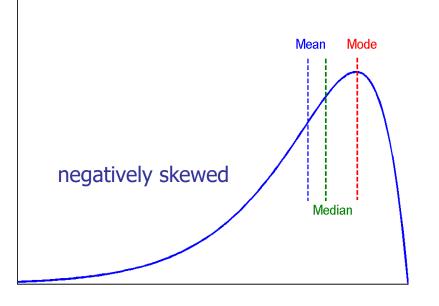
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Symmetric vs. Skewed Da

 Median, mean and mode of symmetric, positively and negatively skewed data







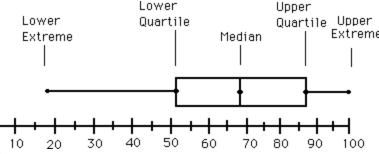
Measuring the Dispersion of Data

- Quartiles, outliers and boxplots
 - **Quartiles**: Q₁ (25th percentile), Q₃ (75th percentile)
 - Inter-quartile range: $IQR = Q_3 Q_1$
 - **Five number summary**: min, Q_1 , median, Q_3 , max
 - Boxplot: ends of the box are the quartiles; median is marked; add whiskers, and plot outliers individually
 - Outlier: usually, a value higher/lower than 1.5 x IQR
- Variance and standard deviation (sample: s, population: σ)
 - **Variance**: (algebraic, scalable computation)

$$s^{2} = \frac{1}{n-1} \sum_{i=1}^{n} (x_{i} - \overline{x})^{2} = \frac{1}{n-1} \left[\sum_{i=1}^{n} x_{i}^{2} - \frac{1}{n} (\sum_{i=1}^{n} x_{i})^{2} \right] \qquad \sigma^{2} = \frac{1}{N} \sum_{i=1}^{n} (x_{i} - \mu)^{2} = \frac{1}{N} \sum_{i=1}^{n} x_{i}^{2} - \mu^{2}$$

Standard deviation s (or σ) is the square root of variance s^2 (or σ^2)

Boxplot Analysis

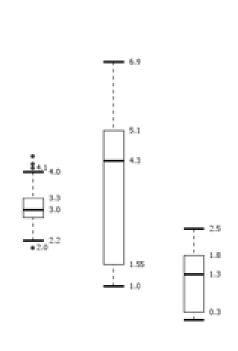


6.4

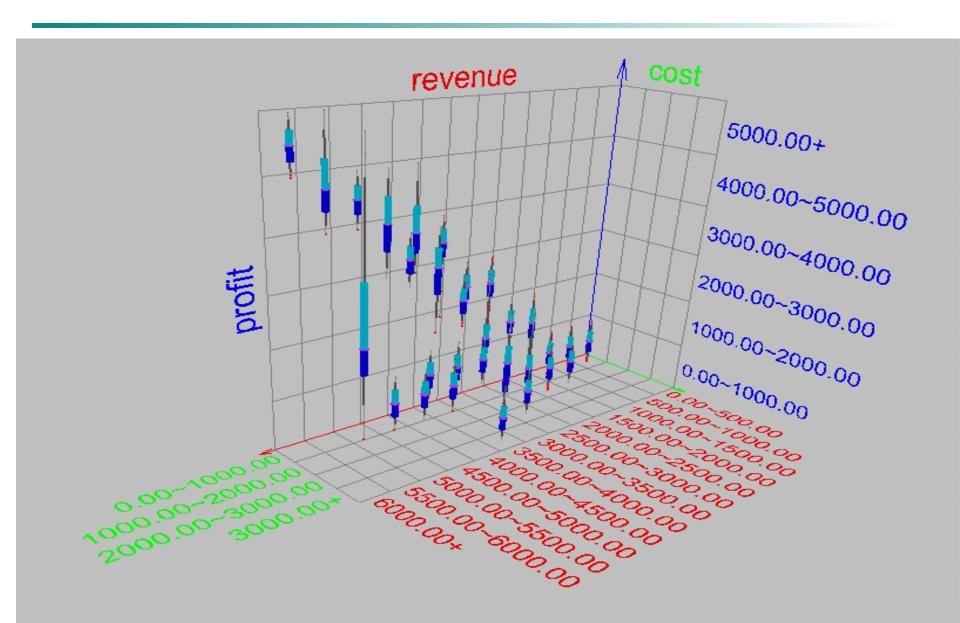
- Five-number summary of a distribution
 - Minimum, Q1, Median, Q3, Maximum

