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**A35 Part A: Hash Table Definitions (Conceptual Understanding)**

Q1. Define "collision" in the context of hash tables.

A1: Keys calculate by hash function has same hash value.  
 It means we need to decide to put those keys where.

Q2. What is a "bucket" in a hash table?

A2: The space that store value.

+5

Q3. Define "load factor ( $\alpha$ )" and explain why it affects performance.

A3: Load factor( $\alpha$ ) shows how strong a hash table's collision has.  
 If a table  $\alpha$  has lot of collision, it doesn't have a good rate using.

Q4. What is "primary clustering," and which probing method suffers from it?

A4: Linear probing may lead to this. It means many keys have the same value after  $h(key)$ , but then place in  $h(key) + i$ ,  $i=0, 1, \dots, n$ . All keys have same hkeys are stored side by side.

Q5. What is "secondary clustering," and how is it different from primary clustering?

A5: All keys have same  $h(key)$  ( $h$  means hash function) are stored by a regular space.  
 for example, key1 is stored at bucket(i), key2 is stored at bucket(i+n), key3 at bucket(2i+n).  
 Secondary clustering is more severe than primary one but may leads to some keys can not get their own space.

Q6. Briefly explain the difference between:

- Open addressing  $\rightarrow$  array only
- Separate chaining  $\rightarrow$  array + linked list

A6: Open addressing:

- need more computing to determine where key is put.
- if collision happened, need a way to find another space to put key
- need space using rate

Separate chaining

- just add the node after  $h(key)$
- don't need to worry about collision.
- May have lots of array spaces don't be

## Part B: Hash Function Calculation (Collision & Pattern Observation)

Show your steps clearly.

Hash Function 1 — Division Method

$$h_1(k) = k \bmod 10$$

Hash Function 2 — Folding Method

Split key into two-digit chunks and sum the chunks.

$$h_2(k) = (\text{sum of 2-digit groups}) \bmod 11$$

Example:

Key = 8429 → groups: 84 + 29 → 113 → 113 mod 11 = 3

Q7. (Compute using Hash Function 1)

Given keys: 27, 37, 47, 57, 67

Compute their hash values using:

$$h_1(k) = k \bmod 10$$

A7:  $h_1(27) = 7$      $h_1(57) = 7$   
 $h_1(37) = 7$      $h_1(67) = 7$   
 $h_1(47) = 7$

Q8. (Identify collision pattern)

From your results in Q7:

- What pattern do you observe?
- Explain why these keys collide.

A8: All keys has same hash values after  $h_1()$ .

because they have same digit.  
first-

Q9. (Compute using Hash Function 2)

Compute  $h_2(k)$  for: 1234, 9217, 4519, 9902

A9:

$$\begin{aligned} h_2(1234) &= 12+34 \Rightarrow 46 \bmod 11 = 2 \\ h_2(9217) &= 92+17 \Rightarrow 109 \bmod 11 = 10 \\ h_2(4519) &= 45+19 \Rightarrow 64 \bmod 11 = 9 \\ h_2(9902) &= 99+02 \Rightarrow 101 \bmod 11 = 2 \end{aligned}$$

Q10. (Compare distribution)

- Which hash function ( $h_1$  or  $h_2$ ) produced more collisions for the input set?
- Which seems to spread keys more evenly?
- Provide 1-2 sentences of explanation.

10:  $h_1$  use  $\bmod 10$ , will lead the hash value only has 0 ~ 9.

$h_1$  has more collisions because

$h_2$  may spread keys more evenly because it has more calculate and also,  $\bmod 11$  will let to determine hash value between 0 ~ 10, more than  $h_1$ .