Algorithms and Data Structures CH08-320201

Homework 3

Fibonacci Numbers and Recurrences

Problem 3.1

a. C++ source file

b.

| (N) | Naïve Recursive | Bottom Up | Closed Form | Matrix Multiplication |
|-------|-----------------|-----------|-------------|-----------------------|
| 10 | 0 | 0 | 0 | 0 |
| 20 | 0.001 | 0 | 0 | 0 |
| 30 | 0.011 | 0 | 0 | 0 |
| 40 | 1.194 | 0 | 0.001 | 0 |
| 50 | - | 0 | 0.001 | 0 |
| 100 | | 0.001 | 0 | 0 |
| 500 | | 0.001 | 0 | 0 |
| 1000 | | 0.001 | | 0.001 |
| 5000 | | 0.001 | | 0.001 |
| 10000 | | | | |

c. For N greater than 40, the naïve recursive algorithm fails to return a value. For N greater than 1000, the closed form algorithm also fails to return an accurate Fibonacci sequence and for N values greater than 10,000 the remaining two algorithms also return inaccurate values for the Fibonacci sequence.

This is because the larger the number gets the algorithm cannot approximate the correct Fibonacci sequence. Because approximation loses its accuracy for the algorithms.

d.

Problem 3.2

a.