Statistical Methods for Discrete Response, Time Series, and Panel Data (W271): Lab 2

Heather Feinstein, David Harding, Charlotte Swavola

Strategic Placement of Products in Grocery Stores

Answer Question 12 of chapter 3 (on page 189 and 190) of Bilder and Loughin's "Analysis of Categorical Data with R". Here is the background of this analysis, taken as an excerpt from this question:

In order to maximize sales, items within grocery stores are strategically placed to draw customer attention. This exercise examines one type of item:breakfast cereal. Typically, in large grocery stores, boxes of cereal are placed on sets of shelves located on one side of the aisle. By placing particular boxes of cereals on specific shelves, grocery stores may better attract customers to them. To investigate this further, a random sample of size 10 was taken from each of four shelves at a Dillons grocery store in Manhattan, KS. These data are given in the **cereal_dillons.csv** file. The response variable is the shelf number, which is numbered from bottom (1) to top (4), and the explanatory variables are the sugar, fat, and sodium content of the cereals.

```
# Load libraries
library(Hmisc)
library(MASS)
library(nnet)
library(stargazer)

# Load dataset
cereal <- read.csv("cereal_dillons.csv")
cereal[1:10,-1]</pre>
```

```
##
      Shelf
                                              Cereal size_g sugar_g fat_g
## 1
           1 Kellog's Razzle Dazzle Rice Crispies
                                                          28
                                                                   10
                                                                         0.0
## 2
           1
                         Post Toasties Corn Flakes
                                                          28
                                                                    2
                                                                         0.0
           1
                                                                    2
## 3
                             Kellogg's Corn Flakes
                                                          28
                                                                        0.0
                                                                    2
## 4
           1
                            Food Club Toasted Oats
                                                          32
                                                                         2.0
## 5
           1
                                   Frosted Cheerios
                                                          30
                                                                   13
                                                                         1.0
## 6
           1
                          Food Club Frosted Flakes
                                                          31
                                                                   11
                                                                        0.0
## 7
           1
                                         Capn Crunch
                                                          27
                                                                   12
                                                                         1.5
           1
               Capn Crunch's Peanut Butter Crunch
                                                          27
                                                                    9
                                                                         2.5
## 8
## 9
           1
                                    Post Honeycomb
                                                          29
                                                                   11
                                                                         0.5
                                                                    2
                                                                         0.0
## 10
           1
                             Food Club Crispy Rice
                                                          33
##
      sodium_mg
## 1
             170
## 2
             270
## 3
             300
## 4
             280
             210
## 5
```

```
## 6 180
## 7 200
## 8 200
## 9 220
## 10 330
```

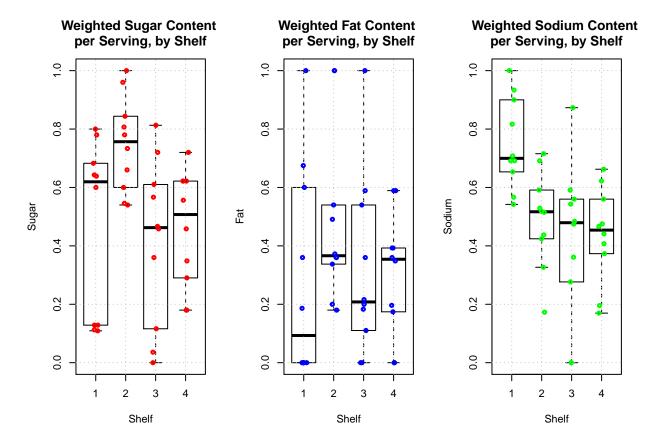
describe(cereal)

