

MineSweeper 2.5 - Decision Making Report

CS 440

[2] [A] [1]

[B] [C] [D]

[E] [3] [F]

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Assignment 2.5 - Decision Making

This project is intended to be an extension of the Minesweeper project in Assignment 2. At this point, you should have an inference engine capable of taking clues from a minesweeper board, and performing inferences to determine information about the remaining squares on the board. (For the purpose of this assignment, we assume the total number of mines is unknown.) When there was nothing more that could be inferred, or there were no squares that were obviously safe to collect, the agent you built should've selected randomly from the available squares. For this assignment, we want to consider the problem of how to select the next square to click more intelligently - what is the best place to click next?

To consider this problem, we first need to devise an operational definition of 'best' - what are we actually hoping to accomplish? Using the paradigm from the first part of the assignment that clicking on a mine doesn't end the game (it simply incurs a one point cost), we could quantify best in at least one of two ways:

- **Minimizing Cost:** The best choice of square is the one that minimizes the expected number of mines stepped on.
- **Minimizing Risk:** The best choice of square is the one that minimizes the expected number of squares you have to unknowingly step on.

In the first case, this leads to a general trend to avoiding squares that are likely to be mines. In the second case, this leads to a general trend of stepping on squares that provide a lot of information about the future. In both cases though, we are dealing with decisions about an uncertain future, which will need to be quantified with probability.

Assessing the Future

Given a partially revealed minesweeper board, the previous project focused on figuring out if any squares were mines or safe. In this case however, we need to consider *how likely a square is to be a mine or safe*. To do this, we need to be able to assess the probability of a given square being a mine. This is easy to do wrong.

Consider the minefield in the following example, with the clues revealed and the unknown squares given by the variables A, B, C, D, E, F :

[2] [A] [1]

[B] [C] [D]

[E] [3] [F]

In the previous project, you implemented a system that should be able to determine that B is a mine and D is safe, but the rest of the board is undetermined. What, then, is the likelihood that A is a mine? Or that E is safe? It's tempting to argue that the probability that A is a mine is $2/3$, based on the clue-value of w and there being three adjacent squares A, B, C . However, you would then also argue that the probability that A is a mine is $1/3$, based on the clue-value of 1 and the three adjacent squares A, C, D . Given that B is a mine, you might even say further that the probability that A is a mine is actually $1/2$, since one of A and C must be a mine to satisfy the clue-value 2. What is the truth?

If you work it out, you'll find that the only satisfying assignments are B is a mine, D as safe, and one of the three following combinations:

- C is a mine, A is not a mine, E is a mine, F is not a mine
- C is a mine, A is not a mine, E is not a mine, F is a mine
- C is not a mine, A is a mine, E is a mine, F is a mine

Because any one of these assignments is equally likely, we can then assess the probability of a given square being a mine as

[− − −] [1/3] [− − −]

[3/3] [2/3] [0/3]

[2/3] [− − −] [2/3]

From the above, we see that the least risky square to click on (in terms of stepping on a mine) is D, but the second least risky is in fact A.

In this way, given a partially revealed board, we can assess the possible states of unknown squares and in doing so determine the probability of any event. (For instance, the probability that A and F are the same thing is $2/3$.)

Computational Comments:

- *You should be able to use your inference engine from Assignment 2 to help bootstrap the computation of these probabilities. How?*
- *Consider dividing the board into ‘active unknowns’, the squares that are touching some clue, and ‘inactive unknowns’, the squares that are touching no clues. For any inactive unknown, that square is equally likely to be a mine as it is to be safe. Why?*

In your writeup, describe in detail how you compute these probabilities and what you utilized from Assignment 2 to do so. If you approximate or estimate anything (not strictly necessary), be clear as to what you approximated, why, and why you feel it was valid.

The Basic Agents

In each of the following subsections, you will compare your agent from Assignment 2 (Pure Random Decision Making) with a (slightly) improved agent.

Minimizing Cost

Consider the following slightly improved agent, built off your agent from Assignment 2:

- Given the current state of the board, use your inference engine from Assignment 2 to figure out as much as possible about the remaining squares.
- If any square can be identified as a mine, flag it to not select it in the future.
- If any square can be identified as safe, click on it, add the clue to your knowledge base, and continue to infer until nothing definite remains.
- Once nothing definite (mines or safe) can be determined, assess for each unrevealed square how likely it is to be a mine.
- Click on the square with the lowest probability of being a mine (breaking ties at random), add the result to your knowledge base.
- Repeat (restarting the inference loop) until the board is cleared.
- The final total cost is taken to be the total number of mines stepped on.

Generate data and plot ‘mine density’ vs ‘average cost’ for both the pure random decision agent from Assignment 2, and the basic cost minimizing agent above. How does the slightly improved agent compare? Why? How frequently is the ‘improved’ decision making necessary?

Minimizing Risk

Consider the following slightly improved agent, built off your agent from Assignment 2:

- Given the current state of the board, use your inference engine from Assignment 2 to figure out as much as possible about the remaining squares.
- If any square can be identified as a mine, flag it to not select it in the future.
- If any square can be identified as safe, click on it, add the clue to your knowledge base, and continue to infer until nothing definite remains.
- Once nothing definite (mines or safe) can be determined, assess for each unrevealed square how likely it is to be a mine.
- For each square, determine *the expected number of squares that can be worked out if you clicked on it*:
 - Let q be the likelihood that the square is a mine, and let R be the number of squares that you could work out if it is a mine.
 - let $1 - q$ be the likelihood that the square is safe, and let S be the number of squares that you could work out if it is safe.
 - The expected number of squares that could be worked out is $qR + (1 - q)S$.
- Click on the square with the highest expected number of solvable squares (breaking ties at random), add the result to your knowledge base.
- Repeat (restarting the inference loop) until the board is cleared.
- The final total cost is taken to be the total number of squares stepped on *without knowing what they are*.

Generate data and plot ‘mine density’ vs ‘average risk’ for both the pure random decision agent from Assignment 2, and the basic risk minimizing agent above. How does the slightly improved agent compare? Why? How frequently is the ‘improved’ decision making necessary?

Bonus

How does the risk minimizing agent compare to the cost minimizing agent when it comes to minimizing the cost? How does the cost minimizing agent compare to the risk minimizing agent when it comes to minimizing risk? Generate data. Discuss. (Points for clarity and thoroughness.)

Improved Agent

For one of either minimizing cost or minimizing risk, build an improved decision making agent that beats the simple agent described in the previous section (that isn’t just the other simple agent!). Plot the relevant data for your original Assignment 2 agent, the slightly improved agent (from the previous section), and your improved agent. Describe in detail, and justify, the logic and construction of your agent. Is your improved agent significantly better than the other two? How frequently does your improved agent make different decisions than the slightly improved agent? Is your improved agent as good as it can be? How could it be improved?

Bonus

Construct and analyze an improved agent for the other metric you didn’t already do.

Minimum Cost Visualization

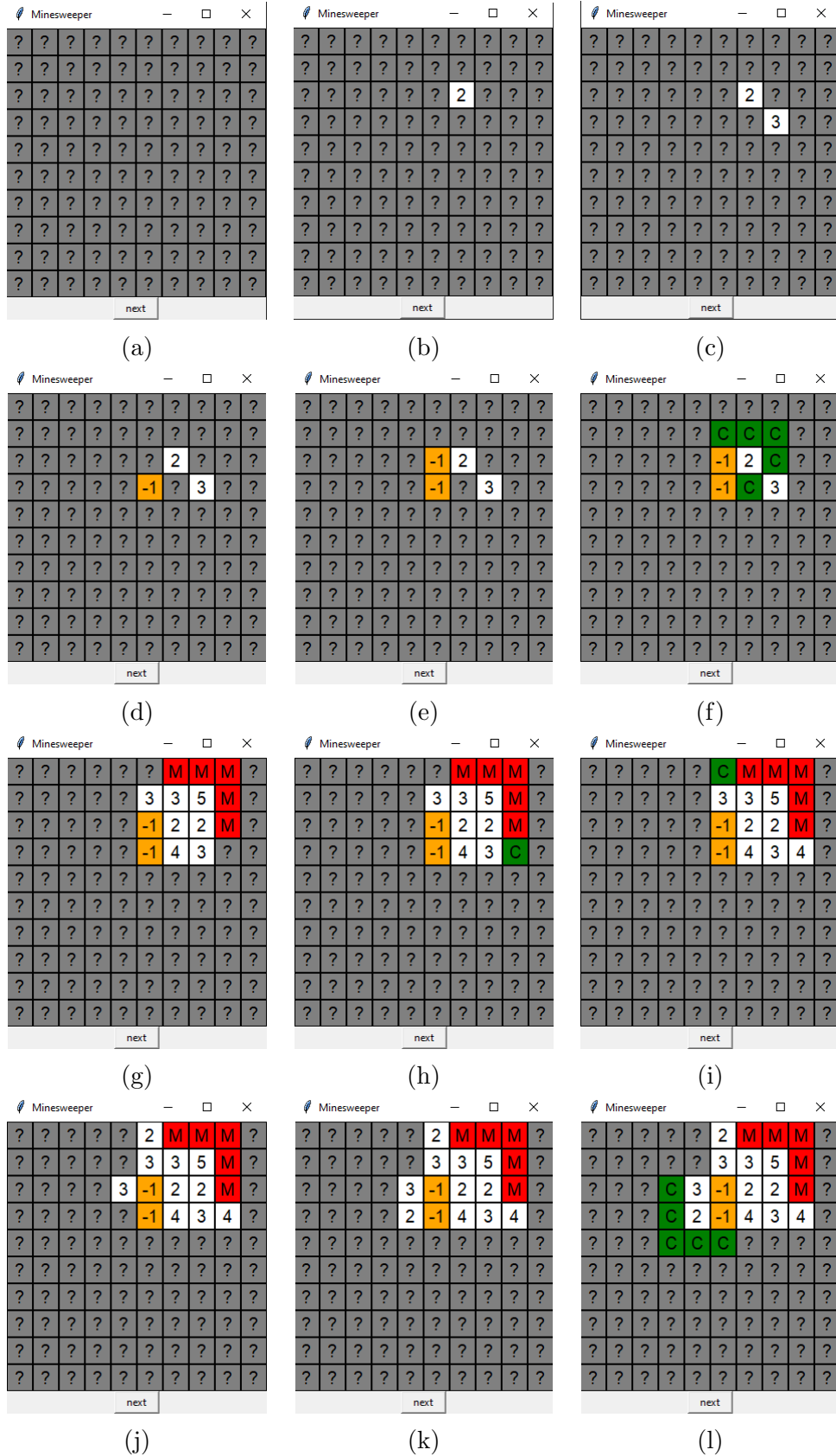
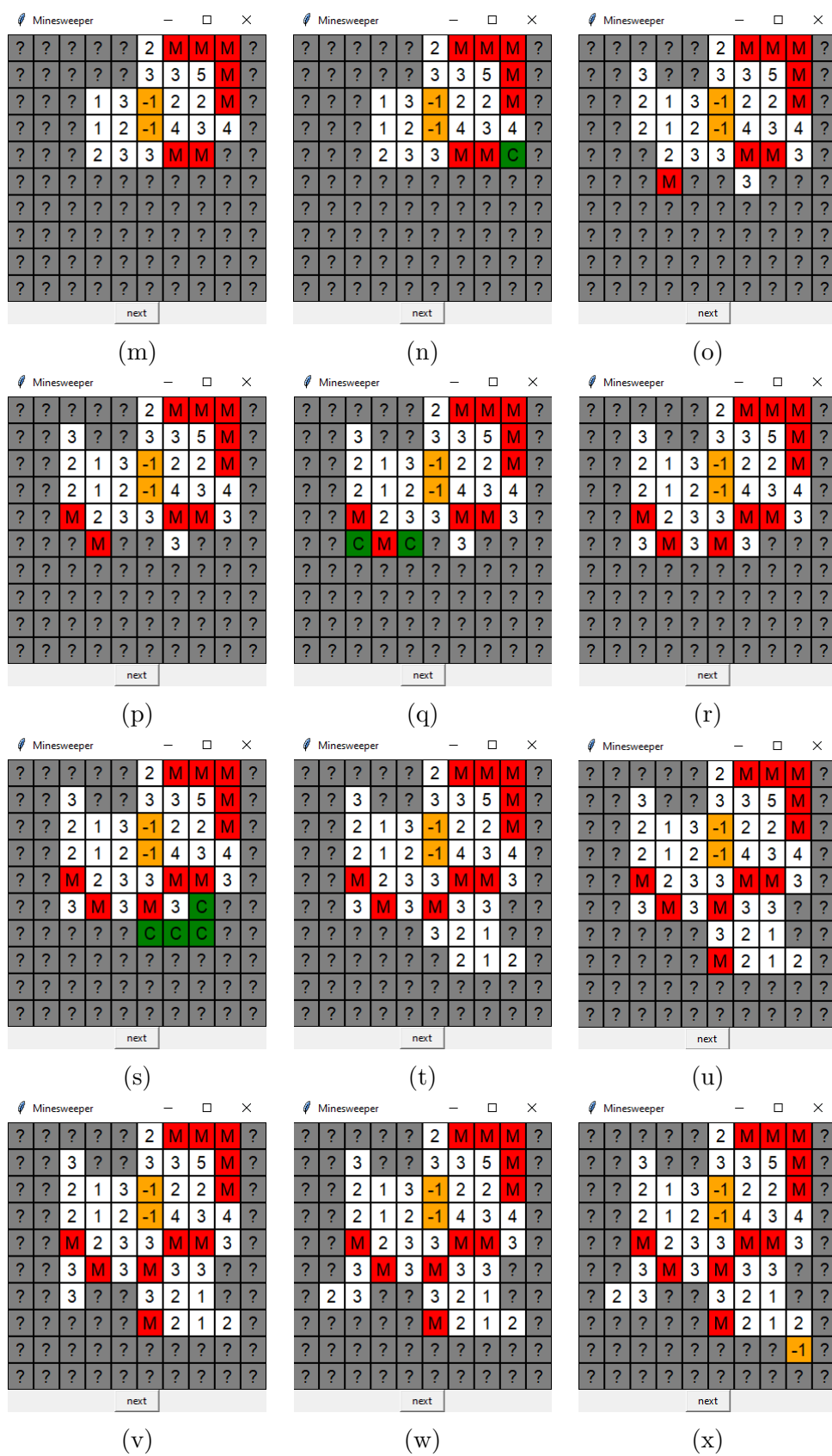
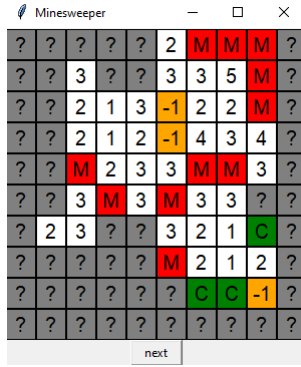
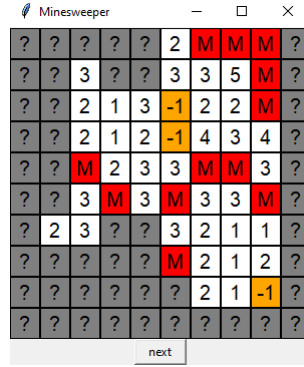


Figure 1: Minimizing Cost Agent Visualization

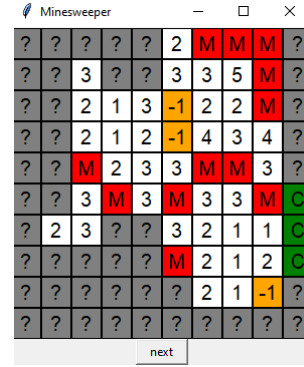




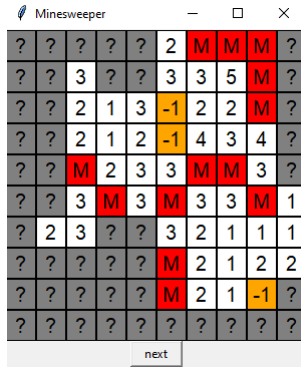
(a)



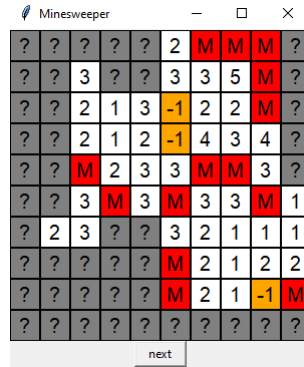
(b)



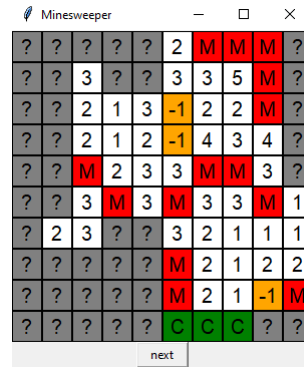
(c)



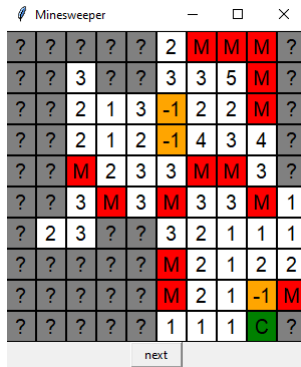
(d)



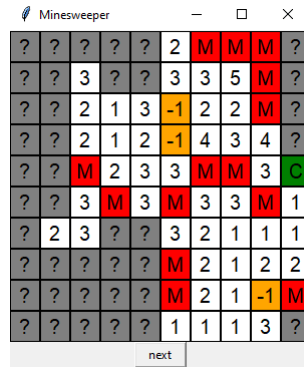
(e)



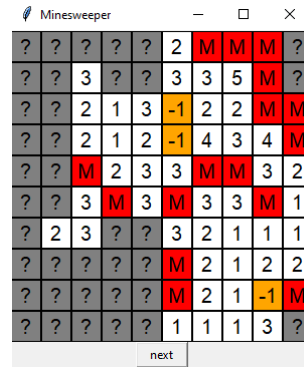
(f)



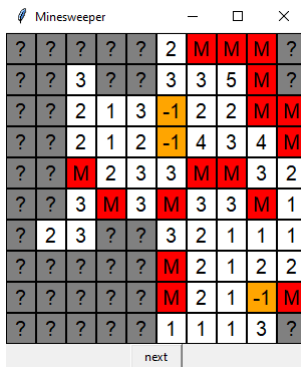
(g)



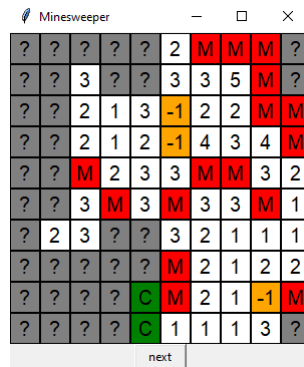
(h)



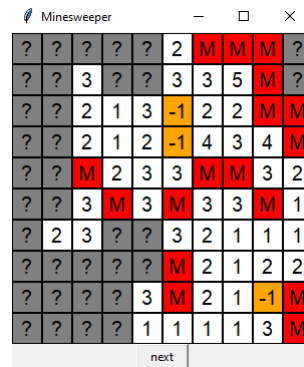
(i)



(j)



(k)



(l)

Figure 2: *Continued...*

MineSweeper — □ ×

| | | | | | | | | | |
|---|---|---|---|---|----|---|---|---|----|
| ? | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| ? | ? | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| ? | ? | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| ? | ? | M | 2 | 3 | 3 | M | M | 3 | 2 |
| ? | ? | 3 | M | 3 | M | 3 | 3 | M | 1 |
| ? | 2 | 3 | ? | ? | 3 | 2 | 1 | 1 | 1 |
| ? | ? | ? | ? | ? | M | 2 | 1 | 2 | 2 |
| ? | ? | ? | ? | C | 3 | M | 2 | 1 | -1 |
| ? | ? | ? | C | 1 | 1 | 1 | 1 | 3 | M |

next

(m)

MineSweeper — □ ×

| | | | | | | | | | |
|---|---|---|---|---|----|---|---|----|---|
| ? | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| ? | ? | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| ? | ? | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| ? | ? | M | 2 | 3 | 3 | M | M | 3 | 2 |
| ? | ? | 3 | M | 3 | M | 3 | 3 | M | 1 |
| ? | 2 | 3 | ? | ? | 3 | 2 | 1 | 1 | 1 |
| ? | ? | ? | ? | ? | M | 2 | 1 | 2 | 2 |
| ? | ? | C | 1 | 3 | M | 2 | 1 | -1 | M |
| ? | ? | C | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(n)

MineSweeper — □ ×

| | | | | | | | | | |
|---|---|---|---|---|----|---|---|----|---|
| ? | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| ? | ? | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| ? | ? | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| ? | ? | M | 2 | 3 | 3 | M | M | 3 | 2 |
| ? | ? | 3 | M | 3 | M | 3 | 3 | M | 1 |
| ? | 2 | 3 | ? | ? | 3 | 2 | 1 | 1 | 1 |
| ? | ? | ? | ? | ? | M | 2 | 1 | 2 | 2 |
| ? | C | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| ? | C | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(o)

MineSweeper — □ ×

| | | | | | | | | | |
|---|---|---|---|---|----|---|---|----|---|
| ? | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| ? | ? | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| ? | ? | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| ? | ? | M | 2 | 3 | 3 | M | M | 3 | 2 |
| ? | ? | 3 | M | 3 | M | 3 | 3 | M | 1 |
| ? | 2 | 3 | ? | ? | 3 | 2 | 1 | 1 | 1 |
| 1 | 1 | 1 | ? | ? | M | 2 | 1 | 2 | 2 |
| ? | 1 | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| ? | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(p)

MineSweeper — □ ×

| | | | | | | | | | |
|---|---|---|---|---|----|---|---|----|---|
| ? | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| ? | ? | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| ? | ? | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| ? | ? | M | 2 | 3 | 3 | M | M | 3 | 2 |
| ? | ? | 3 | M | 3 | M | 3 | 3 | M | 1 |
| ? | 2 | 3 | ? | ? | 3 | 2 | 1 | 1 | 1 |
| 1 | 1 | 1 | M | ? | M | 2 | 1 | 2 | 2 |
| ? | 1 | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| ? | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(q)

MineSweeper — □ ×

| | | | | | | | | | |
|---|---|---|---|---|----|---|---|----|---|
| ? | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| ? | ? | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| ? | ? | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| ? | ? | M | 2 | 3 | 3 | M | M | 3 | 2 |
| ? | ? | 3 | M | 3 | M | 3 | 3 | M | 1 |
| ? | 2 | 3 | ? | ? | 3 | 2 | 1 | 1 | 1 |
| 1 | 1 | 1 | M | ? | M | 2 | 1 | 2 | 2 |
| ? | 1 | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| ? | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(r)

MineSweeper — □ ×

| | | | | | | | | | |
|---|---|---|---|---|----|---|---|----|---|
| ? | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| ? | ? | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| ? | ? | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| ? | ? | M | 2 | 3 | 3 | M | M | 3 | 2 |
| ? | ? | 3 | M | 3 | M | 3 | 3 | M | 1 |
| ? | 2 | 3 | ? | ? | 3 | 2 | 1 | 1 | 1 |
| 1 | 1 | 1 | M | C | M | 2 | 1 | 2 | 2 |
| ? | 1 | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| ? | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(s)

MineSweeper — □ ×

| | | | | | | | | | |
|---|---|---|---|---|----|---|---|----|---|
| ? | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| ? | ? | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| ? | ? | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| ? | ? | M | 2 | 3 | 3 | M | M | 3 | 2 |
| ? | ? | 3 | M | 3 | M | 3 | 3 | M | 1 |
| ? | 2 | 3 | ? | ? | 3 | 2 | 1 | 1 | 1 |
| 1 | 1 | 1 | M | 4 | M | 2 | 1 | 2 | 2 |
| ? | 1 | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| ? | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(t)

MineSweeper — □ ×

| | | | | | | | | | |
|---|---|---|---|---|----|---|---|----|---|
| ? | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| ? | ? | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| ? | ? | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| ? | ? | M | 2 | 3 | 3 | M | M | 3 | 2 |
| ? | ? | 3 | M | 3 | M | 3 | 3 | M | 1 |
| ? | 2 | 3 | C | M | 3 | 2 | 1 | 1 | 1 |
| 1 | 1 | 1 | M | 4 | M | 2 | 1 | 2 | 2 |
| ? | 1 | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| ? | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(u)

MineSweeper — □ ×

| | | | | | | | | | |
|---|---|---|---|---|----|---|---|----|---|
| ? | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| ? | ? | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| ? | ? | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| ? | ? | M | 2 | 3 | 3 | M | M | 3 | 2 |
| ? | M | 3 | M | 3 | M | 3 | 3 | M | 1 |
| ? | 2 | 3 | 3 | M | 3 | 2 | 1 | 1 | 1 |
| 1 | 1 | 1 | M | 4 | M | 2 | 1 | 2 | 2 |
| ? | 1 | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| ? | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(v)

MineSweeper — □ ×

| | | | | | | | | | |
|---|---|---|---|---|----|---|---|----|---|
| ? | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| ? | ? | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| ? | ? | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| ? | C | M | 2 | 3 | 3 | M | M | 3 | 2 |
| ? | M | 3 | M | 3 | M | 3 | 3 | M | 1 |
| ? | 2 | 3 | 3 | M | 3 | 2 | 1 | 1 | 1 |
| 1 | 1 | 1 | M | 4 | M | 2 | 1 | 2 | 2 |
| ? | 1 | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| ? | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(w)

MineSweeper — □ ×

| | | | | | | | | | |
|---|----|---|---|---|----|---|---|----|---|
| ? | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| ? | -1 | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| ? | ? | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| ? | 3 | M | 2 | 3 | 3 | M | M | 3 | 2 |
| ? | M | 3 | M | 3 | M | 3 | 3 | M | 1 |
| ? | 2 | 3 | 3 | M | 3 | 2 | 1 | 1 | 1 |
| 1 | 1 | 1 | M | 4 | M | 2 | 1 | 2 | 2 |
| ? | 1 | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| ? | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(x)

Figure 2: *Continued...*

MineSweeper — □ ×

| | | | | | | | | | |
|---|----|---|---|---|----|---|---|----|---|
| ? | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| ? | -1 | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| ? | C | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| ? | 3 | M | 2 | 3 | 3 | M | M | 3 | 2 |
| ? | M | 3 | M | 3 | M | 3 | 3 | M | 1 |
| ? | 2 | 3 | 3 | M | 3 | 2 | 1 | 1 | 1 |
| 1 | 1 | 1 | M | 4 | M | 2 | 1 | 2 | 2 |
| ? | 1 | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| ? | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(a)

MineSweeper — □ ×

| | | | | | | | | | |
|---|----|---|---|---|----|---|---|----|---|
| 2 | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| ? | -1 | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| ? | 3 | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| ? | 3 | M | 2 | 3 | 3 | M | M | 3 | 2 |
| ? | M | 3 | M | 3 | M | 3 | 3 | M | 1 |
| ? | 2 | 3 | 3 | M | 3 | 2 | 1 | 1 | 1 |
| 1 | 1 | 1 | M | 4 | M | 2 | 1 | 2 | 2 |
| ? | 1 | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| ? | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(b)

