No.

T. T	
Name: Tri Huynh	
Assignment 2	
Part 1	
a) W(n) = 2W/n/3) +1	
Here we have a = 2, b = 3, f(n) = 1 =	no
Here we have $a = 2, b = 3, f(n) = 1 =$ Compare $f(n)$ to $n^{\log_2 a} = n^{\log_3 2}$	
log, 2 = 0.6309. So f(n) = n° is polyn	omally smaller
Master Theorem case 1 applies.	(0 <(033)
20: M(u) = ANAMONIN FVON O(u)	32)
b) W(n) = 5W (n/4)+n	Kenar 190
Hara on homin of 1 - 4 f/1 - 1	
Here we have: a = 5 b = 4, f(n) = n ¹ Compare f(n) +0 n ^{631 a} = n ⁶³⁴⁵	
Compare fin ton - n	1.16096)
log 9 5 × 1.16096, so n is smaller than	n n by a
polynomial factorso case 1 applies	
So: W(n) = 8088 800 (nos45)	
co) W(n) - 7W(n/7) +n	
Here we have: a = 7, b= 7 f(n)=n1	
Compare f(n) to nbook = nbox = n2	
They have the same order so we use cuse	2 of the mase
Theorem	
So = W(n) pr de strange = O(nlogn)	
(8) W(n) - 9W(n/3)tn2	
Hom 1 1 have 1 6 - 9 h- 2 1/10) -12	
Here we have $a = 9$ $b = 3$, $f(n) = n^2$ Compare $f(n)$ to n^{60} , $a = n^{60}$, $a = n^2$	
So Master Theorem Cise 2 applies	and the second s
W(n) = 0 (n2 (ogn)	-
U	Y/BOOK
	11 25 21 21

e) W(n) = 8W (n/2) tn3
We have: $a = 8$, $b = 2$, $f(n) = n^3$
We have: $a - 8$, $b = 2$, $f(n) = n^3$ Compare $f(n)$ to $n^{\log_b a} = n^{\log_2 8} = n^3$
They have the same order = Master Theorem Case 2
$W(n) = O(n^3 \log n)$
$W(n) = O(n^{3}\log n)$ $f) W(n) = 49W(n/25) + n^{3/2} \log n$
We have a = 49 b = 25, f(n) = n ^{3/2} logn nlogg = 10,549 N SNBOBI n. 209
n 69 3 2 103 25 49 N XN 80 91 n 1. 209
n ^{3/2} log n grows polynomially faster than n ^{1.209} (be con n ^{3/2} n ^{3/2} n ^{1.5} , and n ^{1.5} log n definitely grows faster than n ^{1.209}) so
n312 - n , and n log of definitely grows faster than n so) so
Case 3 of Master Theorem applies.
So: W(n) = ((n3/2 (log n))
g) W(n) - W(n-1)+2
Unfolding we get: W(n) = W(n-2)+2+27
(1) 0 (M/M) + (1-1) T L = (M(n-3) at 2 + 2 + 12 +
after n-1 steps we hat WC1)
(1)0+ (s-W(1)+2(n+1))
So W(n) = O(n) + (1) + (1)
h) W(n) = W(n-1) +n°, with c>1
Unroll: W(n) = W(0) + \(\frac{\x}{\k^{\infty}} \) (\(\text{Vertext} \) (\(Vertex
Use the standard power-sum bound (Integral comparison): $\int_{0}^{n} x dz dz \leq \sum_{k} \kappa^{c} \leq \int_{0}^{n} x dx + n = \frac{n^{c+1}}{c+1} + n^{c}$
$\int_0^\infty \frac{d\pi}{d\pi} = \frac{2\pi}{C+1} = \int_0^\infty \frac{d\pi}{C+1} + \frac{\pi}{C+1}$
Therefore $\sum_{k=1}^{n} \kappa^{c} = O(n^{c+1})$, so $W(n) = O(n^{c+1})$
LIBRORIE MANAGEMENT