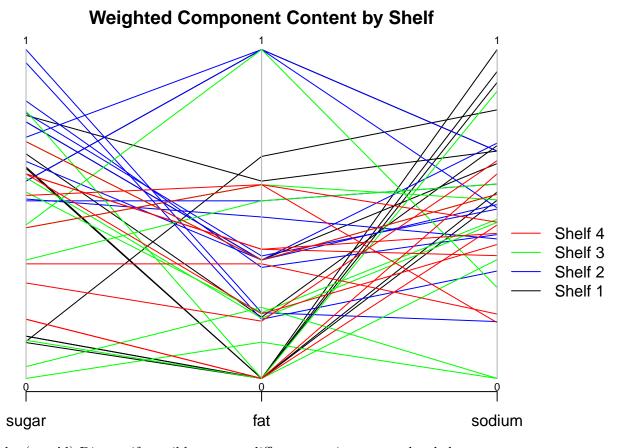
- a. The explanatory variables need to be reformatted before proceeding further.
 - First, divide each explanatory variable by its serving size to account for the different serving sizes among the cereals.
 - Second, rescale each variable to be within 0 and 1.

```
##
        Shelf
                                                           sodium
                       sugar
                                          fat
## Min.
           :1.00
                   Min.
                          :0.0000
                                     Min.
                                            :0.0000
                                                       Min.
                                                              :0.0000
## 1st Qu.:1.75
                   1st Qu.:0.3339
                                     1st Qu.:0.1582
                                                       1st Qu.:0.4200
## Median :2.50
                   Median :0.6000
                                     Median : 0.3542
                                                       Median: 0.5354
## Mean
           :2.50
                   Mean
                           :0.5209
                                     Mean
                                            :0.3476
                                                       Mean
                                                              :0.5240
## 3rd Qu.:3.25
                   3rd Qu.:0.7200
                                     3rd Qu.:0.5400
                                                       3rd Qu.:0.6696
## Max.
           :4.00
                   Max.
                          :1.0000
                                     Max.
                                            :1.0000
                                                       Max.
                                                              :1.0000
```

b. Construct side-by-side box plots with dot plots overlaid for each of the explanatory variables.

```
par(mfrow=c(1,3))
boxplot(formula = sugar ~ Shelf, data = cereal2, ylab = "Sugar", xlab = "Shelf",
        pars = list(outpch = NA), main="Weighted Sugar Content \nper Serving, by Shelf")
stripchart(x = cereal2$sugar ~ cereal2$Shelf, lwd = 2, col = "red", method = "jitter",
           vertical = TRUE, pch = 1, add = TRUE,
           panel.first = grid(col = "gray", lty = "dotted"))
boxplot(formula = fat ~ Shelf, data = cereal2, ylab = "Fat", xlab = "Shelf",
        pars = list(outpch = NA), main="Weighted Fat Content \nper Serving, by Shelf")
stripchart(x = cereal2$fat ~ cereal2$Shelf, lwd = 2, col = "blue", method = "jitter",
           vertical = TRUE, pch = 1, add = TRUE,
           panel.first = grid(col = "gray", lty = "dotted"))
boxplot(formula = sodium ~ Shelf, data = cereal2, ylab = "Sodium", xlab = "Shelf",
        pars = list(outpch = NA), main="Weighted Sodium Content \nper Serving, by Shelf")
stripchart(x = cereal2$sodium ~ cereal2$Shelf, lwd = 2, col = "green", method = "jitter",
           vertical = TRUE, pch = 1, add = TRUE,
           panel.first = grid(col = "gray", lty = "dotted"))
```





b. (cont'd) Discuss if possible content differences exist among the shelves.

Shelf 1 cereals have higher average sodium and lower average fat, relative to the other three shelves, though the range of fat content is wide.

Shelf 2 cereals have a notably higher average sugar content, and all cereals on the shelf have a sugar content above 0.5. The sodium content is average, but has a narrower range, relative to other shelves, with only one cereal in the top or bottom quartile of sodium content.

Shelf 3 maintains a wide distribution across all three components of sugar, fat and sodium. It includes cereals that have the lowest sugar, fat, and sodium content.