MineSweeper — □ ×

| | | | | | | | | | |
|---|----|---|---|---|----|---|---|----|---|
| 2 | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| ? | -1 | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| 2 | 3 | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| ? | 3 | M | 2 | 3 | 3 | M | M | 3 | 2 |
| ? | M | 3 | M | 3 | M | 3 | 3 | M | 1 |
| ? | 2 | 3 | 3 | M | 3 | 2 | 1 | 1 | 1 |
| 1 | 1 | 1 | M | 4 | M | 2 | 1 | 2 | 2 |
| ? | 1 | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| ? | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(c)

MineSweeper — □ ×

| | | | | | | | | | |
|---|----|---|---|---|----|---|---|----|---|
| 2 | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| ? | -1 | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| 2 | 3 | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| ? | 3 | M | 2 | 3 | 3 | M | M | 3 | 2 |
| ? | M | 3 | M | 3 | M | 3 | 3 | M | 1 |
| ? | 2 | 3 | 3 | M | 3 | 2 | 1 | 1 | 1 |
| 1 | 1 | 1 | M | 4 | M | 2 | 1 | 2 | 2 |
| ? | 1 | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| ? | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(d)

MineSweeper — □ ×

| | | | | | | | | | |
|----|----|---|---|---|----|---|---|----|---|
| 2 | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| ? | -1 | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| 2 | 3 | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| ? | 3 | M | 2 | 3 | 3 | M | M | 3 | 2 |
| ? | M | 3 | M | 3 | M | 3 | 3 | M | 1 |
| ? | 2 | 3 | 3 | M | 3 | 2 | 1 | 1 | 1 |
| 1 | 1 | 1 | M | 4 | M | 2 | 1 | 2 | 2 |
| -1 | 1 | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| ? | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(e)

MineSweeper — □ ×

| | | | | | | | | | |
|----|----|---|---|---|----|---|---|----|---|
| 2 | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| ? | -1 | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| 2 | 3 | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| ? | 3 | M | 2 | 3 | 3 | M | M | 3 | 2 |
| ? | M | 3 | M | 3 | M | 3 | 3 | M | 1 |
| ? | 2 | 3 | 3 | M | 3 | 2 | 1 | 1 | 1 |
| 1 | 1 | 1 | M | 4 | M | 2 | 1 | 2 | 2 |
| -1 | 1 | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| C | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(f)

MineSweeper — □ ×

| | | | | | | | | | |
|----|----|---|---|---|----|---|---|----|---|
| 2 | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| ? | -1 | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| 2 | 3 | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| ? | 3 | M | 2 | 3 | 3 | M | M | 3 | 2 |
| ? | M | 3 | M | 3 | M | 3 | 3 | M | 1 |
| C | 2 | 3 | 3 | M | 3 | 2 | 1 | 1 | 1 |
| 1 | 1 | 1 | M | 4 | M | 2 | 1 | 2 | 2 |
| -1 | 1 | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| 1 | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(g)

MineSweeper — □ ×

| | | | | | | | | | |
|----|----|---|---|---|----|---|---|----|---|
| 2 | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| ? | -1 | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| 2 | 3 | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| ? | 3 | M | 2 | 3 | 3 | M | M | 3 | 2 |
| M | M | 3 | M | 3 | M | 3 | 3 | M | 1 |
| 2 | 2 | 3 | 3 | M | 3 | 2 | 1 | 1 | 1 |
| 1 | 1 | 1 | M | 4 | M | 2 | 1 | 2 | 2 |
| -1 | 1 | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| 1 | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(h)

MineSweeper — □ ×

| | | | | | | | | | |
|----|----|---|---|---|----|---|---|----|---|
| 2 | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| ? | -1 | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| 2 | 3 | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| C | 3 | M | 2 | 3 | 3 | M | M | 3 | 2 |
| M | M | 3 | M | 3 | M | 3 | 3 | M | 1 |
| 2 | 2 | 3 | 3 | M | 3 | 2 | 1 | 1 | 1 |
| 1 | 1 | 1 | M | 4 | M | 2 | 1 | 2 | 2 |
| -1 | 1 | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| 1 | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(i)

MineSweeper — □ ×

| | | | | | | | | | |
|----|----|---|---|---|----|---|---|----|---|
| 2 | ? | ? | ? | ? | 2 | M | M | M | ? |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| M | -1 | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| 2 | 3 | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| 2 | 3 | M | 2 | 3 | 3 | M | M | 3 | 2 |
| M | M | 3 | M | 3 | M | 3 | 3 | M | 1 |
| 2 | 2 | 3 | 3 | M | 3 | 2 | 1 | 1 | 1 |
| 1 | 1 | 1 | M | 4 | M | 2 | 1 | 2 | 2 |
| -1 | 1 | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| 1 | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(j)

MineSweeper — □ ×

| | | | | | | | | | |
|----|----|---|---|---|----|---|---|----|---|
| 2 | ? | ? | ? | ? | 2 | M | M | M | 2 |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | ? |
| M | -1 | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| 2 | 3 | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| 2 | 3 | M | 2 | 3 | 3 | M | M | 3 | 2 |
| M | M | 3 | M | 3 | M | 3 | 3 | M | 1 |
| 2 | 2 | 3 | 3 | M | 3 | 2 | 1 | 1 | 1 |
| 1 | 1 | 1 | M | 4 | M | 2 | 1 | 2 | 2 |
| -1 | 1 | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| 1 | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(k)

MineSweeper — □ ×

| | | | | | | | | | |
|----|----|---|---|---|----|---|---|----|---|
| 2 | ? | ? | ? | ? | 2 | M | M | M | 2 |
| ? | ? | 3 | ? | ? | 3 | 3 | 5 | M | C |
| M | -1 | 2 | 1 | 3 | -1 | 2 | 2 | M | M |
| 2 | 3 | 2 | 1 | 2 | -1 | 4 | 3 | 4 | M |
| 2 | 3 | M | 2 | 3 | 3 | M | M | 3 | 2 |
| M | M | 3 | M | 3 | M | 3 | 3 | M | 1 |
| 2 | 2 | 3 | 3 | M | 3 | 2 | 1 | 1 | 1 |
| 1 | 1 | 1 | M | 4 | M | 2 | 1 | 2 | 2 |
| -1 | 1 | 1 | 1 | 3 | M | 2 | 1 | -1 | M |
| 1 | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 3 | M |

next

(l)

Figure 3: *Continued...*

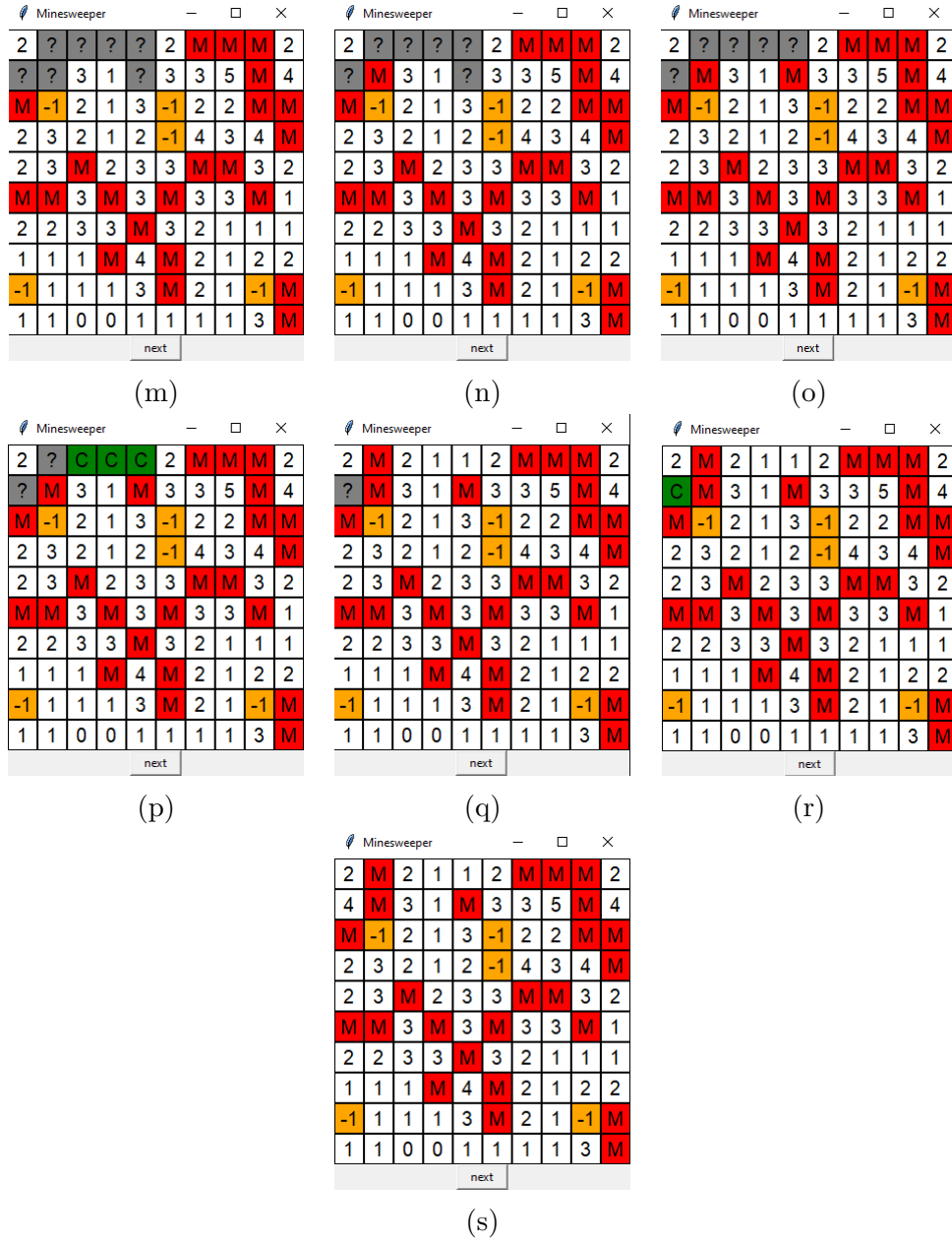


Figure 3: Minimizing Cost Agent Visualization: **Grid:**[10 x 10] **Mines:**[30]
Cost = total # of mines stepped on: 5

Minimum Cost Question Responses

The plot that is below (Figure: 4) is data for both the pure random decision agent from Assignment 2, and the basic cost minimizing agent. The original

basic agent's data is denoted as the red bar graph(s), while the minimizing cost agent is denoted as the green bar graph(s). The graph was generated by calling the `iterateForComparison()` method in the `minimizing_cost_agent.py` file (*Line #: 615*). This method was passed a 10 x 10 grid, with fifty mines where for thirty games, the average cost was calculated for increasing mine densities. These thirty games produced the Figure 4). As one can see from the data the original pure random decision agent from assignment 2, tended to have a higher average cost for the mine densities for the ranges up to sixty. From the mine densities of sixty up to eighty-five both the random decision agent and the minimizing cost agent, had similar costs. And from the ranges of ninety and ninety-five the minimizing cost agent had a slightly higher average cost than that of the original basic agent. However, when the mine density was one-hundred then both were neck and neck again. From these results, we can then say that overall, the basic agent does exactly 'slightly' better than the improved agent overall. This is due to the fact that the minimizing cost agent calculates more accurately which neighbors, and the neighbors of those neighbors are most likely to be mines therefore avoiding those cells. More specifically, the mine densities from ranges of twenty to seventy, is where the minimum cost agent has a lower average cost than the original agent meaning that the frequency that the slightly improved agent was making decisions was greater. To quantify, twelve out of the nineteen densities had the minimizing cost agent lower than when compared to the original agent or around sixty-three percent.

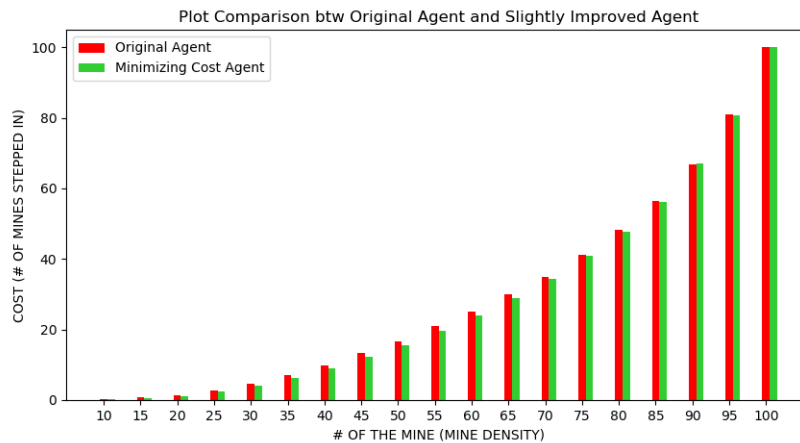


Figure 4: Mine Density vs. Average Cost

Minimum Risk Visualization

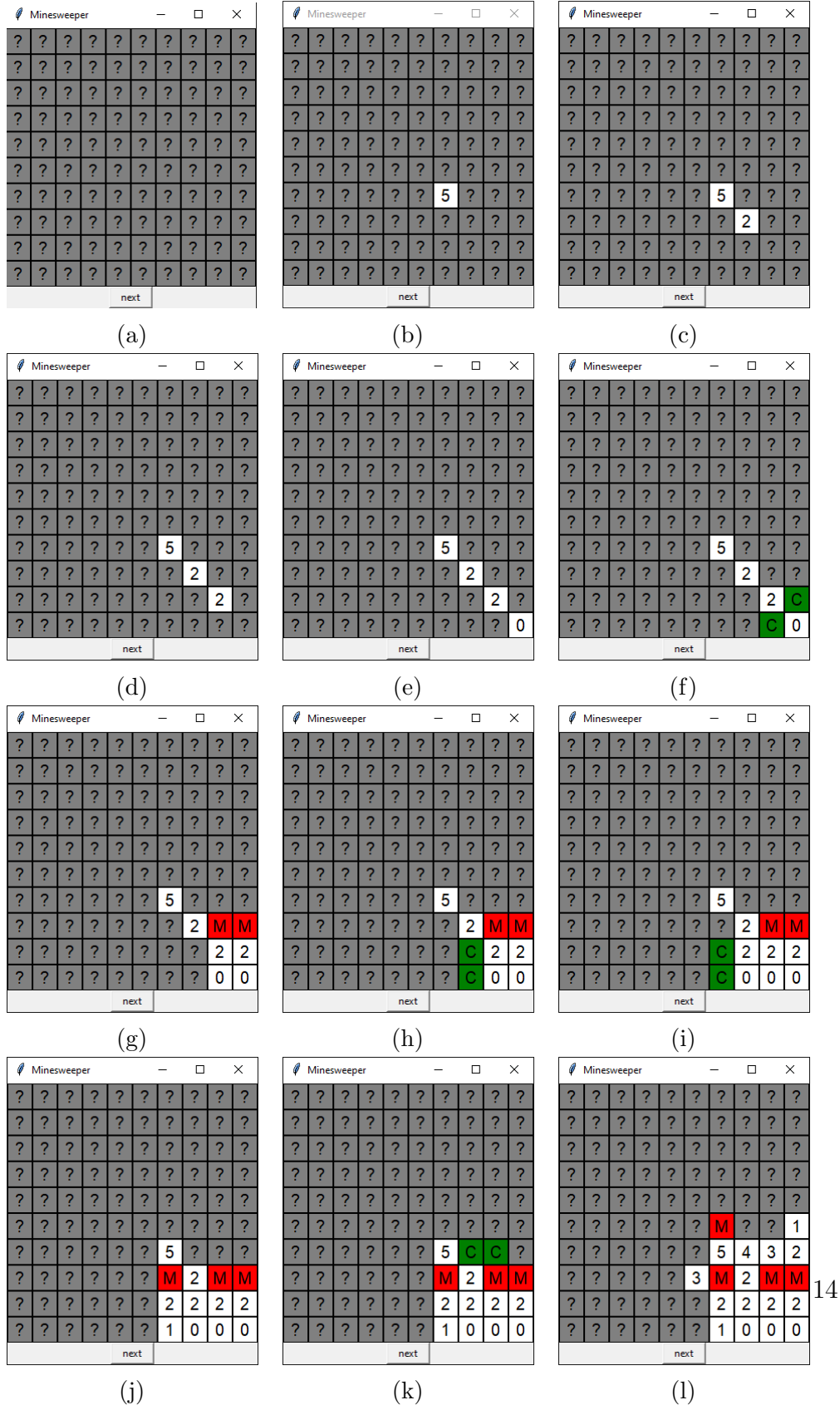


Figure 5: Minimizing Risk Agent Visualization



| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | 4 | M | ? | ? |
| ? | ? | ? | ? | ? | M | M | M | 2 | 1 |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(a)

| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | 4 | M | C | ? |
| ? | ? | ? | ? | ? | M | M | M | 2 | 1 |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(b)

| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | ? | ? | 4 | ? |
| ? | ? | ? | ? | ? | ? | 4 | M | 2 | ? |
| ? | ? | ? | ? | ? | M | M | M | 2 | 1 |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(c)

| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | ? | 4 | M | ? |
| ? | ? | ? | ? | ? | ? | ? | 4 | M | 2 |
| ? | ? | ? | ? | M | M | M | 2 | 1 | ? |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(d)

| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | ? | 4 | M | ? |
| ? | ? | ? | ? | ? | ? | 5 | 4 | M | 2 |
| ? | ? | ? | ? | M | M | M | 2 | 1 | ? |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(e)

| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | ? | M | 4 | M |
| ? | ? | ? | ? | ? | ? | 5 | 4 | M | 2 |
| ? | ? | ? | ? | M | M | M | 2 | 1 | ? |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(f)

| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | C | M | 4 | M |
| ? | ? | ? | ? | ? | ? | 5 | 4 | M | 2 |
| ? | ? | ? | ? | M | M | M | 2 | 1 | ? |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(g)

| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | 1 | 2 | 2 | ? |
| ? | ? | ? | ? | ? | ? | 2 | M | 4 | M |
| ? | ? | ? | ? | ? | ? | 5 | 4 | M | 2 |
| ? | ? | ? | ? | ? | M | M | M | 2 | 1 |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(h)

| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| ? | ? | ? | ? | ? | ? | ? | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | 0 | ? | ? | ? |
| ? | ? | ? | ? | ? | ? | 1 | 2 | 2 | ? |
| ? | ? | ? | ? | ? | ? | 2 | M | 4 | M |
| ? | ? | ? | ? | ? | ? | 5 | 4 | M | 2 |
| ? | ? | ? | ? | ? | M | M | M | 2 | 1 |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(i)

| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| ? | ? | ? | ? | ? | C | C | C | ? | ? |
| ? | ? | ? | ? | ? | C | 0 | C | ? | ? |
| ? | ? | ? | ? | ? | 1 | 2 | 2 | ? | ? |
| ? | ? | ? | ? | ? | 2 | M | 4 | M | ? |
| ? | ? | ? | ? | ? | 5 | 4 | M | 2 | ? |
| ? | ? | ? | ? | M | M | M | 2 | 1 | ? |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(j)

| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| ? | ? | ? | ? | ? | 0 | 0 | 1 | ? | ? |
| ? | ? | ? | ? | ? | 0 | 0 | 2 | ? | ? |
| ? | ? | ? | ? | ? | 1 | 2 | 2 | ? | ? |
| ? | ? | ? | ? | M | 2 | M | 4 | M | ? |
| ? | ? | ? | ? | ? | 5 | 4 | M | 2 | ? |
| ? | ? | ? | ? | M | M | M | 2 | 1 | ? |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(k)

| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| ? | ? | ? | ? | C | 0 | 0 | 1 | ? | ? |
| ? | ? | ? | ? | C | 0 | 0 | 2 | ? | ? |
| ? | ? | ? | ? | ? | 1 | 2 | 2 | ? | ? |
| ? | ? | ? | ? | M | 2 | M | 4 | M | ? |
| ? | ? | ? | ? | ? | 5 | 4 | M | 2 | ? |
| ? | ? | ? | ? | M | M | M | 2 | 1 | ? |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(l)

Figure 6: *Continued...*

| | | | | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|------|---|---|
| Minesweeper | | | | | | | | | | — | □ | × |
| ? | ? | ? | ? | ? | 0 | 0 | 0 | 1 | ? | ? | | |
| ? | ? | ? | ? | ? | 0 | 0 | 0 | 2 | ? | ? | | |
| ? | ? | ? | ? | ? | C | 1 | 2 | 2 | ? | ? | | |
| ? | ? | ? | ? | ? | M | 2 | M | 4 | M | | | |
| ? | ? | ? | ? | ? | ? | 5 | 4 | M | 2 | | | |
| ? | ? | ? | ? | ? | M | M | M | 2 | 1 | | | |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 | | | |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M | | | |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 | | | |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 | | | |
| | | | | | | | | | | next | | |

(m)

| | | | | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|------|---|---|
| Minesweeper | | | | | | | | | | — | □ | × |
| ? | ? | ? | ? | ? | 0 | 0 | 0 | 1 | ? | ? | | |
| ? | ? | ? | ? | ? | 0 | 0 | 0 | 2 | ? | ? | | |
| ? | ? | ? | ? | ? | 1 | 1 | 2 | 2 | ? | ? | | |
| ? | ? | ? | ? | ? | M | 2 | M | 4 | M | | | |
| ? | ? | ? | ? | ? | C | 5 | 4 | M | 2 | | | |
| ? | ? | ? | ? | ? | M | M | M | 2 | 1 | | | |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 | | | |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M | | | |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 | | | |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 | | | |
| | | | | | | | | | | next | | |

(n)

| | | | | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|------|---|---|
| Minesweeper | | | | | | | | | | — | □ | × |
| ? | ? | ? | ? | ? | 0 | 0 | 0 | 1 | ? | ? | | |
| ? | ? | ? | ? | ? | 0 | 0 | 0 | 2 | ? | ? | | |
| ? | ? | ? | ? | ? | 1 | 1 | 2 | 2 | ? | ? | | |
| ? | ? | ? | ? | ? | C | M | 2 | M | 4 | M | | |
| ? | ? | ? | ? | ? | 5 | 5 | 4 | M | 2 | | | |
| ? | ? | ? | ? | ? | M | M | M | 2 | 1 | | | |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 | | | |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M | | | |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 | | | |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 | | | |
| | | | | | | | | | | next | | |

(o)

| | | | | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|------|---|---|
| Minesweeper | | | | | | | | | | — | □ | × |
| ? | ? | ? | C | 0 | 0 | 0 | 1 | ? | ? | | | |
| ? | ? | ? | C | 0 | 0 | 0 | 2 | ? | ? | | | |
| ? | ? | ? | ? | 1 | 1 | 2 | 2 | ? | ? | | | |
| ? | ? | ? | ? | 2 | M | 2 | M | 4 | M | | | |
| ? | ? | ? | ? | ? | 5 | 5 | 4 | M | 2 | | | |
| ? | ? | ? | ? | ? | M | M | M | 2 | 1 | | | |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 | | | |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M | | | |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 | | | |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 | | | |
| | | | | | | | | | | next | | |

(p)

| | | | | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|------|---|---|
| Minesweeper | | | | | | | | | | — | □ | × |
| ? | ? | ? | ? | 1 | 0 | 0 | 0 | 1 | ? | ? | | |
| ? | ? | ? | ? | 1 | 0 | 0 | 0 | 2 | ? | ? | | |
| ? | ? | ? | C | 1 | 1 | 2 | 2 | ? | ? | | | |
| ? | ? | ? | ? | 2 | M | 2 | M | 4 | M | | | |
| ? | ? | ? | ? | ? | 5 | 5 | 4 | M | 2 | | | |
| ? | ? | ? | ? | ? | M | M | M | 2 | 1 | | | |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 | | | |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M | | | |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 | | | |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 | | | |
| | | | | | | | | | | next | | |

(q)

| | | | | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|------|---|---|
| Minesweeper | | | | | | | | | | — | □ | × |
| ? | ? | ? | ? | 1 | 0 | 0 | 0 | 1 | ? | ? | | |
| ? | ? | ? | ? | 1 | 0 | 0 | 0 | 2 | ? | ? | | |
| ? | ? | ? | ? | 0 | 1 | 1 | 2 | 2 | ? | ? | | |
| ? | ? | ? | C | 2 | M | 2 | M | 4 | M | | | |
| ? | ? | ? | ? | ? | 5 | 5 | 4 | M | 2 | | | |
| ? | ? | ? | ? | ? | M | M | M | 2 | 1 | | | |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 | | | |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M | | | |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 | | | |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 | | | |
| | | | | | | | | | | next | | |

(r)

| | | | | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|------|---|---|
| Minesweeper | | | | | | | | | | — | □ | × |
| ? | ? | ? | ? | 1 | 0 | 0 | 0 | 1 | ? | ? | | |
| ? | ? | ? | ? | 1 | 0 | 0 | 0 | 2 | ? | ? | | |
| ? | ? | ? | ? | 0 | 1 | 1 | 2 | 2 | ? | ? | | |
| ? | ? | ? | ? | 1 | 2 | M | 2 | M | 4 | M | | |
| ? | ? | ? | ? | M | 5 | 5 | 4 | M | 2 | | | |
| ? | ? | ? | ? | M | M | M | M | 2 | 1 | | | |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 | | | |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M | | | |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 | | | |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 | | | |
| | | | | | | | | | | next | | |

(s)

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|-------------|---|---|---|---|---|---|---|---|---|------|---|---|
| Minesweeper | | | | | | | | | | — | □ | × |
| ? | ? | ? | ? | 1 | 0 | 0 | 0 | 1 | ? | ? | | |
| ? | ? | ? | ? | 1 | 0 | 0 | 0 | 2 | ? | ? | | |
| ? | ? | ? | ? | 0 | 1 | 1 | 2 | 2 | ? | ? | | |
| ? | ? | ? | ? | 1 | 2 | M | 2 | M | 4 | M | | |
| ? | ? | ? | ? | M | 5 | 5 | 4 | M | 2 | | | |
| ? | ? | ? | C | M | M | M | M | 2 | 1 | | | |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 | | | |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M | | | |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 | | | |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 | | | |
| | | | | | | | | | | next | | |

(t)

| | | | | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|------|---|---|
| Minesweeper | | | | | | | | | | — | □ | × |
| ? | ? | ? | ? | 1 | 0 | 0 | 0 | 1 | ? | ? | | |
| ? | ? | ? | ? | 1 | 0 | 0 | 0 | 2 | ? | ? | | |
| ? | ? | ? | ? | 0 | 1 | 1 | 2 | 2 | ? | ? | | |
| ? | ? | ? | ? | 1 | 2 | M | 2 | M | 4 | M | | |
| ? | ? | ? | C | M | 5 | 5 | 4 | M | 2 | | | |
| ? | ? | ? | 4 | M | M | M | M | 2 | 1 | | | |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 | | | |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M | | | |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 | | | |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 | | | |
| | | | | | | | | | | next | | |

(u)

| | | | | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|------|---|---|
| Minesweeper | | | | | | | | | | — | □ | × |
| ? | ? | ? | ? | 1 | 0 | 0 | 0 | 1 | ? | ? | | |
| ? | ? | C | 1 | 0 | 0 | 0 | 2 | ? | ? | | | |
| ? | ? | C | 0 | 1 | 1 | 2 | 2 | ? | ? | | | |
| ? | ? | C | 1 | 2 | M | 2 | M | 4 | M | | | |
| ? | ? | ? | 2 | M | 5 | 5 | 4 | M | 2 | | | |
| ? | ? | ? | 4 | M | M | M | M | 2 | 1 | | | |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 | | | |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M | | | |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 | | | |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 | | | |
| | | | | | | | | | | next | | |

(v)

| | | | | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|------|---|---|
| Minesweeper | | | | | | | | | | — | □ | × |
| ? | ? | ? | ? | 1 | 0 | 0 | 0 | 1 | ? | ? | | |
| ? | ? | ? | 2 | 1 | 0 | 0 | 0 | 2 | ? | ? | | |
| ? | ? | ? | 1 | 0 | 1 | 1 | 2 | 2 | ? | ? | | |
| ? | ? | ? | 0 | 1 | 2 | M | 2 | M | 4 | M | | |
| ? | ? | C | 2 | M | 5 | 5 | 4 | M | 2 | | | |
| ? | ? | ? | 4 | M | M | M | M | 2 | 1 | | | |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 | | | |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M | | | |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 | | | |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 | | | |
| | | | | | | | | | | next | | |

(w)

| | | | | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|------|---|---|
| Minesweeper | | | | | | | | | | — | □ | × |
| ? | ? | ? | ? | 1 | 0 | 0 | 0 | 1 | ? | ? | | |
| ? | ? | ? | ? | 2 | 1 | 0 | 0 | 0 | 2 | ? | ? | |
| ? | ? | ? | ? | 1 | 0 | 1 | 1 | 2 | 2 | ? | ? | |
| ? | ? | ? | ? | 0 | 1 | 2 | M | 2 | M | 4 | M | |
| ? | ? | ? | ? | 0 | 2 | M | 5 | 5 | 4 | M | 2 | |
| ? | ? | C | 4 | M | M | M | M | 2 | 1 | | | |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 | | | |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M | | | |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 | | | |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 | | | |
| | | | | | | | | | | next | | |

(x)

Figure 6: *Continued...*

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|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| — □ × | | | | | | | | | |
| ? | ? | M | 1 | 0 | 0 | 0 | 1 | ? | ? |
| ? | ? | 2 | 1 | 0 | 0 | 0 | 2 | ? | ? |
| ? | ? | 1 | 0 | 1 | 1 | 2 | 2 | ? | ? |
| ? | ? | 0 | 1 | 2 | M | 2 | M | 4 | M |
| ? | ? | 0 | 2 | M | 5 | 5 | 4 | M | 2 |
| ? | ? | 3 | 4 | M | M | M | M | 2 | 1 |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(a)

| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| — □ × | | | | | | | | | |
| ? | ? | M | 1 | 0 | 0 | 0 | 1 | ? | ? |
| ? | ? | 2 | 1 | 0 | 0 | 0 | 2 | ? | ? |
| ? | C | 1 | 0 | 1 | 1 | 2 | 2 | ? | ? |
| ? | C | 0 | 1 | 2 | M | 2 | M | 4 | M |
| ? | C | 0 | 2 | M | 5 | 5 | 4 | M | 2 |
| ? | ? | 3 | 4 | M | M | M | M | 2 | 1 |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(b)

| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| — □ × | | | | | | | | | |
| ? | ? | M | 1 | 0 | 0 | 0 | 1 | ? | ? |
| ? | ? | 2 | 1 | 0 | 0 | 0 | 2 | ? | ? |
| ? | 1 | 1 | 0 | 1 | 1 | 2 | 2 | ? | ? |
| ? | 0 | 0 | 1 | 2 | M | 2 | M | 4 | M |
| ? | 1 | 0 | 2 | M | 5 | 5 | 4 | M | 2 |
| ? | C | 3 | 4 | M | M | M | M | 2 | 1 |
| ? | ? | ? | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(c)

| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| — □ × | | | | | | | | | |
| ? | ? | M | 1 | 0 | 0 | 0 | 1 | ? | ? |
| ? | ? | 2 | 1 | 0 | 0 | 0 | 2 | ? | ? |
| ? | 1 | 1 | 0 | 1 | 1 | 2 | 2 | ? | ? |
| ? | 0 | 0 | 1 | 2 | M | 2 | M | 4 | M |
| ? | 1 | 0 | 2 | M | 5 | 5 | 4 | M | 2 |
| ? | 3 | 3 | 4 | M | M | M | M | 2 | 1 |
| ? | M | M | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(d)

| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| — □ × | | | | | | | | | |
| ? | ? | M | 1 | 0 | 0 | 0 | 1 | ? | ? |
| ? | ? | 2 | 1 | 0 | 0 | 0 | 2 | ? | ? |
| ? | 1 | 1 | 0 | 1 | 1 | 2 | 2 | ? | ? |
| ? | 0 | 0 | 1 | 2 | M | 2 | M | 4 | M |
| ? | 1 | 0 | 2 | M | 5 | 5 | 4 | M | 2 |
| ? | 3 | 3 | 4 | M | M | M | M | 2 | 1 |
| ? | M | M | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | C | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(e)

| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| — □ × | | | | | | | | | |
| ? | ? | M | 1 | 0 | 0 | 0 | 1 | ? | ? |
| ? | M | 2 | 1 | 0 | 0 | 0 | 2 | ? | ? |
| ? | 1 | 1 | 0 | 1 | 1 | 2 | 2 | ? | ? |
| ? | 0 | 0 | 1 | 2 | M | 2 | M | 4 | M |
| ? | 1 | 0 | 2 | M | 5 | 5 | 4 | M | 2 |
| ? | 3 | 3 | 4 | M | M | M | M | 2 | 1 |
| ? | M | M | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(f)

| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| — □ × | | | | | | | | | |
| ? | ? | M | 1 | 0 | 0 | 0 | 1 | ? | ? |
| ? | M | 2 | 1 | 0 | 0 | 0 | 2 | ? | ? |
| C | 1 | 1 | 0 | 1 | 1 | 2 | 2 | ? | ? |
| C | 0 | 0 | 1 | 2 | M | 2 | M | 4 | M |
| C | 1 | 0 | 2 | M | 5 | 5 | 4 | M | 2 |
| ? | 3 | 3 | 4 | M | M | M | M | 2 | 1 |
| ? | M | M | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(g)

| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| — □ × | | | | | | | | | |
| ? | ? | M | 1 | 0 | 0 | 0 | 1 | ? | ? |
| ? | M | 2 | 1 | 0 | 0 | 0 | 2 | ? | ? |
| 1 | 1 | 1 | 0 | 1 | 1 | 2 | 2 | ? | ? |
| 0 | 0 | 0 | 1 | 2 | M | 2 | M | 4 | M |
| 1 | 1 | 0 | 2 | M | 5 | 5 | 4 | M | 2 |
| M | 3 | 3 | 4 | M | M | M | M | 2 | 1 |
| ? | M | M | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(h)

| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| — □ × | | | | | | | | | |
| ? | ? | M | 1 | 0 | 0 | 0 | 1 | ? | ? |
| ? | M | 2 | 1 | 0 | 0 | 0 | 2 | ? | ? |
| 1 | 1 | 1 | 0 | 1 | 1 | 2 | 2 | ? | ? |
| 0 | 0 | 0 | 1 | 2 | M | 2 | M | 4 | M |
| 1 | 1 | 0 | 2 | M | 5 | 5 | 4 | M | 2 |
| M | 3 | 3 | 4 | M | M | M | M | 2 | 1 |
| C | M | M | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(i)

| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| — □ × | | | | | | | | | |
| ? | ? | M | 1 | 0 | 0 | 0 | 1 | ? | ? |
| ? | M | 2 | 1 | 0 | 0 | 0 | 2 | ? | ? |
| 1 | 1 | 1 | 0 | 1 | 1 | 2 | 2 | ? | ? |
| 0 | 0 | 0 | 1 | 2 | M | 2 | M | 4 | M |
| 1 | 1 | 0 | 2 | M | 5 | 5 | 4 | M | 2 |
| M | 3 | 3 | 4 | M | M | M | M | 2 | 1 |
| 4 | M | M | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(j)

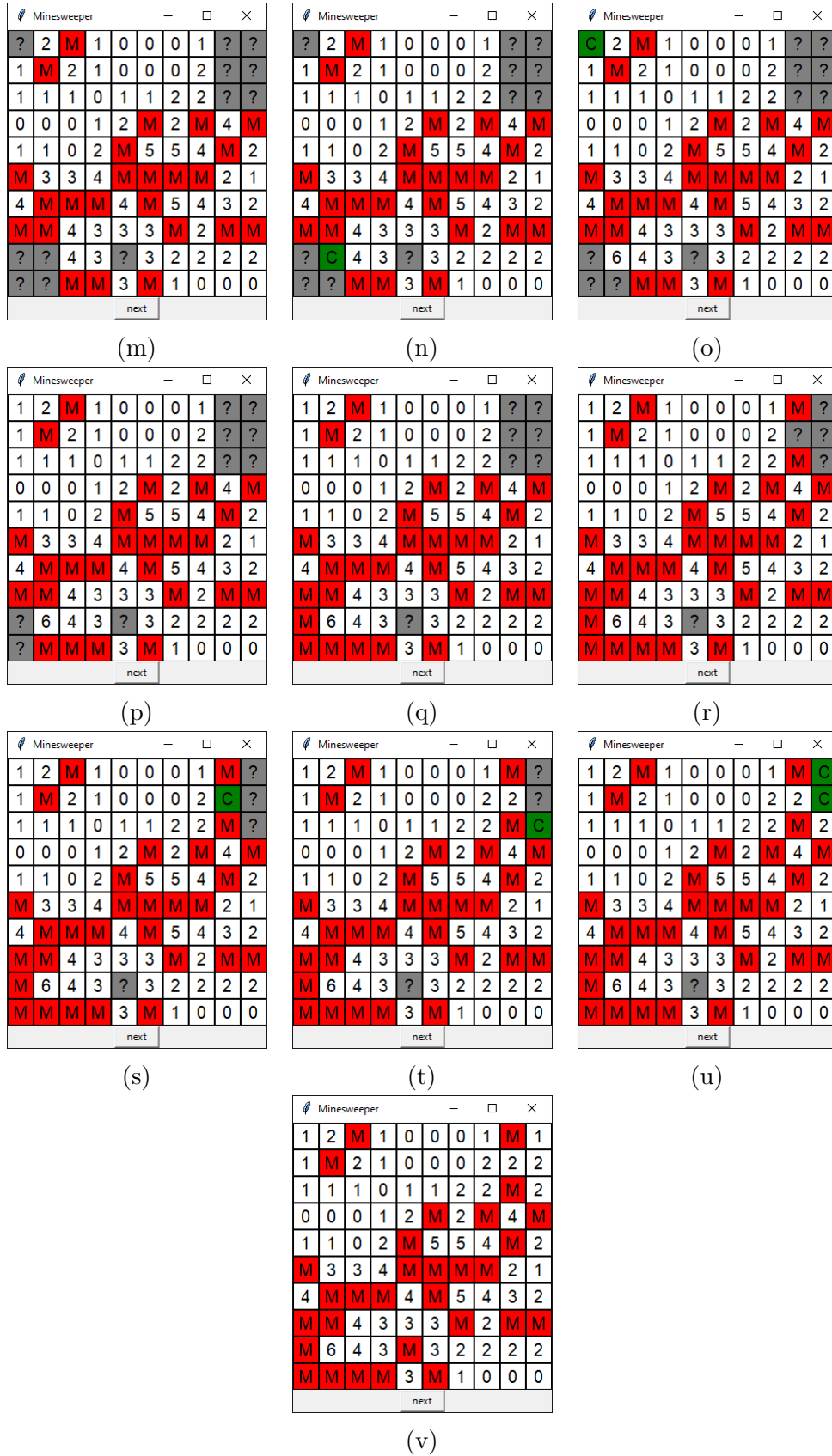
| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| — □ × | | | | | | | | | |
| ? | C | M | 1 | 0 | 0 | 0 | 1 | ? | ? |
| ? | M | 2 | 1 | 0 | 0 | 0 | 2 | ? | ? |
| 1 | 1 | 1 | 0 | 1 | 1 | 2 | 2 | ? | ? |
| 0 | 0 | 0 | 1 | 2 | M | 2 | M | 4 | M |
| 1 | 1 | 0 | 2 | M | 5 | 5 | 4 | M | 2 |
| M | 3 | 3 | 4 | M | M | M | M | 2 | 1 |
| 4 | M | M | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(k)

| | | | | | | | | | |
|-------------|---|---|---|---|---|---|---|---|---|
| Minesweeper | | | | | | | | | |
| — □ × | | | | | | | | | |
| ? | 2 | M | 1 | 0 | 0 | 0 | 1 | ? | ? |
| C | M | 2 | 1 | 0 | 0 | 0 | 2 | ? | ? |
| 1 | 1 | 1 | 0 | 1 | 1 | 2 | 2 | ? | ? |
| 0 | 0 | 0 | 1 | 2 | M | 2 | M | 4 | M |
| 1 | 1 | 0 | 2 | M | 5 | 5 | 4 | M | 2 |
| M | 3 | 3 | 4 | M | M | M | M | 2 | 1 |
| 4 | M | M | M | 4 | M | 5 | 4 | 3 | 2 |
| ? | ? | ? | 3 | 3 | 3 | M | 2 | M | M |
| ? | ? | 4 | 3 | ? | 3 | 2 | 2 | 2 | 2 |
| ? | ? | ? | M | 3 | M | 1 | 0 | 0 | 0 |
| next | | | | | | | | | |

(l)

Figure 7: Continued...

Figure 7: Minimizing Risk Agent Visualization: **Grid:[10 x 10] Mines:[30]**

Minimum Cost Question Responses

The plot that is below (Figure: 8) is data for both the pure random decision agent from assignment 2, and the basic risk minimizing agent. The original basic agent's data is denoted as the yellow bar graph(s), while the minimizing risk agent is denoted as the blue bar graph(s). The graph was generated by calling the `iterateForComparison()` method in the `minimizing_risk_agent.py` file (*Line#: 583*). This method was passed a 10 x 10 grid, with fifty mines where for thirty games, the average risk was calculated for increasing mine densities. (*Mines increased by a factor of five*). These thirty / iterations produced Figure 8. When analyzing the results from Figure 8, one can see that for the most part the average risk was higher for the Original Agent, than that of the minimizing risk agent. In fact, with an increased mine density between the ranges of fifteen and fifty-five the previous statement holds true. Additionally, mine densities between seventy-five and ninety-five yielded the same result. This is due to the fact that the risk minimizing agent considers each hidden tile as either a mine or not a mine. Then using the implemented inferencing system, it calculates the maximum number of squares able to be solved for each of the hidden tiles and chooses the maximum. Hence, it was frequently figuring out information compared to the original agent. Additionally, if we wanted to quantify how frequently 'improved' decision making was necessary, then it would be around seventy-four percent of the time (*fourteen out of the total nineteen mine densities had the minimizing risk agent with a lower average risk.*)

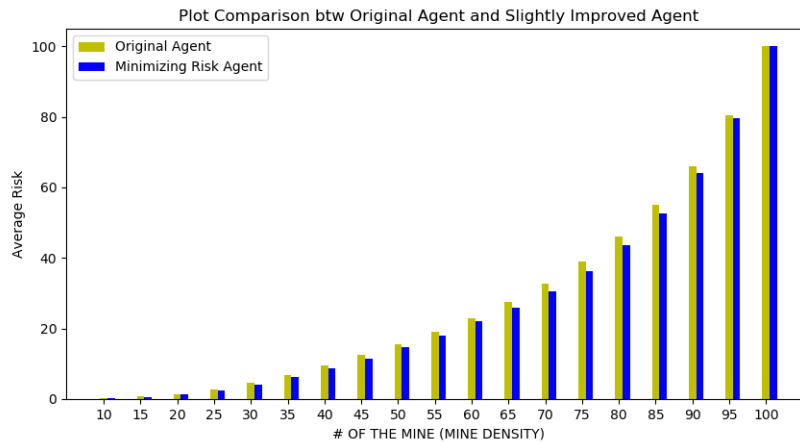
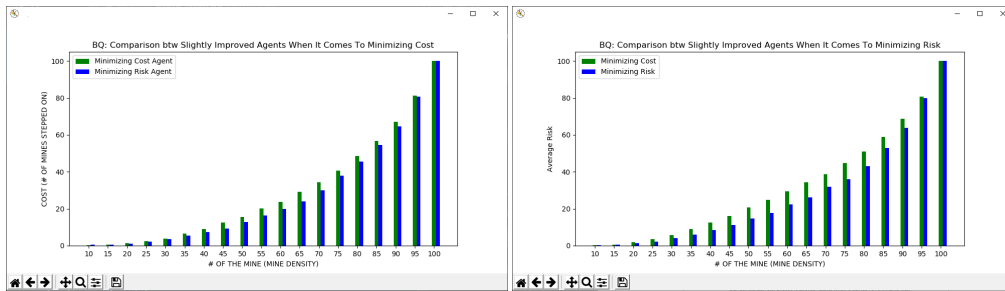


Figure 8: Mine Density vs. Average Risk

Bonus Answer

Now that we have pitted the two different improved agents (*Minimizing Cost* and *Minimizing Risk* agents), against the pure random decision agents, how do the two compare when compared to each other? In order to both answer and see how the risk minimizing agent compares to the minimizing cost agent, we gathered data for both of them, and put them to the test. To give more background, both agents were iterated one thousand times/ games on a 10 x 10 board, starting with 10 mines.

The first question one can ask is how both improved agents would perform when one wanted to test for minimizing cost? Well, after the one thousand iterations we got the following results



(a) Minimizing Cost Comparison

(b) Minimizing Risk Comparison

Figure 9: Minimizing Cost Agent vs. Minimizing Risk Agent