

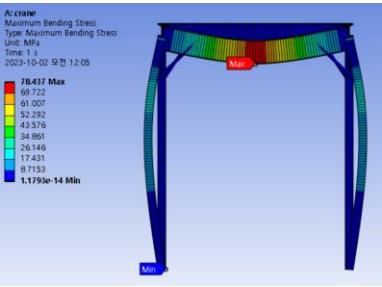
HW3 Simulation : Gantry Crane

(Use SI unit by conversion)

A gantry crane is designed that must be able to lift 10 tons (use 100kN) as it must lift compressors, motors, heat exchangers, and controls. This load should be placed at the center of one of the main 12-ft-long beams (use 1ft=0.3m) as shown below by the hoisting device location. Weight of the structure is ignored in the analysis. Assume you are using ASTM A36 structural steel (SS400). The crane must be 12 feet long, 8 feet wide, and 15 feet high. The beams should all be the same size, the columns all the same size, and the bracing all the same size. Their cross sections are selected from Appendix F (4th ed.) and shown below. You must verify that the structure is safe by checking the beam's bending strength and allowable deflection. A required safety factor against material yielding of the beam is 3. Verify that the beam deflection is less than $L/360$ ($12/360\text{ft}=10\text{mm}$, downward deflection of the beam center with respect to the ground), where L is the span of the beam. Check yielding and Euler buckling of the long columns. A required factor of safety is 3 against yielding of the column and 5 against buckling of the column. (Ignore local buckling of the horizontal beam) Assume the column-to-beam joints to be rigid while the bracing (a total of eight braces) is pinned to the column and beam at each of the four corners. Use appropriate boundary conditions for the four supports of the gantry crane.

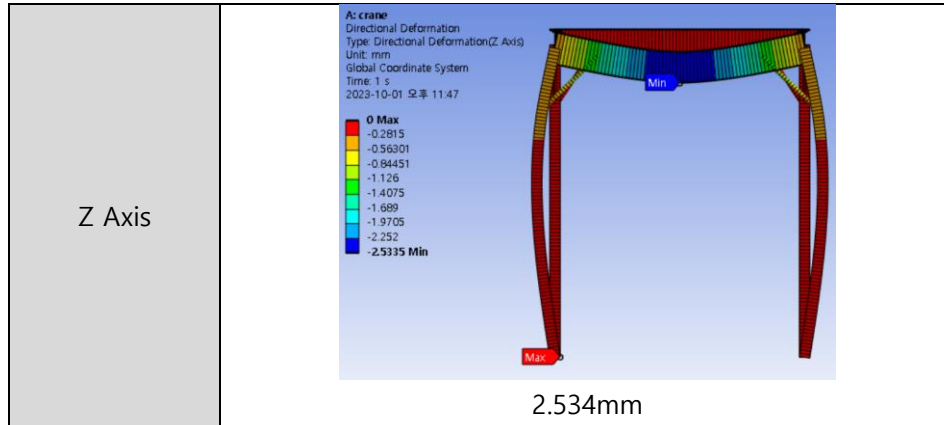
1. Generate an ANSYS beam model and get safety factors and deflections
2. Compare simulation results with appropriate theoretical results (stresses and downward deflections of the horizontal beam, critical buckling load of the columns)
3. Discuss on boundary conditions of the four supports
4. What do you think the function of the braces are?
5. How many number of elements is required to accurately solve this problem?

