问题2

```
In [1]: import os
    import pathlib
    import plotly
    import numpy as np
    import pandas as pd
    from time import time
    from sklearn.cluster import KMeans
    from numba import jit, njit, prange
    import plotly.express as px
    import plotly.graph_objs as go
    from plotly.offline import init_notebook_mode, iplot
    init_notebook_mode(connected=True)

import warnings
warnings.filterwarnings("ignore")
```

```
In [2]: ROOTDIR = pathlib.Path(os.path.abspath('.'))
    IMG_HTML = ROOTDIR / 'img-html'
    IMG_PNG = ROOTDIR / 'img-png'
    IMG_SVG = ROOTDIR / 'img-svg'
    DATA_RAW = ROOTDIR / 'data-raw'
    DATA_COOKED = ROOTDIR / 'data-processed'
```

读数据

```
In [3]: weak_grid_data = pd.read_csv(DATA_RAW / '附件1 弱覆盖栅格数据(筛选).csv')
exist_site_data = pd.read_csv(DATA_RAW / '附件2 现网站址坐标(筛选).csv')
```

处理数据

最终得到问题2已有、新建、总的站点数据(具体如何处理的不小心 x 掉(删除)了,但是已经保存成了 csv 文件,直接读取数据即可,凑合看吧)以下是处理数据过程:

```
In [4]: # TODO judge
```

```
angle45 = np.pi / 4
        angle60 = np.pi / 3
        angle90 = np.pi / 2
        coverage = [10, 30]
        cost = [1, 10]
        @jit
        def get theta(x, y, m, n):
            if abs(x - m) < 1e-5: return angle90</pre>
            return np.arctan((y - n) / (x - m))
        @jit
        def get r th(theta delta, cover):
            if theta delta > angle60: return 0
            return cover * (1 - theta delta / angle60)
        @jit
        def check_angle(th1, th2):
            return abs(th1 - th2) < angle45</pre>
        @jit
        def judge_in(site, grid):
            x, y, i, j, cover = site[0], site[1], grid[0], grid[1], coverage[int(site[5]) - 1]
        # print(site[5], cover)
            if abs(x - i) > cover or abs(y - j) > cover: return False
            elif (x - i)**2 + (y - j)**2 > cover**2: return False
            else: return True
In [5]: q1 exist sites data = pd.read csv(DATA COOKED / "question1-exist site type data.csv", index col=0).iloc[:, 1:]
        q1_build_sites_data = pd.read_csv(DATA_COOKED / "question1-new_build_sites.csv", index_col=0)
        q1 exist sites data, q1 build sites data
        z_build = pd.DataFrame([0 for _ in range(len(q1_build_sites_data))])
        z_exist = pd.DataFrame([0 for _ in range(len(q1_exist_sites_data))])
        for i in range(1, 4):
            q1_build_sites_data.insert(i + 1, f"angle{i}", z_build)
            q1_exist_sites_data.insert(i + 1, f"angle{i}", z_exist)
        q1 exist sites data, q1 build sites data
```

```
Out[5]: (
                        y angle1 angle2 angle3 type
                818 2020
         1
                713 2013
                                0
                                                      2
         2
               2305
                     291
                                                     2
         3
                700 1953
                                0
                                                     2
         4
                949 2293
                                0
                                        0
                                                     2
                     . . .
         1469 2324 1625
                                0
                                        0
                                                      2
         1470 1135
                      852
                                0
                                                     2
         1471 2053 1818
                                0
                                                     2
         1472 1432 1797
                                                     2
         1473 1584
                                                     2
                      898
         [1474 rows x \in columns],
                       y angle1 angle2 angle3 type
                 Χ
         0
               932 2210
               972 1238
                                                    1
         1
                   1894
              1229
                               0
                                                     2
              1311 2005
         3
                               0
                                                     1
              1611 2233
                                                     2
         4
                     . . .
         783 1171
                     812
                                                    1
         784
               250 1065
                               0
                                                    1
         785
              2353
                      24
                                                    1
              2422
                     583
         786
                                                     2
         787 2249 1453
                                                     2
         [788 rows x 6 columns])
In [6]:
        @jit
        def angle(hu):
            return hu / np.pi * 180
In [7]:
        @jit
        def cal_sites_angle():
            q1_weak_grid_data_np = np.array(weak_grid_data.copy()).astype(np.float32)
            q1_exist_sites_data_np = np.array(q1_exist_sites_data.copy()).astype(np.float32)
            q1_build_sites_data_np = np.array(q1_build_sites_data.copy()).astype(np.float32)
            11, 12, 13 = len(q1_weak_grid_data_np), len(q1_exist_sites_data_np), len(q1_build_sites_data_np)
            print(l1)
            site_data = q1_build_sites_data_np
            12 = len(site_data)
            print(12)
            for i in prange(12):
                if i % 50 == 0:
```

```
print(i, '/', 12)
site data[i, 2] = 0
site data[i, 3] = angle60 * 2
site data[i, 4] = angle60 * 4
include weak grid list = []
for j in prange(l1):
    if judge_in(site_data[i, :], q1_weak_grid_data_np[j, :]):
          print("/", end = '')
        include weak grid list.append(q1 weak grid data np[j, :])
if len(include weak grid list) == 0:
    continue
include weak grid list = pd.DataFrame(include weak grid list)
include weak grid list.sort values(by=2, inplace=True, ascending=False)
include weak grid list = np.array(include weak grid list).reshape(-1, 3)
site data[i, 2] = get theta(
    site_data[i, 0], site_data[i, 1],
   include_weak_grid_list[0, 0], include_weak_grid_list[0, 1],
if not len(include_weak_grid_list) > 1:
    continue
idx = 1
while idx < len(include_weak_grid_list):</pre>
      print(",", end = '')
    th = get theta(
        site_data[i, 0], site_data[i, 1],
        include_weak_grid_list[idx, 0], include_weak_grid_list[idx, 1],
    idx += 1
    if check_angle(th, site_data[i, 2]):
        site_data[i, 3] = th
        break
if not len(include_weak_grid_list) > 2:
    continue
while idx < len(include_weak_grid_list):</pre>
      print(".", end = '')
    th = get_theta(
        site_data[i, 0], site_data[i, 1],
        include_weak_grid_list[idx, 0], include_weak_grid_list[idx, 1],
    idx += 1
    if check_angle(th, site_data[i, 2]) and check_angle(th, site_data[i, 3]):
          print(444, end = '')
```

```
return site_data
In [8]: q1_build_sites_data_np = cal_sites_angle()
        182807
        788
        0 / 788
        50 / 788
        100 / 788
        150 / 788
        200 / 788
        250 / 788
        300 / 788
        350 / 788
        400 / 788
        450 / 788
        500 / 788
        550 / 788
        600 / 788
        650 / 788
        700 / 788
        750 / 788
        pd.DataFrame(q1_build_sites_data_np, columns=['x','y','\theta1','\theta2','\theta3','type'])
```

site_data[i, 4] = th

break

print(site_data)

	х	у	θ 1	θ 2	θ 3	type
0	932.0	2210.0	1.570796	2.094395	4.188790	2.0
1	972.0	1238.0	1.570796	2.094395	4.188790	1.0
2	1229.0	1894.0	1.570796	2.094395	4.188790	2.0
3	1311.0	2005.0	1.570796	2.094395	4.188790	1.0
4	1611.0	2233.0	1.570796	1.570796	4.188790	2.0
•••						
783	1171.0	812.0	1.570796	1.570796	1.165905	1.0
784	250.0	1065.0	1.570796	1.152572	1.570796	1.0
785	2353.0	24.0	1.570796	2.094395	4.188790	1.0
786	2422.0	583.0	1.570796	1.012197	1.107149	2.0
787	2249.0	1453.0	-1.107149	-1.438245	-1.107149	2.0

788 rows × 6 columns

Out[9]:

到这就处理数据代码没有了,只有处理好的 csv 文件,直接读取即可

```
In [10]: d1 = pd.read_csv(DATA_COOKED / 'question2-exist_sites_angle.csv', index_col=0)
    d2 = pd.read_csv(DATA_COOKED / 'question2-build_sites_angle.csv', index_col=0)
    data = pd.concat([d1, d2], axis=0)
    data.to_csv(DATA_COOKED / 'question2-total_sites_angle.csv') # 总站点1 (后面还会加入问题2中新的新建站点)
```

