

3.3 Hw Solutions:

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Question 1:

Solution:



Question 2:

Solution:



Question 3:

Solution:



Question 4:

Solution:



Question 5:

Solution:



Question 6:

Solution:



$$\begin{aligned}f(x) &= 2x \\f'(x) &= 2.\end{aligned}$$

$$\begin{aligned}g(x) &= 7 - \tan(x) \\g'(x) &= -\sec^2 x.\end{aligned}$$

Now:

$$\begin{aligned}F'(x) &= \frac{(7 - \tan x)(2) - (2x)(-\sec^2 x)}{(7 - \tan x)^2} \\&= \frac{14 - 2 \tan x + 2x \sec^2 x}{(7 - \tan x)^2} \\&= \frac{2(7 - \tan x + x \sec^2 x)}{(7 - \tan x)^2}.\end{aligned}$$

Question 7:

Solution:



$$F(x) = \frac{1 + \sec w}{1 - \sec w}.$$

If:

$$\begin{aligned}f(w) &= 1 + \sec w \\f'(x) &= \sec w \tan w.\end{aligned}$$

$$\begin{aligned}g(w) &= 1 - \sec w \\g'(x) &= -\sec w \tan w.\end{aligned}$$

Then:

$$\begin{aligned}F'(w) &= \frac{(1 - \sec w)(\sec w \tan w) - (1 + \sec w)(-\sec w \tan w)}{(1 - \sec w)^2} \\&= \frac{\sec w \tan w[(1 - \sec w) - (1 + \sec w)(-1)]}{(1 - \sec w)^2} \\&= \frac{\sec w \tan w[(1 - \sec w) + (-1 - \sec w)(-1)]}{(1 - \sec w)^2} \\&= \frac{\sec w \tan w[1 - \sec w + 1 + \sec w]}{(1 - \sec w)^2} \\&= \frac{\sec w \tan w[2]}{(1 - \sec w)^2} \\&= \frac{2 \sec w \tan w}{(1 - \sec w)^2}.\end{aligned}$$

Question 8:

Solution:



Part 1:

$$\begin{aligned}f(t) &= t \\f'(t) &= 1.\end{aligned}$$

$$\begin{aligned}g(t) &= \sin t \\g'(t) &= \cos t.\end{aligned}$$

So:

$$\begin{aligned}F'(t) &= t \cdot \cos t + \sin t \cdot 1 \\&= t \cos t + \sin t.\end{aligned}$$

Part 2:

$$\begin{aligned}G'(t) &= 0 + 1 \\&= 1.\end{aligned}$$

Part 3:

$$\begin{aligned} F'(t) &= \frac{(1+t)(t \cos t + \sin t) - t \sin t}{(1+t)^2} \\ &= \frac{(1+t)(t \cos t + \sin t) - t \sin t}{(1+t)^2} \\ &= \frac{t \cos t + \sin t + t^2 \cos t + t \sin t - t \sin t}{(1+t)^2} \\ &= \frac{t \cos t + \sin t + t^2 \cos t}{(1+t)^2} . \end{aligned}$$

Question 9:

Solution:

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$$\begin{aligned} \frac{d}{dx} \csc x &= \frac{d}{dx} \frac{1}{\sin x} \\ &= \frac{\sin x \cdot 0 - 1 \cdot \cos x}{\sin^2 x} \\ &= \frac{-\cos x}{\sin^2 x} \\ &= \frac{1}{\sin x} \cdot \frac{\cos x}{\sin x} \\ &= -\csc x \cot x. \end{aligned}$$

Question 10:

Solution:

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$$\begin{aligned} f(x) &= 12x \\ f'(x) &= 12. \end{aligned}$$

$$\begin{aligned} g(x) &= \sin x \\ g'(x) &= \cos x. \end{aligned}$$

Now:

$$\begin{aligned} y' &= 12x \cdot \cos x + \sin x \cdot 12 \\ &= 12x \cos x + 12 \sin x \\ &= 12(x \cos x + \sin x) \end{aligned}$$

Second part of a.)

$$\begin{aligned} &12\left(\frac{\pi}{2} \cos \frac{\pi}{2} + \sin \frac{\pi}{2}\right) \\ &= 12\left(\frac{\pi}{2}(0) + 1\right) \\ &= 12(1) \\ &= 12. \end{aligned}$$

With this:

$$y - y_1 = m(x - x_1)$$

so

$$y - 6\pi = 12\left(x - \frac{\pi}{2}\right)$$

$$\begin{aligned}y - 6\pi &= 12x - 6\pi \\ &= y = 12x.\end{aligned}$$

Question 11:

Solution:



Question 12:

Solution:



Question 13:

Solution:



Question 14:

Solution:

