

8.1

According to Michaelis-Menten's kinetics equations, at low concentrations of substrate, [S], the concentration is almost negligible in the denominator as $K_M \gg [S]$, so the equation is essentially

$$V_0 = k_3[ES]$$

$$K_s = k_2/k_1 = [S][E]/[ES]$$

$$[ES] = [E_{tot}] - [E]$$

$$V_0 = K_3[E_{tot}][S]/(K_s + [S])$$

$$\text{Rate of formation of ES} = k_1[E][S]$$

$$\text{Rate of breakdown of ES} = (k_2 + k_3) [ES]$$

$$k_1[E][S] = (k_2 + k_3) [ES]$$

$$[ES] = [E_{tot}] - [E]$$

$$K_m = (k_2 + k_3)/k_1$$

$$V_0 = V_{max} [S]/(K_m + [S])$$

At High substrate concentrations, $[S] \gg K_M$, and thus the term $[S]/([S] + K_M)$ becomes essentially one and the initial velocity approached V_{max} , which resembles zero order reaction.

The Michaelis-Menten equation is:

$$V_0 = V_{max}[S]/([S] + K_m)$$

8.2

Python:

$$k_1 = 100.0 / 60.0 \quad \# \mu\text{M}/\text{min}$$

$$k_2 = 600.0 / 60.0 \quad \# / \text{min}$$

$$k_3 = 150.0 / 60.0 \quad \# / \text{min}$$

$$E_0 = 1.0 \quad \# \mu\text{M}$$

$$S_0 = 10.0 \quad \# \mu\text{M}$$

$$ES_0 = 0.0 \quad \# \mu\text{M}$$

$$P_0 = 0.0 \quad \# \mu\text{M}$$

$$t_0 = 0.0 \quad \# \text{min}$$

$$t_{end} = 20.0 \quad \# \text{min}$$

$$dt = 0.01 \quad \# \text{min}$$

def f(y, t):

$$E, S, ES, P = y$$

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dEdt = -k1 * E * S + k2 * ES
dSdt = -k1 * E * S + k2 * ES
dESdt = k1 * E * S - k2 * ES - k3 * ES
dPdt = k3 * ES
return [dEdt, dSdt, dESdt, dPdt]

t = np.arange(t0, tend + dt, dt)
n = t.size
y = np.zeros((n, 4))
y[0, :] = [E0, S0, ES0, P0]

k1 = f(y[i, :], t[i])
k2 = f(y[i, :] + 0.5 * dt * k1, t[i] + 0.5 * dt)
k3 = f(y[i, :] + 0.5 * dt * k2, t[i] + 0.5 * dt)
k4 = f(y[i, :] + dt * k3, t[i] + dt)
y[i + 1, :] = y[i, :] + dt / 6.0 * (k1 + 2.0 * k2 + 2.0 * k3 + k4)

plt.plot(t, y[:, 0], label="E")
plt.plot(t, y[:, 1], label="S")
plt.plot(t, y[:, 2], label="ES")
plt.plot(t, y[:, 3], label="P")
plt.legend()
plt.xlabel("Time (min)")
plt.ylabel("Concentration (μM)")
plt.show()

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8.3