Shelf 4 does have two cereals with no fat, otherwise it is notable for not having cereals with extremely high or low sugar or sodium content.

c. The response has values of 1, 2, 3, and 4. Under what setting would it be desirable to take into account ordinality. Do you think that this setting occurs here?

If there are specific criteria that can be used to compare and rank shelves, then ordinality would be an important consideration. For example, if cereal manufacturers are charged for shelf space, the shelves could be ranked by cost. Alternatively, they could be ranked for visibility by a specific audience, such as children or adults. It seems likely that the rank order would vary by criteria: For example, if you were considering children, the shelves might have the rank order 2,1,3,4 for most to least visible. For adults, it might be 3,4,2,1. In this case, we haven't specified any criteria, so it is not appropriate to assign an ordinal ranking.

d. Estimate a multinomial regression model with linear forms of the sugar, fat, and sodium variables. Perform LRTs to examine the importance of each explanatory variable.

```
#Estimate model
mod.fit<-multinom(formula = Shelf ~ sugar + fat + sodium, data=cereal2)</pre>
## # weights:
               20 (12 variable)
## initial value 55.451774
## iter 10 value 37.329384
## iter
        20 value 33.775257
## iter
        30 value 33.608495
        40 value 33.596631
## iter
## iter
        50 value 33.595909
## iter
        60 value 33.595564
## iter
        70 value 33.595277
## iter 80 value 33.595147
## final value 33.595139
## converged
summary(mod.fit)
## Call:
## multinom(formula = Shelf ~ sugar + fat + sodium, data = cereal2)
##
## Coefficients:
##
     (Intercept)
                                           sodium
                      sugar
                                    fat
        6.900708
## 2
                   2.693071 4.0647092 -17.49373
## 3
       21.680680 -12.216442 -0.5571273 -24.97850
##
       21.288343 -11.393710 -0.8701180 -24.67385
##
## Std. Errors:
##
     (Intercept)
                    sugar
                                fat
                                      sodium
## 2
        6.487408 5.051689 2.307250 7.097098
## 3
        7.450885 4.887954 2.414963 8.080261
## 4
        7.435125 4.871338 2.405710 8.062295
##
## Residual Deviance: 67.19028
## AIC: 91.19028
```

```
# LRT for sugar_q:
mod.fit.Ho_sugar<-multinom(formula = Shelf ~ fat + sodium, data=cereal2, trace=FALSE)</pre>
anova(mod.fit.Ho_sugar, mod.fit)
## Likelihood ratio tests of Multinomial Models
##
## Response: Shelf
                     Model Resid. df Resid. Dev
##
                                                   Test
                                                            Df LR stat.
             fat + sodium
                                 111
                                        89.95511
## 2 sugar + fat + sodium
                                 108
                                        67.19028 1 vs 2
                                                             3 22.76484
##
          Pr(Chi)
## 1
## 2 4.520699e-05
The p-value for the likelihood ratio test is less than 0.05, therefore we can reject the null hypothesis
for sugar, concluding that sugar is significant to the model.
# LRT for fat_g:
mod.fit.Ho_fat<-multinom(formula = Shelf ~ sugar + sodium, data=cereal2, trace=FALSE)
anova(mod.fit.Ho_fat, mod.fit)
## Likelihood ratio tests of Multinomial Models
##
## Response: Shelf
##
                     Model Resid. df Resid. Dev
                                                   Test
                                                            Df LR stat.
           sugar + sodium
                                        72.47384
## 1
                                 111
## 2 sugar + fat + sodium
                                 108
                                        67.19028 1 vs 2
                                                             3 5.28356
       Pr(Chi)
##
## 1
## 2 0.1521727
We cannot reject the null hypothesis that fat is not significant to the model.
# LRT for sodium_mq:
mod.fit.Ho_sodium<-multinom(formula = Shelf ~ sugar + fat, data=cereal2, trace=FALSE)
anova(mod.fit.Ho_sodium, mod.fit)
## Likelihood ratio tests of Multinomial Models
## Response: Shelf
##
                     Model Resid. df Resid. Dev
                                                   Test
                                                            Df LR stat.
## 1
              sugar + fat
                                 111
                                       93.81001
## 2 sugar + fat + sodium
                                 108 67.19028 1 vs 2 3 26.61974
##
          Pr(Chi)
## 1
## 2 7.073281e-06
```