1. Generate an ANSYS beam model and get safety factors and deflections



Safety Factor = $\frac{250 \text{ MPa}}{78.437 \text{ MPa}} = 3.187$

Mode	Deflections
Total	<div><p>Ac crane Total Deformation Type: Total Deformation Unit: mm Time: 1 s 2023-09-30 오후 10:44</p><p>2.5366 Max 2.2549 1.9733 1.6916 1.41 1.1289 0.8467 0.56506 0.28342 0.0017799 Min</p></div> <p>2.537mm</p>
X Axis	<div><p>Ac crane Directional Deformation Type: Directional Deformation(X Axis) Unit: mm Global Coordinate System Time: 1 s 2023-10-01 오후 11:46</p><p>0.59714 Max 0.51703 0.43693 0.35982 0.27671 0.19561 0.1165 0.036395 -0.043711 -0.12382 Min</p></div> <p>0.597mm</p>
Y Axis	<div><p>Ac crane Directional Deformation Type: Directional Deformation(Y Axis) Unit: mm Global Coordinate System Time: 1 s 2023-10-01 오후 11:46</p><p>2.0336 Max 1.5817 1.1298 0.67788 0.22596 -0.22596 -0.67788 -1.1298 -1.5817 -2.0336 Min</p></div> <p>2.034mm</p>



The beam deflections are less than 10mm, so it's safe.

2. Compare simulation results with appropriate theoretical results (stresses and downward deflections of the horizontal beam, critical buckling load of the columns)

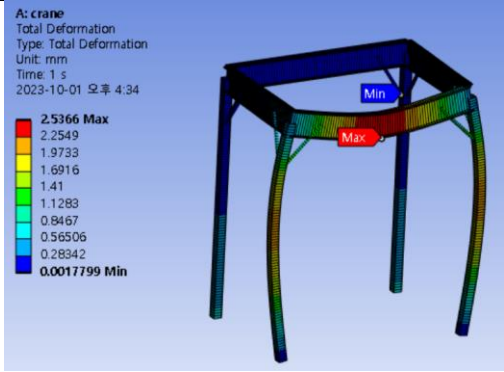
$$I = \frac{bh^3}{12}$$

The following cross-sectional moments were obtained using the above formula.

$$I_{beam} = 250.73 \times 10^6 \text{ mm}^4 = 250.73 \times 10^{-6} \text{ m}^4$$

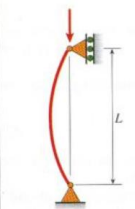
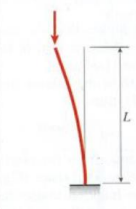
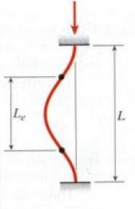
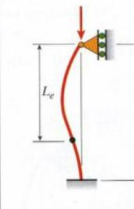
$$I_{RectTube} = 10.23 \times 10^6 \text{ mm}^4 = 10.23 \times 10^{-6} \text{ m}^4$$

	Theoretical	Simulation
Stress of the horizontal beam	$M = \frac{FL}{4} = \frac{10^5 \times (12 \times 0.3)}{4} = 90000 \text{ N} \cdot \text{m}$ $\sigma = \frac{MC}{I} = \frac{90000 \times \frac{454.66}{2}}{250.73 \times 10^{-6}} = 81.6 \text{ MPa}$	<p>A: crane Maximum Bending Stress Type: Maximum Bending Stress Unit: MPa Time: 1 s 2023-10-01 오전 10:53</p> <p>78.437 Max 69.722 61.007 52.292 43.576 34.861 26.146 17.431 8.7153 1.1793e-14 Min</p> <p>78.437 MPa</p>

