Homework 05: Formal properties. Consider a square matrix B of size N. Let A represent the initial configuration of the matrix B.

(1) Write a UNITY program that transposes the rows and columns of matrix B and preserves the following invariant:

```
inv. p\leqq ∧ \left\langle \ \forall \ i,j: (1\leq i
```

Program Transpose

```
declare
A: array of[1...N, 1...N] of integer p, q: integer
initially
A = B
1 < p, q < N \land p \le q
assign
< \forall i,j: 1 \le i < p \land 1 \le j \le N :: A[i,j] = B[i,j] > []
< \forall i,j: 1 \le i \le N \land 1 \le j < p :: A[i,j] = B[i,j] > []
< \forall i,j: q < i \le N \land 1 \le j \le N :: A[i,j] = B[i,j] > []
< \forall i,j: 1 \le i \le N \land q < j \le N :: A[i,j] = B[i,j] > []
```

end

(2) Write a formal specification of the correctness of the program you designed. Such a specification often assumes the following general form:

```
a. init —> Postb. stable Post
```

Init:
$$B = \Gamma = A \land p \le q$$

Post: $B = \Gamma \land p \le q \land$

$$\langle \forall i,j : (1 \le i
// slightly modified from Inv.$$

(3) Explain in narrative form (no formal proof) the steps involved in proving these two properties.