For sodium, the p-value is less than 0.05. We can reject the null hypothesis and conclude that sodium is significant to the model.

e. Show that there are no significant interactions among the explanatory variables (including an interaction among all three variables).

```
# The existing model is the null hypothesis model with no interaction terms.
# LRT for alternative model with sugar*sodium interaction term:
mod.fit.Ha_sugar_sodium <- multinom(formula = Shelf ~ sugar + fat + sodium + sugar:sodium,
                                    data=cereal2, maxit=200, trace=FALSE)
anova(mod.fit.Ha_sugar_sodium, mod.fit)
## Likelihood ratio tests of Multinomial Models
## Response: Shelf
##
                                   Model Resid. df Resid. Dev
                                                                 Test
                                                                         Df
## 1
                    sugar + fat + sodium
                                               108
                                                      67.19028
## 2 sugar + fat + sodium + sugar:sodium
                                               105
                                                      64.83988 1 vs 2
                                                                          3
    LR stat. Pr(Chi)
## 1
## 2 2.350397 0.502935
# LRT for alternative model with sugar*fat interaction term:
mod.fit.Ha_sugar_fat <- multinom(formula = Shelf ~ sugar + fat + sodium + sugar:fat,</pre>
                                 data=cereal2, maxit=200, trace=FALSE)
anova(mod.fit.Ha_sugar_fat, mod.fit)
## Likelihood ratio tests of Multinomial Models
## Response: Shelf
                                Model Resid. df Resid. Dev
##
                                                              Test
                                                                      Df
                 sugar + fat + sodium
                                           108
                                                   67.19028
## 2 sugar + fat + sodium + sugar:fat
                                            105
                                                   61.82907 1 vs 2
                                                                       3
##
    LR stat.
               Pr(Chi)
## 1
## 2 5.36121 0.1471795
# LRT for alternative model with fat*sodium interaction term:
mod.fit.Ha_fat_sodium <- multinom(formula = Shelf ~ sugar + fat + sodium + sugar:sodium,</pre>
                                  data=cereal2, maxit=200, trace=FALSE)
anova(mod.fit.Ha_fat_sodium, mod.fit)
## Likelihood ratio tests of Multinomial Models
##
## Response: Shelf
##
                                   Model Resid. df Resid. Dev
                                                                 Test
                                                                         Df
                    sugar + fat + sodium
                                               108
                                                      67.19028
## 2 sugar + fat + sodium + sugar:sodium
                                               105
                                                      64.83988 1 vs 2
                                                                          3
##
     LR stat. Pr(Chi)
## 1
## 2 2.350397 0.502935
# LRT for alternative model with sugar*fat*sodium interaction term:
mod.fit.Ha_sugar_fat_sodium <- multinom(formula = Shelf ~ sugar + fat + sodium +</pre>
```

```
sugar:fat:sodium, data=cereal2, maxit=200, trace=FAL
anova(mod.fit.Ha_sugar_fat_sodium, mod.fit)
## Likelihood ratio tests of Multinomial Models
## Response: Shelf
##
                                        Model Resid. df Resid. Dev
                                                                      Test
## 1
                        sugar + fat + sodium
                                                    108
                                                          67.19028
## 2 sugar + fat + sodium + sugar:fat:sodium
                                                    105
                                                          65.04570 1 vs 2
                      Pr(Chi)
##
        Df LR stat.
## 1
         3 2.14458 0.5429468
## 2
```

