

Q4 :

(a) A

(b) A

(C) For this reason, we start writing the "Analysis of Deviance" table. we have factor variables that create $(L-1)$ coefficients. L is number of levels in that factor variable.

	Res-Df	Res.Dev	Df	Deviance	pr(>chi)
mod 0	736	832.28	14	15.04	P
mod 1	750	847.32			

⇒ based on Appendix table, Chi-square score of S^2 is 23.68. So we can't reject the null hypothesis. Hence, m1 is an adequate simplification of m0

we repeat the test :

	Res. DF	Res. Dev	DF	Deviance	pr(>chi)
mod 1	750	847.32	1	3.21	p
mod 2	751	850.53			

based on Appendix table, p is larger than 5% so we can't reject the null hypothesis. Hence, m2 is an adequate simplification of m1.

For m3 :

	Res. DF	Res. Dev	DF	Deviance	pr(>chi)
mod 2	751	850.53	1	0.03	p
mod 3	752	850.56			

⇒ we can't reject the null hypothesis ⇒ m3 is a simplification of m2

for m4 :

	Res. DF	Res. Dev	DF	Deviance	pr(>chi)
mod 3	752	850.56	2	7.77	p
mod 4	754	858.33			

⇒ based on table, p is less than 5%, so we reject the null hypothesis.

⇒ m4 is not an adequate simplification of m3.

Test the rest of models with m3 :

	Res. DF	Res. Dev	DF	Deviance	pr(>chi)
mod 3	752	850.56			
mod 5	756	864.09	4	13.53	reject H_0
mod 6	757	867.82	5	17.26	reject H_0
mod 7	758	940.66	6	90.1	reject H_0

⇒ m3 is an adequate simplification of m0 and we can't simplify it more.

$$(d) \quad \log\left(\frac{M}{1-M}\right) = \beta_0 + \beta_1(\text{bmi}) + \beta_2(\text{age}) + \beta_3(\text{diastolic})$$

$$\Rightarrow \frac{\text{odds of diabetes with (age+1)}}{\text{odds of diabetes with (age)}} = e^{\beta_2} = 1.04$$

\Rightarrow if age is increasing by 1 unit, the odds of getting diabetes increases by factor of 1.04.

$$(e) \quad \beta_2 \pm 1.96(\text{standard error } \beta_2) \Rightarrow CI = \left[e^{\overbrace{\beta_2 - 1.96 \text{Se}(\beta_2)}^{0.0346}}, e^{\overbrace{\beta_2 + 1.96 \text{Se}(\beta_2)}^{0.0625}} \right]$$

$$\Rightarrow [1.035, 1.06]$$

(f) based on lecture notes, the χ^2_{n-p} approximation makes sense only under H_0 when the grouped format is used.

since we don't know the format of data entry, we can't tell if we can use goodness of fit test with χ^2_{756} \Rightarrow ☒ C

(g) ☐ A