# Car Engine Dynamics and Fuel Consumption Simulation

Your Name

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## 1 Introduction

This document outlines the formulas used to simulate the dynamics and fuel consumption of a car engine. The model considers the engine angular velocity, fuel consumption rate, fuel efficiency, power output, torque, and time-varying factors such as gas valve open level and load torque.

# 2 Formulas

# 2.1 Fuel Consumption Rate

The fuel consumption rate,  $\dot{m}(t)$ , depends on the time-varying gas valve open level, V(t), and the engine angular velocity,  $\omega(t)$ :

$$\dot{m}(t) = k_{\text{fuel}} \cdot V(t) \cdot \omega(t) \tag{1}$$

where  $k_{\text{fuel}}$  is a proportional constant for the fuel consumption rate.

#### 2.2 Fuel Efficiency

The fuel efficiency,  $\eta_f(\omega(t))$ , is a function of the engine angular velocity,  $\omega(t)$ :

$$\eta_f(\omega(t)) = \eta_{\text{max}} \cdot \left(1 - e^{-\alpha \cdot (\omega(t) - \omega_{\text{opt}})^2}\right)$$
(2)

where  $\eta_{\rm max}$  is the maximum fuel efficiency,  $\alpha$  is a constant, and  $\omega_{\rm opt}$  is the optimal angular velocity for maximum efficiency.

#### 2.3 Power Output

The power output, P(t), is determined by the fuel consumption rate and the fuel efficiency:

$$P(t) = \dot{m}(t) \cdot \eta_f(\omega(t)) \tag{3}$$

## 2.4 Total Torque

The total torque produced by the engine,  $T_{\text{total}}(t)$ , is related to the power output and angular velocity:

$$T_{\text{total}}(t) = \frac{P(t)}{(2\pi \cdot \omega(t)/60)} \tag{4}$$

#### 2.5 Internal Friction Torque

The internal friction torque,  $T_f(t)$ , as a function of angular velocity is given by:

$$T_f(t) = k_{\text{friction}} \cdot \omega(t) + c_f \tag{5}$$

where  $k_{\text{friction}}$  is the internal friction coefficient and  $c_f$  is a constant representing static friction.

#### 2.6 Net Torque

The net torque,  $T_{\text{net}}(t)$ , is the difference between the total torque, internal friction torque, and load torque:

$$T_{\text{net}}(t) = T_{\text{total}}(t) - T_f(t) - T_{\text{load}}(t)$$
(6)

## 2.7 Angular Acceleration

The angular acceleration,  $\alpha(t)$ , is determined by the net torque and the engine's moment of inertia, I:

$$\alpha(t) = \frac{T_{\text{net}}(t)}{I} \tag{7}$$

#### 2.8 Update Angular Velocity

The angular velocity is updated using the angular acceleration over a small time step, dt:

$$\omega(t+dt) = \omega(t) + \alpha(t) \cdot dt \tag{8}$$

# 3 Conclusion

These formulas provide a comprehensive model for simulating car engine dynamics and fuel consumption, considering the time-varying nature of the gas valve open level and load torque. Adjust the constants and functions based on empirical data or specific engine characteristics for more accurate simulations.