

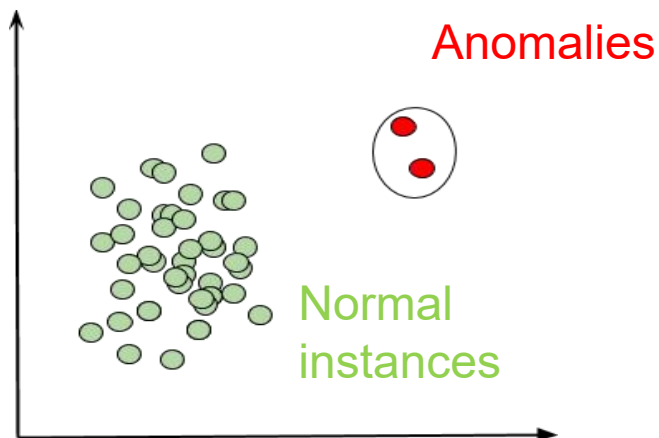
AnomalyGFM: Graph Foundation Model for Zero/Few-shot Anomaly Detection

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Background-Introduction to Anomalies and Graph Anomalies

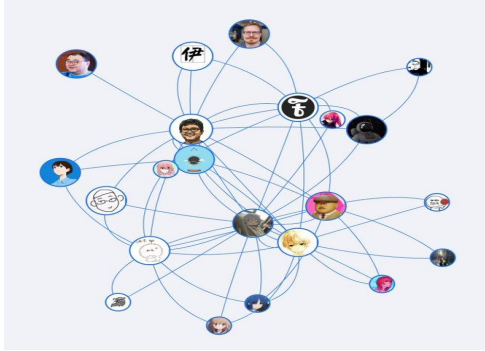
Anomalies (a.k.a., outliers, novelties): Instances that are significantly different from most of the data.

Graph Anomalies: Unexpected, irregular, or suspicious instance in graph-structured data that significantly different from most of the data.

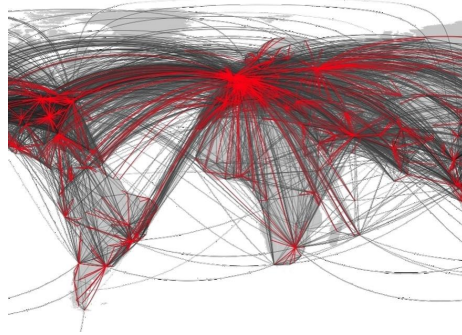


Background-Introduction to GAD

Social network



Bank transaction



Web client-server



Social spam

Financial fraud

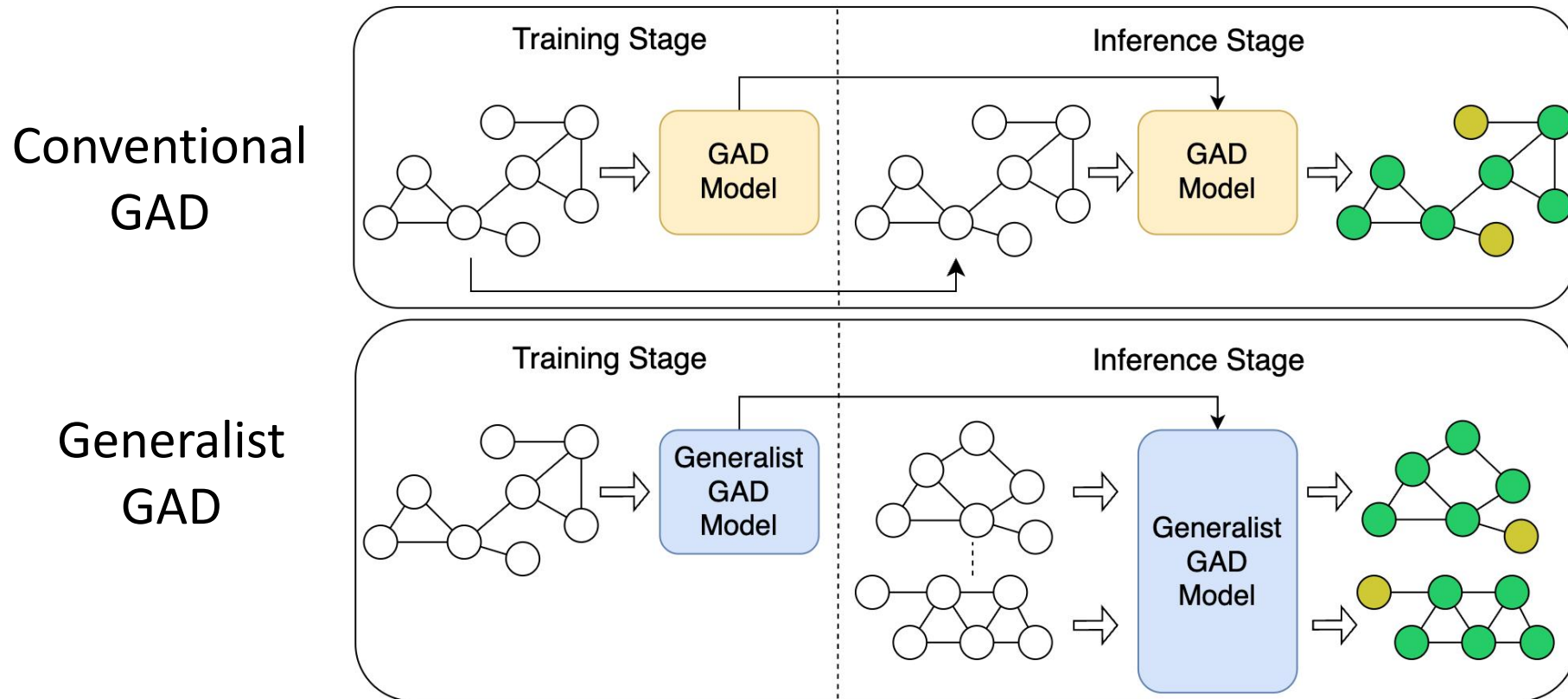
Network intrusion

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Graph Anomaly Detection (GAD), which aims to identify the rare observations in graphs.

