Woodbury Matrix Identity	$(A + UCV)^{-1} = A^{-1} - A^{-1}U(C^{-1} + VA^{-1}U)^{-1}VA^{-1}$
Sherman Morrison Formula	Given invertible $A \in R^{n \times n}$ and $u, v \in R^n$ vectors. Then $A + uv^T$ is invertible iff $1 + v^T A^{-1} u \neq 0$ . Then $(A + uv^T)^{-1} = A^{-1} - \frac{A^{-1} uv^T A^{-1}}{1 + v^T A^{-1} u}$
Cauchy Schwarz Inequality	$ \langle U, V \rangle  \le \langle U, U \rangle \dot{\langle} V, V \rangle$
Markov Inequality	X is a non-negative rv and $a > 0$ then $P(X \ge a) \le \frac{E(X)}{a}$
Minkowski inequality	$  f + g  _p \le   f  _p +   g  _p$
Holder Inequality	Let $p,q\in [1,\infty], 1/p+1/q=1$ . Then for all real/complex functions $f,g,\ fg\ _1\leq \ f\ _p\ g\ _q$
Jensen Inequality	Given X is a rv and $\phi$ is convex. Then $\phi(E(X)) \leq E(\phi(X))$
Johnson Lindenstrauss Property	A distribution on matrices $S \in \mathbb{R}^{k \times n}$ has $(\epsilon, \delta, l)$ -JL moment property if $\forall x \in \mathbb{R}^n,  x _2 = 1, E_S(  Sx _2^2 - 1 ^l) \le \epsilon^l \delta$
Hoeffding Inequality	Let $X_1, \dots, X_n$ be independent rv in $[0,1]$ . Let $\bar{X} = \frac{1}{n} \sum_i X_i$ . Then $P(\bar{X} - E(\bar{X}) \ge t) \le \exp(-2nt^2)$
Chebyshev Inequality	$P( X - E(X)  \ge a) \le \frac{Var(X)}{a^2}$
Golden Thompson	For Hermitian matrices A,B $tr \exp(A + B) \le tr(\exp(A) \exp(B))$
Oppenheimer Inequality	For PSD matrices A, B, $\det(A \circ B) \ge (\prod a_{ii}) \det(B)$
Ky Fan Matrix Inequality	Let A, B be $n \times n$ Hermitian matrices. Then $\lambda(A) + \lambda(B) > \lambda(A+B)$ , where $>$ denotes the majorization relation.
McDiarmid Inequality	Multidimensional Hoeffding. Let $X_1,X_m$ be independent rv taking values in $\chi$ . Further, let $f: \chi^m \mapsto \mathbb{R}$ be a function of $X_1,,X_m$ that satisfies coordinate-wise bounded differences, $\forall i \forall x_1,x_m, x_i^* \in \chi$ , $ f(x_1,,x_i,x_m) - f(x_1,,x_i^*,x_m)  \leq c_i$ . Then $\mathbb{P}( f - \mathbb{E}(f)  \geq \epsilon) \leq \exp\left(\frac{-2\epsilon^2}{\sum_{i=1}^m c_i^2}\right)$ .
Cortes Sampling Concentration Inequality	Let $X_i, i \in [m]$ be a set of drawn without replacement from an underlying finite set of $m+u$ elements. Let $f: \chi^m \mapsto \mathbb{R}$ be a function of $X_1,, X_m$ be symmetric (up to permutation of parameters) and obey coordinate-wise bounded differences, then $\mathbb{P}( f-\mathbb{E}(f)  \ge \epsilon) \le \exp\left(\frac{-2\epsilon^2}{\alpha(m,u)c^2}\right)$ , where $\alpha(m,u) = \frac{mu}{m+u-0.5} \times \frac{1}{1-1/(2\max(m,u))}$ .
Simple Gaussian Concentration Inequality	Let $X_1, X_n$ be iid $(0,1)$ Gaussian rv. Let $f: \mathbb{R}^n \to \mathbb{R}$ be 1-Lipschitz. Then for any $\lambda > 0$ , $\mathbb{P}( f(X) - \mathbb{E}(f(X))  \ge \lambda) \le C \exp(-c\lambda^2)$ for constants $c, C$ .
Bounds for central term in binomial coefficient	$\frac{4^n}{2n+1} \le \binom{2N}{N} \le 4^n$

Generating function of Catalan Numbers	$G(z) = \sum_{i=0}^{\infty} \frac{1}{n+1} {2n \choose n} z^i = \frac{1-\sqrt{1-4z}}{2z} = \frac{2}{1+\sqrt{1-4z}}$
Weyl Matrix Perturbation Inequality	If $M = H + P$ are $n \times n$ matrices with eigenvalues $\mu_i, \nu_i, \rho_i$ (ordered in descending order) respectively, then $\nu_i + \rho_n \leq \mu_i \leq \nu_i + \rho_1$
Walds Identity	Let $X_1,$ be a sequence of (potentially infinite) independent random variables with identical means. Let $N$ be any <i>stopping time</i> (or independent of $X_s$ ). Let $S_N = \sum_{i=1}^N X_i$ . Then $\mathbb{E}(S_N) = \mathbb{E}(N)\mathbb{E}(X)$ . Note $N$ can be weakly dependent on $X$ .
Variance of Random Sum	If N and $X_i$ are independent and Xs have equal variance, $\operatorname{Var}(\sum_{i=1} X) = \mathbb{E}(N)\operatorname{Var}(X_i) + \mathbb{E}(X)^2\operatorname{Var}(N)$
Eckart-Young-Mirsky Theorem	The k-truncated SVD of a matrix $A$ gives the best rank-k approximation for $A$ in the spectral and frobenius norm. $A_k = U\Sigma_k V^T = argmin_{\rm B\ rank-k} A-B _2 = \sigma_{k+1}(A)$
Wolfe Conditions	(i) (Armijo rule) $f(\mathbf{x}_k + \alpha_k \mathbf{p}_k) \leq f(\mathbf{x}_k) + c_1 \alpha_k \mathbf{p}_k^{\mathrm{T}} \nabla f(\mathbf{x}_k)$ (ii) (Curvature) $-\mathbf{p}_k^{\mathrm{T}} \nabla f(\mathbf{x}_k + \alpha_k \mathbf{p}_k) \leq -c_2 \mathbf{p}_k^{\mathrm{T}} \nabla f(\mathbf{x}_k)$ , where $\alpha_k$ is step size, $\mathbf{p}_k$ is descent direction and $0 < c_1 < c_2 < 1$