

- 6.6 A forward PWM converter is supplied by a European single-phase rectified utility line voltage, $V_o = 12$ V, and $n_1 = n_3 = 8$. Find the minimum, nominal, and maximum duty cycle.

$$V_o = 12 \text{ V} \quad n_1 = n_3 = 8$$

$$V_{Z_{min}} = (220 - 0.1 \times 220) \times \sqrt{2} = 280 \text{ V}$$

$$V_{Z_{nom}} = \sqrt{2} \times 220 = 311 \text{ V}$$

$$V_{Z_{max}} = \sqrt{2} \times (220 + 0.1 \times 220) = \sqrt{2} \times 242 = 342 \text{ V}$$

$$M V_{D_{min}} = \frac{V_o}{V_{Z_{max}}} = \frac{12}{342} = \frac{1}{28.5}$$

$$M V_{D_{min}} = \frac{V_o}{V_{Z_{max}}} = \frac{12}{280} = \frac{1}{23.3}$$

$$\text{min: } D_{min} = n_1 M V_{D_{min}} = 8 \times 0.03509 / 0.9 = 0.3119$$

$$\text{nominal: } D = 8 \times 0.03856 / 0.9 = 0.3428$$

$$\text{Max: } D = 8 \times 0.04286 / 0.9 = 0.381$$

- 6.11 A forward PWM converter has $V_o = 12$ V, $I_o = 4-40$ A, $n_1 = n_3 = 8$, $L = 20$ μH , $V_{I_{max}} = 342$ V, $D_{min} = 0.3119$, and $f_s = 75$ kHz. Find the magnetizing inductance such that its peak current is less than 12% of the maximum peak current of the primary of the ideal transformer.

$$f_s = 75 \text{ kHz}$$

$$V_{Z_{max}} = 342 \text{ V}$$

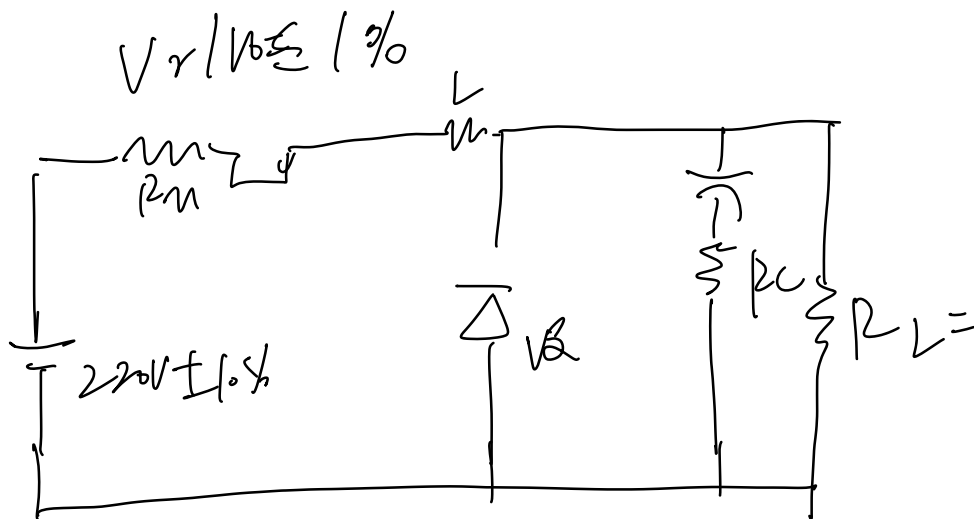
$$I_{Lmax} = I_{Omax} / n_1 = 42.753 / 8 = 5.344 \text{ A}$$

$$\Delta i_{Lm} = 0.12 I_{Lmax} = 0.12 \times 5.344 = 0.641 \text{ A}$$

$$L_{m(min)} = D_{min} V_{Lmax} / f_s \Delta i_{Lm(max)} = 2.219 \text{ mH}$$

we pick $L_m = 2.3 \text{ mH}$

6.14 Design a PWM forward converter that will meet the following specifications: the CCM, V_i is the European single-phase rectified line voltage with $V_{rms} = 220 \text{ V} \pm 10\%$, $V_O = 14 \text{ V}$, $I_{Omin} = 2 \text{ A}$, $I_{Omax} = 20 \text{ A}$, and $V_r/V_O \leq 1\%$. Assume $r_{DS} = 1 \Omega$, $V_F = 0.56 \text{ V}$, $R_F = 25 \text{ m}\Omega$, $r_{L(dc)} = 20 \text{ m}\Omega$, $r_{T1} = 100 \text{ m}\Omega$, $r_{T2} = 25 \text{ m}\Omega$, $C_o = 100 \text{ pF}$, $L_m = 5 \text{ mH}$, and $f_s = 100 \text{ kHz}$. Find component values, component stresses, and converter efficiency.