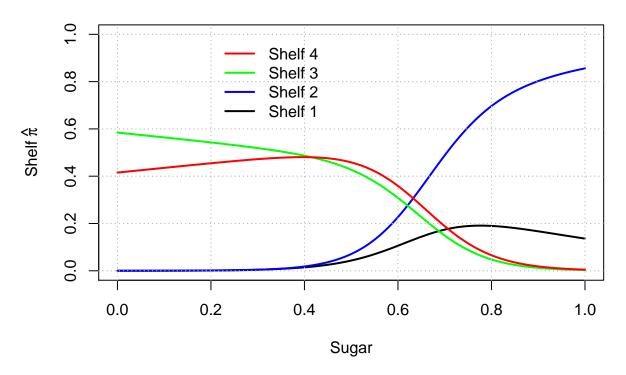
Comparing alternative models that contain interaction terms with a null hypothesis model that has no interaction terms, we cannot reject the null hypothesis for any of the interaction coefficients. These interaction coefficients are not significant to the model.

f. Kellogg's Apple Jacks (http://www.applejacks.com) is a cereal marketed toward children. For a serving size of 28 grams, its sugar content is 12 grams, fat content is 0.5 grams, and sodium content is 130 milligrams. Estimate the shelf probabilities for Apple Jacks.

The estimated shelf probabilities for Apple Jacks are: 0.05, 0.47, 0.2, 0.27

g. Construct a plot similar to **Figure 3.3** where the estimated probability for a shelf is on the y-axis and the sugar content is on the x-axis. Use the mean overall fat and sodium content as the corresponding variable values in the model. Interpret the plot with respect to sugar content.