Boxplot

- Data is represented with a box
- The ends of the box are at the first and third quartiles, i.e., the height of the box is IQR
- The median is marked by a line within the box
- Whiskers: two lines outside the box extended to Minimum and Maximum
- Outliers: points beyond a specified outlier threshold, plotted individually

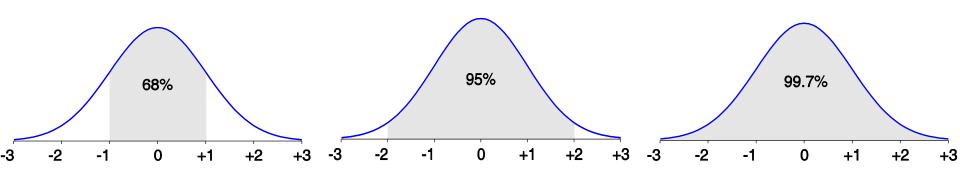


Visualization of Data Dispersion: 3-D Boxplots



Properties of Normal Distribution Curve

- The normal (distribution) curve
 - From μ – σ to μ + σ : contains about 68% of the measurements (μ : mean, σ : standard deviation)
 - From μ –2 σ to μ +2 σ : contains about 95% of it
 - From μ –3 σ to μ +3 σ : contains about 99.7% of it

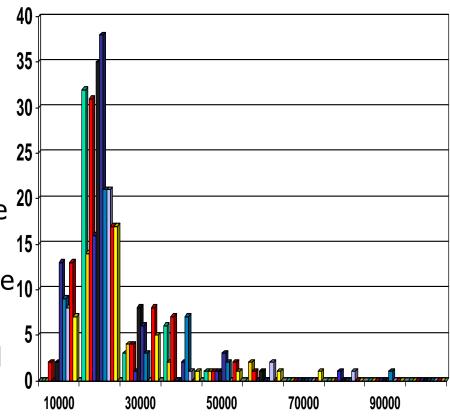


Graphic Displays of Basic Statistical Descriptions

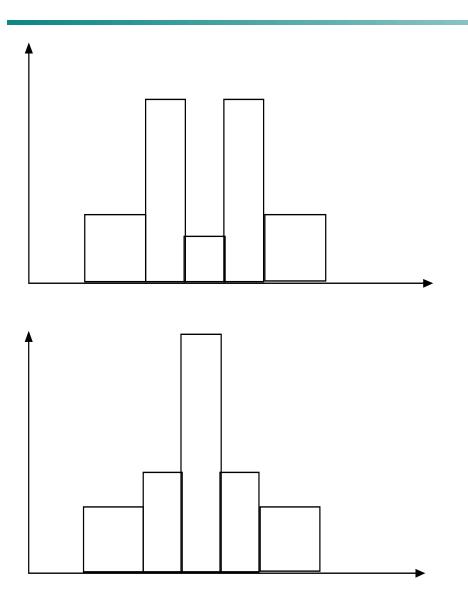
- Boxplot: graphic display of five-number summary
- Histogram: x-axis are values, y-axis repres. frequencies
- **Quantile plot**: each value x_i is paired with f_i indicating that approximately 100 f_i % of data are $\leq x_i$
- Quantile-quantile (q-q) plot: graphs the quantiles of one univariant distribution against the corresponding quantiles of another
- Scatter plot: each pair of values is a pair of coordinates and plotted as points in the plane

