STA S380 HW2

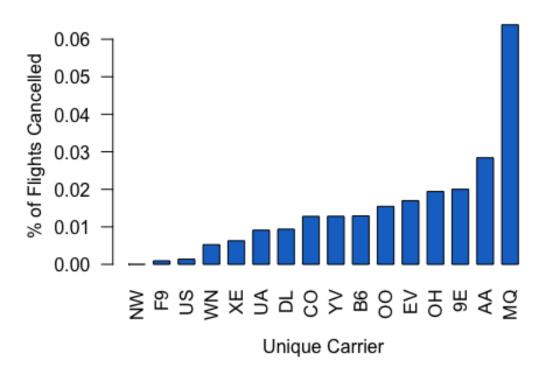
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8/17/2018

Flights at ABIA

```
library(tm)
#setwd('/users/chelseamatthews/Documents')
airlinedata = read.csv('~/Documents/UT/Summer Classes/Intro to Predictive
Modeling/Part 2/HW 2/ABIA.csv', header=TRUE)
#percentage of flights cancelled for each airline
dfcancelled =
data.frame(aggregate(airlinedata$Cancelled~airlinedata$UniqueCarrier,airlined
ata, sum))
df=data.frame(aggregate(airlinedata$FlightNum ~
airlinedata$UniqueCarrier,airlinedata, length))
finaldf = merge(dfcancelled,df)
finaldf = within(finaldf, percent <-</pre>
airlinedata.Cancelled/airlinedata.FlightNum)
finaldf = finaldf[order(finaldf$percent),]
barplot(finaldf$percent, names = finaldf$arrivaldelays.UniqueCarrier,
        xlab = 'Unique Carrier', ylab = '% of Flights Cancelled',
        main = "% of Flights Cancelled per Airline", las=2, space = .5, col =
'dodgerblue3',
        names.arg = c("NW","F9","US","WN","XE","UA","DL","CO","YV","B6",
"00", "EV", "0H", "9E", "AA", "MQ"))
```

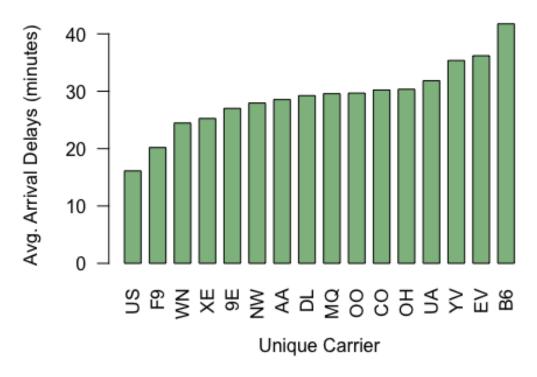
% of Flights Cancelled per Airline



American Eagle (MQ) had the highest percentage of cancelled flights. American Airlines (AA) had the next highest percent of cancelled flights.

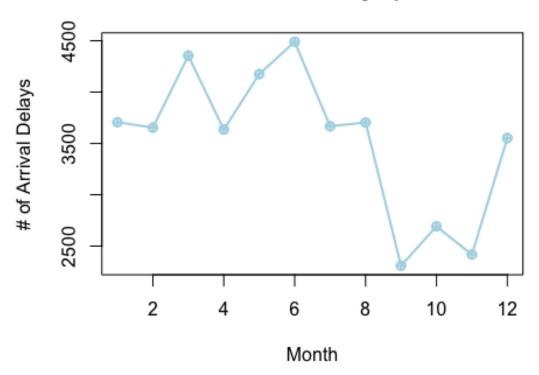
Arrivals

Avg. Arrival Delay times per Airline



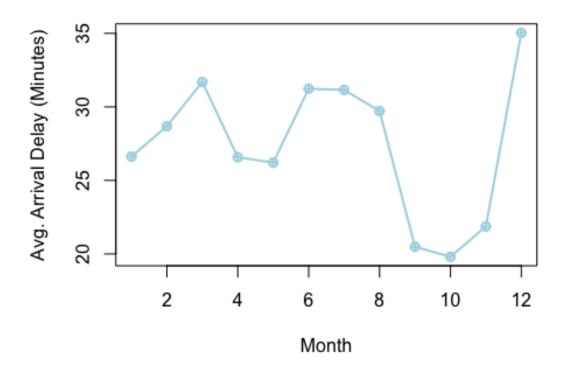
JetBlue(B6) has the longest average arrival delays, followed by ExpressJet (EV) and Mesa Airlines(YV).

Number of Arrival delays per month



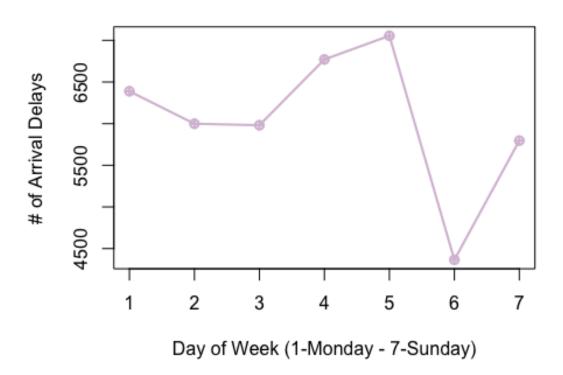
March and June had the highest number of arrival delays, while September and November had the smallest number of arrival delays.

Avg. Arrival delays per month



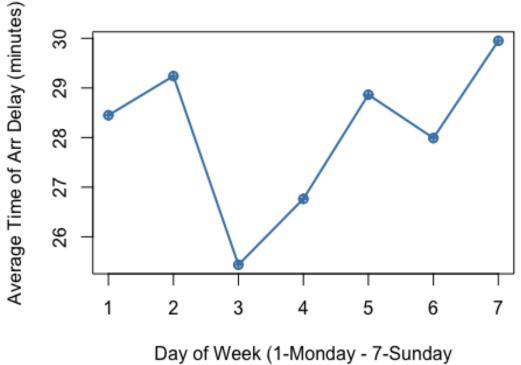
September, October and November had the shortest average arrival delays, while December had the longest.

Number of Arrival delays by Day of Week



Saturdays had the lowest amount of arrival delays, while Thursdays and Fridays had the most.



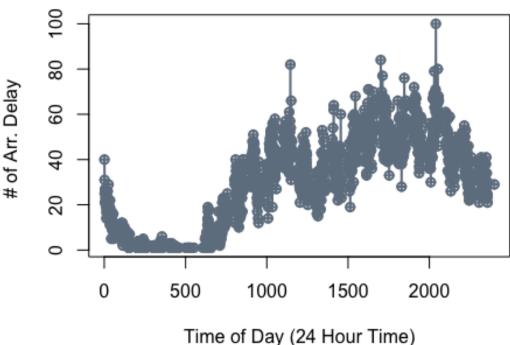


The

Average time of arrival delays is the lowest on Wednesdays and highest on Sundays.

average time of arrival delays by time of day

Number of Arrival Delay by Time of Day

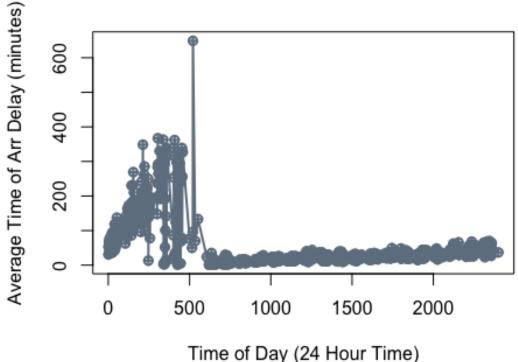


Between

1 am and 6 am there are the fewest amount of arrival delays. This is probably due to the lesser amount of flights during this time, since many airports don't have flights bewtween 2 am and 5 am. Around 11 am and 8 pm seem to ahve the highest number of arrival delays. The best time for arrivals seems to be from around 6 am to 8 am. The number stays pretty consistent throughout the day after 10 am.

```
#average time of arrival delays by time of day
df arrdelaytime = data.frame(aggregate(arrdelay$ArrDelay ~
arrdelay$ArrTime,arrdelay,mean))
plot(df_arrdelaytime$arrdelay.ArrTime, df_arrdelaytime$arrdelay.ArrDelay,
     xlab = "Time of Day (24 Hour Time)", ylab = "Average Time of Arr Delay
(minutes)",
     main = "Avg. Time of Arrival Delay by Time of Day", type ='o',
col='slategray',lwd=2, pch=10)
```

Avg. Time of Arrival Delay by Time of Day

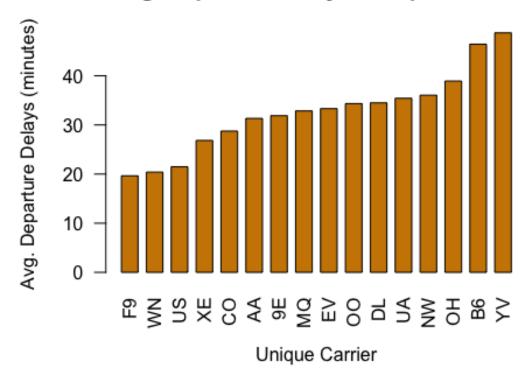


Between

Midnight and 5 am the average time of arrival delay is the highest (with a peak at around 5:30am). After about 6 am, average arrival delay by time of day is pretty low.

Departures

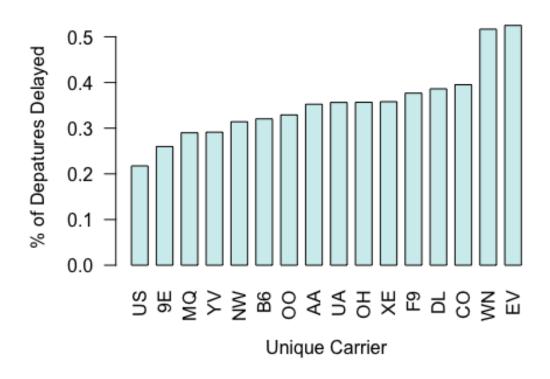
Avg. Departure Delay times per Airline



Departure delays are usually linked to arrival delays. Looking at departure delays is more important in understanding the likelihood of arriving at your destination on time/ or making connections at another airport. The top three airlines with the longest departure delay times were Mesa Airlines (YV), PSA Airlines (OH), and Jet Blue(B6). The airlines with the longest delayed departure times is similar to the airlines with the longest avergae arrival delays.

```
xlab = "Unique Carrier", ylab = "% of Depatures Delayed",
    main = "% of Departures Delayed per Airline", las=2, space=.5,
col='lightcyan2')
```

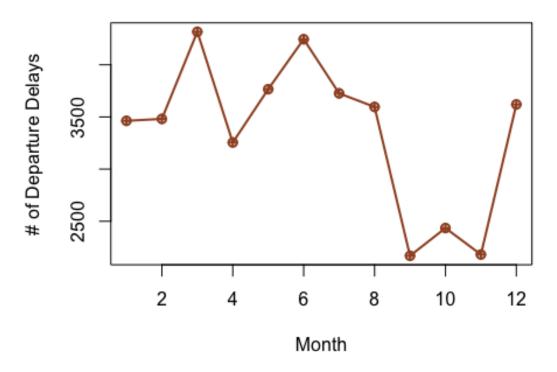
% of Departures Delayed per Airline



Looking

at the % of Departures delayed per Airline, ExpressJet(EV) has 50% of flights delayed. Southwest (WN) also has close to 50% of flights delayed. The three airlines with the highest % of departures delayed (EpressJet, Southwest and Continential Airlines) are not the same airlines with the highest average departure delay times. This means that while one might have longer average departure delays, it does not mean they are delayed the most.

Number of Departure delays per month

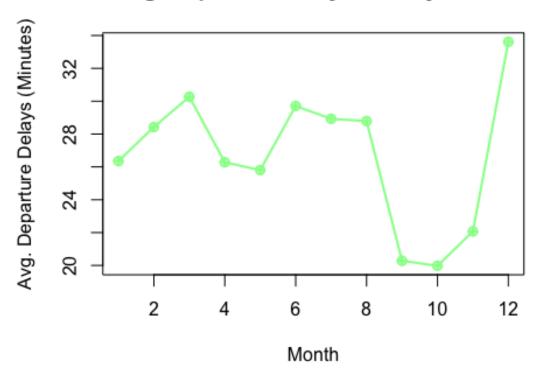


The

highest number of departure delays occur in March and June. The months with the least amount of departure delays were September and November. Next, we will look at which months had the longest average delays.

```
#average departure delays per month
dfmm =data.frame(aggregate(depdelay$DepDelay*DepDelay*Month, depdelay,mean))
plot(dfmm$depdelay.Month, dfmm$depdelay.DepDelay,
     xlab = "Month", ylab="Avg. Departure Delays (Minutes)",
     main = "Avg. Departure Delay times by Month", type='o',
     col = 'palegreen', lwd=2, pch =10)
```

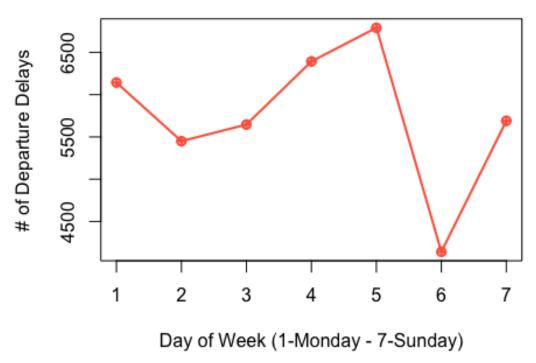
Avg. Departure Delay times by Month



While

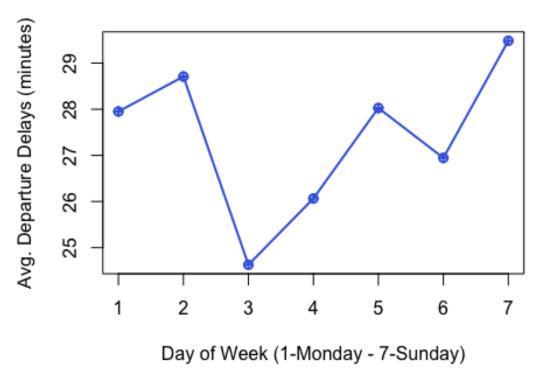
March and June had highest number of delays. December had the longest average delays. September and October had the shortest average departure delays.

Number of Departure delays by Day of Week



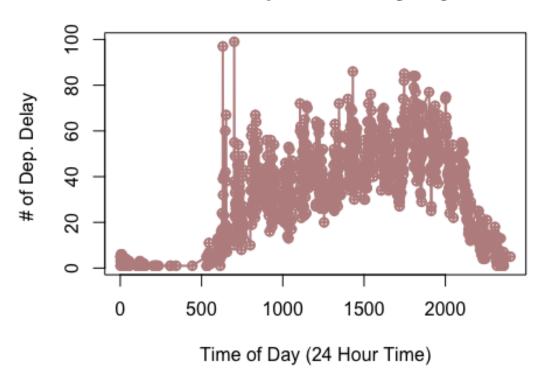
Fridays have the most number of Departure delays, followed by Thursdays. Saturdays had the lowest number of departure delays.

Avg. Departure delays by Day of Week



Wednesdays had the shortest average time of departure delays, while Sunday had the longest delays. Tuesdays had the second longest average departure delays.