计算总业务量

```
In [11]:
    @jit
    def cal_total_business():
        total_bussiness = 0
        data = np.array(pd.read_csv(DATA_COOKED / 'question2-total_sites_angle.csv', index_col=0))
        LEN = len(data)

    grid = np.array(weak_grid_data.copy()).astype(np.float32)
    L = len(grid)

    for i in prange(LEN):
        for j in prange(L):
```

```
if grid[j,3]:
            continue
       if judge_in(data[i], grid[j]):
           x1,y1=data[i,0],data[i,1]
           x2,y2=grid[i,1],grid[j,1]
           if get r th(
                get theta(x1 - x2, y1 - y2) - data[i, 3],
                coverage[int(data[i, 5]) - 1]
           )**2 > (x1 - x2)**2 + (y1 - y2)**2:
                grid[j,3] = 1
               total bussiness += grid[j, 2]
return total bussiness
```

```
In [12]: weak_grid_data
```

Out[12]: X у **0** 66 1486 140.581390

> **1** 67 1486 140.518829 **2** 177 1486 48.919178

traffic

3 187 1486 4.322495

4 284 1486 71.528404

182802 2350 2123 0.178571 **182803** 2353 2123 5.159708 **182804** 2354 2123 5.134017 **182805** 2355 2123 2.599999

182806 2372 2123 57.814999

182807 rows × 3 columns

```
In [13]: weak_grid_data_cp = weak_grid_data.copy()
         weak_grid_data_cp
```

182807 rows × 3 columns

```
In [14]: weak_grid_data_cp.insert(3, "ed", pd.DataFrame([0 for _ in range(len(weak_grid_data))]))
    weak_grid_data_cp
```

Out[14]:		х	у	traffic	ed
	0	66	1486	140.581390	0
	1	67	1486	140.518829	0
	2	177	1486	48.919178	0
	3	187	1486	4.322495	0
	4	284	1486	71.528404	0
	•••				
	182802	2350	2123	0.178571	0
	182803	2353	2123	5.159708	0
	182804	2354	2123	5.134017	0
	182805	2355	2123	2.599999	0
	182806	2372	2123	57.814999	0

182807 rows × 4 columns

```
In [15]: @jit
         def cal_total_business():
             t0 = time()
             total_bussiness = 0
             data = np.array(pd.read_csv(DATA_COOKED / 'question2-total_sites_angle.csv', index_col=0))
             LEN = len(data)
             grid = np.array(weak_grid_data_cp.copy()).astype(np.float32)
             L = len(grid)
             for i in prange(LEN):
                 if i % 300 == 0:
                     print(i, '/', LEN)
                 for j in prange(L):
                     if grid[j,3]:
                         continue
                     if judge_in(data[i], grid[j]):
                         if not np.random.randint(10):
                             continue
                         x1,y1=data[i,0],data[i,1]
                         x2,y2=grid[i,1],grid[j,1]
                         grid[j,3] = 1
                         total_bussiness += grid[j, 2]
```

```
print('用时: ', time() - t0)
             return total bussiness, data, grid
In [16]: to bu = cal total business() # 1000s
         0 / 1576
         300 / 1576
         600 / 1576
         900 / 1576
         1200 / 1576
         1500 / 1576
         用时: 741.3745419979095
In [17]: # todo 计算总业务量
         total bussiness, data, grid = to bu
         total bussiness, data, grid
Out[17]: (3922204.01093581,
          array([[9.3200000e+02, 2.2100000e+03, 1.5707964e+00, 2.0943952e+00,
                  4.1887903e+00, 2.0000000e+00],
                 [9.7200000e+02, 1.2380000e+03, 1.5707964e+00, 2.0943952e+00,
                  4.1887903e+00, 1.0000000e+00],
                 [1.2290000e+03, 1.8940000e+03, 1.5707964e+00, 2.0943952e+00,
                  4.1887903e+00, 2.0000000e+00],
                 [2.3530000e+03, 2.4000000e+01, 1.5482696e+00, 4.7776027e+00,
                  5.3622860e+00, 1.0000000e+00],
                 [2.4220000e+03, 5.8300000e+02, 1.7090038e+00, 4.0597887e+00,
                  6.1582727e+00, 2.0000000e+00],
                 [2.2490000e+03, 1.4530000e+03, 4.2226570e+00, 4.9158216e+00,
                 1.0833534e+00, 2.0000000e+00]]),
          array([[ 66.
                            , 1486.
                                       , 140.58139 ,
                                                                   ],
                           , 1486. , 140.51883 ,
                                                                  ],
                 [ 67.
                                                           0.
                           , 1486.
                 [ 177.
                                       , 48.919178,
                                                                   1,
                 . . . ,
                            , 2123.
                                                                  ],
                 [2354.
                                       , 5.134017,
                 [2355.
                            , 2123.
                                      , 2.599999,
                                                           0.
                                                                   ],
                            , 2123.
                 [2372.
                                             57.815 ,
                                                                  ]],
                dtype=float32))
         remain_ggrid = pd.DataFrame(grid).copy()
In [18]:
         remain ggrid
```

```
Out[18]:
                  66.0 1486.0 140.581390 0.0
                   67.0 1486.0 140.518829 0.0
               2 177.0 1486.0
                                48.919178 0.0
               3 187.0 1486.0
                                 4.322495 0.0
               4 284.0 1486.0
                               71.528404 1.0
          182802 2350.0 2123.0
                                 0.178571 0.0
          182803 2353.0 2123.0
                                 5.159708 0.0
          182804 2354.0 2123.0
                                 5.134017 0.0
          182805 2355.0 2123.0
                                 2.599999 0.0
          182806 2372.0 2123.0
                               57.814999 0.0
```

182807 rows × 4 columns

```
In [19]: # todo 根据总业务量排序
    cond = remain_ggrid.iloc[:, 3] == 0
    remain_grid = remain_ggrid[cond]
    remain_grid.sort_values(by=2, inplace=True, ascending=False)
    remain_grid
```

Out[19]:		0	1	2	3
	103182	844.0	1962.0	47795.011719	0.0
	96789	1356.0	2271.0	43295.000000	0.0
	110362	869.0	2292.0	32200.953125	0.0
	57442	881.0	1256.0	24688.421875	0.0
	107373	1096.0	1658.0	23715.160156	0.0
	•••				
	179506	2212.0	2423.0	0.000192	0.0
	181329	2195.0	2433.0	0.000192	0.0
	179502	2208.0	2423.0	0.000192	0.0
	11838	2223.0	2460.0	0.000192	0.0
	154838	2059.0	2358.0	0.000192	0.0

108338 rows × 4 columns

kmeans 聚类

```
In [20]: # todo kmeans 聚类
kmeans = KMeans(n_clusters=100)
kmeans.fit(remain_grid.iloc[:, :2])
kmeans.labels_

Out[20]: array([24, 61, 24, ..., 45, 45, 89])

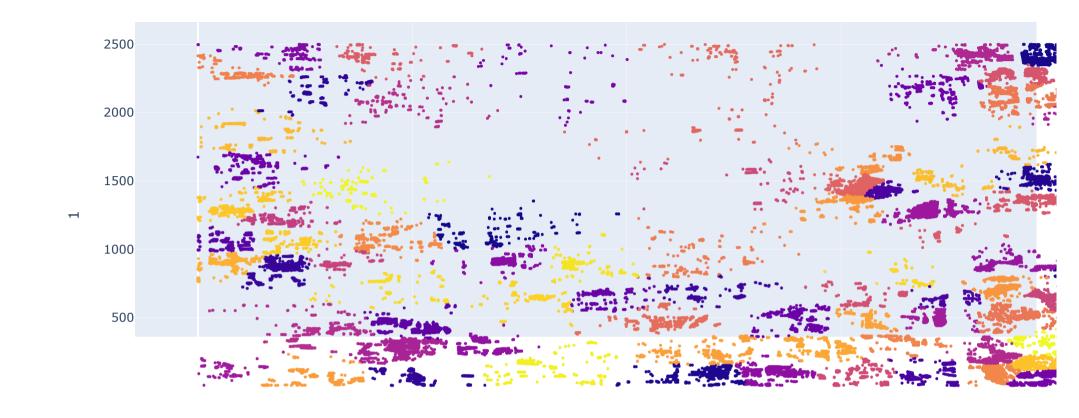
In [21]: remain_grid.insert(4, "labels", kmeans.labels_)
remain_grid
```

	0	1	2	3	labels
103182	844.0	1962.0	47795.011719	0.0	24
96789	1356.0	2271.0	43295.000000	0.0	61
110362	869.0	2292.0	32200.953125	0.0	24
57442	881.0	1256.0	24688.421875	0.0	1
107373	1096.0	1658.0	23715.160156	0.0	60
•••					
179506	2212.0	2423.0	0.000192	0.0	45
181329	2195.0	2433.0	0.000192	0.0	45
179502	2208.0	2423.0	0.000192	0.0	45
11838	2223.0	2460.0	0.000192	0.0	45
154838	2059.0	2358.0	0.000192	0.0	89