Histogram Analysis

- Histogram: Graph display of tabulated frequencies, shown as bars
- It shows what proportion of cases fall into each of several categories
- Differs from a bar chart in that it is the area of the bar that denotes the value, not the height as in bar charts, a crucial distinction when the categories are not of uniform width
- The categories are usually specified as non-overlapping intervals of some variable. The categories (bars) must be adjacent



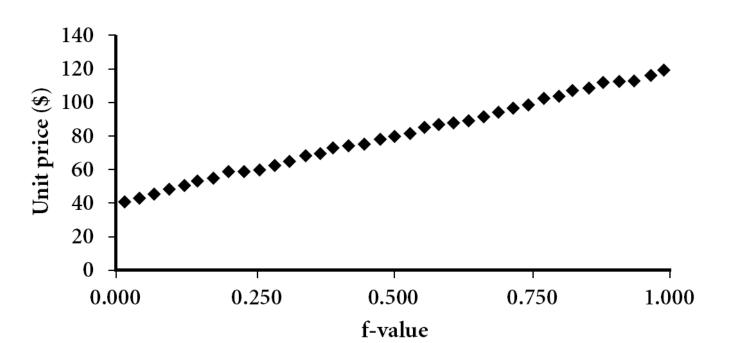
Histograms Often Tell More than Boxplots



- The two histograms shown in the left may have the same boxplot representation
 - The same values for: min, Q1, median, Q3, max
- But they have rather different data distributions

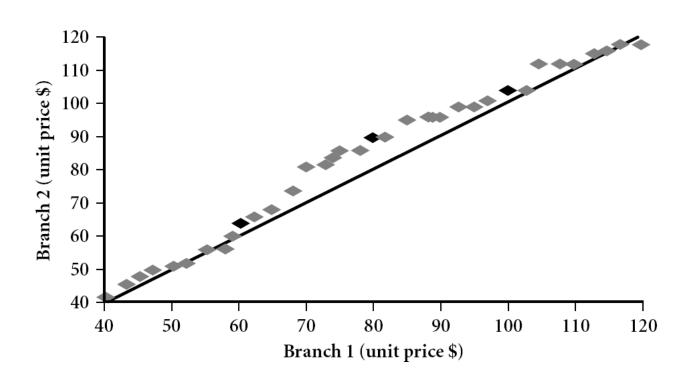
Quantile Plot

- Displays all of the data (allowing the user to assess both the overall behavior and unusual occurrences)
- Plots quantile information
 - For a data x_i data sorted in increasing order, f_i indicates that approximately 100 f_i % of the data are below or equal to the value x_i



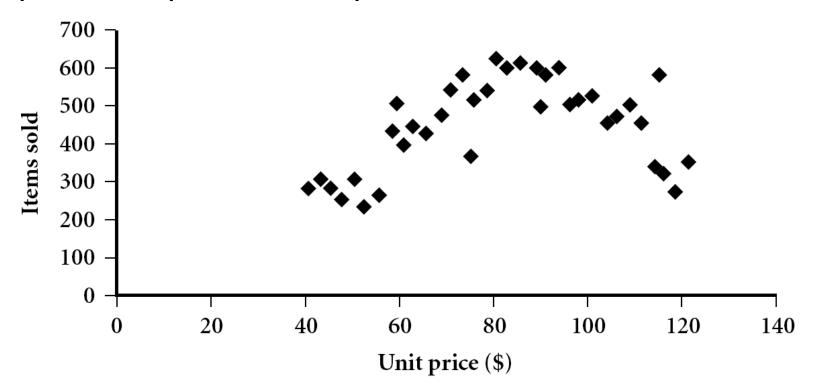
Quantile-Quantile (Q-Q) Plot

- Graphs the quantiles of one univariate distribution against the corresponding quantiles of another
- View: Is there is a shift in going from one distribution to another?
- Example shows unit price of items sold at Branch 1 vs. Branch 2 for each quantile. Unit prices of items sold at Branch 1 tend to be lower than those at Branch 2.