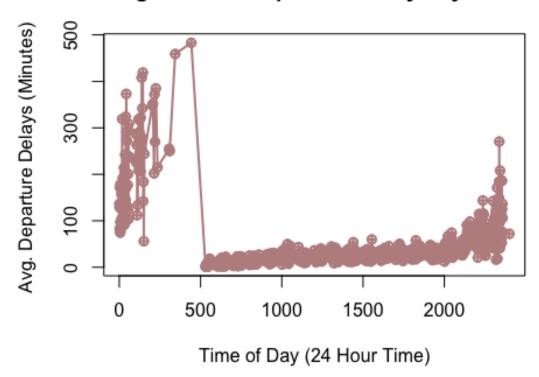
Number of Departure Delays by Hour



It seems

like the most delayed happen in the middle of the day between 6 am and 8 pm. There a re a coupleof peaks between 6 am and 7 pm. After 8pm, there are less departure delays and between midnight and 5 am there are almost zero. But, then again there are not many departing flights between midnight and 5 am.

Avg. Time of Departure Delays by Hour



While

there are not many departure delays between midnight and 5 am, the ones that do occur are long delays. In contrast the delays during the peak delay times seem to be shorts. The night delays (after 8pm) are longer, but not as long as the early morning delays.

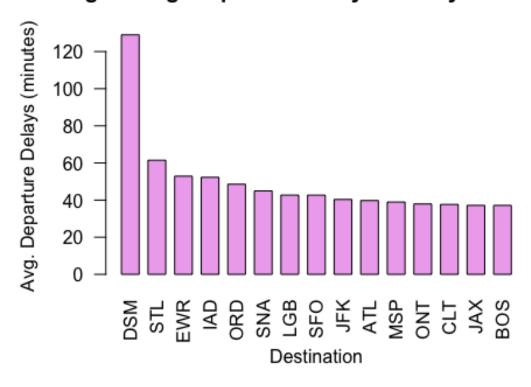
Destinations and Origins

```
departures = subset(airlinedata, Origin == 'AUS')

#average departure delay by destination
departdelay = departures[which(departures[,16]>0),]
df_depdelays = data.frame(aggregate(departdelay$DepDelay ~ departdelay$Dest,
departdelay, mean))
df_depdelays2 = df_depdelays[order(-
df_depdelays$departdelay.DepDelay),][1:15,]

barplot(df_depdelays2$departdelay.DepDelay, names =
df_depdelays2$departdelay.Dest,xlab = "Destination", ylab = 'Avg. Departure
Delays (minutes)', main = 'Longest Avg. Departure Delay times by
Destination', las =2, space=.5, col='plum2')
```

Longest Avg. Departure Delay times by Destinatio



The

above graph shows which airports are the destinations in which there are the longest average delays. The longest delays happen for flights headed to Des Moines, Iowa (DSM). The second longest are for St. Louis (STL) and the third longest delays are for flights headed to Newark, NJ (EWR).

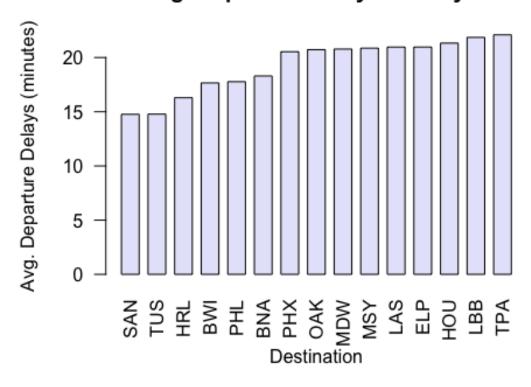
```
#destinations with the shortest average delays

departures = subset(airlinedata, Origin == 'AUS')

#average departure delay by destination
departdelay = departures[which(departures[,16]>0),]
df_depdelays = data.frame(aggregate(departdelay$DepDelay ~ departdelay$Dest,
departdelay, mean))
df_depdelays2 =
df_depdelays[order(df_depdelays$departdelay.DepDelay),][1:15,]

barplot(df_depdelays2$departdelay.DepDelay, names =
df_depdelays2$departdelay.Dest,xlab = "Destination", ylab = 'Avg. Departure
Delays (minutes)', main = ' Shortest Avg. Departure Delay times by
Destination', las =2, space=.5, col='lavender')
```

Shortest Avg. Departure Delay times by Destination



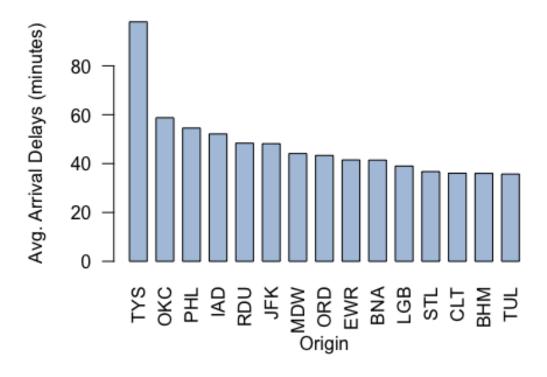
The

three destinations with the shortest average departure delays are San Diego (SAN), Tucson (TUS) and Valley International Airport (HRL).

```
#average arrival delay by Origin
arrivals = subset(airlinedata, Origin != 'AUS')
arrivedelay = arrivals[which(arrivals[,15]>0),]
df_arrdelays = data.frame(aggregate(arrivedelay$ArrDelay ~
arrivedelay$Origin, arrivedelay, mean))
df_arrdelays2 = df_arrdelays[order(-df_arrdelays$arrivedelay.ArrDelay),
][1:15,]

barplot(df_arrdelays2$arrivedelay.ArrDelay, names =
df_arrdelays2$arrivedelay.Origin,xlab = "Origin", ylab = 'Avg. Arrival Delays
(minutes)', main = 'Longest Avg. Arrival Delay times by Origin', las =2,
space=.5, col='lightsteelblue')
```

Longest Avg. Arrival Delay times by Origin

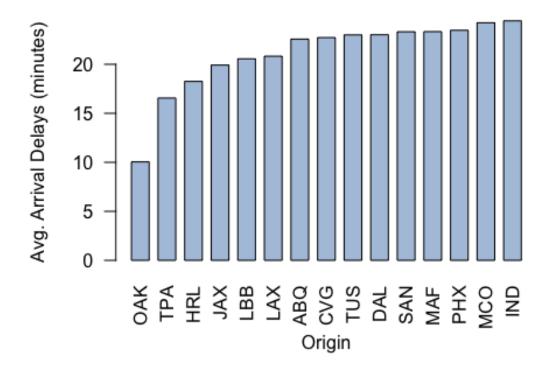


The

longest average arrival delays happens with planes coming from McGhee Tyson Airport in Knoxville, TN (TYS), Will Rogers World Airport in Oklahoma City, and Philadelphia (PHL).

```
#average shortest arrival delay by Origin
arrivals = subset(airlinedata, Origin != 'AUS')
arrivedelay = arrivals[which(arrivals[,15]>0),]
df_arrdelays = data.frame(aggregate(arrivedelay$ArrDelay ~
arrivedelay$Origin, arrivedelay, mean))
df_arrdelays2 = df_arrdelays[order(df_arrdelays$arrivedelay.ArrDelay),
][1:15,]
barplot(df_arrdelays2$arrivedelay.ArrDelay, names =
df_arrdelays2$arrivedelay.Origin,xlab = "Origin", ylab = 'Avg. Arrival Delays
(minutes)', main = 'Shortest Avg. Arrival Delay times by Origin', las =2,
space=.5, col='lightsteelblue')
```

Shortest Avg. Arrival Delay times by Origin



The shorest average arrival delays happen with planes coming from Oakland, California (OAK), Tampa, Florida (TPA) and Valley International (HRL).

