问题4

```
In [1]: # TODO import
        import re
        import os
        import sys
        import hmz
        import pathlib
        import mitosheet
        import numpy as np
        import pandas as pd
        import matlab.engine
        import scipy
        from scipy.integrate import odeint
        from scipy.optimize import minimize
        import time
        from time import time, sleep
        import copy
        import random
        import sympy
        from sympy import limit
        from sympy import diff
        from sympy import integrals
        import sklearn
        import graphviz
        from sklearn import tree
        from sklearn.model_selection import cross_val_score
        from sklearn.model_selection import train_test_split
        from sklearn.metrics import r2_score
        from sklearn.metrics import mean_squared_error as MSE
        from sklearn.metrics import mean_absolute_error as MAE
        from sklearn.metrics import classification_report, roc_auc_score
        import sko
        from sko.GA import GA
```

```
import numba
from numba import jit
import plotly
import plotly.express as px
import plotly.graph objects as go
import plotly.figure factory as ff
plotly.offline.init notebook mode()
import cufflinks as cf
cf.set config file(
    offline=True,
    world readable=True,
    theme='pearl', # cf.getThemes()
import matplotlib.pyplot as plt
plt.rcParams['font.sans-serif'] = ['SimHei'] # KaiTi
plt.rcParams['axes.unicode_minus'] = False
from IPython.core.interactiveshell import InteractiveShell
InteractiveShell.ast_node_interactivity = 'all'
# InteractiveShell.ast node interactivity = 'last'
import cv2 as cv
# import torch
# import torchvision
# import torch.nn as nn
# import torch.nn.functional as F
# import torch.utils.data as Data
# from torch.utils.data import DataLoader
# from torch.utils.data.dataset import Dataset
import pylatex
import latexify
import warnings
warnings.filterwarnings("ignore")
```

```
import logging
        fmt = '%(asctime)s - %(levelname)8s - %(message)s'
        formatter = logging.Formatter(fmt)
        handler control = logging.StreamHandler() # stdout to console
        handler control.setLevel('INFO') # 设置 INFO 级别
        handler control.setFormatter(formatter)
        logger = logging.getLogger()
        # Logger.setLevel('INFO')
        logger.addHandler(handler control)
        def timeit(text):
            def func deco(func):
                """ 用来计时的装饰器函数 """
                def func wrapper(*args, **kwargs):
                    from time import time
                    t0 = time()
                     Logging.info(text + "开始计时")
                   print(Fore.RED, text + "开始计时: ", Fore.RESET)
                    res = func(*args, **kwargs)
                   t1 = time()
                     logging.info(text + "用时: " + str(t1 - t0) + "s")
                   print(Fore.RED, text + "结束计时, 用时: ", str(t1 - t0), "s", Fore.RESET)
                    return res
                return func wrapper
            return func deco
In [3]: # TODO DIR
        ROOTDIR = pathlib.Path(os.path.abspath('.'))
        IMG_HTML = ROOTDIR / 'img-html'
        IMG SVG = ROOTDIR / 'img-svg'
        DATA RAW = ROOTDIR / 'data-raw'
        DATA_COOKED = ROOTDIR / 'data-processed'
In [4]: # TODO 附件4参数
```

```
扭转弹簧刚度 = 250000 # N·m
静水恢复力矩系数 = 8890.7 # N·m
```

In [74]: # TODO 附件3参数 class question1234: """设置具体问题几的参数""" def init (self, question): global 入射波浪频率 global 垂荡附加质量 global 纵摇附加转动惯量 global 垂荡兴波阻尼系数 global 纵摇兴波阻尼系数 global 垂荡激励力振幅 global 纵摇激励力矩振幅 global 波浪频率 global 波浪周期 if question == 1: # 问题1: 参数 # 纵摇附加转动惯量 = 6779.315 # kq·m^2 # 纵摇兴波阻尼系数 = 151.4388 # N·m·s # 纵摇激励力矩振幅 = 1230 # N·m 纵摇附加转动惯量 = None # 问题1未使用,为避免使用/误用,初始化为 None 纵摇兴波阻尼系数 = None # 问题1未使用,为避免使用/误用,初始化为 None 纵摇激励力矩振幅 = None # 问题1未使用,为避免使用/误用,初始化为 None 入射波浪频率 = 1.4005 # s^{-1} 垂荡附加质量 = 1335.535 # ka 垂荡兴波阻尼系数 = 656.3616 # N·s/m 垂荡激励力振幅 = 6250 # N 波浪频率 = 入射波浪频率 波浪周期 = 1 / 波浪频率 elif question == 2: # 问题2: 参数 # 纵摇附加转动惯量 = 7131.29 # 纵摇兴波阻尼系数 = 2992.724 # 纵摇激励力矩振幅 = 2560 纵摇附加转动惯量 = None # 问题2未使用,为避免使用/误用,初始化为 None 纵摇兴波阻尼系数 = None # 问题2未使用,为避免使用/误用,初始化为 None 纵摇激励力矩振幅 = None # 问题2未使用,为避免使用/误用,初始化为 None 入射波浪频率 = 2.2143 垂荡附加质量 = 1165.992 垂荡兴波阻尼系数 = 167.8395 垂荡激励力振幅 = 4890 波浪频率 = 入射波浪频率