Introduction to Generalist GAD

Generalist GAD: Pre-train a graph neural network designed to generalize across diverse graph domains and anomaly types.



Challenges of Generalist GAD

❖ Generalist Node Classification ❖ Generalist GAD

- **Feature Heterogeneity**
- **Domain Difference**
- **Fine Tuning Mechanism**



Challenges of General
Node Classification

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- **Abnormality/Normality Difference**
- **Generalized Scoring Measurement**

Motivation-Residual Feature

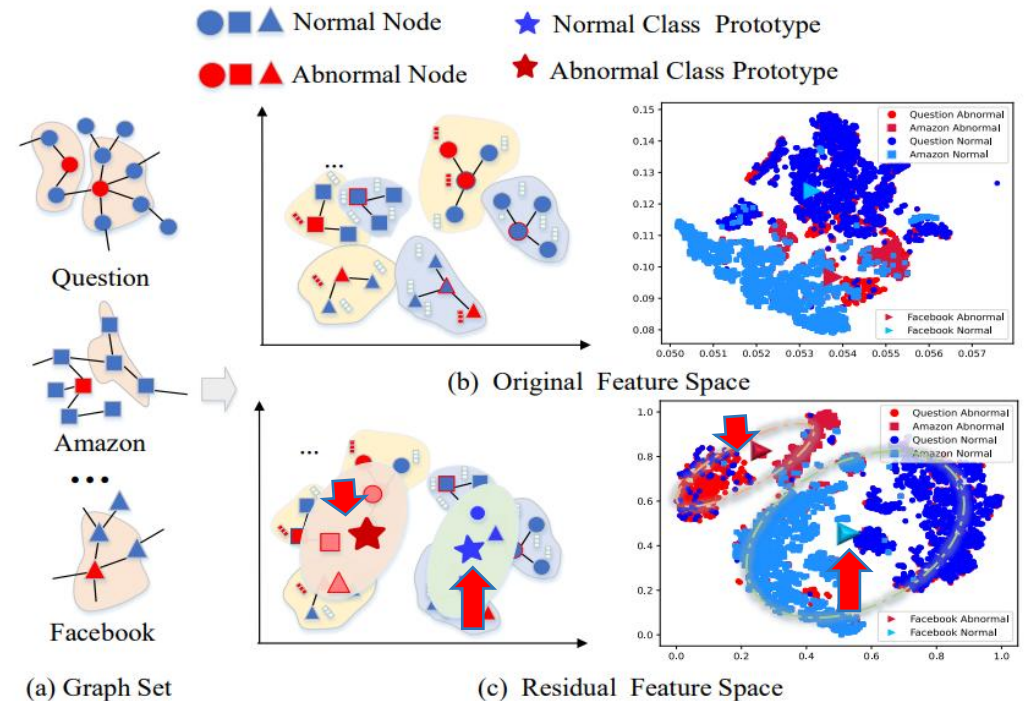
- ❑ The residual features essentially project the node information into a **unified feature** space where we can effectively measure the **abnormality** of nodes from different graphs in a **consistent way**.

- **Residual Feature**

$$\mathbf{r}_i = \mathbf{h}_i - \frac{1}{|\mathcal{N}(v_i)|} \sum_{v_j \in \mathcal{N}(v_i)} \mathbf{h}_j$$

- **Abnormality Measure**

$$s_i = \exp(\mathbf{r}_i^T \mathbf{p}_a) + \beta_{\exp}(-\mathbf{r}_i^T \mathbf{p}_n)$$



Preliminaries

Feature Unification

- Due to the feature dimension difference across the graphs, we need to align the node features/ attributes into a shared feature space

$$\mathbf{X}^{(i)} \in \mathbb{R}^{N^{(i)} \times d^{(i)}} \xrightarrow[\text{Projection}]{\text{Feature}}$$

GNN for Representation Learning

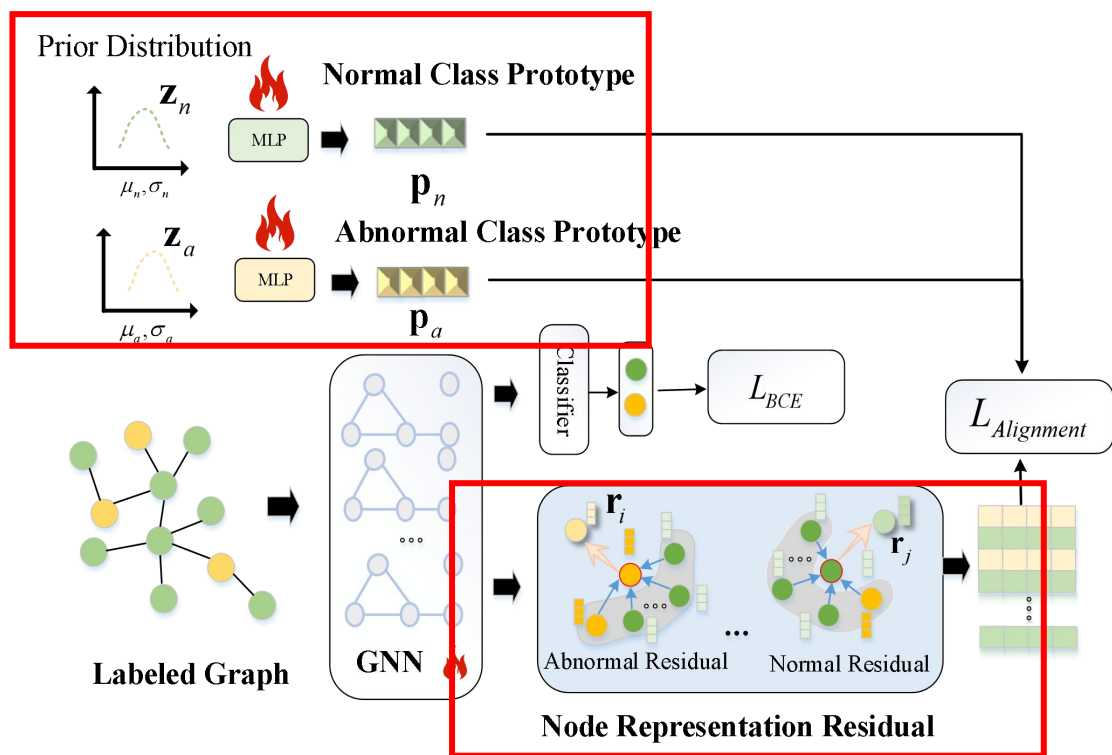
- We adopt a 2-layer GCN to model the graph due to its efficient and simple architecture.

$$\mathbf{H}^{(\ell)} = \text{GNN} \left(\mathbf{A}, \mathbf{H}^{(\ell-1)}; \mathbf{W}^{(\ell)} \right)$$

AnomalyGFM-Pre-training Loss

- Learn the **graph-agnostic, discriminative** prototypes for the normal and abnormal classes using alignment

data-independent, learnable class prototypes



(a) Pre-training

- Supervised Loss

$$L_{BCE} = \sum_{i=1}^{|\mathcal{V}|} y_i \log(p_i) + (1 - y_i) \log(1 - p_i)$$

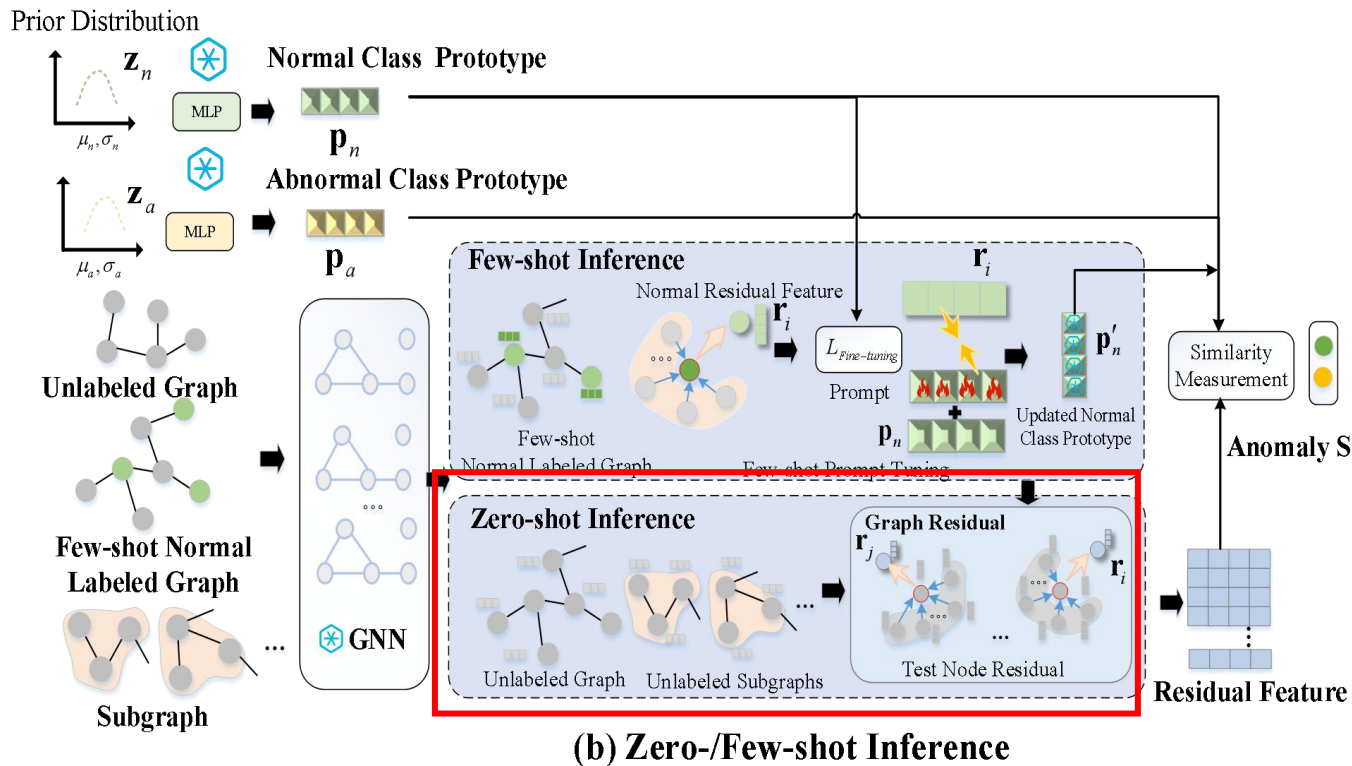
- Alignment Loss

$$L_{Alignment} = \sum_{i=1}^{|\mathcal{V}|} I_{y_i=0} \|\mathbf{r}_i - \mathbf{p}_n\|_2^2 + I_{y_i=1} \|\mathbf{r}_i - \mathbf{p}_a\|_2^2$$

$$L_{total} = L_{BCE} + \alpha L_{Alignment}$$

AnomalyGFM Zero-shot Inference

- During the inference, we use the similarity between node representation and prototypes of **normal** and **abnormal** class as the anomaly score.