ngay
i) W(n) = W(vn)+18) W8 = (1) W(0)
lot n = 2 and define v(m) - W(2m). Then:
$V(m) = W(2^m) - W(2^{m/2}) + 1 = V(m/2) + 1$
Unrolling for $t = \lceil \log_2 m \rceil$ steps reaches a constant: $V(m) = V(\frac{m}{2^t}) + t = O(1) + t = O(\log m)$ Since $m = \log_2 n$
$V(m) = V(m) + t = O(1) + t = O(\log m)$
Since m - log n, 2t show of show
$W(n) = V(\log_2 n) = O(\log\log n)$
Cos in reason to the contract of the contract
Part 2 moses pleamenting swarp and "18
* Algorithm A: T(n) - 5T(n/2) + (AK) O(n)
Use Master Theorem with a = 5, b = 2, f(n) = n 1001, a = n 10025 x n 2.3219
not, a = note = 2.3219 stand = (NOW)
Since $f(n) = n = o(n^{6025})$, this is case 1. So $T(n) = O(n^{6025})$
So T(n) = O(n 6325) W 1 top ow probled N
* Algorithm B: T(n) = 2T(n-1) + (1) (0(1)
Unroll 10 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
T(n) = 2(2T(n-2)+0(1))+0(1)
$ = 2^{n-1} T(1) + \sum_{i=1}^{n} 2^{i} $
The sum is 2 1-1- 1 w at (1-n) w = (n) w
S. T(n) = 0(2n)0) W = (n)W : 101m
* Algorithm C: T(n) = 9T(n/3) + O(n2)
Apply the Master Theorem with a = 9, b=3, f(n) = n2
$n^{\log 3} = n^{\log_3 9} = n^2$
This matches are 2 of the Master Theorem.
So: T(n) - O (n2 log n)
Algorithm Chas the best running time so we choose algorith
VIBOOK
INTERNATIONAL

	Ngay		NO.
Part 3 0 - (1)0+(sin) 8 = (n)	ر ج در	Scan	
mo(n) = S(a/2) + O(1) - O(lon a)	12 Sep	ر دو مله	
by Let n be the length of the inpu	A list	110	
* WOCK W(n)			and the same for the same and the same
tach element causes one call to purent	- upde	we who	ch 15 (0(1)
we vit all nin segvence.	10 ni	midine	
Recurrence: w(0) = O(1). W(n)	= W	(n-1)	+0(1)
Solution W(n)=0(n)	ander	- Term	
So O(n) for the norst case.			
(n)0	= (N) m/ (3	
b) + Work: Each character in the input	is pro	cessed	exactly
once Each Step is O(1).			
Recurrence: W(0) - O(1), W(n)	= WC	1-1)+0	(1)
=) $W(n) = O(n)$			
* 5 pan: 5 reps are dependent, so	expen	tien is s	rictly_
segliential.		\	
Recurrence: S(0) = (9(1), S(n)-	5(n-1	L) † O(1)
-) s(n) = 0 (n)			
	Z-1/		
d) * Work:			
Map: $W_{map}(n) = O(n)$ Scan: $W_{scan}(n) = 2W(n/2) + O$	(1)	()	
Scan: Wscan(n) = 2W(n/2) + 0	(1)	0(n)
Reduce: Wredna (n) = 2W (n/z) + C)(1)	= 0(n)
Total :w(n) = O(n)			
*Span:			
Map: Smap (n) = O(1)			
ana i		1	VIBOOK



Scan Sc. (n) = S(n/2) + O(1) = O(log n)
Scan Sscan(n) = 3(n/2) + O(1) = O(log n) Reduce Sreduce(n) = S(n/2) + O(1) - O(log n)
Total SCn) = O(logn)
(n) Wasawi Y
F) tot n= length of mylist. Split indo to halves, solve both, then
Combine in O(1).
*Work Want:
Tecurrence: W(1)-O(1), W(n) = W([n/2])
So O(n) for the norse case
f) W(n) = O(n)
Lois (n) = O (log n) released dus 3 : How (d)
ance Fails Step is O(1)
Recurrence W(0) - O(1), W(n) = W(n-14)
(3)(3) (N)VV (E
t Span: Steps are depocably so expending so
A-PARTIE DE L'ANDRE L'
Recommend: S(b) = O(1), S(n)- S(n-1)+ S(n)
(4) 0 - (4) 2 (-
12470W K (b)
Map Was (n) - (n)
SAME WE DINGER DINGER OF BUILDING
Caracter Caracter Contraction of the Contraction of
CANCE CANCELOSO
190 ×
May Smay (N) 2 2
VIBOOK

CMPS 2200 Assignment 2

In this assignment we'll work on applying the methods we've learned to analyze recurrences, and also see their behavior in practice. As with previous assignments, some of of your answers will go in main.py and test_main.py. You should feel free to edit this file with your answers; for handwritten work please scan your work and submit a PDF titled assignment-02.pdf and push to your github repository.

Part 1. Asymptotic Analysis

Derive asymptotic upper bounds of work for each recurrence below.

Part 2. Algorithm Comparison

Suppose that for a given task you are choosing between the following three algorithms:

- Algorithm \mathcal{A} solves problems by dividing them into five subproblems of half the size, recursively solving each subproblem, and then combining the solutions in linear time.
- Algorithm \mathcal{B} solves problems of size n by recursively solving two subproblems of size n-1 and then combining the solutions in constant time.
- Algorithm \mathcal{C} solves problems of size n by dividing them into nine subproblems of size n/3, recursively solving each subproblem, and then combining the solutions in $O(n^2)$ time.

What are the asymptotic running times of each of these algorithms? Which algorithm would you choose?

.

· ·

Part 3: Parenthesis Matching

A common task of compilers is to ensure that parentheses are matched. That is, each open parenthesis is followed at some point by a closed parenthesis. Furthermore, a closed parenthesis can only appear if there is a corresponding open parenthesis before it. So, the following are valid:

```
• ((a)b)
• a()b(c(d))
```

but these are invalid:

```
• ((a)
• (a))b(
```

Below, we'll solve this problem three different ways, using iterate, scan, and divide and conquer.

3a. iterative solution Implement parens_match_iterative, a solution to this problem using the iterate function. Hint: consider using a single counter variable to keep track of whether there are more open or closed parentheses. How can you update this value while iterating from left to right through the input? What must be true of this value at each step for the parentheses to be matched? To complete this, complete the parens_update function and the parens_match_iterative function. The parens_update function will be called in combination with iterate inside parens_match_iterative. Test your implementation with test_parens_match_iterative.

.

3b. What are the recurrences for the Work and Span of this solution? What are their Big Oh solutions?

enter answer here

.

3c. scan solution Implement parens_match_scan a solution to this problem using scan. Hint: We have given you the function paren_map which maps (to 1,) to -1 and everything else to 0. How can you pass this function to scan to solve the problem? You may also find the min_f function useful here. Implement parens_match_scan and test with test_parens_match_scan

.

3d. Assume that any maps are done in parallel, and that we use the efficient implementation of scan from class. What are the recurrences for the Work and Span of this solution?

enter answer here

.

3e. divide and conquer solution Implement parens_match_dc_helper, a divide and conquer solution to the problem. A key observation is that we cannot simply solve each subproblem using the above solutions and combine the results. E.g., consider '((()))', which would be split into '((('and ')))', neither of which is matched. Yet, the whole input is matched. Instead, we'll have to keep track of two numbers: the number of unmatched right parentheses (R), and the number of unmatched left parentheses (L). parens_match_dc_helper returns a tuple (R,L). So, if the input is just '(', then parens_match_dc_helper returns (0,1), indicating that there is 1 unmatched left parens and 0 unmatched right parens. Analogously, if the input is just ')', then the result should be (1,0). The main difficulty is deciding how to merge the returned values for the two recursive calls. E.g., if (i,j) is the result for the left half of the list, and (k,l) is the output of the right half of the list, how can we compute the proper return value (R,L) using only i,j,k,l? Try a few example inputs to guide your solution, then test with test_parens_match_dc_helper.

.

3f. Assuming any recursive calls are done in parallel, what are the recurrences for the Work and Span of this solution? What are their Big Oh solutions?

enter answer here

•