# Problem Set 3 Solution

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## Resources

Read chapter 3 and 5 in The Art of R Programming. You can leave out the Extended Examples once again and Section 5.3.

# **Keyboard Shortcuts**

Try incorporating the following shortcuts into your workflow for this weeks exercise sheet:

(On Mac you can replace CTRL with CMD but don't have to)

Shortcut	What does it do?
CTRL + Shift + N F1 F2	opens new R-Script file Go to function help page (cursor over function) Get function code in new tab
CTRL + Shift + F	Search for keyword in all files in your directory

# Exercise 1

Consider the bundesliga vector from the first exercise sheet.

```
bundesliga <- c(</pre>
    "FC Bayern"
                          = 55L,
    "BVB"
                          = 51L,
   "RB Leipzig"
                          = 50L
    "Borussia MGB"
                          = 49L,
    "Bayer 04"
                          = 47L,
    "FC Schalke 04"
                          = 37L,
   "VfL Wolfsburg"
                          = 36L,
    "SC Freiburg"
                          = 36L,
    "TSG Hoffenheim"
                          = 35L,
    "1. FC Köln"
                          = 32L,
   "Union Berlin"
                          = 30L,
    "Eintracht Frankfurt" = 28L,
    "Hertha Berlin"
                         = 28L,
   "FC Augsburg"
                          = 27L,
    "Mainz 05"
                          = 26L,
    "Fortuna Duesseldorf" = 22L,
    "Werder Bremen"
                          = 18L,
   "SC Paderborn"
                          = 16L)
```

a. Convert the bundesliga vector to a matrix with one column and 18 rows. Store this matrix in an object called bundesliga\_mat (*Hint*: ARP, Section 3.1). The resulting matrix is given below:

```
bundesliga_mat <- matrix(bundesliga, ncol = 1)</pre>
bundesliga_mat
##
          [,1]
##
    [1,]
            55
##
    [2,]
            51
##
    [3,]
            50
##
    [4,]
            49
##
    [5,]
            47
##
    [6,]
            37
##
    [7,]
            36
##
   [8,]
            36
   [9,]
##
            35
## [10,]
            32
## [11,]
            30
## [12,]
            28
## [13,]
            28
## [14,]
            27
## [15,]
            26
## [16,]
            22
## [17,]
            18
## [18,]
            16
  b. What is the data type of bundesliga_mat. What is its class?
typeof(bundesliga_mat)
## [1] "integer"
class(bundesliga_mat)
## [1] "matrix" "array"
  c. Extract the points for the first 3 teams from this matrix. Then extract the last three teams. Store them
     in in the objects first3 and last3 respectively (Hint: ARP, Section 3.2. Also consider PS01, E2 and
     think about the equivalent of length for matrices (e.g. ARP, Section 3.5)). The resulting output is
     given below:
first3 <- bundesliga_mat[1:3, ]</pre>
last3 <- bundesliga_mat[(nrow(bundesliga_mat)-2):nrow(bundesliga_mat), ]</pre>
first3
## [1] 55 51 50
last3
## [1] 22 18 16
  d. What is the data type of first3 and last3. What is their class.
typeof(first3)
## [1] "integer"
typeof(last3)
## [1] "integer"
```

```
class(first3)
## [1] "integer"
class(last3)
## [1] "integer"
    e. Repeat c., but make sure, that the class of first3 and last3 remains a matrix (Hint: See ?"[" and ARP, Section 3.6).
first3 <- bundesliga_mat[1:3, , drop = FALSE]
first3 <- head(bundesliga_mat, 3)
last3 <- bundesliga_mat[(nrow(bundesliga_mat)-2):nrow(bundesliga_mat), , drop = FALSE]
last3 <- tail(bundesliga_mat, 3)
class(first3)
## [1] "matrix" "array"
class(last3)
## [1] "matrix" "array"</pre>
```

f. Currently, bundesliga\_mat only contains the information about the points, but not the team that collected them. Create a copy of bundesliga\_mat called bundesliga\_mat2. Store the team names as row names in bundesliga\_mat2 (*Hint*: ARP, Section 3.7). The resulting output is given below:

```
bundesliga_mat2 <- bundesliga_mat
rownames(bundesliga_mat2) <- names(bundesliga)</pre>
```