- Zero-shot Inference

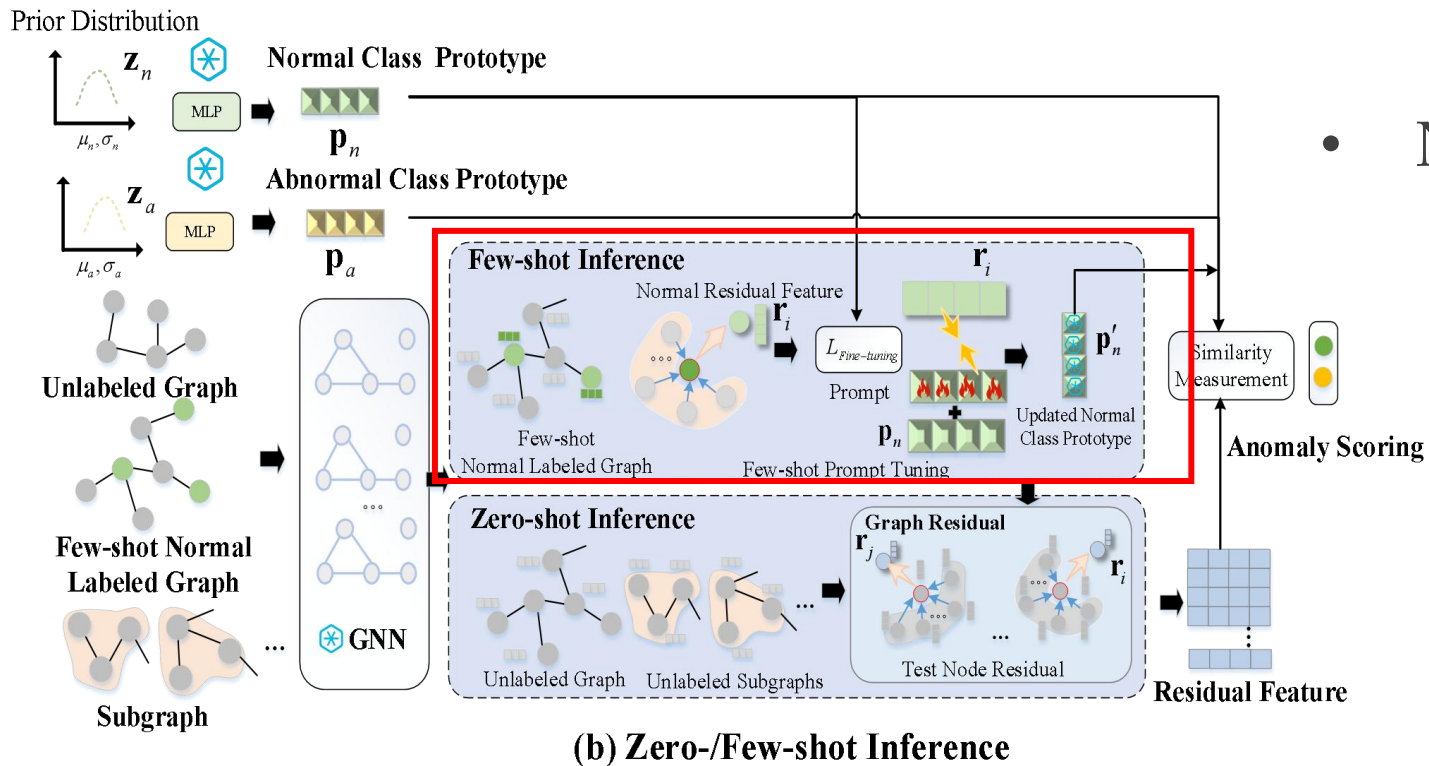
$$s_i = \exp(\mathbf{r}_i^T \mathbf{p}_a) + \beta_{\exp}(-\mathbf{r}_i^T \mathbf{p}_n)$$

- Few-shot Inference?

How to exploit some labeled normal nodes ?

AnomalyGFM Few-shot Inference

- A small **learnable prompt** and **adaptivation layer** were involved into the normal class prototype to **better align** it with the normal node representation residuals on the test graph during a prompt fine-tuning step