Downward deflections of the horizontal beam	$\delta = \frac{F \cdot L^3}{48EI} + \frac{F}{2} \cdot \frac{L_{col}}{EA}$ $= \frac{10^5 \times (12 \times 0.3)^3}{48 \times 200 \times 10^9 \times 250.73 \times 10^{-6}}$ $+ \frac{\frac{10^5}{2} \times 15 \times 0.3}{200 \times 10^9 \times 2812.5 \times 10^{-6}}$ $= 2.34 \times 10^{-3} m = 2.34 mm$	<div><div>As crane Total Deformation Type: Total Deformation Unit: mm Time: 1 s 2023-10-01 오후 4:34</div><div><div>2.5366 Max 2.2549 1.9733 1.6916 1.41 1.1283 0.8467 0.56506 0.28342 0.0017799 Min</div></div><div>2.5366mm</div></div>															
Critical buckling load of the columns	$P_{cr} = \frac{n \pi^2 EI}{L^2}$ $= 249299 N$	<table><tr><td></td><td>Mode</td><td><input checked="" type="checkbox"/> Load Multiplier</td></tr><tr><td>1</td><td>1.</td><td>-4.2233</td></tr><tr><td colspan="2">X Component</td><td>0. N (ramped)</td></tr><tr><td colspan="2">Y Component</td><td>0. N (ramped)</td></tr><tr><td colspan="2">Z Component</td><td>-1.e+005 N (ramped)</td></tr></table> $P_{cr} = 4.2233 \times \frac{10^5}{2} = 211165 N$		Mode	<input checked="" type="checkbox"/> Load Multiplier	1	1.	-4.2233	X Component		0. N (ramped)	Y Component		0. N (ramped)	Z Component		-1.e+005 N (ramped)
	Mode	<input checked="" type="checkbox"/> Load Multiplier															
1	1.	-4.2233															
X Component		0. N (ramped)															
Y Component		0. N (ramped)															
Z Component		-1.e+005 N (ramped)															

The theoretical value and the simulation value came out similar.

3. Discuss on boundary conditions of the four supports

(a) Pinned-pinned column	(b) Fixed-free column	(c) Fixed-fixed column	(d) Fixed-pinned column
$P_{cr} = \frac{\pi^2 EI}{L^2}$	$P_{cr} = \frac{\pi^2 EI}{4L^2}$	$P_{cr} = \frac{4\pi^2 EI}{L^2}$	$P_{cr} = \frac{2.046 \pi^2 EI}{L^2}$
			

As you can see in the picture above, the buckling value comes out differently depending on the boundary condition. Therefore, buckling may occur better depending on the boundary conditions of the four supports of the crane. In the case of Fixed support, also called pinned support, The support is completely fixed to the ground, making it impossible to move and rotate. In the case of Roller support, it is fixed up and down, but it can be moved left and right. In the case of Hinge, it can't move from side to side, up and down, but only rotate.

4. What do you think the function of the braces are?

Brace distributes the load and reduces the stress concentration. This prevents the structure from being destroyed. In other words, it increases stability and strength.

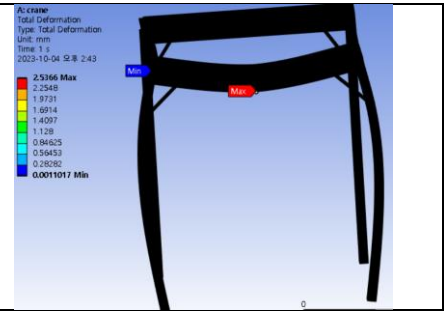
5. How many number of elements is required to accurately solve this problem?

Mesh sizing	Elements	Simulation
311.15(default)	<div> <div>Statistics</div> <div> <input type="checkbox"/> Nodes 256 <input type="checkbox"/> Elements 132 </div> </div>	
100	<div> <div>Statistics</div> <div> <input type="checkbox"/> Nodes 768 <input type="checkbox"/> Elements 388 </div> </div>	
50	<div> <div>Statistics</div> <div> <input type="checkbox"/> Nodes 1544 <input type="checkbox"/> Elements 776 </div> </div>	
30	<div> <div>Statistics</div> <div> <input type="checkbox"/> Nodes 2584 <input type="checkbox"/> Elements 1296 </div> </div>	

10

Statistics

<input type="checkbox"/> Nodes	7736
<input type="checkbox"/> Elements	3872



Changes in mesh sizing 50 or less did not appear as much as 50 or more. Element values differ when switching to values below 50, but total deformation changes are insignificant. Also, it takes a lot of time. Therefore, when the element number is 776 when the mesh sizing is 50, it is accurate.