

ALGORITHM

A sequence of unambiguous instructions for solving a problem

Properties of an algorithm:

- ① Definite : Each step must be unambiguously specified
- ② Effective : Each step is sufficiently simple and basic.
- ③ Finite : Terminates after a finite number of steps
- ④ Input : Valid inputs are clearly specified
- ⑤ Output : Can produce the correct output for a given valid input.

Theoretical Importance of algorithms:

It is the core of Computer Science.

Practical Importance of algorithms:

- Searching & Sorting
- GPS, Air travel routes, page ranking, etc.

Problem: Find the GCD of 'm' and 'n'

Method-1

ALGORITHM EUCLID(m,n)

while $n \neq 0$ do

$r \leftarrow m \bmod n$

$m \leftarrow n$

$n \leftarrow r$

return m

(eg)

$m = 60$

$n = 24$

$r \Rightarrow 60 \bmod 24 = 12$

$m \Rightarrow 24$

$n \Rightarrow 12$

$r \Rightarrow 24 \bmod 12 = 0$

$m \Rightarrow 12$

$n \Rightarrow 0$ STOP

GCD of 60 & 24 is 12

Method-2 : Consecutive Integer Checking Algorithm GCD(m, n)

Step-1: Assign $\min(m, n)$ to 't'

Step-2: Divide m by t. If the remainder is 0, go to Step-3. If the remainder is non-zero, go to Step-4.

Step-3: Divide n by t; If the remainder is 0, then return 't' as the GCD of m and n; otherwise go to Step-4.

Step-4: Decrease the value of 't' by 1. Go to Step-2.

(eg) GCD(60, 24)

$$t = 24$$

$$60 \bmod 24 = 12$$

$$t = 23$$

$$60 \bmod 23 \neq \underline{0}$$

$$t = 22$$

$$60 \bmod 22 \neq \underline{0}$$

$$t = 21$$

$$60 \bmod 21 \neq 0$$

$$t = 20$$

$$60 \bmod 20 = 0$$

$$24 \bmod 20 = \cancel{4} 4 \neq 0$$

$$t = 19$$

.....

.....