#### bundesliga\_mat2

```
##
                        [,1]
## FC Bayern
                          55
## BVB
                          51
## RB Leipzig
                          50
## Borussia MGB
                          49
## Bayer 04
                          47
## FC Schalke 04
                          37
## VfL Wolfsburg
                          36
## SC Freiburg
                          36
## TSG Hoffenheim
                          35
## 1. FC Köln
                          32
## Union Berlin
                          30
## Eintracht Frankfurt
                          28
## Hertha Berlin
## FC Augsburg
                          27
## Mainz 05
                          26
## Fortuna Duesseldorf
                          22
## Werder Bremen
                          18
## SC Paderborn
                          16
```

g. Is data type, class or dimension (?dim) of bundesliga\_mat different then the one of bundesliga\_mat2?

**Solution:** No, data type, class and dimensions of the two matrices are the same.

h. Create another copy of bundesliga\_mat called bundesliga\_mat3. Add a second column to this matrix that contains the teams rank ("Tabellenplatz") names (*Hint*: ARP, Section 3.4.1). The resulting output is given below:

```
bundesliga_mat3 <- bundesliga_mat</pre>
bundesliga_mat3 <- cbind(bundesliga_mat3, 1:18)</pre>
bundesliga_mat3
##
         [,1] [,2]
           55
##
   [1,]
                  1
##
   [2,]
           51
                  2
   [3,]
##
           50
                  3
##
   [4,]
           49
                  4
##
   [5,]
           47
                  5
##
   [6,]
           37
                  6
                  7
##
   [7,]
           36
##
   [8,]
                  8
           36
## [9,]
           35
                  9
## [10,]
           32
                 10
## [11,]
           30
                 11
## [12,]
           28
                 12
## [13,]
                 13
           28
## [14,]
           27
                 14
## [15,]
           26
                 15
## [16,]
           22
                 16
## [17,]
           18
                 17
## [18,]
           16
                 18
  i. What is the data type, class and dimension of bundesliga_mat3?
typeof(bundesliga_mat3)
## [1] "integer"
class(bundesliga mat3)
## [1] "matrix" "array"
dim(bundesliga mat3)
## [1] 18 2
  j. Add a third column to bundesliga_mat3, that indicates in which German federal state the team is
     located. The states vector and the resulting output are given below:
c("BAY", "NRW", "SXN", "NRW", "NRW", "NRW", "NSX", "BWB", "BWB", "NRW", "BER", "HES",
  "BER", "BAY", "RLP", "NRW", "BRE", "NRW")
bundesliga_mat3 <- cbind(</pre>
    bundesliga_mat3,
    c("BAY","NRW","SXN","NRW","NRW","NRW","NSX","BWB","BWB","NRW","BER","HES",
      "BER", "BAY", "RLP", "NRW", "BRE", "NRW"))
bundesliga_mat3
##
         [,1] [,2] [,3]
    [1,] "55" "1"
##
                    "BAY"
   [2,] "51" "2"
                    "NRW"
##
   [3,] "50" "3"
                    "SXN"
##
    [4,] "49" "4"
##
                    "NRW"
  [5,] "47" "5"
                    "NRW"
##
   [6,] "37" "6"
                    "NRW"
```

```
[7,] "36" "7"
##
                    "NSX"
    [8,] "36" "8"
##
                    "BWB"
    [9,] "35" "9"
                    "BWB"
   [10,] "32" "10" "NRW"
##
   [11,]
         "30" "11" "BER"
   [12,] "28" "12" "HES"
  [13.] "28" "13" "BER"
   [14,] "27" "14" "BAY"
   ſ15.]
         "26" "15" "RLP"
   [16,] "22" "16" "NRW"
## [17,] "18" "17" "BRE"
## [18,] "16" "18" "NRW"
```

k. What is the data type, class and dimension of bundesliga\_mat3? What changed compared to bundesliga\_mat and bundesliga\_mat2 and why? Discuss why this is not a desirable behaviour.

```
typeof(bundesliga_mat3)

## [1] "character"

class(bundesliga_mat3)

## [1] "matrix" "array"

dim(bundesliga_mat3)

## [1] 18 3
```