波浪周期 = 1 / 波浪频率

```
elif question == 3:
                # 问题3: 参数
                入射波浪频率 = 1.7152
                垂荡附加质量 = 1028.876
                纵摇附加转动惯量 = 7001.914
                垂荡兴波阻尼系数 = 683.4558
                纵摇兴波阻尼系数 = 654.3383
                垂荡激励力振幅 = 3640
                纵摇激励力矩振幅 = 1690
                波浪频率 = 入射波浪频率
                波浪周期 = 1 / 波浪频率
             elif question == 4:
                # 问题4: 参数
                入射波浪频率 = 1.9806
                垂荡附加质量 = 1091.099
                纵摇附加转动惯量 = 7142.493
                垂荡兴波阻尼系数 = 528.5018
                纵摇兴波阻尼系数 = 1655.909
                垂荡激励力振幅 = 1760
                纵摇激励力矩振幅 = 2140
                波浪频率 = 入射波浪频率
                波浪周期 = 1 / 波浪频率
             return None
      class trange:
          """设置时间区间和间隔的参数"""
         def __init__(self, left, right, step):
             global t_left
             global t_right
             global t_step
             t left = left
             t_right = right
             t_step = step
             return None
      _{\rm } = question1234(4)
      _ = trange(0, 200, 0.2)
In [6]: # TODO 跟变量有关的参数函数(这个后面有用,但是用处不大)
```

def S浮子底面积_func(r=浮子底半径):
 return np.pi * r**2
S浮子底面积 = S浮子底面积_func()

