

Due: December 16, 2025, 17:00 (Room R1102)

Important Notice: You must print this take-home quiz and write your answers by hand with a pen.

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Q1 Figure	Q2 Figure
<pre> graph TD 0((0)) --> 1((1)) 0((0)) --> 2((2)) 0((0)) --> 3((3)) 1((1)) --> 4((4)) 1((1)) --> 5((5)) 2((2)) --> 4((4)) 2((2)) --> 6((6)) 3((3)) --> 7((7)) 4((4)) --> 5((5)) 5((5)) --> 6((6)) 6((6)) --> 7((7)) </pre>	<pre> graph TD minus(-) --- plus(+) minus(-) --- div(÷) minus(-) --- num3((3)) plus(+) --- num3((3)) plus(+) --- num4((4)) div(÷) --- num10((10)) div(÷) --- num2((2)) </pre>

Q1. (30 pts) Explain Breadth-First Search (BFS) on the graph and provide the BFS traversal order for the graph shown in Q1 Figure.

A1: BFS start from root, and go through the vertices that have higher level first.
(closer to root)

order: $0 \rightarrow 1 \rightarrow 4 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 6 \rightarrow 7$

queue, revisiting

Q2. (30 pts) In tree traversal, one common method is inorder traversal. Please use inorder traversal to print the arithmetic expression represented by the expression tree in Q2 Figure, and then evaluate it to compute the final result.

A2:

$$: 3 \times 4 + 10 \div 2 - 3$$

$$\Rightarrow 12 + 5 - 3 = \underline{\underline{14}}$$

Q3. (40 pts) A binary tree is a fascinating data structure with many variations, including binary search trees, AVL trees, red-black trees, complete binary trees, and max/min heaps. These variations can be classified as shape-based (structural constraints) or criteria-based (rules such as ordering). Choose one shape-based tree and one criteria-based tree, and provide a brief description of each.

A3:

shape-based: AVL tree:

- a kind of binary search tree (left node & right node)
- A left subtree and right subtree from same node can't have a height difference more than 1.
- this tree make binary search tree more balance. $O(\log n)$
- Each node has a BF value, when $BF > 1$, do rotate to avoid illegal.
or
left, right
1. $\text{Max}(\text{left tree height}, \text{right tree height}) + 1$ $BF < -1$
2. $(\text{left tree height} - \text{right tree height})$

p.s 我在路上找到這兩種算法，兩種的數字不太一樣但好像都可以用)

criteria-based: red-black tree:

- also a binary search tree
- rule:
 - every nodes ^{can only be} red or black tree.
 - root must be black
 - leaf must be black and NULL
 - red node's child must be black
 - each node to every child leaf, number of black nodes must be same.
from
- more balance than other binary tree, $O(\log n)$

May be

→ balance: no balance lead to  (close to linked list, worse case become $O(n)$).