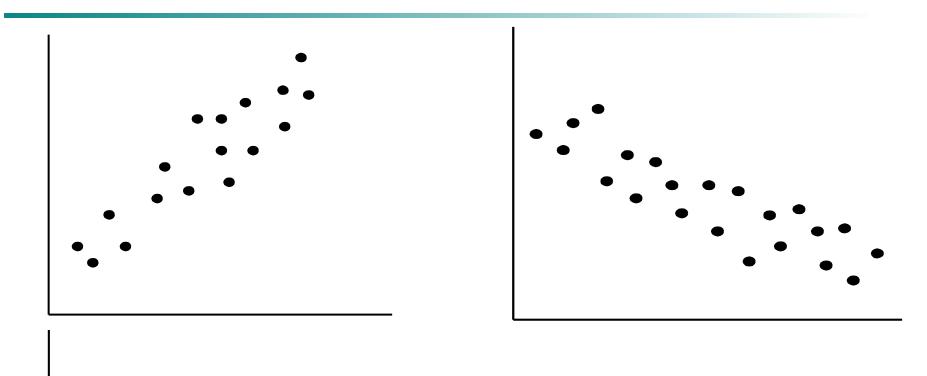


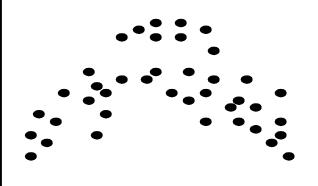
Scatter plot

- Provides a first look at bivariate data to see clusters of points, outliers, etc
- Each pair of values is treated as a pair of coordinates and plotted as points in the plane



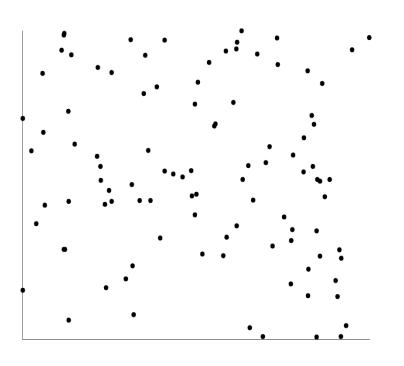
Positively and Negatively Correlated Data

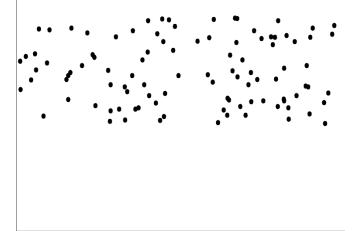


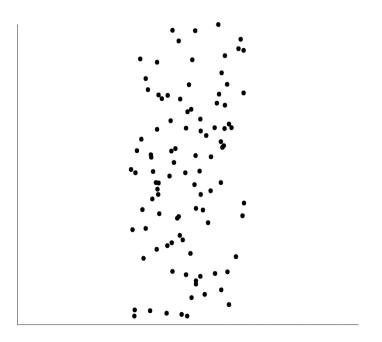


- The left half fragment is positively correlated
- The right half is negative correlated

Uncorrelated Data







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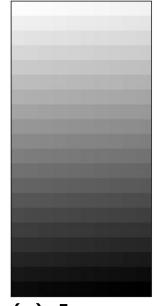
- Measuring Data Similarity and Dissimilarity
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Data Visualization

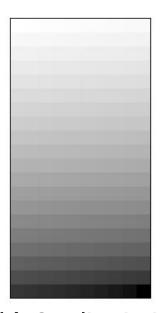
- Why data visualization?
 - Gain insight into an information space by mapping data onto graphical primitives
 - Provide qualitative overview of large data sets
 - Search for patterns, trends, structure, irregularities, relationships among data
 - Help find interesting regions and suitable parameters for further quantitative analysis
 - Provide a visual proof of computer representations derived
- Categorization of visualization methods:
 - Pixel-oriented visualization techniques
 - Geometric projection visualization techniques
 - Icon-based visualization techniques
 - Hierarchical visualization techniques
 - Visualizing complex data and relations