$$I_{Lmax} = 20 \text{ A}$$

$$I_{Lmin} = 2 \text{ A}$$

$$\text{ratio } D = \frac{V_O}{V_{in}} = \frac{14}{242} = 0.0579$$

$$D_2 = \frac{V_O}{V_{in}} = \frac{14}{198} = 0.0707$$

$$\Delta I_L = \frac{V_{STP}}{L} \times 10^{-7} =$$

$$\textcircled{1} \quad 0.2 < \Delta I < 0.7$$

$$\textcircled{2} \quad I_{avg} \text{ desired} = 27 \text{ mA}$$

$$\textcircled{3} \quad \text{efficiency} = 87.8\%$$

Full Bridge PWM DC-DC Converter 523

7.6 A half-bridge converter has $V_{min} = 280 \text{ V}$, $V_{max} = 342 \text{ V}$, $V_o = 12 \text{ V}$, $I_o = 1\text{--}20 \text{ A}$, $L = 25 \text{ } \mu\text{H}$, $n = 9$, $\Delta i_{Lmax} = 1.513$, and $f_s = 50 \text{ kHz}$. Determine the minimum magnetizing inductance at which its peak-to-peak current is less than 10% of the maximum peak current of the ideal transformer primary.

$$I_1 = I_{max} / n = 20 / 9 = 2.2222 \text{ A}$$

$$I_i = \frac{\Delta i_{im}}{n} = 1.513 / (2 \times 9) = 0.084 \text{ A}$$

$$I_{ux} = 0.084 + 2.2222 = 2.3066 \text{ A}$$

$$\Delta i_{ux} = 0.1 \times I_{ux} = 0.1 \times 2.3066 = 0.2306 \text{ A}$$

$$L_{m(min)} = \frac{D_{min} V_{max}}{2 f_s \Delta i_{ux}} = \frac{0.5414 \times 342}{2 \times 50 \times 10^3 \times 0.2306} = 5.08 \text{ } \mu\text{H}$$

We pick $L_m = 5.1 \text{ } \mu\text{H}$

- 7.8 Design a half-bridge converter operating in CCM to meet the following specifications: V_L is the single-phase rectified European line voltage with V_{rms} is $220\text{ V} \pm 10\%$, $V_O = 5\text{ V}$, $I_{Omin} = 2\text{ A}$, $I_{Omax} = 20\text{ A}$, and $V_r/V_O \leq 1\%$. Assume $r_{DS} = 1\ \Omega$, $r_{T1} = 150\text{ m}\Omega$, $r_{T2} = r_{T3} = 40\text{ m}\Omega$, $r_L = 9\text{ m}\Omega$, $r_C = 35\text{ m}\Omega$, $r_{Cb} = 350\text{ m}\Omega$, $R_F = 10\text{ m}\Omega$, $V_F = 0.3\text{ V}$, and $C_o = 80\text{ pF}$. Assume initially the converter efficiency $\eta = 85\%$.

$$P_{Omax} = V_O \cdot I_{Omax} = 20 \times 5 = 100\text{ W}$$

$$P_{Omin} = V_O I_{Omin} \eta = 2 \times 5 = 10\text{ W}$$

$$R_{Lmin} = \frac{V_O}{I_{Omax}} = \frac{5\text{ V}}{20\text{ A}} = 0.25\ \Omega$$

$$R_{Lmax} = \frac{V_O}{I_{Omin}} = \frac{5\text{ V}}{2\text{ A}} = 2.5\ \Omega$$

$$MVR_{Cmax} = \frac{V_O}{V_{Lmax}} = \frac{5}{198} = 0.0253$$

$$MVR_{Cmin} = \frac{V_O}{V_{Lmin}} = \frac{5}{242} = 0.0207$$

$$MVR_{C\eta} = \frac{V_O}{V_{L\eta}} = \frac{5}{220} = 0.0227 \quad \text{power}$$