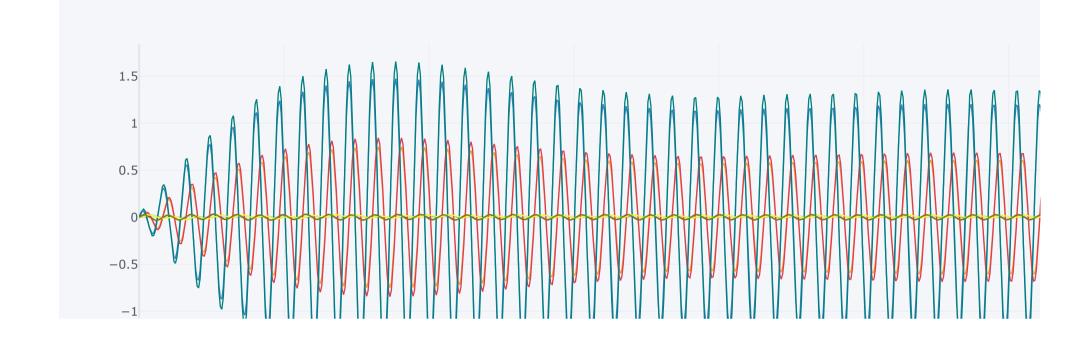
```
def V排 func(h, pprint=True):
   :param h: 圆柱壳体的入水深度
   :param pprint: 是否打印状态
   :return: V排 (m^3)
   if h >= 0:
      print("圆锥壳体完全浸没")
      V排 = (1/3 * S浮子底面积 * 浮子圆锥部分高度) + (S浮子底面积 * h)
   else:
      print("圆锥壳体漂浮")
      depth = 浮子圆锥部分高度 + h
      r = 浮子底半径 * depth / 浮子圆锥部分高度
      V排 = 1/3 * S浮子底面积 func(r) * depth
   return V排
# print("浮子入水体积: ", V排 func(3))
# print("浮子入水体积: ", V排_func(2.4147))
# print("浮子入水体积: ", V排_func(0))
# print("浮子入水体积: ", V排_func(-0.001))
# print("浮子入水体积: ", V排 func(-0.8))
def F静水恢复力_func(h, pprint=False):
   """ 类似(就是)浮力 方向向上
   :param h: 圆柱壳体的入水深度
   :param pprint: 是否打印状态
   :return: F静水恢复力 (N)
   F静水恢复力 = 海水的密度 * 重力加速度 * V排_func(h, pprint)
   return F静水恢复力
# F静水恢复力_func(2.4147)
def F兴波阻尼力_func(v, k=垂荡兴波阻尼系数):
   """ 方向同速度方向
   :param v: 速度
   :return:
   F兴波阻尼力 = k * v
   return F兴波阻尼力
def F波浪激励力_func(t, omega=入射波浪频率, f=垂荡激励力振幅):
   """ 方向向上
   :param t: 时间
   :return: F波浪激励力 (N)
   F波浪激励力 = f * np.cos(omega * t)
```

```
return F波浪激励力
       # F波浪激励力 func(0)
       def F附加惯性力 func(m=垂荡附加质量, g=重力加速度):
          """ 方向向下 """
          F附加惯性力 = m * g
          return F附加惯性力
       F附加惯性力 = F附加惯性力 func()
       def F重力 func(m=浮子质量+振子质量, g=重力加速度):
          """ 方向向下 """
          F重力 = m * g
          return F重力
       F重力 = F重力 func()
       def c直线阻尼器的阻尼系数 func1():
          c直线阻尼器的阻尼系数 = 10000 # N·s/m
          return c直线阻尼器的阻尼系数
       def c直线阻尼器的阻尼系数_func2(v浮子, v振子, k=10000, a=0.5):
          c直线阻尼器的阻尼系数 = k * abs(v \% \% \% \% \% )**a # N·s/m
          return c直线阻尼器的阻尼系数
In [82]: # TODO 问题3: 参数
       m1, m2, me = 浮子质量, 振子质量, 垂荡附加质量
       j2 \text{ func} = 1 \text{ambda y3}: ((0.969588 + y3)**3 - (0.469558 + y3)**3) * m2 / 1.5 # y3
       j1, je = 33000, 纵摇附加转动惯量
       omega = 入射波浪频率
       c = 10000 # 直线阻尼器
       f = 垂荡激励力振幅
       k = 弹簧刚度
       k1 = -垂荡兴波阻尼系数
       k2 = -海水的密度 * 重力加速度 * S浮子底面积
       C = 1000 # 旋转阻尼器
       L = 纵摇激励力矩振幅
       K = 扭转弹簧刚度
       K1 = -纵摇兴波阻尼系数
       K2 = -静水恢复力矩系数
```

查看何时稳定

大约在 100s 左右稳定,取 100 - 200s

```
In [83]: # TODO ode func
         c = 10000 # 直线阻尼器
         C = 1000 # 旋转阻尼器
         def ode func(y, t):
             dy1 = y[2-1]
             dy3 = y[4-1]
             dy4 = c * (y[2-1] - y[4-1] * np.cos(y[7-1])) + k * (y[1-1] - y[3-1] * np.cos(y[7-1]))
             dy2 = f * np.cos(omega * t) + k1 * y[2-1] + k2 * y[1-1] - dy4
             dv2 /= m1 + me
             dy4 /= m2 * np.cos(y[7-1])
             j2 = j2 \text{ func}(y[3-1])
             dy5 = y[6-1]
             dv7 = v[8-1]
             dy8 = C * (y[6-1] - y[8-1]) + K * (y[5-1] - y[7-1])
             dy6 = L * np.cos(omega * t) + K1 * y[6-1] + K2 * y[5-1] - dy8
             dy6 /= j1 + je
             dy8 /= j2
             return [dy1, dy2, dy3, dy4, dy5, dy6, dy7, dy8]
In [84]: # TODO solve
         t = np.linspace(t_left, t_right, num=int(t_right / t_step) + 1)
         y0 = [0 \text{ for } in \text{ range}(8)]
         res4 = odeint(ode_func, y0, t)
In [85]: # TODO 绘图 (不保存该结果)
         def get_result4_df(t=t, result4=res4):
             columns = ['时间 (s)', '浮子垂荡位移 (m)', '浮子垂荡速度 (m/s)', '振子垂荡位移 (m)', '振子垂荡速度 (m/s)',
                        '浮子纵摇角位移 (rad)', '浮子纵摇角速度 (rad/s)', '振子纵摇角位移 (rad)', '振子纵摇角速度 (rad/s)']
             shijian = pd.DataFrame(t, columns=columns[:1])
             result4 = pd.DataFrame(result4, columns=columns[1:])
             result4 df = pd.concat([shijian, result4], axis=1)
             result4_df = result4_df.iloc[:, [0, 1, 2, 5, 6, 3, 4, 7, 8]]
             return result4 df
         result4 df = get result4 df()
         result4 df.iplot(x='时间 (s)',)
```



平均输出功率公式

平均输出功率:
$$P=rac{1}{t_2-t_1}\int_{t_1}^{t_2}F_G\Delta v+M_G\Delta\omega dt=rac{1}{t_2-t_1}\int_{t_1}^{t_2}c\Delta v^2+C\Delta\omega^2 dt$$

```
dy4 /= m2 * np.cos(y[7-1])
    i2 = i2 \text{ func}(v[3-1])
    dy5 = y[6-1]
    dv7 = v[8-1]
    dy8 = C * (y[6-1] - y[8-1]) + K * (y[5-1] - y[7-1])
    dy6 = L * np.cos(omega * t) + K1 * y[6-1] + K2 * y[5-1] - dy8
    dy6 /= j1 + je
    dy8 /= j2
    return [dy1, dy2, dy3, dy4, dy5, dy6, dy7, dy8]
def Power func(res, c, C):
    :param res: [X1, X1', X2, X2', theta1, theta1', theta2, theta2']
                [X1, V1, X2, V2, theta1, omega1, theta2, omega2]
    :param c: 直线
    :param C: 旋转
    :return: P
    0.00
    t stable = 100
    begin = int(t stable / t step)
   end = int(t_right / t_step)
   end = -2
    delta_V = (res[:, 1] - res[:, 3])**2
    delta_omega = (res[:, 5] - res[:, 7])**2
    power_i = c * delta_V + C * delta_omega
    power_ = power_i[begin:end+1]
   power = power_ * t_step # 矩形
   P = power.sum() / (t_right - t_stable)
    power = (power_[1:] + power_[:-1]) * t_step / 2 # 梯形
    P = power.sum() / (t right - t stable - t step)
   print(P)
    return P
def LMS_func(c, C, pprint=False):
    res = odeint(
        ode_func,
        [0 for _ in range(8)],
        np.linspace(t_left, t_right, num=int(t_right / t_step) + 1),
       args=(c, C),
    P = Power_func(res, c, C)
    if pprint:
        print("平均输出功率: ", P)
```

```
return P

def GA_func(c, C, pprint=False):
    """ sko 遗传目标函数 """
    P = LMS_func(c, C)
    target = -P
    return target

def Program_func(x):
    return GA_func(x[0], x[1], pprint=False)
```

解微分方程组

```
In [109... # TODO 求解器类
         class Solver:
             def init (self):
                 self.lb = 0
                 self.ub = 1e5
                 self.cs = None
                 self.CS = None
                self.pss = None
                self.jit = False
                self.epoch = 100
                self.pprint = False
             # TODO 遗传
             @timeit("遗传")
             def run_GA(self):
                ga = GA(
                    func=GA_func,
                    n_dim=2,
                    size_pop=50,
                    max_iter=200,
                    prob_mut=0.001,
                    lb=[self.lb, self.lb],
                    ub=[self.ub, self.ub],
                    constraint_eq=tuple(),
                    constraint_ueq=tuple(),
                    precision=1e-06,
                    early_stop=True,
                xbest, ybest = ga.run()
                 print("[直线阻尼器的阻尼系数,旋转阻尼器的阻尼系数]: ", xbest, "最大输出功率", -ybest)
                return xbest, -ybest
```

