

## QTM 200 - Applied Linear Regression

### Exam One Review

**Disclaimer:** The following questions are meant to serve as preparation, and are examples of what may appear on the first exam. Do not rely on this content as your sole means of preparation, this is meant to guide your studying.

## 1 Terms

Be able to define these terms and describe why they're important:

- Describing data:
  - Parameter vs. statistic
  - Data
  - Observations
  - Population
  - Sample
  - Variable
  - Qualitative/quantitative data
  - Nominal/ordinal
  - Granularity (continuous/discrete)
  - Skew
  - Outliers
- Measures of Central Tendency and Dispersion:
  - Mean
  - Median
  - Variance
  - Standard deviation
- Distributions
  - Normal Distribution
  - T Distribution
  - Degrees of Freedom
  - Standard deviation/variance
  - Sampling distribution
  - Central Limit Theorem
  - Standard error
- Estimation
  - Point estimate
  - Confidence interval
  - Confidence level
  - Bias
  - Efficiency

- Hypothesis testing
  - Hypothesis
  - Null/alternative hypotheses
  - Test statistic
  - P-value
  - Significance level ( $\alpha$ -level)
  - Type I & Type II error
- Regression
  - Linear regression
  - Regression analysis
  - Y-intercept
  - Slope
  - Least squares line
  - Sum of squared error
  - Residual sum of squares
  - Total sum of squares
  - Correlation coefficient ( $r/R$ )

## 2 Calculate/execute these concepts:

- Describing Data:
  - Classify variables as nominal/ordinal
  - Classify variables as continuous/discrete
- Measures of position:
  - Find hat values ( $h_i$ ) and outliers
  - Identify the skew of a data set
- Measures of central tendency:
  - Mean
  - Median
  - Mode
- Measures of dispersion:
  - Variance
  - Standard deviation
  - Standard error
- Distributions and probability:
  - Define a sampling distribution of a mean
  - Calculate a Z-score
  - Use the Z-score to find p-value

- Regression
  - Interpret y-intercept and slope for a linear function
  - Write a prediction equation
  - Calculate Sum of Squared Errors
  - Calculate Total Sum of Squares
  - Interpret a scatter plot
  - Construct a confidence interval around  $\beta$
  - Conduct a hypothesis test for  $\beta$
  - Calculate standard error for  $\beta$
  - Calculate  $S_x$  and  $S_y$
  - Calculate  $r$  and interpret its meaning
  - Calculate  $r^2/R^2$
  - Interpret a regression analysis table
  - Interpret regression coefficients
  - Interpret the significance of a multiple regression using the F-distribution
  - Interpret a regression line with an interaction term
  - Interpret residuals plotted together
  - Transform variables

### 3 Practice problem set:

- Identify each variable as nominal/ordinal/interval and discrete/continuous:
  1. Type of car driven
  2. General health (poor, reasonably good, excellent)
  3. College tuition
  4. Number of political parties in a country
  5. Religious affiliation
  6. Distance between home and work
- The following table contains the GDP per capita (in thousands of international dollars) for four European countries.

Belgium	Germany	France	Luxembourg
38	38	35	90

- Find the variance.
  - Find the standard deviation.
  - Would you say that one of these observations is an outlier?
- The Freshman Fifteen is an expression that commonly refers to an amount (somewhat arbitrarily set at fifteen pounds) of weight often gained during a student's first year at college. You decide to test whether this expression holds true for Washington University in St. Louis. You randomly select 16 sophomores and gather data on how much weight (in pounds) they gained the previous year. The mean of your data is 14.5 lbs. and the sample standard deviation is 0.8 lbs.

1. Identify the population for this study.
  2. Describe the sample distribution for this study.
  3. Describe the sampling distribution for this study as precisely as possible.
  4. Calculate the point estimate and a 95% confidence interval for the population mean. Explain what your confidence interval means.
- Apple claimed that iPhone 5 is “the biggest thing to happen to iPhone since the iPhone.” Among other improvements, the iPhone 5 claimed improved battery life over the old versions. For example, the standby time has been improved to 225 hours (a 25-hour improvement over iPhone 4S). To test this claim, you collect a sample of battery longevity from 100 randomly selected owners of the iPhone 5. Among these 100 owners, you find that the battery life in the new iPhone 5 is 217 hours with a standard deviation of 40 hours. Test the research hypothesis that the batteries in the new iPhone 5 differ from the 225 hours claimed by Apple. Use a 0.05 level of significance.
  - Imagine you are interested in the different patterns of support for the Spanish government among citizens of Catalan population. You decide to conduct a survey asking people “Do you have confidence in the national government?” Possible answers include Yes or No. You were able to poll 243 Catalans. Of these 243 respondents, 86 said, “Yes.”
    1. Provide a point estimate for the percent of Catalans that have confidence in the government.
    2. Identify the sampling distribution of this study. Be precise.
    3. Construct a 92% confidence interval of the percent of Catalans that have confidence in the government.
    4. Test the theory that less than 40% of Greeks support the government using a 0.05 significance level.
  - Suppose a random sample is taken of 200 rat-hunting dogs in New York City. The mean number of rats killed by a dog is 19, with a standard deviation of 2. Construct and interpret a 92% confidence interval for the mean number of rats killed.