Author Attribution

Preprocessing

First we need to read in all of our data and then preprocess it to make everything lowercase, remove numbers, remove punctuation, remove excess white spaces, and remove stopwords. We then create the document term matrix for both the train and test together to address the issue of some terms appearing in the test but not train or vice versa.

```
authors test = Sys.glob('~/Documents/UT/Summer Classes/Intro to Predictive
Modeling/Part 2/HW 2/ReutersC50/C50test/*')
file list_test = NULL
labels_test = NULL
for(i in authors train) {
  author name train = substring(i, first = 84)
  files to add train = Sys.glob(paste0(i, '/*.txt'))
  file list train = append(file list train, files to add train)
  labels_train = append(labels_train, rep(author_name_train,
length(files_to_add_train)))
author names = NULL
for(i in authors test) {
  author_name_test = substring(i, first = 83)
  author names = append(author names, author name test)
  files to_add_test = Sys.glob(paste0(i, '/*.txt'))
  file_list_test = append(file_list_test, files_to_add_test)
  labels_test = append(labels_test, rep(author_name_test,
length(files_to_add_test)))
file list <- append(file list train, file list test) #combine train and test
for simplicity
labels <- unique(append(labels train, labels test))</pre>
all docs = lapply(file list, readerPlain)
names(all_docs) = file_list
names(all_docs) = sub('.txt', '', names(all_docs))
all corpus = Corpus(VectorSource(all docs))
#names(all corpus) = labels
all_corpus = tm_map(all_corpus, content_transformer(tolower)) # make
everything lowercase
## Warning in tm map.SimpleCorpus(all corpus, content transformer(tolower)):
## transformation drops documents
all_corpus = tm_map(all_corpus, content_transformer(removeNumbers)) # remove
numbers
## Warning in tm map.SimpleCorpus(all corpus,
## content transformer(removeNumbers)): transformation drops documents
all corpus = tm map(all corpus, content transformer(removePunctuation)) #
remove punctuation
## Warning in tm map.SimpleCorpus(all corpus,
## content transformer(removePunctuation)): transformation drops documents
```

```
all_corpus = tm_map(all_corpus, content_transformer(stripWhitespace)) ##
remove excess white-space

## Warning in tm_map.SimpleCorpus(all_corpus,
## content_transformer(stripWhitespace)): transformation drops documents

all_corpus = tm_map(all_corpus, content_transformer(removeWords),
stopwords("en")) #remove stop words

## Warning in tm_map.SimpleCorpus(all_corpus,
## content_transformer(removeWords), : transformation drops documents

#creating a document term matrix with tf idf scores

dtm <- DocumentTermMatrix(all_corpus,control = list(weighting = function(x)
weightTfIdf(x, normalize = FALSE)))
dtm <- removeSparseTerms(dtm, 0.95)</pre>
```

Naive Bayes

We first try the Naive Bayes model on the training data set. We find the weight vector for each author that contains the weight of each word used by that author. We smooth the data so that when words are not in an author's bag of words, a small non-zero probability is given so that the posterior probabilities don't become zero.

```
#Naive Bayes
x <- as.matrix(dtm)</pre>
x_{train} <- x[1:2500,]
x_{\text{test}} <- x[2501:5000,]
smooth count = 1/nrow(x train)
author sums <- rowsum(x train +smooth count, labels train)</pre>
wt <- rowSums(author sums)</pre>
author wt <- log(author sums/wt) # log of prob of word occurring with
particular author
predicted_probabilities <- x test***t(author_wt) #use x test to multiply log</pre>
probabilities from weights of training set authors
predicted authors = NULL
for( i in 1:2500) {
  predicted authors =
c(predicted_authors, which.max(predicted_probabilities[i,]))
predicted authors <- as.data.frame(predicted authors)</pre>
predicted authors$actual <- rep(1:50,each = 50)</pre>
#assign author with max sum of probabilities for each of 2500 test points in
new list
```

```
results bayes=table(predicted authors$predicted authors,
predicted authors$actual)
results_bayes
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correct = NULL
for (i in 1:nrow(results_bayes)) {
  correct = append(correct, results_bayes[i,i])
}
correct_by_author = data.frame(correct, row.names = author_names)
correct_by_author
##
                                               correct
## HW 2/ReutersC50/C50test/AaronPressman
                                                    42
## HW 2/ReutersC50/C50test/AlanCrosby
                                                    30
## HW 2/ReutersC50/C50test/AlexanderSmith
                                                    28
## HW 2/ReutersC50/C50test/BenjaminKangLim
                                                     7
## HW 2/ReutersC50/C50test/BernardHickey
                                                    27
## HW 2/ReutersC50/C50test/BradDorfman
                                                    36
## HW 2/ReutersC50/C50test/DarrenSchuettler
                                                    21
## HW 2/ReutersC50/C50test/DavidLawder
                                                     4
## HW 2/ReutersC50/C50test/EdnaFernandes
                                                    10
## HW 2/ReutersC50/C50test/EricAuchard
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## HW 2/ReutersC50/C50test/FumikoFujisaki
                                                    48
## HW 2/ReutersC50/C50test/GrahamEarnshaw
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## HW 2/ReutersC50/C50test/HeatherScoffield
                                                    16
## HW 2/ReutersC50/C50test/JanLopatka
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## HW 2/ReutersC50/C50test/JaneMacartney
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## HW 2/ReutersC50/C50test/JimGilchrist
                                                    48
## HW 2/ReutersC50/C50test/JoWinterbottom
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## HW 2/ReutersC50/C50test/JonathanBirt
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## HW 2/ReutersC50/C50test/KarlPenhaul
                                                    37
## HW 2/ReutersC50/C50test/KeithWeir
                                                    30
## HW 2/ReutersC50/C50test/KevinDrawbaugh
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## HW 2/ReutersC50/C50test/KevinMorrison
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## HW 2/ReutersC50/C50test/KirstinRidley
                                                    34
## HW 2/ReutersC50/C50test/KouroshKarimkhany
                                                    28
## HW 2/ReutersC50/C50test/LydiaZajc
                                                    31
## HW 2/ReutersC50/C50test/LynneO'Donnell
                                                    39
## HW 2/ReutersC50/C50test/LynnleyBrowning
                                                    47
## HW 2/ReutersC50/C50test/MarcelMichelson
                                                    24
```

```
## HW 2/ReutersC50/C50test/MarkBendeich
                                                   23
## HW 2/ReutersC50/C50test/MartinWolk
                                                   17
## HW 2/ReutersC50/C50test/MatthewBunce
                                                   44
## HW 2/ReutersC50/C50test/MichaelConnor
                                                   36
                                                   14
## HW 2/ReutersC50/C50test/MureDickie
## HW 2/ReutersC50/C50test/NickLouth
                                                   36
## HW 2/ReutersC50/C50test/PatriciaCommins
                                                   24
## HW 2/ReutersC50/C50test/PeterHumphrey
                                                   27
## HW 2/ReutersC50/C50test/PierreTran
                                                   31
## HW 2/ReutersC50/C50test/RobinSidel
                                                   36
## HW 2/ReutersC50/C50test/RogerFillion
                                                   30
## HW 2/ReutersC50/C50test/SamuelPerry
                                                   34
## HW 2/ReutersC50/C50test/SarahDavison
                                                   28
## HW 2/ReutersC50/C50test/ScottHillis
                                                   11
## HW 2/ReutersC50/C50test/SimonCowell
                                                   24
## HW 2/ReutersC50/C50test/TanEeLyn
                                                   22
## HW 2/ReutersC50/C50test/TheresePoletti
                                                   21
## HW 2/ReutersC50/C50test/TimFarrand
                                                   32
## HW 2/ReutersC50/C50test/ToddNissen
                                                   20
## HW 2/ReutersC50/C50test/WilliamKazer
                                                   16
sum(correct_by_author)/2500 #accuracy
## [1] 0.4936
```

Naive Bayes only acheives an accuracy of 49% which is not very good. Jim Gilchrist and Fumiko Fujisaki are predicted best (48 correct, 2 wrongly attributed), while authors like John Mastrini are predicted poorly. Some of the most common misclassifications were Scott Hillis for Jane Macartney and Tan Eelyn for Peter Humphrey.

Random Forest

The next model we will try is Random Forest. Since our dataset is large, we specify 200 as our number of trees and limit mtry to 6.

```
#Random Forest

library(randomForest)

## randomForest 4.6-14

## Type rfNews() to see new features/changes/bug fixes.

set.seed(11)

rf.fit = randomForest(x = x_train, y = as.factor(labels_train), mtry=6, ntree=200)

rf.pred = predict(rf.fit, data=x_test)

rf_results = table(labels_test, rf.pred)

rf_correct = NULL

for (i in 1:nrow(rf results)) {
```

```
rf_correct = append(rf_correct, rf_results[i, i])
}
rf correct by author = data.frame(rf correct, row.names = author names)
rf_correct_by_author
##
                                              rf correct
## HW 2/ReutersC50/C50test/AaronPressman
                                                      48
## HW 2/ReutersC50/C50test/AlanCrosby
                                                      41
## HW 2/ReutersC50/C50test/AlexanderSmith
                                                      30
## HW 2/ReutersC50/C50test/BenjaminKangLim
                                                      32
## HW 2/ReutersC50/C50test/BernardHickey
                                                      33
## HW 2/ReutersC50/C50test/BradDorfman
                                                      29
## HW 2/ReutersC50/C50test/DarrenSchuettler
                                                      42
## HW 2/ReutersC50/C50test/DavidLawder
                                                      42
## HW 2/ReutersC50/C50test/EdnaFernandes
                                                      30
## HW 2/ReutersC50/C50test/EricAuchard
                                                      32
## HW 2/ReutersC50/C50test/FumikoFujisaki
                                                      45
## HW 2/ReutersC50/C50test/GrahamEarnshaw
                                                      38
## HW 2/ReutersC50/C50test/HeatherScoffield
                                                      41
## HW 2/ReutersC50/C50test/JanLopatka
                                                      23
## HW 2/ReutersC50/C50test/JaneMacartney
                                                      43
## HW 2/ReutersC50/C50test/JimGilchrist
                                                      50
## HW 2/ReutersC50/C50test/JoWinterbottom
                                                      37
## HW 2/ReutersC50/C50test/JoeOrtiz
                                                      33
## HW 2/ReutersC50/C50test/JohnMastrini
                                                      34
## HW 2/ReutersC50/C50test/JonathanBirt
                                                      45
## HW 2/ReutersC50/C50test/KarlPenhaul
                                                      45
## HW 2/ReutersC50/C50test/KeithWeir
                                                      37
## HW 2/ReutersC50/C50test/KevinDrawbaugh
                                                      27
## HW 2/ReutersC50/C50test/KevinMorrison
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## HW 2/ReutersC50/C50test/KirstinRidley
                                                      28
## HW 2/ReutersC50/C50test/KouroshKarimkhany
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## HW 2/ReutersC50/C50test/LydiaZajc
                                                      45
## HW 2/ReutersC50/C50test/LynneO'Donnell
                                                      49
## HW 2/ReutersC50/C50test/LynnleyBrowning
                                                      37
## HW 2/ReutersC50/C50test/MarcelMichelson
                                                      45
## HW 2/ReutersC50/C50test/MarkBendeich
                                                      41
## HW 2/ReutersC50/C50test/MartinWolk
                                                      32
## HW 2/ReutersC50/C50test/MatthewBunce
                                                      44
## HW 2/ReutersC50/C50test/MichaelConnor
                                                      36
## HW 2/ReutersC50/C50test/MureDickie
                                                      24
## HW 2/ReutersC50/C50test/NickLouth
                                                      37
## HW 2/ReutersC50/C50test/PatriciaCommins
                                                      35
## HW 2/ReutersC50/C50test/PeterHumphrey
                                                      36
## HW 2/ReutersC50/C50test/PierreTran
                                                      37
## HW 2/ReutersC50/C50test/RobinSidel
                                                      42
## HW 2/ReutersC50/C50test/RogerFillion
                                                      47
## HW 2/ReutersC50/C50test/SamuelPerry
                                                      29
## HW 2/ReutersC50/C50test/SarahDavison
                                                      28
```

```
## HW 2/ReutersC50/C50test/ScottHillis
                                                      19
## HW 2/ReutersC50/C50test/SimonCowell
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## HW 2/ReutersC50/C50test/TanEeLyn
## HW 2/ReutersC50/C50test/TheresePoletti
                                                      26
## HW 2/ReutersC50/C50test/TimFarrand
                                                      36
## HW 2/ReutersC50/C50test/ToddNissen
                                                      38
## HW 2/ReutersC50/C50test/WilliamKazer
                                                      19
sum(rf_correct_by_author)/2500
## [1] 0.7192
```

Our random forest produces a higher accuracy of around 72% and is therefore my preferred model. Authors like Aaron Pressman and Jim Gilchrist are predicted well, meaning that perhaps they have strong characteristic writing styles specific to them. Other authors like Jan Lopatka and William Kazer are not well predicted, and thus potentially have less of a distinguishable vocabularly in their writing.

Practice with Association Rule Mining

```
library(arules)
## Loading required package: Matrix
##
## Attaching package: 'arules'
## The following object is masked from 'package:tm':
##
##
       inspect
## The following objects are masked from 'package:base':
##
##
       abbreviate, write
library(arulesViz)
## Loading required package: grid
groceries = read.transactions("~/Documents/UT/Summer Classes/Intro to
Predictive Modeling/Part 2/HW 2/groceries.txt", format = 'basket', sep = ',')
summary(groceries)
## transactions as itemMatrix in sparse format with
## 9835 rows (elements/itemsets/transactions) and
##
  169 columns (items) and a density of 0.02609146
##
## most frequent items:
##
         whole milk other vegetables
                                            rolls/buns
                                                                   soda
##
                                                  1809
                                                                   1715
               2513
                                1903
##
             yogurt
                              (Other)
                               34055
##
               1372
##
```

```
## element (itemset/transaction) length distribution:
## sizes
                           5
                                                              12
##
      1
           2
                3
                     4
                                6
                                     7
                                          8
                                                9
                                                    10
                                                         11
                                                                    13
                                                                         14
                                                                              15
                                                   246
## 2159 1643 1299 1005
                        855
                              645
                                   545
                                        438
                                              350
                                                        182
                                                             117
                                                                    78
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     16
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                                     4
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                                                               1
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                                                                          1
##
     46
               14
##
##
     Min. 1st Qu. Median
                               Mean 3rd Ou.
                                               Max.
##
     1.000
             2.000
                     3.000
                              4.409
                                      6.000
                                              32.000
##
## includes extended item information - examples:
               labels
## 1 abrasive cleaner
## 2 artif. sweetener
## 3
       baby cosmetics
groceries rules = apriori(groceries, parameter=list(support=.005,
confidence=.5, maxlen=8))
## Apriori
##
## Parameter specification:
## confidence minval smax arem aval originalSupport maxtime support minlen
##
                  0.1
                          1 none FALSE
                                                   TRUE
                                                              5
                                                                  0.005
## maxlen target
                    ext
##
         8 rules FALSE
##
## Algorithmic control:
## filter tree heap memopt load sort verbose
##
       0.1 TRUE TRUE FALSE TRUE
                                     2
                                           TRUE
##
## Absolute minimum support count: 49
##
## set item appearances ...[0 item(s)] done [0.00s].
## set transactions ...[169 item(s), 9835 transaction(s)] done [0.00s].
## sorting and recoding items ... [120 item(s)] done [0.00s].
## creating transaction tree ... done [0.00s].
## checking subsets of size 1 2 3 4 done [0.00s].
## writing ... [120 rule(s)] done [0.00s].
## creating S4 object ... done [0.00s].
inspect(groceries_rules)
##
         1hs
                                        rhs
                                                                support
confidence
               lift count
         {baking powder}
                                     => {whole milk}
## [1]
                                                            0.009252669
0.5229885 2.046793
## [2]
         {oil,
##
          other vegetables}
                                     => {whole milk}
                                                            0.005083884
0.5102041 1.996760
                       50
## [3] {onions,
```

```
root vegetables}
                                 => {other vegetables} 0.005693950
0.6021505 3.112008
                      56
## [4] {onions,
                                    => {other vegetables} 0.006609049
##
         whole milk}
0.5462185 2.822942
                      65
## [5]
         {hygiene articles,
##
          other vegetables}
                                   => {whole milk}
                                                          0.005185562
0.5425532 2.123363
                      51
## [6]
        {other vegetables,
                                    => {whole milk}
##
          sugar}
                                                          0.006304016
0.5849057 2.289115
                      62
       {long life bakery product,
## [7]
          other vegetables}
                                    => {whole milk}
                                                          0.005693950
##
0.5333333 2.087279
                      56
## [8]
        {cream cheese,
                                    => {whole milk}
                                                          0.006609049
         yogurt}
0.5327869 2.085141
## [9]
        {chicken,
          root vegetables}
                                   => {other vegetables} 0.005693950
##
0.5233645 2.704829
                      56
## [10] {chicken,
                                   => {whole milk}
          root vegetables}
                                                          0.005998983
0.5514019 2.157993
                      59
## [11] {chicken,
          rolls/buns}
                                   => {whole milk}
                                                          0.005287239
0.5473684 2.142208
                      52
## [12] {coffee,
                                    => {whole milk}
##
          yogurt}
                                                          0.005083884
0.5208333 2.038359
                      50
## [13] {frozen vegetables,
                                    => {other vegetables} 0.006100661
##
          root vegetables}
0.5263158 2.720082
## [14] {frozen vegetables,
                                    => {whole milk}
         root vegetables}
                                                          0.006202339
0.5350877 2.094146
## [15] {frozen vegetables,
##
                                    => {whole milk}
          rolls/buns}
                                                          0.005083884
0.5000000 1.956825
                      50
## [16] {frozen vegetables,
          other vegetables}
                                    => {whole milk}
                                                          0.009659380
0.5428571 2.124552
                      95
## [17] {beef,
##
          yogurt}
                                    => {whole milk}
                                                          0.006100661
0.5217391 2.041904
                      60
## [18] {beef,
##
          rolls/buns}
                                    => {whole milk}
                                                          0.006812405
0.5000000 1.956825
                      67
## [19] {curd,
##
          whipped/sour cream}
                                   => {whole milk}
                                                          0.005897306
0.5631068 2.203802
```