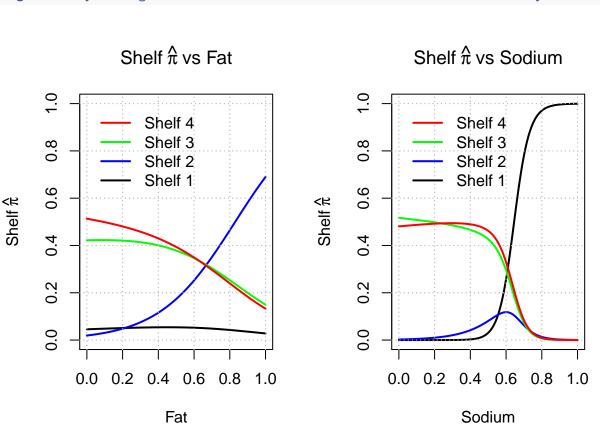
Shelf $\hat{\pi}$ vs Sugar content



For cereals with an average fat and sodium content, those with a below average sugar content have a high estimated probability to be found on the higher shelves, either 3 or 4. As the sugar content increases from average to very high, the cereal is more and more likely to be found on shelf 2, while the probability of being located on a higher shelf declines toward zero. Cereals with average fat and sodium content have a low estimated probability of being found on shelf 1, not exceeding 20%, regardless of their sugar content.

```
par(mfrow=c(1,2))
curve(expr = predict(object = mod.fit, newdata = data.frame(sugar = mean(cereal2$sugar),
      fat =x, sodium = mean(cereal2$sodium)), type = "probs")[,1],
     main= expression(Shelf~hat(pi)~"vs Fat"),
     ylab = expression(Shelf~hat(pi)), xlab = "Fat", xlim = c(min(cereal2$fat),
                                                               max(cereal2$fat)),
     ylim = c(0,1), col = "black", lty = "solid", lwd = 2, n = 1000,
      panel.first = grid(col = "gray", lty = "dotted"))
curve(expr = predict(object = mod.fit, newdata = data.frame(sugar = mean(cereal2$sugar),
      fat =x, sodium = mean(cereal2$sodium)), type = "probs")[,2],
      col = "blue", lty = "solid", lwd = 2, n = 1000,
      add = TRUE, panel.first = grid(col = "gray", lty = "dotted"))
curve(expr = predict(object = mod.fit, newdata = data.frame(sugar = mean(cereal2$sugar),
      fat =x, sodium = mean(cereal2$sodium)), type = "probs")[,3],
      col = "green", lty = "solid", lwd = 2, n = 1000,
      add = TRUE, panel.first = grid(col = "gray", lty = "dotted"))
curve(expr = predict(object = mod.fit, newdata = data.frame(sugar = mean(cereal2$sugar),
      fat =x, sodium = mean(cereal2$sodium)), type = "probs")[,4],
      col = "red", lty = "solid", lwd = 2, n = 1000,
      add = TRUE, panel.first = grid(col = "gray", lty = "dotted"))
legend(x=0,y=1, legend=c("Shelf 4", "Shelf 3", "Shelf 2", "Shelf 1"), lty=c("solid"),
       col=c("red", "green", "blue", "black"), bty="n", lwd = c(2,2,2))
curve(expr = predict(object = mod.fit, newdata = data.frame(sugar = mean(cereal2$sugar),
      fat = mean(cereal2$fat), sodium = x), type = "probs")[,1],
      main= expression(Shelf~hat(pi)~"vs Sodium"),
      ylab = expression(Shelf~hat(pi)), xlab = "Sodium", xlim = c(min(cereal2$sodium), max(cere
      ylim = c(0,1), col = "black", lty = "solid", lwd = 2, n = 1000,
      panel.first = grid(col = "gray", lty = "dotted"))
curve(expr = predict(object = mod.fit, newdata = data.frame(sugar = mean(cereal2$sugar),
      fat = mean(cereal2$fat), sodium = x), type = "probs")[,2],
      col = "blue", lty = "solid", lwd = 2, n = 1000,
      add = TRUE, panel.first = grid(col = "gray", lty = "dotted"))
curve(expr = predict(object = mod.fit, newdata = data.frame(sugar = mean(cereal2$sugar),
      fat = mean(cereal2$fat), sodium = x), type = "probs")[,3],
      col = "green", lty = "solid", lwd = 2, n = 1000,
      add = TRUE, panel.first = grid(col = "gray", lty = "dotted"))
curve(expr = predict(object = mod.fit, newdata = data.frame(sugar = mean(cereal2$sugar),
      fat = mean(cereal2$fat), sodium = x), type = "probs")[,4],
      col = "red", lty = "solid", lwd = 2, n = 1000,
```

```
add = TRUE, panel.first = grid(col = "gray", lty = "dotted"))
legend(x=0,y=1, legend=c("Shelf 4", "Shelf 3", "Shelf 2", "Shelf 1"), lty=c("solid"), col=c("red
```



h. Estimate odds ratios and calculate corresponding confidence intervals for each explanatory variable. Relate your interpretations back to the plots constructed for this exercise.

```
# Information about each variable to help with choosing c. Leave out Shelf column
sd.cereal2 < -apply(X = cereal2[,-c(1)], MARGIN = 2, FUN = sd)
# sd.cereal2
#convert sd into (g/serving) units for interpretation.
#0-1 are percentages of the overall range for q/serving
sd_convert<-function(sd,df_column,df_serving=cereal$size_g){</pre>
 var range<-max(df column/df serving)-min(df column/df serving)</pre>
 return(sd*var range)
}
c.value<-c(1, sd.cereal2) # class = 1 is first value</pre>
c.value<-c.value[2:4] # drop intercept from c.value</pre>
round(c.value,2)
    sugar
             fat sodium
##
     0.27
            0.30
                    0.23
units<-c(g_serving=sd_convert(c.value[1],cereal$sugar_g),g_serving=sd_convert(c.value[2],
round(units,2)
##
     g_serving.sugar
                          g_serving.fat mg_serving.sodium
##
                0.15
                                   0.03
                                                       2.46
# beta.hat_jr for r = 1, 2, 3 and j = 2, 3, 4
beta.hat2<-coefficients(mod.fit)[1,2:4]</pre>
beta.hat3<-coefficients(mod.fit)[2,2:4]
beta.hat4<-coefficients(mod.fit)[3,2:4]
beta.hat4
##
        sugar
                      fat
                              sodium
## -11.393710 -0.870118 -24.673847
# Odds ratios for j = 2 vs. j = 1
OR2_1<-exp(c.value*beta.hat2)</pre>
OR1_2<-1/exp(c.value*beta.hat2)</pre>
# Odds ratios for j = 3 vs. j = 1
OR3_1<-exp(c.value*beta.hat3)
OR1_3<-1/exp(c.value*beta.hat3)
# Odds ratios for j = 4 vs. j = 1
OR4_1<-exp(c.value*beta.hat4)</pre>
OR1_4<-1/exp(c.value*beta.hat4)
# Odds ratios for j = 3 vs j = 2
OR3_2<-exp(c.value*(beta.hat3 - beta.hat2))</pre>
```

```
OR2_3<-1/OR3_2
# Odds ratios for j = 4 vs j = 3
OR4_3<-exp(c.value*(beta.hat4-beta.hat3))</pre>
OR3 4<-1/OR4 3
# Odds ratios for j = 4 vs j = 2
OR4_2<-exp(c.value*(beta.hat4-beta.hat2))</pre>
OR2_4<-1/OR4_2
#build dataframes
OR_base=data.frame(OR2_1=round(OR2_1,2),
                    OR3_1=round(OR3_1,2),
                    OR4_1=round(OR4_1,2),
                    "-"=c("-","-","-"),
                    OR1_2=round(OR1_2,2),
                    OR3_2=round(OR3_2,2),
                    OR4 2=round(OR4_2,2),
                    "-"=c("-","-","-"),
                    OR1 3=round(OR1 3,2),
                    OR2_3 = round(OR2_3, 2),
                    OR4_3=round(OR4_3,2),
                    "-"=c("-","-","-"),
                    OR1_4=round(OR1_4,2),
                    OR2_4 = round(OR2_4, 2),
                    OR3_4=round(OR3_4,2))
OR_base
          OR2_1 OR3_1 OR4_1 X. OR1_2 OR3_2 OR4_2 X..1 OR1_3 OR2_3 OR4_3 X..2
## sugar
         2.06 0.04 0.05 - 0.48 0.02 0.02 -
                                                       26.81 55.35 1.25
          3.37 0.85 0.77 - 0.30 0.25 0.23
## fat
                                                        1.18 3.98 0.91
## sodium 0.02 0.00 0.00 - 55.74 0.18 0.19 - 311.36 5.59 1.07
##
          OR1_4 OR2_4 OR3_4
## sugar
           21.48 44.36 0.80
## fat
           1.30 4.37 1.10
## sodium 290.31 5.21 0.93
# Wald CIs
conf.beta<-confint(object = mod.fit, level = 0.95)</pre>
# round(conf.beta,2) # Results are stored in a 3D array
\# conf.beta[2:4,1:2,1] \# C.I.s for beta_2r
# conf.beta[2:4,1:2,2] # C.I.s for beta_3r
# conf.beta[2:4,1:2,3] # C.I.s for beta_4r
#CI for probability based on variable entry
# CIs for OR
ci.OR2 < -exp(c.value*conf.beta[2:4,1:2,1])
ci.OR3 < -exp(c.value*conf.beta[2:4,1:2,2])
```

```
ci.OR4 < -exp(c.value*conf.beta[2:4,1:2,3])
"Shelf 2,3,4 vs Shelf 1"
## [1] "Shelf 2,3,4 vs Shelf 1"
round(data.frame(low = ci.OR2[,1], up = ci.OR2[,2]), 2) #RELATIVE TO SHELF 1
##
           low
                  up
## sugar 0.14 29.68
## fat
          0.87 13.04
## sodium 0.00 0.44
round(data.frame(low = ci.OR3[,1], up = ci.OR3[,2]), 2)
##
           low
                 up
## sugar 0.00 0.49
          0.21 3.49
## fat
## sodium 0.00 0.12
round(data.frame(low = ci.OR4[,1], up = ci.OR4[,2]), 2)
##
          low
                 up
## sugar 0.00 0.61
## fat
          0.19 3.16
## sodium 0.00 0.13
"Shelf 3 vs Shelf 2"
## [1] "Shelf 3 vs Shelf 2"
round(data.frame(low = ci.OR3[,1]/ci.OR2[,1], up = ci.OR3[,2]/ci.OR2[,2]), 2) #shelf 3 relativ
##
           low
## sugar 0.02 0.02
          0.24 0.27
## fat
## sodium 0.11 0.28
"Shelf 4 vs Shelf 2"
## [1] "Shelf 4 vs Shelf 2"
round(data.frame(low = ci.OR4[,1]/ci.OR2[,1], up = ci.OR4[,2]/ci.OR2[,2]), 2) #shelf 4 relativ
##
           low
                 up
## sugar 0.02 0.02
## fat
          0.22 0.24
## sodium 0.12 0.30
"Shelf 4 vs Shelf 3"
## [1] "Shelf 4 vs Shelf 3"
round(data.frame(low = ci.OR4[,1]/ci.OR3[,1], up = ci.OR4[,2]/ci.OR3[,2]), 2) #shelf 4 relativ
```

```
## sugar 1.26 1.24
## fat 0.92 0.91
## sodium 1.08 1.06
```

Odds ratio interpretations: The c values (in $e^{c\beta_{jr}}$) used to evaluate the odds ratios for each component were calculated as 1 standard deviation unit. In grams per serving, these c values are 0.15 g/serving of sugar, 0.03 g/serv fat, and 2.46 mg/serv sodium.

Evaluating sugar first, for each c-value increase in sugar, the odds that the cereal would be on shelf 2 are 2.06 times as large as the odds it would be on shelf 1, 55.4 times as large that it'd be on shelf 2 as shelf 3, and 44.4 times as large that it would be on shelf 2 as shelf 4. This matches the $\hat{\pi}$ graph for sugar as shelves 2 and then 1 have the highest probabilities for increased sugar content.

Incorporating the confidence intervals, the CI of the odds ratio that the cereal will appear on shelf 2 vs shelf 1 includes 1, so we cannot definitively say the odds the cereal will be on shelf 2 are larger than shelf 1. We can, however, say that the odds the cereal will be on shelves 3 or 4 relative to either shelf 1 or 2 are less than 1 for each unit increase in sugar.

Looking at fat, for each c-value increase in fat the odds that a cereal will be on shelf 2 are at least twice as large as the odds of the other shelves. The $\hat{\pi}$ graphs echo this, for as the fat content increases, the likelihood the cereal will appear 2 increases while all others decrease. Again, The odds ratio confidence intervals span 1 for shelf 2 vs shelf 1, however they are entirely below 1 for shelf 3 vs shelf 2 and shelf 4 vs shelf 3, indicating that the odds of the cereal to be on shelf 2 are larger than shelf 3 or 4 for an increase in fat.

Now, the odds ratios for sodium reach extreme numbers, especially relative to shelf 1. The behavior of the /hat/pi vs sodium content for shelf 1 increases from 0 to 1 in about 0.3 units, almost the same as our c-value, potentially because only high-sodium samples appear on shelf 1. This is reiterated by the confidence intervals, as all the other shelf intervals are below 0.5 relative to shelf 1. This means that for each unit increase in sodium, the odds that a cereal appears on any other shelf are at most 1/2 as large as the odds that the cereal appears on shelf 1.