1) 
$$T(n) = 3T(n/2) + n^2$$
  
 $a = 3, b = 2$   
 $c = log_2^3 = 1.5$   
 $h^2 > n^{1.5}$   
 $\therefore T(n) = O(n^2)$ 

3) 
$$T(n) = T(n/2) + 2^n$$

$$a = 1 b = 2$$

$$c = 0 (n^c = 1)$$

$$T(n) = 0(2^n)$$

5) 
$$T(n) = 16 T(n|4) + n$$
 $a = 16$ ,  $b = 4$ 
 $c = 2$ 
 $f(n) \le n^{c}$ 
 $t(n) = \theta(n^{2})$ 

$$(7) \quad \Gamma(n) = 2\tau(n/2) + n\log n$$

$$\alpha = 2 + b = 2$$

$$C = 1$$

$$\log n \leq n$$

$$\tau(n) = \Theta(n)$$

(a) 
$$T(n) = 4T(n/2) + n^2$$

$$0 = 4, b = 2$$

$$1 = log_2 4$$

$$1 = 2$$

$$1 = log_2 n^2$$

$$1 = n^2$$

$$1 =$$

(4) 
$$T(n) = 2^{n} T(n/2) + 2^{n}$$

$$a = 2^{n} b = 2$$

$$c = cog_{2} 2^{n}$$

$$c = n$$

$$f(n) < n < con$$

$$T(n) = o(n^{n})$$

(6) 
$$T(n) = 27(n) + n \log n$$
  
 $a = 2, b = 2$   
 $c = \log_2 2 = 1$   
 $n \log n > n$   
 $T(n) = 0 (n \log n)$ 

(8) QT(
$$n$$
)= 2T( $n$ / $y$ )+ $n$ 0.5/

 $a = 2, b = 4$ 
 $c = logu^2$ .  $c = 1/2$ 
 $f(n) = n^c$ 
 $n^{0.5} = n^{0.5}$ 

Tin1= O(an<sup>0.5</sup> logn)

9) 
$$T(n) = 0.5T(n/2) + 1/n$$

$$C = \log_2 1/2 = -1$$

$$n^{-1} = n^{-1}$$

$$T(n) = O(n^{-1} \log n)$$

(1) 
$$T(n) = 4T(n)_2 + \log n$$
  
 $a = 4, b = 2$   
 $c = \log_2 4 = 2$   
 $\log n < n^2$   
 $T_{n=0}(n^2)$ 

13) 
$$T(n) = 37(n) + n$$
  
 $a = 3, b = 2$   
 $c - \log_2 3 = 1.5$   
 $n < n^{1.5}$   
 $T(n) = O(n^{1.5})$ 

15) 
$$T(n) = 4P(n/2) + (n + 2)$$

$$a = 4, b = 2$$

$$c = 2$$

$$f(n) = n^{2}$$

$$ch < n^{2}$$

$$f(n) = O(n^{2})$$

(10) 
$$T(n) = 16T(n/4) + n/6$$
 $a = 16, b = 4$ 
 $c - log = 16 = 2$ 
 $n/6 > n = 16$ 
 $T(n) = 0 + 16$ 

(12) 
$$T(n) = \sqrt{n} T(n/2) + \log n$$

$$a = \sqrt{n}, b = 2$$

$$c + \log_2 n^{1/2}$$
and appliedths.

(14) 
$$T(n) = 3T(n)/3 + 3qxt(n)$$
  
 $a = 3 b = 3$   
 $C = log_{\beta} = 1$   
 $f(n) = r l/2$   
 $r = n l$   
 $f(n) = 0 cn l$ 

17) 
$$T(n) = 3\tau \ln (a) + n \log n$$

$$\alpha = 3 \quad b = 4$$

$$C = \log 4 \quad 3 = 0.7$$

$$\delta \ln n = n \log n$$

$$n^{c} = n^{0.7}$$

$$\delta \ln n \geq n^{c}$$

$$\tau(n) \geq n^{c}$$

$$\tau(n) = 0 \left(n \log n\right)$$

19) 
$$T(m) = 4\tau(nl_2) + nlogn)$$

$$0 = 4, b = 2$$

$$c = .2$$

$$6(n) = nlogn$$

$$n^2 = n^2$$

$$nlogn < n^2$$

$$T(n) = O(n^2)$$

$$21) \quad T(n) = 7 + T(n/3) n + n^{2}$$

$$\alpha = 7 \cdot b > 3$$

$$C = \log_{3} 7 = 1.77$$

$$\delta(n) > n^{2}$$

$$n^{2} > n^{1} 7^{4}$$

$$T(n) = \theta(n^{2})$$

(18) 
$$T(n) = 6T(n/3) + n^2 \log n$$
  
 $a = 6$ ,  $b = 3$   
 $c = \log_3 6 = 1.6$   
 $6(n) > n^2$   
 $T(n) = O(n^2 \log n)$ 

(20) 
$$T(n) = 64 T(n/8) - n^2 \log n$$
)
$$A = 64, b = 8$$

$$C = 2$$

$$b(n) > n^2$$

$$n^2 \log n > n^2$$

$$T(n) = O(n^2 \log n)$$

22) 
$$T(n) = T(n|2) + n(2-\omega e_n)$$
  
 $M = 1, b = 2$   
 $\log_2 1 = 0$   
 $f(n) > h^c$   
 $n(2-\omega e_n) > n^o$   
 $T(n) = O(n(2-\omega e_n))$