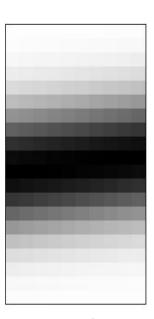
Pixel-Oriented Visualization Techniques

- For a data set of m dimensions, create m windows on the screen, one for each dimension
- The m dimension values of a record are mapped to m pixels at the corresponding positions in the windows
- The colors of the pixels reflect the corresponding values

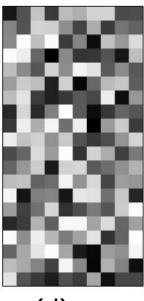


Income



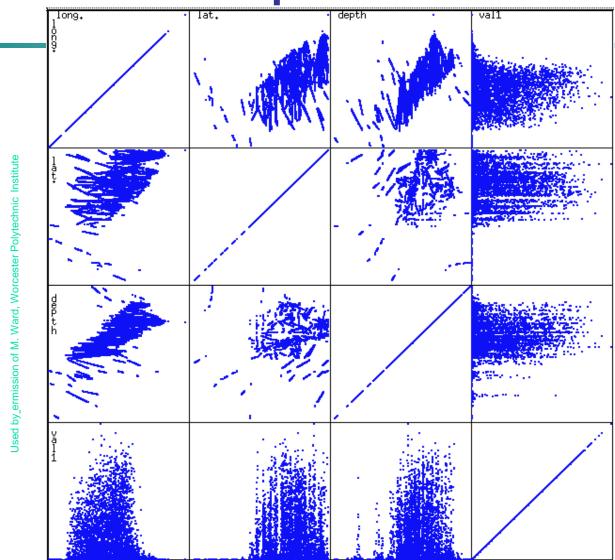


(b) Credit Limit (c) transaction volume



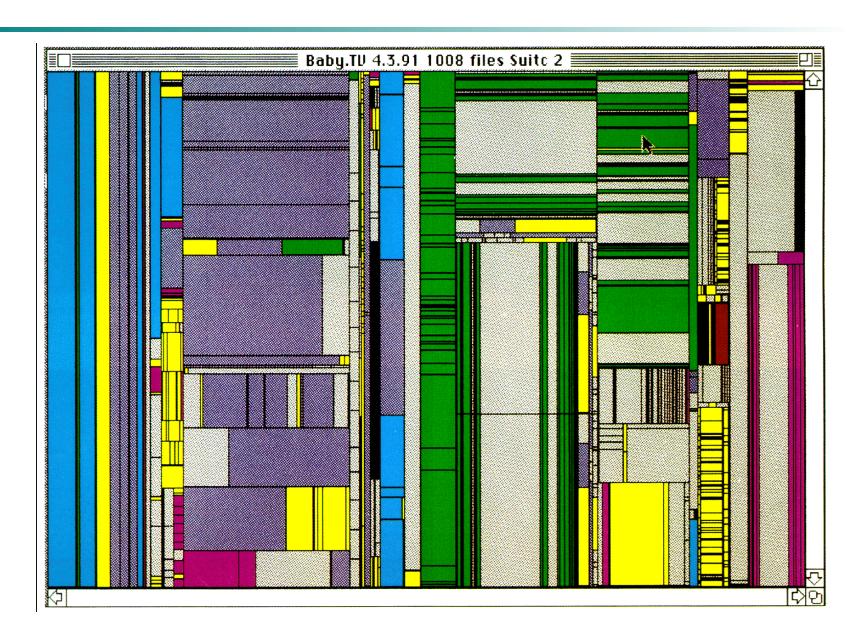
(d) age

Scatterplot Matrices



Matrix of scatterplots (x-y-diagrams) of the k-dim. data [total of (k2/2-k) scatterplots]

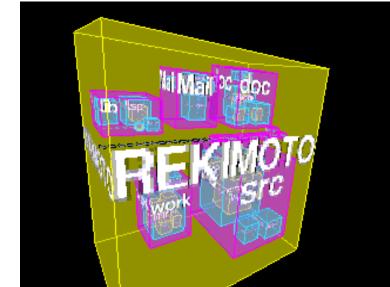
Tree-Map of a File System (Schneiderman)