## [20] {cu	ropical fru	=	=>	{yogurt	t}	0.005287239
0.5148515 3. ## [21] {cu	urd,	52 :+1		(a+ban	vogotables)	0 005287220
## 0.5148515 2. ## [22] {cu	.660833	it} 52	=>	{orner	vegetables}	0.005287239
## tr	ropical fru		=>	{whole	milk}	0.006507372
## [23] {cu	urd,	les}	=>	{other	vegetables}	0.005490595
0.5046729 2. ## [24] {cu	.608228	54			-	
0.5700935 2	.231146	les} 61	=>	{whole	milk}	0.006202339
## [25] {cu	ogurt}	00	=>	{whole	milk}	0.010066090
0.5823529 2. ## [26] {cu ## rd	urd,	99	->	{whole	milk}	0.005897306
0.5858586 2. ## [27] {cu	.292845	58	-/	JIOH	milik j	0.003037300
## of 0.5739645 2.	ther vegeta	bles} 97	=>	{whole	milk}	0.009862735
	oot vegetab	les}	=>	{other	vegetables}	0.007015760
0.5149254 2. ## [29] {pd	ork,	69		6 1 7		
0.5000000 1.	.956825	les} 67	=>	{wno1e	milk}	0.006812405
## [30] {pc ## rc 0.5495495 2.	olls/buns}	61	=>	{whole	milk}	0.006202339
## [31] {fr	rankfurter,		=>	{whole	milk}	0.005185562
0.5483871 2. ## [32] {fr	.146195	51				
0.5000000 1.		50	=>	{whole	milk}	0.005083884
•	ogurt}		=>	{whole	milk}	0.006202339
0.5545455 2. ## [34] {bd			-\	{whole	milk}	0.005185562
0.5604396 2. ## [35] {br	.193364	51	-/	TOTIE	mitk)	0.009189902
	ropical fru		=>	{whole	milk}	0.005693950
## [36] {br	rown bread, oot vegetab		=>	{whole	milk}	0.005693950

```
0.5600000 2.191643
## [37] {brown bread,
                                  => {whole milk}
         other vegetables}
                                                        0.009354347
0.5000000 1.956825
                     92
## [38] {domestic eggs,
                                  => {whole milk}
                                                        0.005185562
         margarine}
0.6219512 2.434099
## [39] {margarine,
         root vegetables}
                                 => {other vegetables} 0.005897306
0.5321101 2.750028
                     58
## [40] {margarine,
                                 => {whole milk}
##
         rolls/buns}
                                                        0.007930859
0.5379310 2.105273
                     78
## [41] {butter,
         domestic eggs}
                                 => {whole milk}
                                                        0.005998983
##
0.6210526 2.430582
## [42] {butter,
                                 => {other vegetables} 0.005795628
         whipped/sour cream}
0.5700000 2.945849
                     57
## [43] {butter,
                                  => {whole milk}
         whipped/sour cream}
                                                        0.006710727
0.6600000 2.583008
                     66
## [44] {butter,
         citrus fruit}
                                  => {whole milk}
                                                        0.005083884
0.5555556 2.174249
## [45] {bottled water,
                                  => {whole milk}
                                                        0.005388917
         butter}
0.6022727 2.357084
                     53
## [46] {butter,
         tropical fruit}
                                 => {other vegetables} 0.005490595
0.5510204 2.847759
                     54
## [47] {butter,
         tropical fruit}
                                => {whole milk} 0.006202339
0.6224490 2.436047
## [48] {butter,
                                 => {other vegetables} 0.006609049
         root vegetables}
0.5118110 2.645119
                     65
## [49] {butter,
         root vegetables}
                                 => {whole milk}
                                                        0.008235892
0.6377953 2.496107
## [50] {butter,
         yogurt}
                                   => {whole milk}
                                                        0.009354347
0.6388889 2.500387
                     92
## [51] {butter,
                                 => {whole milk}
         other vegetables}
                                                        0.011489578
0.5736041 2.244885
                    113
## [52] {newspapers,
                                 => {other vegetables} 0.005998983
         root vegetables}
0.5221239 2.698417
## [53] {newspapers,
```

```
## root vegetables}
                               => {whole milk} 0.005795628
0.5044248 1.974142
                     57
## [54] {domestic eggs,
                                  => {other vegetables} 0.005083884
         whipped/sour cream}
0.5102041 2.636814
                     50
## [55] {domestic eggs,
                                 => {whole milk}
         whipped/sour cream}
                                                       0.005693950
0.5714286 2.236371
## [56] {domestic eggs,
                                  => {whole milk}
##
         pip fruit}
                                                       0.005388917
0.6235294 2.440275
## [57] {citrus fruit,
                                 => {whole milk}
         domestic eggs}
                                                       0.005693950
0.5490196 2.148670
## [58] {domestic eggs,
                                => {whole milk}
                                                       0.006914082
         tropical fruit}
0.6071429 2.376144
                     68
## [59] {domestic eggs,
                                => {other vegetables} 0.007320793
         root vegetables}
0.5106383 2.639058
                    72
## [60] {domestic eggs,
                                 => {whole milk}
         root vegetables}
                                                       0.008540925
0.5957447 2.331536
## [61] {domestic eggs,
                                 => {whole milk}
         yogurt}
                                                       0.007727504
0.5390071 2.109485
                     76
## [62] {domestic eggs,
                               => {whole milk}
##
         other vegetables}
                                                       0.012302999
0.5525114 2.162336
                    121
## [63] {fruit/vegetable juice,
                                  => {other vegetables} 0.006609049
         root vegetables}
0.5508475 2.846865
                    65
## [64] {fruit/vegetable juice,
                                  => {whole milk}
         root vegetables}
                                                       0.006507372
0.5423729 2.122657
                    64
## [65] {fruit/vegetable juice,
                                  => {whole milk}
##
         yogurt}
                                                       0.009456024
0.5054348 1.978094
                    93
## [66] {pip fruit,
         whipped/sour cream}
                                 => {other vegetables} 0.005592272
0.6043956 3.123610
                     55
## [67] {pip fruit,
                                 => {whole milk}
         whipped/sour cream}
                                                       0.005998983
0.6483516 2.537421
                     59
## [68] {citrus fruit,
##
         whipped/sour cream} => {other vegetables} 0.005693950
0.5233645 2.704829
## [69] {citrus fruit,
         whipped/sour cream}
                                => {whole milk} 0.006304016
0.5794393 2.267722 62
```

```
## [70] {sausage,
                               => {whole milk} 0.005083884
         whipped/sour cream}
0.5617978 2.198679
                     50
## [71] {tropical fruit,
                                => {other vegetables} 0.007829181
##
         whipped/sour cream}
0.5661765 2.926088
                     77
## [72] {tropical fruit,
                                 => {whole milk}
         whipped/sour cream}
                                                       0.007930859
0.5735294 2.244593
                    78
## [73] {root vegetables,
         whipped/sour cream}
                                 => {other vegetables} 0.008540925
0.5000000 2.584078
                     84
## [74] {root vegetables,
         whipped/sour cream}
                                 => {whole milk}
                                                       0.009456024
0.5535714 2.166484
                     93
## [75] {whipped/sour cream,
         yogurt}
                                  => {whole milk}
                                                       0.010879512
0.5245098 2.052747
                    107
## [76] {rolls/buns,
##
         whipped/sour cream}
                                 => {whole milk}
                                                       0.007829181
0.5347222 2.092715
                     77
## [77] {other vegetables,
         whipped/sour cream}
                                => {whole milk}
                                                       0.014641586
0.5070423 1.984385
                    144
## [78] {pip fruit,
         sausage}
                                  => {whole milk}
                                                       0.005592272
0.5188679 2.030667
                     55
## [79] {pip fruit,
                                => {other vegetables} 0.008134215
         root vegetables}
0.5228758 2.702304
## [80] {pip fruit,
                                 => {whole milk}
         root vegetables}
                                                       0.008947636
0.5751634 2.250988
                     88
## [81] {pip fruit,
                                 => {whole milk}
##
         yogurt}
                                                       0.009557702
0.5310734 2.078435
                     94
## [82] {other vegetables,
##
                                  => {whole milk}
                                                       0.013523132
         pip fruit}
0.5175097 2.025351
                    133
## [83] {pastry,
                                 => {whole milk}
         tropical fruit}
                                                       0.006710727
0.5076923 1.986930
## [84] {pastry,
                                 => {other vegetables} 0.005897306
##
         root vegetables}
0.5370370 2.775491
                     58
## [85] {pastry,
         root vegetables}
                                 => {whole milk}
                                                       0.005693950
0.5185185 2.029299
                     56
## [86] {pastry,
                             => {whole milk} 0.009150991
## yogurt}
```

```
0.5172414 2.024301 90
## [87] {citrus fruit,
         root vegetables}
                                  => {other vegetables} 0.010371124
0.5862069 3.029608
                    102
## [88] {citrus fruit,
                                 => {whole milk}
                                                        0.009150991
         root vegetables}
0.5172414 2.024301
                     90
## [89] {root vegetables,
                                  => {other vegetables} 0.006609049
         shopping bags}
0.5158730 2.666112
                     65
## [90] {sausage,
         tropical fruit}
                                  => {whole milk}
##
                                                        0.007219115
0.5182482 2.028241
                     71
## [91] {root vegetables,
                                   => {whole milk}
                                                        0.007727504
##
         sausage}
0.5170068 2.023383
                     76
## [92] {root vegetables,
                                  => {other vegetables} 0.012302999
         tropical fruit}
0.5845411 3.020999
                    121
## [93] {root vegetables,
                                  => {whole milk}
         tropical fruit}
                                                        0.011997966
0.5700483 2.230969
                    118
## [94] {tropical fruit,
         yogurt}
                                   => {whole milk}
                                                        0.015149975
0.5173611 2.024770
                    149
## [95] {root vegetables,
                                   => {other vegetables} 0.012913066
         yogurt}
0.5000000 2.584078
                    127
## [96] {root vegetables,
                                   => {whole milk}
                                                        0.014539908
##
         yogurt}
0.5629921 2.203354
                    143
## [97] {rolls/buns,
         root vegetables}
                                  => {other vegetables} 0.012201322
0.5020921 2.594890
                    120
## [98] {rolls/buns,
                                 => {whole milk}
##
         root vegetables}
                                                        0.012709710
0.5230126 2.046888
                    125
## [99] {other vegetables,
                                   => {whole milk}
                                                        0.022267412
         yogurt}
0.5128806 2.007235
                    219
## [100] {fruit/vegetable juice,
##
         other vegetables,
                                   => {whole milk}
##
         yogurt}
                                                        0.005083884
0.6172840 2.415833
                     50
## [101] {fruit/vegetable juice,
##
         whole milk,
##
         yogurt}
                                   => {other vegetables} 0.005083884
0.5376344 2.778578
                     50
## [102] {other vegetables,
## root vegetables,
```

```
whipped/sour cream} => {whole milk}
                                                           0.005185562
0.6071429 2.376144
                      51
## [103] {root vegetables,
          whipped/sour cream,
                                    => {other vegetables} 0.005185562
##
          whole milk}
0.5483871 2.834150
                      51
## [104] {other vegetables,
##
          whipped/sour cream,
                                    => {whole milk}
##
          yogurt}
                                                           0.005592272
0.5500000 2.152507
                      55
## [105] {whipped/sour cream,
##
          whole milk,
                                    => {other vegetables} 0.005592272
##
          yogurt}
0.5140187 2.656529
                      55
## [106] {other vegetables,
          pip fruit,
##
          root vegetables}
                                   => {whole milk}
                                                           0.005490595
0.6750000 2.641713
                      54
## [107] {pip fruit,
##
          root vegetables,
##
          whole milk}
                                    => {other vegetables} 0.005490595
0.6136364 3.171368
                      54
## [108] {other vegetables,
##
          pip fruit,
##
          yogurt}
                                    => {whole milk}
                                                           0.005083884
0.6250000 2.446031
                      50
## [109] {pip fruit,
##
          whole milk,
                                    => {other vegetables} 0.005083884
##
          yogurt}
0.5319149 2.749019
                      50
## [110] {citrus fruit,
          other vegetables,
##
          root vegetables}
                                   => {whole milk}
                                                           0.005795628
0.5588235 2.187039
## [111] {citrus fruit,
##
          root vegetables,
                                    => {other vegetables} 0.005795628
##
          whole milk}
0.6333333 3.273165
                      57
## [112] {root vegetables,
##
          tropical fruit,
##
          yogurt}
                                    => {whole milk}
                                                           0.005693950
0.7000000 2.739554
## [113] {other vegetables,
##
          root vegetables,
                                    => {whole milk}
                                                           0.007015760
##
          tropical fruit}
0.5702479 2.231750
                      69
## [114] {root vegetables,
##
          tropical fruit,
##
          whole milk}
                                    => {other vegetables} 0.007015760
0.5847458 3.022057 69
```