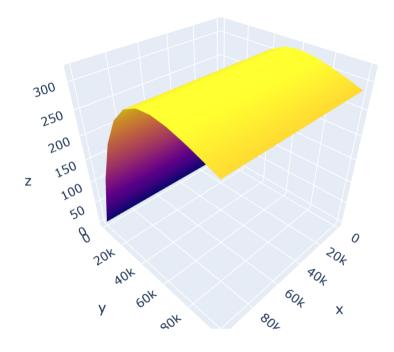
```
# TODO 规划
@timeit("规划")
def run Program(self, x0=[50000, 50000]):
    """ 规划 Program """
    opt = minimize(
       Program func,
       x0=x0
       bounds=((self.lb, self.ub), (self.lb, self.ub), ),
       method='trust-constr', # SLSQP trust-constr
         options={'xtol': 1e-30, 'qtol': 1e-30, 'disp': True},
    xbest = opt.x
   ybest = -Program func(xbest)
    print("[直线阻尼器的阻尼系数,旋转阻尼器的阻尼系数]: ", xbest, "最大输出功率", ybest)
    return xbest, ybest
# TODO 变步长
@timeit("变步长")
def run_LMS(self, *args, **kwargs):
    if self.jit:
       return self. run LMS jit(*args, **kwargs)
    else:
       return self._run_LMS_nojit(*args, **kwargs)
def _find_LMS_best(self, cs, CS, pss):
    self.cs = cs
    self.CS = CS
    self.pss = pss
   index = np.unravel_index(self.pss.argmax(), self.pss.shape)
    return [self.cs[index[0]], self.CS[index[1]]], self.pss[index]
def LMS main(self,
             cs_lb=0, cs_ub=1e5, cs_num=100, cs_alpha=0,
             CS lb=0, CS ub=1e5, CS num=100, CS alpha=0):
    t0 = time()
    batch_size = cs_num // self.epoch
    num len = len(str(cs num))
   fm = "%" + str(num_len) + "d/%" + str(num_len) + "d"
   if self.epoch is not None: # 用户的分割
       batch_size = cs_num // self.epoch
       if batch_size == 0: # 用户非法分割
           self.epoch = None
   if self.epoch is None: # 自动处理非法分割
       batch_size = cs_num // 100 # 分割 100 份
       self.epoch = 100
```

```
batch size = cs num // 10 if batch size == 0 else batch size # 分割 10 份
        self.epoch = 10
        batch size = cs num // 1 if batch size == 0 else batch size # 分割 1 份
        self.epoch = 1
    pss = np.zeros([cs num+1, CS num+1])
     cs0 = 58467,62477501568
     CS0 = 47662.22129472001
    cs lb = cs lb * (1 - cs alpha)
    cs ub = cs ub * (1 + cs alpha)
    CS lb = CS lb * (1 - CS alpha)
    CS ub = CS ub * (1 + CS alpha)
    cs = np.linspace(cs lb, cs ub, cs num+1)
   CS = np.linspace(CS lb, CS ub, CS num+1)
   for i, c in enumerate(cs):
       for j, C in enumerate(CS):
           pss[i, j] = LMS_func(c, C, pprint=False)
       if i % batch_size == 0:
           t1 = time()
           stars = '[' + '*' * (i // batch size) + '.' * ((cs num - i) // batch size) + ']'
           print(fm % (i, cs_num), _stars, round(t1 - t0, 2), "s/iter")
           t0 = time()
   xbest, ybest = self._find_LMS_best(cs, CS, pss)
    print("[直线阻尼器的阻尼系数,旋转阻尼器的阻尼系数]: ",xbest,"最大输出功率",ybest)
    return xbest, ybest
def _run_LMS_nojit(self, *args, **kwargs):
    return self._LMS_main(*args, **kwargs)
@jit
def _run_LMS_jit(self, *args, **kwargs):
    return self. LMS main(*args, **kwargs)
# TODO 绘图
def plot Surface(self, show=True, save=False):
   fig = go.Figure(data=[go.Surface(
       x=self.cs,
       y=self.CS,
       z=self.pss,
    )])
    if save:
       fig.write_image(IMG_SVG / '问题4-3D曲线图.svg')
    if show:
```