- Normal Prototype-based Fine-tuning

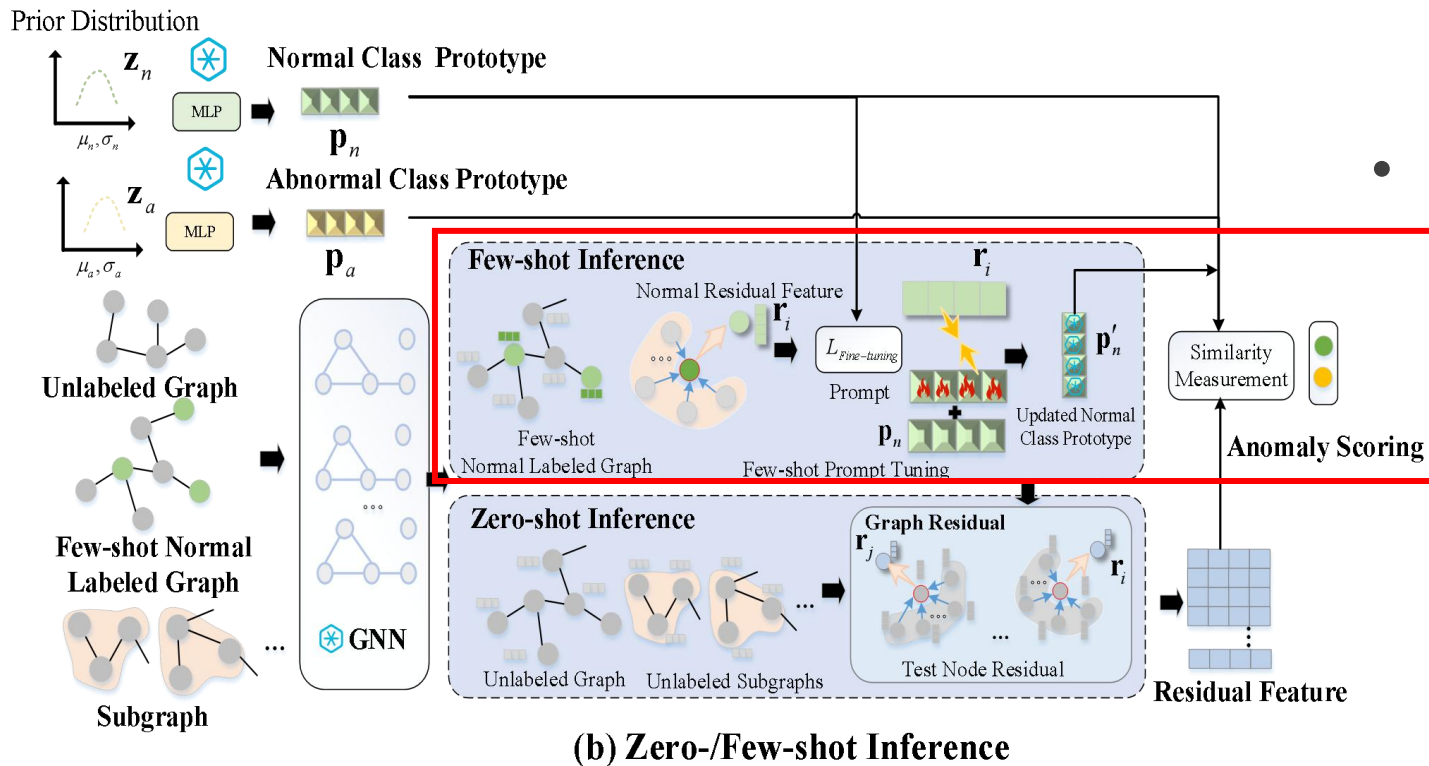
adaptation layer learnable prompt

$$\mathbf{p}'_n = \mathbf{p}_n - \boxed{g(\mathbf{p}_n; \phi)} + \boxed{\Psi_{\mathbf{p}_n}}$$

$$L_{pt} = \sum_{i=1}^{|v_i^{\text{Test}}|} \|\mathbf{r}_i - \mathbf{p}'_n\|_2^2$$

AnomalyGFM Few-shot Inference

- During the inference, we use the similarity between node representation and **abnormal** class and refined prototypes of **normal** as the anomaly score.



- Few-shot Inference Refined prototype

$$s_i = \exp(\mathbf{r}_i^T \mathbf{p}_a) + \beta \exp(-\mathbf{r}_i^T \mathbf{p}'_n)$$

Datasets and Competing Methods

Dataset	Domain	#Nodes	#Edges	#Feat.	Ano.	Sim.
Facebook	Social Networks	1,081	55,104	576	27(2.49%)	0.690
Reddit	Social Networks	10,984	168,016	64	366(3.33%)	0.997
Amazon	Co-review	10,244	175,608	25	693(6.66%)	0.645
Disney	Co-purchase	124	335	28	6(4.8%)	0.804
Amazon-all	Co-review	11,944	4,398,392	25	821(6.87%)	0.645
YelpChi-all	Co-review	45,941	3,846,979	32	6,674(14.52%)	0.905
Tolokers	Work Collaboration	11,758	519,000	10	2,566(21.8%)	0.814
Question	Social Networks	48,921	153,540	301	1,460(2.98%)	0.679
Elliptic	Bitcoin Transaction	46,564	73,248	93	4,545 (9.8%)	0.356
T-Finance	Transaction Record	39,357	21,222,543	10	1,803(4.6%)	0.107
T-Social	Social Friendship	5,781,065	73,105,508	10	174,280(3.0%)	0.307

- ❑ **Unsupervised methods:**
AnomalyDAE, CoLA , TAM , and GADAM;
- ❑ **Supervised methods:**
GCN , GAT , BWGNN, GHRN, and XGBGraph;
- ❑ **General GFM methods:**
GraphPrompt for general graph tasks, and the one for zero-shot GAD UNPrompt

Main Results — Zero-shot Inference

- AnomalyGFM performs inference based on two discriminative graph-agonistic prototypes distilled from the node residual feature, supporting strong generalization across the datasets.

Metric	Method	Dataset									Avg.	p-value
		Reddit	Amazon	Disney	Aamzon-all	YelpChi-all	Tolokers	Question	Elliptic	T-Finance		
AUROC	Unsupervised Methods											
	AnomalyDAE (ICASSP'20)	0.5016	0.5818	0.4853	0.7228	0.5002	0.5948	0.4311	0.4197	0.2324	0.4966	0.007
	CoLA (TNNLS'21)	0.4623	0.4580	0.4696	0.4091	0.4879	0.4501	0.4945	0.5572	0.4889	0.4752	0.003
	TAM (NeurIPS'23)	0.5725	0.4720	0.4773	0.7543	0.4216	0.5351	0.5119	0.3282	0.2990	0.4857	0.003
	GADAM (ICLR'24)	0.4532	0.6646	0.4288	0.5959	0.4829	0.4832	0.5594	0.3922	0.1382	0.4664	0.007
	Supervised Methods											
	GCN (ICLR'17)	0.5645	0.5988	0.5000	0.7195	0.5486	0.5319	0.5161	0.7640	0.2345	0.5531	0.039
	GAT (ICLR'18)	0.5000	0.4981	0.5175	0.5005	0.4802	0.5030	0.4577	0.6588	0.5072	0.5136	0.007
	BWGNN (ICML'22)	0.5208	0.4769	0.6073	0.3648	0.5282	0.4877	0.4404	0.5843	0.5457	0.5062	0.003
	GHRN (WebConf'23)	0.5253	0.4560	0.5336	0.3382	0.5125	0.4860	0.4535	0.5400	0.5324	0.4863	0.003
	XGBGraph (NeurIPS'23)	0.4601	0.4179	0.6692	0.7950	0.4945	0.5462	0.5095	0.4274	0.3402	0.5177	0.003
	Generalist Methods											
	GraphPrompt (WebConf'23)	0.4677	0.4904	0.5192	0.3215	0.4976	0.4779	0.4204	0.3221	0.5405	0.4508	0.003
	UNPrompt (Arxiv'24)	0.5337	0.7525	0.6412	0.7962	0.5558	0.6853	0.4757	0.5901	0.2318	0.5847	0.074
	AnomalyGFM	0.5974	0.8417	0.6751	0.9032	0.5791	0.5843	0.5280	0.6195	0.5614	0.6544	/
AUPRC	Unsupervised Methods											
	AnomalyDAE (ICASSP'20)	0.0327	0.0833	0.0566	0.1921	0.1484	0.1876	0.0241	0.0798	0.0274	0.0924	0.003
	CoLA (TNNLS'21)	0.0391	0.0669	0.0701	0.0861	0.1466	0.0848	0.0292	0.0998	0.0430	0.0739	0.007
	TAM (NeurIPS'23)	0.0413	0.0666	0.0628	0.1736	0.1240	0.0970	0.0307	0.0697	0.0332	0.0776	0.007
	GADAM (ICLR'24)	0.0293	0.1562	0.0651	0.1595	0.1371	0.1001	0.0395	0.0733	0.0261	0.0873	0.003
	Supervised Methods											
	GCN (ICLR'17)	0.0439	0.0891	0.0484	0.1536	0.1735	0.1060	0.0387	0.1963	0.0274	0.0974	0.074
	GAT (ICLR'18)	0.0329	0.0688	0.0530	0.0696	0.1400	0.0822	0.0259	0.1366	0.0463	0.0728	0.003
	BWGNN (ICML'22)	0.0389	0.0652	0.0624	0.0586	0.1605	0.1030	0.0257	0.1158	0.0479	0.0753	0.007
	GHRN (WebConf'23)	0.0407	0.0633	0.0519	0.0569	0.1505	0.0957	0.0259	0.1148	0.0457	0.0717	0.007
	XGBGraph (NeurIPS'23)	0.0330	0.0536	0.1215	0.2307	0.1449	0.1256	0.0306	0.0816	0.0754	0.0996	0.027
	Generalist Methods											
	GraphPrompt (WebConf'23)	0.0334	0.0661	0.0610	0.0666	0.1542	0.2070	0.0266	0.0664	0.0492	0.0811	0.003
	UNPrompt (Arxiv'24)	0.0351	0.1602	0.1236	0.2430	0.1810	0.2219	0.0348	0.1278	0.0279	0.1283	0.003
	AnomalyGFM	0.0387	0.5790	0.1242	0.6820	0.1819	0.2749	0.0397	0.1371	0.0593	0.2352	/

Main Results — Few-shot Inference

❑ Few shot methods:
GPPT, GraphPrompt, and
ARC

❑ AnomalyGFM achieves
better sample-efficiency
tuning due to the learning
of class-level prototypes
that are agnostic to
different domains of
graphs

Metric	Setting	Method	Dataset										Avg.	p-value
			Reddit	Amazon	Disney	Aamzon-all	YelpChi-all	Tolokers	Question	Elliptic	T-Finance			
AUROC	1-shot	GPPT (KDD'22)	<u>0.5000</u>	<u>0.5303</u>	<u>0.4997</u>	<u>0.5010</u>	<u>0.5000</u>	0.5061	0.4921	<u>0.6162</u>	0.3647	<u>0.5011</u>	0.003	
		GraphPrompt (WebConf'23)	0.4216	0.4882	0.4223	0.2631	0.4811	<u>0.5328</u>	0.4086	0.6001	<u>0.4000</u>	0.4464	0.004	
		ARC (NeurIPS'24)	0.4899	0.4571	0.3578	0.4570	<u>0.4910</u>	0.4667	0.5865	0.2904	0.2484	0.4272	0.008	
		AnomalyGFM	0.5922	0.8531	0.6649	0.8972	0.5872	0.5898	<u>0.5303</u>	0.6199	0.5916	0.6584	/	
	5-shot	GPPT (KDD'22)	<u>0.5000</u>	<u>0.5098</u>	0.5000	<u>0.5051</u>	0.5000	0.5181	0.4959	0.5736	0.2609	0.4848	0.003	
		GraphPrompt (WebConf'23)	0.4406	0.4900	<u>0.6497</u>	0.4726	<u>0.5359</u>	<u>0.5381</u>	0.4069	<u>0.6012</u>	<u>0.4069</u>	<u>0.5046</u>	0.003	
		ARC (NeurIPS'24)	<u>0.4720</u>	0.4458	0.4435	0.4473	0.5112	0.4746	0.5906	0.2714	0.2168	0.4303	0.007	
		AnomalyGFM	0.6023	0.8600	0.6613	0.9011	0.5951	0.6095	<u>0.5426</u>	0.6119	0.6248	0.6676	/	
	10-shot	GPPT (KDD'22)	<u>0.5000</u>	<u>0.5087</u>	0.4769	0.5023	0.5000	0.4971	0.5047	0.4212	0.5539	0.4961	0.003	
		GraphPrompt (WebConf'23)	0.4321	0.4906	<u>0.6314</u>	<u>0.7167</u>	<u>0.5367</u>	<u>0.5329</u>	0.3826	<u>0.6221</u>	<u>0.4260</u>	<u>0.5301</u>	0.007	
		ARC (NeurIPS'24)	<u>0.4867</u>	<u>0.4323</u>	<u>0.4769</u>	<u>0.4467</u>	<u>0.5145</u>	<u>0.4786</u>	0.5901	<u>0.2644</u>	<u>0.2298</u>	<u>0.4355</u>	0.003	
		AnomalyGFM	0.6252	0.8649	0.6649	0.9215	0.6064	0.6140	<u>0.5611</u>	0.6303	0.6283	0.6796	/	
AUPRC	1-shot	GPPT (KDD'22)	<u>0.0333</u>	<u>0.0766</u>	<u>0.0488</u>	<u>0.0687</u>	<u>0.1453</u>	0.2204	0.0294	<u>0.1239</u>	<u>0.0432</u>	<u>0.0877</u>	0.003	
		GraphPrompt (WebConf'23)	0.0283	0.0680	0.0486	0.0426	0.1113	<u>0.2321</u>	0.0448	0.1108	0.0302	0.0796	0.012	
		ARC (NeurIPS'24)	0.0332	0.0581	0.0453	0.0590	0.1402	0.2122	<u>0.0468</u>	0.0701	0.0277	0.0769	0.011	
		AnomalyGFM	0.0398	0.5801	0.1223	0.6921	0.1852	0.2786	0.0332	0.1401	0.0601	0.2368	/	
	5-shot	GPPT (KDD'22)	<u>0.0333</u>	<u>0.0692</u>	0.0504	<u>0.0716</u>	0.1453	0.2265	0.0297	0.1127	<u>0.0365</u>	0.0861	0.004	
		GraphPrompt (WebConf'23)	0.0285	0.0681	<u>0.0892</u>	0.0600	<u>0.1661</u>	0.2957	0.0327	<u>0.1416</u>	0.0360	<u>0.1019</u>	0.009	
		ARC (NeurIPS'24)	0.0312	0.0571	0.0546	0.0572	0.1464	0.2150	0.0471	0.0726	0.0267	0.0786	0.011	
		AnomalyGFM	0.0401	0.5831	0.1257	0.6985	0.1918	0.2866	<u>0.0336</u>	0.1437	0.0622	0.2405	/	
	10-shot	GPPT (KDD'22)	<u>0.0334</u>	<u>0.0691</u>	0.0526	0.0698	0.1453	0.2178	0.0301	0.0905	<u>0.0511</u>	0.0844	0.004	
		GraphPrompt (WebConf'23)	0.0278	0.0681	<u>0.0848</u>	<u>0.1427</u>	<u>0.1649</u>	0.2922	0.0263	<u>0.1421</u>	0.0382	<u>0.1096</u>	0.007	
		ARC (NeurIPS'24)	<u>0.0327</u>	<u>0.0557</u>	<u>0.0743</u>	<u>0.0583</u>	<u>0.1491</u>	<u>0.2168</u>	0.0463	<u>0.0677</u>	<u>0.0272</u>	<u>0.0809</u>	0.011	
		AnomalyGFM	0.0444	0.5895	0.1399	0.7124	0.1990	0.2897	0.0346	0.1570	0.0644	0.2478	/	

Scale up to Very Large Graphs

- ❑ AnomalyGFM can effectively infer the anomaly score without considering the **entire graph structure**, eliminating the bottleneck of loading the full graph for GAD inference.



$$\mathbf{r}_i = \mathbf{h}_i - \frac{1}{|\mathcal{S}(v_i)|} \sum_{v_j \in \mathcal{S}(v_i)} \mathbf{h}_j$$

- ❖ Privacy-sensitive settings where we do not want to reveal the entire graph structure

Table 4: Subgraph inference on the very large-scale graphs. ‘/’ indicates that the model cannot handle the dataset.

Metric	Method	Dataset	
		T-Finance	T-Social
AUROC	Unsupervised Methods		
	TAM (NeurIPS’23)	0.2990	/
	GADAM (ICLR’24)	0.1382	<u>0.5155</u>
	Supervised Methods		
	BWGNN (ICML’22)	<u>0.5457</u>	0.4964
	GHRN (WebConf’23)	0.5324	0.4934
	XGBGraph (NeurIPS’23)	0.3402	0.4602
AUPRC	AnomalyGFM	0.7852	0.5991
	Unsupervised Methods		
	TAM (NeurIPS’23)	0.0332	/
	GADAM (ICLR’24)	0.0261	0.0285
	Supervised Methods		
	BWGNN (ICML’22)	0.0479	0.0301
	GHRN (WebConf’23)	0.0457	0.0303
	XGBGraph (NeurIPS’23)	<u>0.0754</u>	<u>0.0305</u>
	AnomalyGFM	0.1059	0.0398

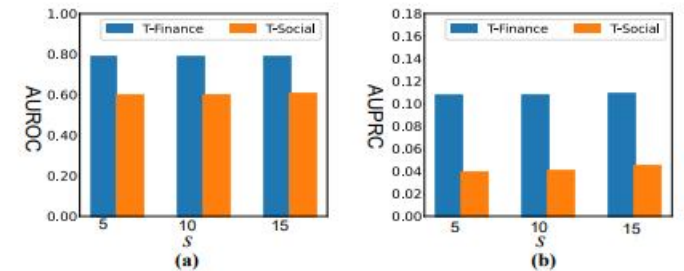
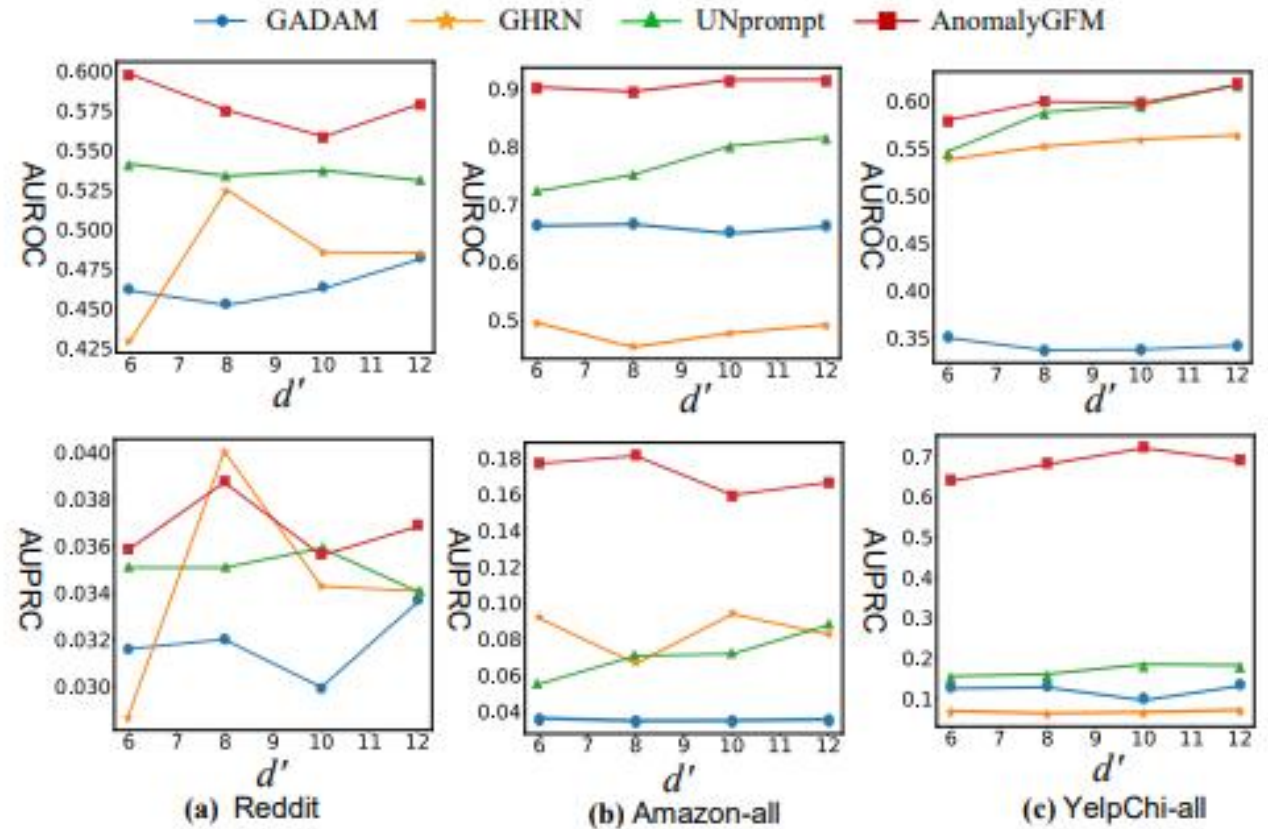


Figure 3: AnomalyGFM performance w.r.t subgraph size s .

Sensitivity of AnomalyGFM w.r.t common dimensionality

❖ Feature Unification

$$\mathbf{X}^{(i)} \in \mathbb{R}^{N^{(i)} \times d^{(i)}} \xrightarrow[\text{Projection}]{\text{Feature}} \tilde{\mathbf{X}}^{(i)} \in \mathbb{R}^{N^{(i)} \times d'}$$



Conclusion

- ❑ We build a GAD-oriented graph foundation model, AnoamlyGFM, that can work effectively under both **few-shot** and **zero-shot** scenarios.
- ❑ AnomalyGFM is pre-trained to learn discriminative and data-independent prototypes by aligning them with the **graph-agnostic** node representation residuals.
- ❑ This provides a consistent and identical way for abnormality measurement using the similarity between **residual node representation** and the **learned class prototypes**, facilitating the strong generalization in both zero-shot and few-shot inference.