108338 rows × 5 columns

Out[21]:

```
In [22]: # todo 绘制聚类结果
fig = px.scatter(data_frame=remain_grid, x=0, y=1, color='labels')
fig.update_traces(marker={"size": 3})
fig.write_html(IMG_HTML / "question2-kmeans100.html")
fig.write_image(IMG_PNG / "question2-kmeans100.png")
fig.write_image(IMG_SVG / "question2-kmeans100.svg")
fig.show()
del fig
```



根据聚类结果和总业务量选择新建基站

```
In [23]: # 业务量
    now_bn = 5905185.385538206 # 现有业务量
    targe_bn = 6350607.1031652 # 目标业务量

In [24]: def existed(x, y):
    return x not in data[:, 0] and y not in data[:, 1]

In [25]: remain_grid
```

Out[25]:		0	1	2	3	labels
	103182	844.0	1962.0	47795.011719	0.0	24
	96789	1356.0	2271.0	43295.000000	0.0	61
	110362	869.0	2292.0	32200.953125	0.0	24
	57442	881.0	1256.0	24688.421875	0.0	1
	107373	1096.0	1658.0	23715.160156	0.0	60
	•••					
	179506	2212.0	2423.0	0.000192	0.0	45
	181329	2195.0	2433.0	0.000192	0.0	45
	179502	2208.0	2423.0	0.000192	0.0	45
	11838	2223.0	2460.0	0.000192	0.0	45
	154838	2059.0	2358.0	0.000192	0.0	89

108338 rows × 5 columns

```
In [26]: angle37_5 = np.pi * 37.5 / 180
         anglex = np.pi * 60 / 180
         @jit
         def is_far(x,y,m,n,c):
             return abs(x-m) > c or abs(y-n) > c
         @jit
         def is_in(x,y,m,n,c):
             return (x-m)^{**2} + (y-n)^{**2} < c^{**2}
         @jit
         def calcal(remain_grid=remain_grid):
             total_data = []
             now_bn = 5905185.385538206
             targe_bn = 6350607.1031652
             remain_grid = np.array(remain_grid.copy())
             for i in prange(len(remain_grid)):
                  if not remain_grid[i, 3]:
                     x, y, t = int(remain_grid[i, 0]), int(remain_grid[i, 1]), np.random.randint(2) + 1
                     t1, t2, t3 = [(angle60*2*(j-1)+i+np.random.uniform(-anglex, anglex)) % (np.pi*2) \
                                    for j in range(2, 5)]
                      total_data.append([x, y, t1, t2, t3, t])
                      now_bn += remain_grid[i, 2]
```

```
Out[28]:
                                               4 5
           0 844 1962 2.941118 3.542697 5.843110 1
           1 1356 2271 2.985915 5.858931 1.994340 2
             869 2292 3.323346 0.426135 2.267055 1
              881 1256 4.109999 0.009277 3.834270 2
           4 1096 1658 0.579936 2.522800 3.615235 1
           5 683 2198 6.118514 3.457958 4.685333 2
              865 2012 2.266906 2.992941 5.307013 2
          7 1335 2206 4.453241 6.275982 1.811592 1
           8 1357 1086 5.313147 0.607825 2.838493 2
            675 1957 5.664622 1.837217 3.970463 1
          10 1019 1593 0.152704 2.747127 4.986251 2
          11 935 1665 0.874917 4.206048 4.716827 1
          12 1489 1228 2.727830 5.605429 0.155014 2
          13 699 2014 2.525903 6.121284 1.445451 1
          14 1172 1797 4.327217 5.576492 1.411652 1
          15 1314 1125 0.174048 1.978144 2.504269 2
In [29]:
         pd.DataFrame(
              total data,
             columns=['x','y','\theta1','\theta2','\theta3','type'],
          ).to_csv(DATA_COOKED / "question2-add_sites_angle.csv")
         total_sites_data = pd.read_csv(DATA_COOKED / "question2-total_sites_angle.csv", index_col=0)
In [30]:
          total sites data
          add_sites_data = pd.read_csv(DATA_COOKED / "question2-add_sites_angle.csv", index_col=0)
          add_sites_data
          total_sites_data.append(add_sites_data).to_csv(DATA_COOKED / "question2-total_sites_angle.csv")
          total_sites_data # 最终所有站点数据
```

```
Out[30]:
                                                     \theta3 type
            0 932.0 2210.0 1.570796 2.094395 4.188790
                                                           2.0
            1 972.0 1238.0 1.570796 2.094395 4.188790
                                                           1.0
            2 1229.0 1894.0 1.570796 2.094395 4.188790
                                                           2.0
            3 1311.0 2005.0 1.570796 2.094395 4.188790
                                                           1.0
            4 1611.0 2233.0 1.570796 1.570796 4.188790
                                                           2.0
          783 1171.0 812.0 6.095762 2.418297 4.759339
                                                           1.0
          784 250.0 1065.0 0.680948 3.113659 3.892996
                                                           1.0
          785 2353.0
                        24.0 1.548270 4.777603 5.362286
                                                          1.0
          786 2422.0
                       583.0 1.709004 4.059789 6.158273
                                                           2.0
          787 2249.0 1453.0 4.222657 4.915822 1.083353
                                                           2.0
```