InfoCube

- A 3-D visualization technique where hierarchical information is displayed as nested semi-transparent cubes
- The outermost cubes correspond to the top level data, while the subnodes or the lower level data are represented as smaller cubes inside the

outermost cubes, and so on



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Summary

Similarity and Dissimilarity

Similarity

- Numerical measure of how alike two data objects are
- Value is higher when objects are more alike
- Often falls in the range [0,1]
- Dissimilarity (e.g., distance)
 - Numerical measure of how different two data objects are
 - Lower when objects are more alike
 - Minimum dissimilarity is often 0
 - Upper limit varies
- Proximity refers to a similarity or dissimilarity

Data Matrix and Dissimilarity Matrix

Data matrix

- n data points with p dimensions
- Two modes

$$\begin{bmatrix} x_{11} & \dots & x_{1f} & \dots & x_{1p} \\ \dots & \dots & \dots & \dots \\ x_{i1} & \dots & x_{if} & \dots & x_{ip} \\ \dots & \dots & \dots & \dots \\ x_{n1} & \dots & x_{nf} & \dots & x_{np} \end{bmatrix}$$

Dissimilarity matrix

- n data points, but registers only the distance
- A triangular matrix
- Single mode

```
\begin{bmatrix} 0 & & & & & \\ d(2,1) & 0 & & & \\ d(3,1) & d(3,2) & 0 & & \\ \vdots & \vdots & \vdots & & \\ d(n,1) & d(n,2) & \dots & \dots & 0 \end{bmatrix}
```

Proximity Measure for Nominal Attributes

- Can take 2 or more states, e.g., red, yellow, blue, green (generalization of a binary attribute)
- Method 1: Simple matching
 - m: # of matches, p: total # of variables

$$d(i,j) = \frac{p-m}{p}$$

- Method 2: Use a large number of binary attributes
 - creating a new binary attribute for each of the M nominal states

Proximity Measure for Binary Attributes

- A contingency table for binary data
- Distance measure for symmetric binary variables:
- Distance measure for asymmetric binary variables:
- Jaccard coefficient (similarity)
 measure for asymmetric binary
 variables):

	- Ol	oject <i>j</i>	
ta	1	0	sum
Object $i = \frac{1}{0}$	q	r	q+r
Object r_0	s	t	s+t
sum	q + s	r+t	p

$$d(i,j) = \frac{r+s}{q+r+s+t}$$

$$d(i,j) = \frac{r+s}{q+r+s}$$

$$sim_{Jaccard}(i, j) = \frac{q}{q + r + s}$$

Note: Jaccard coefficient is the same as "coherence":

$$coherence(i,j) = \frac{sup(i,j)}{sup(i) + sup(j) - sup(i,j)} = \frac{q}{(q+r) + (q+s) - q}$$

Dissimilarity between Binary Variables

Example

Name	Gender	Fever	Cough	Test-1	Test-2	Test-3	Test-4
Jack	M	Y	N	P	N	N	N
Mary	F	Y	N	P	N	P	N
Jim	M	Y	P	N	N	N	N

- Gender is a symmetric attribute
- The remaining attributes are asymmetric binary
- Let the values Y and P be 1, and the value N 0

$$d(jack, mary) = \frac{0+1}{2+0+1} = 0.33$$
$$d(jack, jim) = \frac{1+1}{1+1+1} = 0.67$$
$$d(jim, mary) = \frac{1+2}{1+1+2} = 0.75$$

Standardizing Numeric Data

• Z-score:
$$z = \frac{x - \mu}{\sigma}$$

- X: raw score to be standardized, μ: mean of the population, σ: standard deviation
- the distance between the raw score and the population mean in units of the standard deviation
- negative when the raw score is below the mean, "+" when above
- An alternative way: Calculate the mean absolute deviation