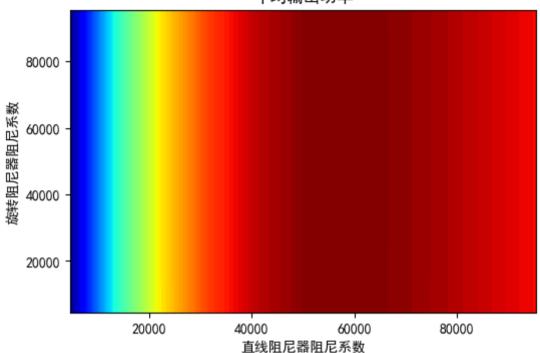
```
return True
            def plt contourf(self, show=True, save=False):
                mi, mx = self.pss.min(), self.pss.max()
                lb1, ub1, lb2, ub2 = self.cs.min(), self.cs.max(), self.CS.min(), self.CS.max()
                plt.figure(dpi=100)
                plt.contourf(self.pss.T, np.arange(mi, mx+1, (mx - mi) / 100), origin='lower', extent=[lb1, ub1, lb2, ub2], cmap=plt.cm.jet)
                plt.xlabel('直线阻尼器阻尼系数')
                plt.ylabel('旋转阻尼器阻尼系数')
                plt.title("平均输出功率")
                if save:
                   plt.savefig(IMG SVG / '问题4-二维等高线图.svg')
                if show:
                   plt.show()
                return True
            def plot_result(self, *args, **kwargs):
                self. plot Surface(*args, **kwargs)
                self. plt contourf(*args, **kwargs)
                return None
In [118... # TODO 单独运行求解
         _{\rm } = question1234(4)
         _ = trange(0, 150, 0.2)
         solver = Solver()
         solver.run GA() # 遗传
         solver.run Program() # 规划
         solver.run_LMS(cs_num=10, CS_num=10) # 变步长
         # solver.run LMS(cs num=100, CS num=100) # 遍历: 一般考验电脑性能, 预计用时: ∞(没试过不知道)
         # solver.run LMS(cs num=1000, CS num=1000) # 遍历:比较考验电脑性能,预计用时: ∞(没试过不知道)
         # solver.run_LMS(cs_num=10000, CS_num=10000) # 遍历: 究极考验电脑性能, 预计用时: ∞(没试过不知道)
         # solver.run LMS(cs num=100000, CS num=100000) # 遍历: 地狱考验电脑性能, 预计用时: ∞(没试过不知道)
         solver.plot_result(show=True, save=False) # 画图
         遗传开始计时:
         [直线阻尼器的阻尼系数,旋转阻尼器的阻尼系数]: [57536.87948714 31004.29883511] 最大输出功率 [317.69786004]
         遗传结束计时,用时: 25.64826989173889 s
Out[118]: (array([57536.87948714, 31004.29883511]), array([317.69786004]))
         规划开始计时:
         [直线阻尼器的阻尼系数,旋转阻尼器的阻尼系数]: [50000.23073816 49999.8185654 ] 最大输出功率 314.74575018315727
         规划结束计时,用时: 111.9183702468872 s
Out[118]: (array([50000.23073816, 49999.8185654]), 314.74575018315727)
```

fig.show()

Out[118]: ([60000.0, 50000.0], 317.6470046262132)

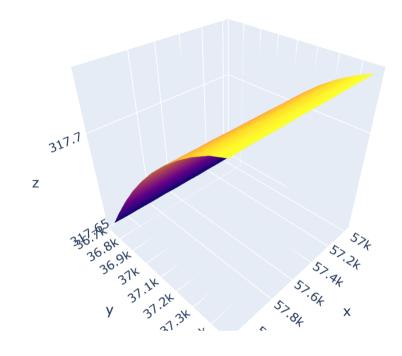


平均输出功率

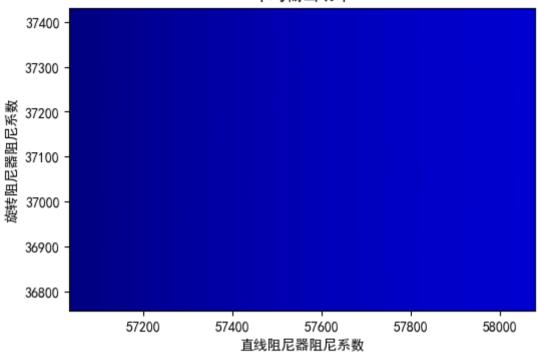


```
In [117... # TODO 联合运行求解
         _{\rm =} question1234(4)
         _ = trange(0, 150, 0.2)
         solver = Solver()
         solver.epoch = 10
         solver.pprint = False
         solver.jit = False
         # TODO GA + LMS
         t0 = time()
         xbest, ybest = solver.run_GA() # 遗传
         # xbest = (58467.64816206559, 47662.22129472)
         solver.run_LMS(cs_lb=xbest[0], cs_ub=xbest[0], cs_num=10, cs_alpha=0.1,
                        CS_lb=xbest[1], CS_ub=xbest[1], CS_num=10, CS_alpha=0.1) # 变步长
         print("总用时: ", time() - t0)
         solver.plot_result(show=True, save=False) # 绘图
         print('-' * 100)
         # TODO Program + LMS
         t0 = time()
         xbest, ybest = solver.run_Program() # 规划
```

```
# xbest = (58467.64816206559, 47662.22129472)
         solver.run LMS(cs lb=xbest[0], cs ub=xbest[0], cs num=10, cs alpha=0.1,
                      CS lb=xbest[1], CS ub=xbest[1], CS num=10, CS alpha=0.1) # 变步长
         print("总用时: ", time() - t0)
         solver.plot result(show=True, save=False) #绘图
          遗传开始计时:
         [直线阻尼器的阻尼系数,旋转阻尼器的阻尼系数]: [57556.41995171 37094.13072674] 最大输出功率 [317.70030272]
          遗传结束计时,用时: 26.062267065048218 s
          变步长开始计时:
          0/10 [.....] 5.01 s/iter
          1/10 [*.....] 5.0 s/iter
          2/10 [**.....] 5.01 s/iter
          3/10 [***.....] 4.94 s/iter
          4/10 [****.....] 5.07 s/iter
          5/10 [*****....] 5.12 s/iter
          6/10 [******....] 5.23 s/iter
          7/10 [****** ...] 5.16 s/iter
          8/10 [********..] 5.27 s/iter
          9/10 [********.] 5.13 s/iter
         10/10 [******** ] 4.93 s/iter
         [直线阻尼器的阻尼系数,旋转阻尼器的阻尼系数]: [58131.98415122411, 37316.695511103295] 最大输出功率 317.7262368268232
          变步长结束计时,用时: 55.871594190597534 s
Out[117]: ([58131.98415122411, 37316.695511103295], 317.7262368268232)
         总用时: 81.93683743476868
```



平均输出功率



规划开始计时:

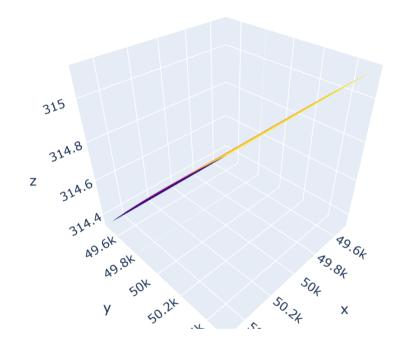
[直线阻尼器的阻尼系数,旋转阻尼器的阻尼系数]: [50000.23073816 49999.8185654] 最大输出功率 314.74575018315727 规划结束计时,用时: 126.50902438163757 s 变步长开始计时:

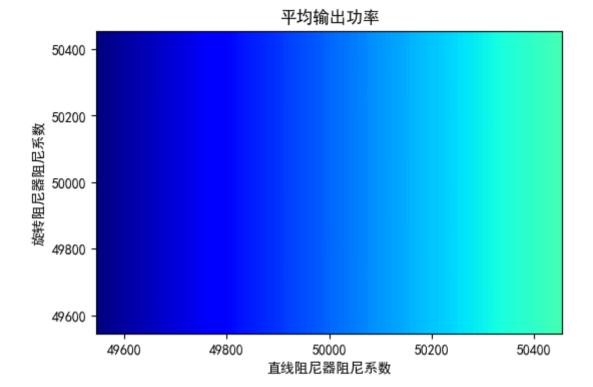
```
0/10 [......] 6.46 s/iter
1/10 [*.....] 5.82 s/iter
2/10 [**.....] 5.26 s/iter
3/10 [***....] 5.65 s/iter
4/10 [****....] 5.61 s/iter
5/10 [*****....] 5.31 s/iter
6/10 [******...] 5.57 s/iter
7/10 [******...] 7.26 s/iter
8/10 [*******..] 5.92 s/iter
9/10 [********.] 5.25 s/iter
10/10 [*********] 5.21 s/iter
```

[直线阻尼器的阻尼系数,旋转阻尼器的阻尼系数]: [50500.23304554521, 49499.82037974576] 最大输出功率 315.11129621858487 变步长结束计时,用时: 63.31871557235718 s

Out[117]: ([50500.23304554521, 49499.82037974576], 315.11129621858487)

总用时: 189.8307318687439





```
In []:
In []:
```