$$\eta = \frac{P_{Omax}}{P_{Omax}} = \frac{85\% \times 0.4}{0.0253} = 13.44$$

$$D_{min} = \frac{P_{Omin}}{\eta} = 0.3273$$

$$P_{max} = 0.4$$

$$\eta_{pom} = 0.3589$$

$$\Delta I_{min} = \frac{P_{max} \left(\frac{1}{2} - \eta_{min} \right)}{2 f_s} = \frac{5V \left(\frac{1}{2} - 0.3273 \right)}{2 \times 10^6 \times 10^{-6}}$$

$$\approx 0.43175 A$$

$$L_{min} = \frac{I_{Lmax} \left(\frac{1}{2} - \eta_{min} \right)}{2 f_s} = 2.16 \mu H$$

$$V_r = \frac{V_o}{T_o} = 50 \mu V$$

$$r_{Lmax} = \frac{V_r}{\Delta I_{min}} = \frac{50 \mu V}{0.43175} = 115.8 \mu \Omega$$

$$C_{min} = \max \left\{ \frac{\sqrt{P_{max}}}{2 f_s r_L}, \frac{\frac{1}{2} - \eta_{min}}{2 f_s r_L} \right\}$$

$$= 17.27 \mu H$$

Pick C $27 \text{ W/}^\circ\text{F} / 1000^\circ\text{C} / 16 \text{ V}$

$$V_{\text{max}} = \frac{V_{\text{max}}}{n} = \frac{242}{13} = 18.62 \text{ V}$$

$$I_{\text{max}} = I_{\text{max}} + \frac{\Delta i_{\text{max}}}{2} = 20 \times (0.4315/4) \\ = 20.216 \text{ A}$$

$$I_{\text{max}} = \frac{I_{\text{max}}}{n} = \frac{20.216}{13} = 1.555 \text{ A}$$

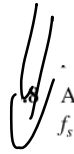
$$\Delta i_{\text{max}} = 0.1 \times 1.555 \text{ A} = 0.1555 \text{ A}$$

$$L_{\text{in}}(\text{min}) = \frac{P_{\text{in}} V_{\text{max}}}{2 \Delta i_{\text{max}}} = \frac{0.323 \times 242}{2 \times 1.5 \times 0.1555} \\ = 2546.1 \text{ mH}$$

$$V_{\text{max}} = V_{\text{max}} = 242 \text{ V}$$

$$I_{\text{max}} = \frac{I_{\text{max}}}{n} + \frac{\Delta i_{\text{max}}}{2} = \frac{20.216}{13} + \frac{0.1555}{2}$$

$$= 1.633 \text{ A}$$



A full-bridge PWM converter has $V_{Imin} = 127 \text{ V}$, $V_{Imax} = 187 \text{ V}$, $n = 2$, $V_O = 48 \text{ V}$, $P_O = 1-2.5 \text{ kW}$, and $f_s = 35 \text{ kHz}$. Find the current stresses of the transistors and the diodes.

same $I_{Omax} = 2500 \text{ kW} / 48 \text{ V} = 52 \text{ A}$

$$\Delta i_{Lmax} = \frac{V_O (1 - D_{min})}{f_s L} = 31.542 \text{ A}$$

$$d i_{Kmax} = 0.1 \times I_{Lmax} = 3.318 \text{ A}$$

$$n = \frac{\eta_{max}}{M_{Vmax}} = \frac{n \times P_{max}}{0.318} = 2$$

$$M_{Vmax} = \frac{V_O}{V_{Imin}} = \frac{48}{127} = 0.378$$

$$\begin{aligned} I_{Gmax} &= \frac{I_{Omax}}{n} + \frac{\Delta i_{Lmax}}{2n} + \frac{d i_{Lmax}}{2n} \\ &= \frac{52}{2} + \frac{31.542}{2 \times 2} + \frac{3.318}{2} \\ &= 35.6 \text{ A} \end{aligned}$$

$$I_{h_{max}} = I_{aux} + \frac{0.7L_{cr}}{2}$$

$$\Rightarrow 52 + \frac{31.6}{2} = 67.8 \text{ A}$$