1576 rows × 6 columns

```
In [31]: SUM = 0
for i in range(len(total_sites_data)):
    SUM += cost[int(total_sites_data.iloc[i, 5]) - 1]
SUM # 问题2新建站点之前总站点数
```

Out[31]: 10324

In [32]: add_sites_data

```
1 1356 2271 2.985915 5.858931 1.994340
                                                     2
              869 2292 3.323346 0.426135 2.267055
              881 1256 4.109999 0.009277 3.834270
           4 1096 1658 0.579936 2.522800 3.615235
              683 2198 6.118514 3.457958 4.685333
              865 2012 2.266906 2.992941 5.307013
          7 1335 2206 4.453241 6.275982 1.811592
           8 1357 1086 5.313147 0.607825 2.838493
                                                     2
              675 1957 5.664622 1.837217 3.970463
          10 1019 1593 0.152704 2.747127 4.986251
              935 1665 0.874917 4.206048 4.716827
          12 1489 1228 2.727830 5.605429 0.155014
                                                     2
              699 2014 2.525903 6.121284 1.445451
          14 1172 1797 4.327217 5.576492 1.411652
          15 1314 1125 0.174048 1.978144 2.504269
In [33]: for i in range(len(add_sites_data)):
             SUM += cost[int(add_sites_data.iloc[i, 5]) - 1]
         SUM # 问题2新建站点之后总站点数
```

 θ 3 type

844 1962 2.941118 3.542697 5.843110

绘制所有站点散点图

Out[33]: **10412**

Out[32]:

```
In [34]: def plot_4kinds_sites():
    trace1 = go.Scatter(
        mode='markers',
        x=weak_grid_data.loc[:, "x"],
        y=weak_grid_data.loc[:, "y"],
        marker={"color": "blue", "size": 0.5},
        name="弱覆盖点",
```

```
trace2 = go.Scatter(
    mode='markers',
    x=total sites data.iloc[:1474, 0],
    y=total sites data.iloc[:1474, 1],
    marker={"color": "pink", "size": 4},
    name="现网基站",
trace3 = go.Scatter(
    mode='markers',
    x=total sites data.iloc[1474:, 0],
    y=total sites data.iloc[1474:, 1],
    marker={"color": "orange", "size": 5},
    name="新建基站-1",
trace4 = go.Scatter(
    mode='markers',
    x=add_sites_data.iloc[:, 0],
    y=add sites data.iloc[:, 1],
    marker={"color": "red", "size": 6},
    name="新建基站-2",
data = [trace1, trace2, trace3]
fig = go.Figure(data=data)
fig.write_html(IMG_HTML / "question2-3kinds sites.html")
fig.write image(IMG PNG / "question2-3kinds sites.png")
fig.write_image(IMG_SVG / "question2-3kinds_sites.svg")
fig.show()
del fig
data = [trace1, trace2, trace3, trace4]
fig = go.Figure(data=data)
fig.write_html(IMG_HTML / "question2-4kinds_sites.html")
fig.write_image(IMG_PNG / "question2-4kinds_sites.png")
fig.write_image(IMG_SVG / "question2-4kinds sites.svg")
fig.show()
del fig
return None
```

In [35]: plot_4kinds_sites()

这里文件太大,不方便展示,自行查看 question2-3kinds_sites.html question2-4kinds_sites.html 文件

In []: