

# Homework Assignment #1

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ex=1 a) Please see provided python code.

b)  $V_L$  is minimum ~~at~~ when  $\frac{\partial V}{\partial r} = 0$  (ignoring the "ij" for the moment)

$$V(r) = 4\epsilon \left[ \left( \frac{\sigma}{r} \right)^{12} - \left( \frac{\sigma}{r} \right)^6 \right]$$

$$\frac{\partial V}{\partial r} = 4\epsilon \left[ \sigma^{12} \frac{\partial}{\partial r} \left( \frac{1}{r^{12}} \right) - \sigma^6 \frac{\partial}{\partial r} \left( \frac{1}{r^6} \right) \right] = 0$$

$$= 4\epsilon \left[ \sigma^{12} \cdot (-12) \cdot \frac{1}{r^{13}} - \sigma^6 \cdot (-6) \cdot \frac{1}{r^7} \right] = 0$$

$$0 = 4\epsilon \left[ -\frac{12\sigma^{12}}{r^{13}} + \frac{6\sigma^6}{r^7} \right] \Rightarrow \text{oxygen-oxygen}$$

$$\sigma = 0.295 \text{ nm} = 0.295 \times 10^{-9} \text{ m}$$

$$\epsilon = 61.6 \times k_B$$

plug them in

$$\rightarrow 1.38 \times 10^{-23} \frac{\text{m}^2 \text{kg}}{\text{s}^2 \text{K}}$$

$$\therefore r = 3.31 \times 10^{-10} \text{ m} = \underline{\underline{3.31 \text{ Angstrom}}}$$

$$F = -\frac{\partial V}{\partial r} = 4\epsilon \left[ \frac{12\sigma^{12}}{r^{13}} - \frac{6\sigma^6}{r^7} \right]$$

$$= 7.07885 \times 10^{-14} \text{ Newtons}$$

$$c) \sum_i^{2N-1} F_i(\vec{r}_1, \dots, \vec{r}_{2N-1}, \vec{v}_i) = \sum_i^{2N-1} m_i \frac{d^2 \vec{r}_i}{dt^2}$$

d) Please see provided python code.

$$e) 6 \cdot \binom{10^{23}}{2} \text{ operations}$$

$$10^{12} \text{ operations}$$

x time

1 second

→ Butinath

$$\underline{\underline{10^{23} \text{ particles}}}$$

$$= \frac{6 \times \binom{10^{23}}{2}}{10^{12}} \times \frac{1 \text{ min}}{60 \text{ sec}} \times \frac{1 \text{ h}}{60 \text{ min}} \times \frac{1 \text{ day}}{24 \text{ h}} = \underline{\underline{3.47 \times 10^{29} \text{ days}}}$$

$$\underline{\underline{10^4 \text{ particles}}}$$

$$= \frac{6 \times \binom{10^4}{2}}{10^{12}} \times \frac{1 \text{ min}}{60 \text{ sec}} \times \frac{1 \text{ h}}{60 \text{ min}} \times \frac{1 \text{ day}}{24 \text{ h}} = \underline{\underline{3.47 \times 10^{-9} \text{ days}}}$$

$$e_x = 2$$

a)  $\frac{d^2x}{dt^2} \Rightarrow x(t) = a \cos \omega t + b \sin \omega t \rightarrow$  general second-order differential solution

$$x(0) = a \cos \phi + b \sin \phi \xrightarrow{t=0} = a \cos \phi = a = x(0).$$

$$v(0) = \frac{dx(0)}{dt} = -a\omega \sin \omega t + b\omega \cos \omega t \xrightarrow{t=0} = -a\omega \sin \phi + b\omega \cos \phi$$

$$= b\omega \cos \phi \xrightarrow{t=0} = b\omega = v(0)$$

$$b = \frac{v(0)}{\omega}$$

Therefore,  $x(t) = x(0) \cos \omega t + \frac{v(0)}{\omega} \sin \omega t$

$$p(t) = m \cdot v(t) = m \cdot \left[ -x(0) \omega \sin(\omega t) + \frac{v(0)}{\omega} \cos(\omega t) \right]$$

$$= \frac{m \cdot v(0)}{\omega} \cos \omega t - \underline{\underline{m \cdot x(0) \omega \sin \omega t}}$$