logic pset5

Resources: Chapter 6 (pp 99-113) of How Logic Works.

Prove the following sequents using the propositional logic rules plus UE, UI, EI, and EE.

1.
$$\exists x(Fx \to Gx) \vdash \forall xFx \to \exists xGx$$

2.
$$\forall x \exists y (Fy \to Gx) \vdash \forall y Fy \to \forall x Gx$$

3.
$$\exists x(Fx \lor Gx), \neg \exists xFx \vdash \exists yGy$$

4.
$$P \to \exists x Fx \vdash \exists x (P \to Fx)$$