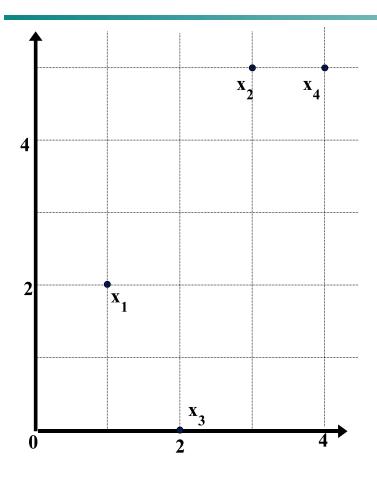
$$s_f = \frac{1}{n}(|x_{1f} - m_f| + |x_{2f} - m_f| + ... + |x_{nf} - m_f|)$$
 where
$$m_f = \frac{1}{n}(x_{1f} + x_{2f} + ... + x_{nf})$$

$$z_{if} = \frac{x_i - m_f}{s_f}$$
 standardized measure (*z-score*):

Using mean absolute deviation is more robust than using standard deviation

Example:





Data Matrix

point	attribute1	attribute2
<i>x1</i>	1	2
<i>x2</i>	3	5
<i>x3</i>	2	0
<i>x4</i>	4	5

Dissimilarity Matrix

(with Euclidean Distance)

	<i>x1</i>	<i>x</i> 2	<i>x3</i>	<i>x4</i>
<i>x1</i>	0			
<i>x</i> 2	3.61	0		
<i>x3</i>	5.1	5.1	0	
<i>x4</i>	4.24	1	5.39	0

Distance on Numeric Data: Minkowski Distance

Minkowski distance: A popular distance measure

$$d(i,j) = \sqrt[h]{|x_{i1} - x_{j1}|^h + |x_{i2} - x_{j2}|^h + \dots + |x_{ip} - x_{jp}|^h}$$

where $i = (x_{i1}, x_{i2}, ..., x_{ip})$ and $j = (x_{j1}, x_{j2}, ..., x_{jp})$ are two p-dimensional data objects, and h is the order (the distance so defined is also called L-h norm)

- Properties
 - d(i, j) > 0 if $i \neq j$, and d(i, i) = 0 (Positive definiteness)
 - d(i, j) = d(j, i) (Symmetry)
 - $d(i, j) \le d(i, k) + d(k, j)$ (Triangle Inequality)
- A distance that satisfies these properties is a metric

Special Cases of Minkowski Distance

- h = 1: Manhattan (city block, L₁ norm) distance
 - E.g., the Hamming distance: the number of bits that are different between two binary vectors

$$d(i,j) = |x_{i_1} - x_{j_1}| + |x_{i_2} - x_{j_2}| + ... + |x_{i_p} - x_{j_p}|$$

• h = 2: (L₂ norm) Euclidean distance

$$d(i,j) = \sqrt{(|x_{i1} - x_{j1}|^2 + |x_{i2} - x_{j2}|^2 + ... + |x_{ip} - x_{jp}|^2)}$$

- $h \to \infty$. "supremum" (L_{max} norm, L_{∞} norm) distance.
 - This is the maximum difference between any component (attribute) of the vectors

$$d(i,j) = \lim_{h \to \infty} \left(\sum_{f=1}^{p} |x_{if} - x_{jf}|^h \right)^{\frac{1}{h}} = \max_{f} |x_{if} - x_{jf}|$$

Example: Minkowski Distance

Dissimilarity Matrices

point	attribute 1	attribute 2
x1	1	2
x2	3	5
x3	2	0
x4	4	5

	АТ		T		J		
1	•						
						Ť	
				X ₂	X ₄		
4							
2		X ₁					
		1					
	I	:		:	1	1	

 $\mathbf{x}_{\mathbf{3}}$

Manhattan (L₁)

L	x 1	x2	х3	x4
x1	0			
x2	5	0		
х3	3	6	0	
x4	6	1	7	0

Euclidean (L₂)

L2	x1	x2	х3	x4
x1	0			
x2	3.61	0		
х3	2.24	5.1	0	
x4	4.24	1	5.39	0

Supremum

L_{∞}	x1	x2	х3	x4
x1	0			
x2	3	0		
x 3	2	5	0	
x4	3	1	5	0

Ordinal Variables

- An ordinal variable can be discrete or continuous
- Order is important, e.g., rank
- Can be treated like interval-scaled
 - replace x_{if} by their rank $r_{if} \in \{1,...,M_f\}$
 - map the range of each variable onto [0, 1] by replacing
 i-th object in the f-th variable by

$$z_{if} = \frac{r_{if} - 1}{M_f - 1}$$

 compute the dissimilarity using methods for intervalscaled variables

Attributes of Mixed Type

- A database may contain all attribute types
 - Nominal, symmetric binary, asymmetric binary, numeric, ordinal
- One may use a weighted formula to combine their effects

$$d(i,j) = \frac{\sum_{f=1}^{p} \delta_{ij}^{(f)} d_{ij}^{(f)}}{\sum_{f=1}^{p} \delta_{ij}^{(f)}}$$

f is binary or nominal:

$$d_{ij}^{(f)} = 0$$
 if $x_{if} = x_{jf}$, or $d_{ij}^{(f)} = 1$ otherwise

- f is numeric: use the normalized distance
- f is ordinal
 - Compute ranks r_{if} and
 - Treat z_{if} as interval-scaled

$$Z_{if} = \frac{r_{if} - 1}{M_{f} - 1}$$

Cosine Similarity

 A document can be represented by thousands of attributes, each recording the frequency of a particular word (such as keywords) or phrase in the document.

Document	team	coach	hockey	baseball	soccer	penalty	score	win	loss	season
Document1	5	0	3	0	2	0	0	2	0	0
Document2	3	0	2	0	1	1	0	1	0	1
Document3	0	7	0	2	1	0	0	3	0	0
Document4	0	1	0	0	1	2	2	0	3	0

- Other vector objects: gene features in micro-arrays, ...
- Applications: information retrieval, biologic taxonomy, gene feature mapping, ...
- Cosine measure: If d_1 and d_2 are two vectors (e.g., term-frequency vectors), then

$$cos(d_1, d_2) = (d_1 \cdot d_2) / ||d_1|| ||d_2||,$$

where \bullet indicates vector dot product, ||d||: the length of vector d

Example: Cosine Similarity

- $cos(d_1, d_2) = (d_1 \cdot d_2) / ||d_1|| ||d_2||$, where • indicates vector dot product, ||d|: the length of vector d
- Ex: Find the similarity between documents 1 and 2.

$$d_{1} = (5, 0, 3, 0, 2, 0, 0, 2, 0, 0)$$

$$d_{2} = (3, 0, 2, 0, 1, 1, 0, 1, 0, 1)$$

$$d_{1} \bullet d_{2} = 5*3+0*0+3*2+0*0+2*1+0*1+0*1+2*1+0*0+0*1 = 25$$

$$||d_{1}|| = (5*5+0*0+3*3+0*0+2*2+0*0+0*0+2*2+0*0+0*0)^{0.5} = (42)^{0.5}$$

$$= 6.481$$

$$||d_{2}|| = (3*3+0*0+2*2+0*0+1*1+1*1+0*0+1*1+0*0+1*1)^{0.5} = (17)^{0.5}$$

$$= 4.12$$

$$\cos(d_{1}, d_{2}) = 0.94$$

Chapter 2: Getting to Know Your Data

- Data Objects and Attribute Types
- Basic Statistical Descriptions of Data
- Data Visualization
- Measuring Data Similarity and Dissimilarity
- Summary



Summary

- Data attribute types: nominal, binary, ordinal, interval-scaled, ratioscaled
- Many types of data sets, e.g., numerical, text, graph, Web, image.
- Gain insight into the data by:
 - Basic statistical data description: central tendency, dispersion, graphical displays
 - Data visualization: map data onto graphical primitives
 - Measure data similarity
- Above steps are the beginning of data preprocessing.
- Many methods have been developed but still an active area of research.

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