## **STAT 500**

## t Distribution Information

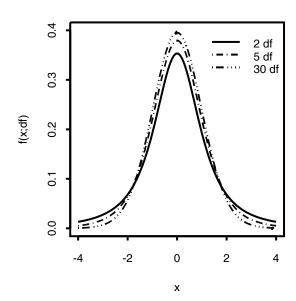
• Definition: A continuous random variable T has a t distribution with  $\nu$  degrees of freedom if T can be expressed as:

$$T = \frac{Z}{\sqrt{W/\nu}}$$

where  $Z \sim N(0,1), W \sim \chi^2_{\nu}$  and Z and W are independent.

- The parameter of the t distribution is the degrees of freedom  $\nu$ .
- A t distribution is usually denoted as  $t_{\nu}$ . A particular percentile p of the t distribution is denoted as  $t_{\nu,p}$ .
- $\bullet$  Here is a picture of the density function of a t distribution. The distribution is bell-shaped, centered at 0, and has a larger variance than a standard normal distribution.





• As  $\nu \to \infty$ , the t distribution tends to the standard normal distribution  $Z \sim N(0,1)$ .