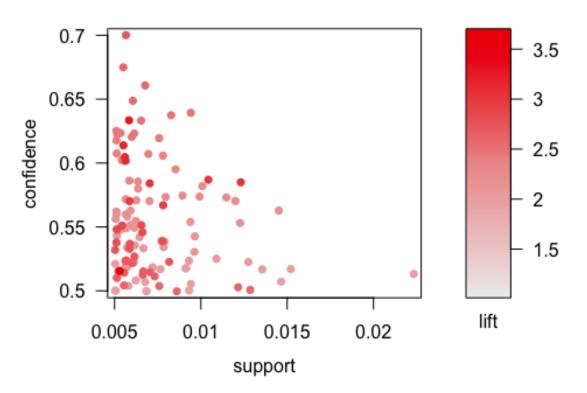
```
## [115] {other vegetables,
##
         tropical fruit,
                                   => {whole milk}
##
         yogurt}
                                                         0.007625826
0.6198347 2.425816
## [116] {tropical fruit,
         whole milk,
         yogurt}
##
                                  => {other vegetables} 0.007625826
0.5033557 2.601421
## [117] {other vegetables,
##
         root vegetables,
##
         yogurt}
                                   => {whole milk}
                                                   0.007829181
0.6062992 2.372842
                     77
## [118] {root vegetables,
         whole milk,
         yogurt}
                                   => {other vegetables} 0.007829181
##
                     77
0.5384615 2.782853
## [119] {other vegetables,
##
         rolls/buns,
##
         root vegetables}
                                 => {whole milk}
                                                         0.006202339
0.5083333 1.989438
## [120] {other vegetables,
         rolls/buns,
                                   => {whole milk}
                                                         0.005998983
         yogurt}
0.5221239 2.043410
                     59
inspect(subset(groceries rules, subset=lift > 3))
##
      1hs
                                                     support confidence
                              rhs
lift count
## [1] {onions,
       root vegetables} => {other vegetables} 0.005693950 0.6021505
3.112008
           56
## [2] {curd,
       tropical fruit} => {yogurt}
                                                 0.005287239 0.5148515
3.690645
           52
## [3] {pip fruit,
       whipped/sour cream} => {other vegetables} 0.005592272 0.6043956
3.123610
           55
## [4] {citrus fruit,
       root vegetables} => {other vegetables} 0.010371124 0.5862069
3.029608
          102
## [5] {root vegetables,
       tropical fruit} => {other vegetables} 0.012302999 0.5845411
##
3.020999
          121
## [6] {pip fruit,
##
       root vegetables,
       whole milk}
                           => {other vegetables} 0.005490595 0.6136364
##
3.171368
           54
## [7] {citrus fruit,
## root vegetables,
```

```
## whole milk} => {other vegetables} 0.005795628 0.6333333
3.273165
           57
## [8] {root vegetables,
       tropical fruit,
##
       whole milk}
                         => {other vegetables} 0.007015760 0.5847458
           69
3.022057
inspect(subset(groceries rules, subset=confidence > 0.6))
       1hs
##
                                  rhs
                                                        support confidence
lift count
## [1] {onions,
                              => {other vegetables} 0.005693950 0.6021505
        root vegetables}
3.112008
           56
## [2] {curd,
        tropical fruit}
                              => {whole milk}
                                                    0.006507372 0.6336634
2.479936
           64
## [3] {domestic eggs,
                               => {whole milk}
                                                    0.005185562 0.6219512
##
        margarine}
2.434099
           51
## [4] {butter,
                              => {whole milk}
##
        domestic eggs}
                                                    0.005998983 0.6210526
2.430582
           59
## [5] {butter,
##
        whipped/sour cream}
                              => {whole milk}
                                                    0.006710727 0.6600000
2.583008
           66
## [6] {bottled water,
        butter}
                               => {whole milk}
                                                    0.005388917 0.6022727
##
2.357084
           53
## [7] {butter,
                               => {whole milk}
                                                    0.006202339 0.6224490
##
        tropical fruit}
2.436047
           61
## [8] {butter,
        root vegetables}
                              => {whole milk}
                                                    0.008235892 0.6377953
2.496107
           81
## [9] {butter,
                               => {whole milk}
                                                    0.009354347 0.6388889
        yogurt}
2.500387
           92
## [10] {domestic eggs,
                               => {whole milk}
##
        pip fruit}
                                                    0.005388917 0.6235294
2.440275
           53
## [11] {domestic eggs,
##
        tropical fruit}
                              => {whole milk}
                                                    0.006914082 0.6071429
2.376144
           68
## [12] {pip fruit,
        whipped/sour cream}
                               => {other vegetables} 0.005592272 0.6043956
##
3.123610
           55
## [13] {pip fruit,
        whipped/sour cream}
                              => {whole milk}
                                               0.005998983 0.6483516
2.537421 59
```

```
## [14] {fruit/vegetable juice,
##
        other vegetables,
                               => {whole milk}
##
        yogurt}
                                                     0.005083884 0.6172840
2.415833
           50
## [15] {other vegetables,
        root vegetables,
                               => {whole milk}
##
        whipped/sour cream}
                                                    0.005185562 0.6071429
2.376144
           51
## [16] {other vegetables,
##
        pip fruit,
                                                    0.005490595 0.6750000
##
        root vegetables}
                               => {whole milk}
2.641713
           54
## [17] {pip fruit,
##
        root vegetables,
##
        whole milk}
                               => {other vegetables} 0.005490595 0.6136364
3.171368
           54
## [18] {other vegetables,
##
        pip fruit,
##
        yogurt}
                               => {whole milk}
                                                0.005083884 0.6250000
2.446031
           50
## [19] {citrus fruit,
        root vegetables,
##
        whole milk}
                               => {other vegetables} 0.005795628 0.6333333
3.273165
           57
## [20] {root vegetables,
##
        tropical fruit,
                               => {whole milk}
                                                     0.005693950 0.7000000
##
        yogurt}
2.739554
           56
## [21] {other vegetables,
##
        tropical fruit,
                               => {whole milk}
                                                     0.007625826 0.6198347
##
        yogurt}
2.425816
           75
## [22] {other vegetables,
        root vegetables,
                               => {whole milk}
##
        yogurt}
                                                     0.007829181 0.6062992
2.372842
           77
inspect(subset(groceries rules, subset=lift > 3 & confidence > 0.6))
      lhs
##
                              rhs
                                                     support confidence
lift count
## [1] {onions,
        root vegetables} => {other vegetables} 0.005693950 0.6021505
##
3.112008
           56
## [2] {pip fruit,
       whipped/sour cream} => {other vegetables} 0.005592272 0.6043956
3.123610
## [3] {pip fruit,
##
        root vegetables,
       whole milk} => {other vegetables} 0.005490595 0.6136364
##
```

```
3.171368 54
## [4] {citrus fruit,
## root vegetables,
## whole milk} => {other vegetables} 0.005795628 0.6333333
3.273165 57
plot(groceries_rules)
## To reduce overplotting, jitter is added! Use jitter = 0 to prevent jitter.
```

Scatter plot for 120 rules



A lot of the item sets are very similar products grouped together, like citrus fruit and tropical fruit or root vegetables and other vegetables. The highest lift values were primarily sets of items that inform the purchase of 'other vegetables.' We chose a threshhold for lift of 3, because most of the lift values ranged from 1-3, so the values with lift >3 showed us the highly informative baskets. Most of the confidence values ranged from 0.5-0.7 so we chose a threshhold of confidence > 0.6. The rules we found made sense, and primarily tell us about what groups of items tell us about the liklihood of buying whole milk and vegetables.