**Solution:** Since matrices can only handle one data type, and a column of type character got added, the matrix gets converted to type character. This is undesireable because it makes calculations on the numeric columns more difficult.

l. Currently, bundesliga\_mat3 doesn't have column names. Add column names "points", "rank" and "state" to the matrix. The resulting output is given below:

```
colnames(bundesliga_mat3) <- c("points", "rank", "state")
bundesliga_mat3</pre>
```

```
##
         points rank state
                 "1"
                       "BAY"
##
    [1,] "55"
##
    [2,] "51"
                       "NRW"
##
    [3,] "50"
                 "3"
                       "SXN"
    [4.] "49"
                       "NRW"
##
                       "NRW"
    [5,] "47"
                 "5"
##
##
    [6,]
         "37"
                 "6"
                       "NRW"
                 "7"
    [7,] "36"
                       "NSX"
##
    [8,]
         "36"
                 "8"
                       "BWB"
##
         "35"
    [9,]
                 "9"
                       "BWB"
##
   [10,]
         "32"
                 "10" "NRW"
##
##
   [11,]
         "30"
                 "11" "BER"
         "28"
   [12,]
                 "12" "HES"
         "28"
   [13,]
                 "13" "BER"
##
  [14,] "27"
                 "14" "BAY"
                 "15" "RLP"
## [15,] "26"
## [16,] "22"
                 "16" "NRW"
## [17,] "18"
                 "17" "BRE"
## [18,] "16"
                 "18" "NRW"
```

m. To overcome the problem in k., convert bundesliga\_mat3 to a data.frame by applying the function as.data.frame and store the result in object bundesliga\_df.

```
bundesliga_df <- as.data.frame(bundesliga_mat3)
```

bundesliga\_df

```
##
       points rank state
## 1
           55
                  1
                       BAY
## 2
           51
                  2
                       NRW
## 3
           50
                  3
                       SXN
## 4
           49
                  4
                       NRW
           47
                       NRW
## 5
                  5
## 6
           37
                  6
                       NRW
                  7
## 7
           36
                       NSX
## 8
            36
                  8
                       BWB
## 9
            35
                  9
                       BWB
## 10
           32
                 10
                       NRW
           30
                       BER
## 11
                 11
## 12
           28
                 12
                       HES
## 13
           28
                 13
                       BER
## 14
           27
                 14
                       BAY
## 15
           26
                 15
                       RLP
## 16
           22
                 16
                       NRW
## 17
            18
                 17
                       BRE
## 18
            16
                 18
                       NRW
```

n. What is the data type, class and dimension of bundesliga\_df?

```
typeof(bundesliga_df)
```

```
## [1] "list"
class(bundesliga_df)
```

```
## [1] "data.frame"
```

```
dim(bundesliga_df)
```

```
## [1] 18 3
```

o. Use the apply function in order to extract the class of each column in bundesliga\_df (*HInt:* ARP, Section 3.3.1 and 5.2.4). The resulting output is given below:

```
apply(bundesliga_df, 2, class)
```

```
## points rank state
## "character" "character" "character"
```

p. Internally, data.frame objects are stored as lists. Individual components of the list (columns in this case), can therefore be manipulated and overwritten the same way as list components (see ARP, Section 4.2.2). Use this knowledge to add two new columns to bundesliga\_df that contain the points and rank as integer, rather then character. Call them points\_int and rank\_int. Delete the columns points and rank. The resulting output is shown below

```
bundesliga_df$points_int <- bundesliga
bundesliga_df$rank_int <- 1:18
bundesliga_df$points <- bundesliga_df$rank <- NULL</pre>
```

## ${\tt bundesliga\_df}$

```
##
      state points_int rank_int
## 1
        BAY
                      55
## 2
        NRW
                      51
                                 2
## 3
        SXN
                      50
                                 3
## 4
        NRW
                      49
                                 4
                      47
                                 5
## 5
        NRW
## 6
                      37
                                 6
        NRW
## 7
                                 7
        NSX
                      36
## 8
                      36
                                 8
        BWB
## 9
        {\tt BWB}
                      35
                                 9
## 10
        NRW
                      32
                                10
## 11
                      30
        BER
                                11
## 12
        HES
                      28
                                12
## 13
                      28
                                13
        BER
## 14
                      27
                                14
        BAY
## 15
        RLP
                      26
                                15
## 16
        NRW
                      22
                                16
## 17
        BRE
                      18
                                17
## 18
        NRW
                      16
                                18
```

## str(bundesliga\_df)

```
## 'data.frame': 18 obs. of 3 variables:
## $ state : chr "BAY" "NRW" "SXN" "NRW" ...
## $ points_int: int 55 51 50 49 47 37 36 36 35 32 ...
## $ rank_int : int 1 2 3 4 5 6 7 8 9 10 ...
```

q. Repeat o. to check the class of the columns of bundesliga\_df. Discuss with us during the live-sessions why this contradicts the output of str(bundesliga\_df).

# Exercise 2

No

```
Create the following data frame (Hint: ARP, Section 5.1). Call the data frame df.
```

```
<- c("Alex", "Lilly", "Mark", "Oliver", "Martha", "Lucas", "Caroline")
       <- c(25, 31, 23, 52, 76, 49, 26)
height <- c(177, 163, 190, 179, 163, 183, 164)
weight \leftarrow c(57, 69, 83, 75, 70, 83, 53)
gender <- c("D", "F", "M", "M", "F", "M", "F")</pre>
       <- data.frame(name, age, height, weight, gender)</pre>
df
##
         name age height weight gender
## 1
         Alex 25
                      177
                                       F
## 2
               31
                      163
                               69
        Lilly
## 3
         Mark
               23
                      190
                               83
                                       М
## 4
       Oliver 52
                      179
                              75
                                       М
## 5
               76
                      163
                              70
                                       F
       Martha
## 6
        Lucas
               49
                      183
                              83
                                       Μ
## 7 Caroline
               26
                      164
                               53
                                       F
str(df)
## 'data.frame':
                    7 obs. of 5 variables:
## $ name : chr "Alex" "Lilly" "Mark" "Oliver" ...
                    25 31 23 52 76 49 26
## $ age
            : num
    $ height: num
                    177 163 190 179 163 183 164
                    57 69 83 75 70 83 53
## $ weight: num
                    "D" "F" "M" "M" ...
## $ gender: chr
  a. The variable gender should be of class factor. Change the variable accordingly if necessary and change
     the levels to female, male and diverse instead of F, M and D.
df$gender <- factor(df$gender, levels = c("F", "M", "D"), labels = c("female", "male", "diverse"))</pre>
df$gender
## [1] diverse female male
                                 male
                                         female male
                                                           female
## Levels: female male diverse
df[["gender"]]
## [1] diverse female male
                                 male
                                         female male
                                                           female
## Levels: female male diverse
df[, "gender"]
## [1] diverse female male
                                 male
                                         female male
                                                           female
## Levels: female male diverse
  b. Create a data frame that contains the column working, that indicates whether the person has a job
     ("Yes") or not ("No"). Call the data frame df2. The expected output is given below:
df2 <- data.frame(working = c("Yes","No","No","Yes","Yes","No","Yes"))</pre>
df2
##
     working
## 1
         Yes
## 2
          No
## 3
```

```
## 4 Yes
## 5 Yes
## 6 No
## 7 Yes
```

c. Combine the two data frames df and df2 columnwise. Store the result in object df3. The resulting output is given below:

```
df3 <- cbind(df, df2)
df3
##
         name age height weight gender working
## 1
         Alex
               25
                      177
                               57 diverse
## 2
               31
                                   female
                                                No
        Lilly
                      163
                               69
## 3
         Mark
               23
                      190
                               83
                                     male
                                                No
## 4
               52
                      179
                                     male
       Oliver
                               75
                                               Yes
## 5
       Martha
                76
                      163
                               70
                                   female
                                               Yes
```

d. Transform the working column to type logical, that contains TRUE if the person is working (Yes), and FALSE if the person is not working (No)).

No

Yes

```
df3$working <- df3$working == "Yes"
```

e. How many rows and columns does df3 have?

183

164

83

53

male

female

```
dim(df3)
```

```
## [1] 7 6
```

## 6

Lucas

## 7 Caroline

49

26

```
# Oder:
nrow(df3)
```

```
## [1] 7
```

ncol(df3)

## [1] 6

f. What data type and class is each column? Hint: Use sapply, ARP, Section 4.4.1 (remember, columns of data frames are equivalent to components of lists)

```
str(df3)
```

```
##
  'data.frame':
                    7 obs. of 6 variables:
                    "Alex" "Lilly" "Mark" "Oliver" ...
##
   $ name
            : chr
##
   $ age
             : num
                    25 31 23 52 76 49 26
   $ height : num
                    177 163 190 179 163 183 164
                    57 69 83 75 70 83 53
   $ weight : num
   $ gender : Factor w/ 3 levels "female", "male", ...: 3 1 2 2 1 2 1
                    TRUE FALSE FALSE TRUE TRUE FALSE ...
   $ working: logi
sapply(df3, typeof)
```

```
## name age height weight gender working
## "character" "double" "double" "integer" "logical"
sapply(df3, class)
```

```
## name age height weight gender working
## "character" "numeric" "numeric" "factor" "logical"
```

g. Create a new column bmi for which you calculate the BMI for each person (see https://de.wikipedia.org/wiki/Body-Mass-Index).

```
df3$bmi <- df3$weight / (df3$height / 100)^2
  h. Create a subset of df3 that only contains entries of males. Call it males_df (Hint: ARP, Section 5.2.1).
males_df <- subset(df3, gender == "male")</pre>
# oder
males_df <- df3[df3$gender == "male", ]</pre>
  i. Print out all the rows in males_df which have a bmi over 23.
males_df[males_df$bmi > 23, ]
       name age height weight gender working
## 4 Oliver 52
                    179
                             75
                                  male
                                           TRUE 23.40751
## 6 Lucas 49
                                  male
                                          FALSE 24.78426
                    183
                             83
# Oder
subset(males df, bmi > 23)
       name age height weight gender working
## 4 Oliver 52
                    179
                             75
                                  male
                                           TRUE 23.40751
## 6 Lucas 49
                    183
                             83
                                  male
                                          FALSE 24.78426
  j. Print out a subset of males_df that only contains the columns name and bmi.
males_df[, c("name", "bmi")]
##
       name
                  bmi
## 3
       Mark 22.99169
## 4 Oliver 23.40751
## 6 Lucas 24.78426
```

## Session info

```
sessionInfo()
## R version 4.3.0 (2023-04-21)
## Platform: x86_64-apple-darwin20 (64-bit)
## Running under: macOS Big Sur 11.7.10
##
## Matrix products: default
          /Library/Frameworks/R.framework/Versions/4.3-x86_64/Resources/lib/libRblas.0.dylib
## BLAS:
## LAPACK: /Library/Frameworks/R.framework/Versions/4.3-x86_64/Resources/lib/libRlapack.dylib; LAPACK
##
## locale:
## [1] en_US.UTF-8/en_US.UTF-8/en_US.UTF-8/C/en_US.UTF-8/en_US.UTF-8
## time zone: Europe/Berlin
## tzcode source: internal
##
## attached base packages:
## [1] stats
                 graphics grDevices utils
                                               datasets methods
                                                                   base
##
## loaded via a namespace (and not attached):
## [1] compiler_4.3.0 fastmap_1.1.1
                                      cli_3.6.1
                                                        tools_4.3.0
```

```
## [5] htmltools_0.5.5 rstudioapi_0.14 yaml_2.3.7 rmarkdown_2.21 ## [9] knitr_1.43 xfun_0.39 digest_0.6.31 rlang_1.1.1
```

## [13] evaluate\_0.21