

# Predicting Consumer Sentiment Towards Amazon Fashion Products Using a Product-Reviewer Network

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1 **Product reviews form a goldmine of text data that is helpful to both  
2 consumers and businesses in making buying decisions and under-  
3 standing consumer needs respectively. In this study, we present a  
4 method to convert review text data into a product-reviewer network  
5 that can be used to predict consumer sentiment towards a product  
6 they have not previously reviewed. Our method utilizes two key tech-  
7 niques in this process: the first is natural language processing to  
8 extract the sentiment from thousands of reviews and the second is  
9 balance theory to analyze the signed network. We address the chal-  
10 lenges in drawing insights from a signed, bipartite network and make  
11 use of existing literature on modified balance theory to overcome  
12 them. With a carefully sampled dataset of Amazon fashion products'  
13 reviews, we demonstrate the effectiveness of our method in predict-  
14 ing the signs of consumer sentiment. We explore three sign predic-  
15 tion methods, namely the Signed Caterpillar (SCsc), Random Walk  
16 Based Models (SBRW), and Matrix Factorization (MFwBT), and suc-  
17 cessfully implement two of the three with remarkable accuracy. We  
18 recognize the several limitations in our processes, including discrete  
19 sentiment values and a limited dataset. Future work would expand  
20 these promising results into a more comprehensive study address-  
21 ing the mentioned limitations.**

Sign Prediction | Undirected Signed Bipartite Network | Balance Theory  
| Signed Butterfly | Signed Caterpillars | Sentiment Analysis | Amazon  
Fashion

1 **T**ext data has become increasingly available and relevant  
2 in the past decade with the rise of global internet. Social  
3 media posts, review websites, and online surveys have all con-  
4 tributed to the wealth of information we can use to understand  
5 evolving human behavior. Of particular interest to businesses  
6 have been reviews and ratings, which aid in constructing rec-  
7 commender systems (2), increasing sales (3), and improving  
8 consumer satisfaction. Reviews — rather than ratings — are  
9 especially useful to analyze because words provide a more  
10 meaningful interpretation that is masked by one-dimensional  
11 ratings. There is an abundance of research on sentiment anal-  
12 ysis of product reviews which has achieved remarkable results  
13 using state-of-the-art machine learning techniques (4), deep  
14 neural networks (5), and feature specific analysis (6). However,  
15 existing work has been lacking in either one of two aspects.  
16 On one hand, previous studies have exclusively focused on  
17 accurately classifying reviews as positive or negative rather  
18 than predicting the sentiment of consumers towards unfamiliar  
19 products. On the other hand, businesses' internal systems  
20 that do prioritize the latter exploit consumer metadata such  
as demographics (2). We contribute to the existing research  
in a multi-fold manner. Firstly, we create a process to predict  
consumer sentiment towards unknown products. Secondly, we  
achieve this by exploiting the network structures of products

and reviewers rather than their metadata. Previous research  
on the ethics of collecting and using user data has revealed the  
existence of risks related to privacy and opacity (7). By relying  
solely on the review text and no identifying information, we  
hope to mitigate such risks in our method while providing an  
accurate, powerful predictive functionality. Another motivation  
to make use of network science in drawing from the results  
of sentiment analysis includes the proven wide-ranging benefits  
of the analysis of social networks and technological networks  
(1, 10). Previous network studies in e-commerce have also  
understood online reviewer characteristics which would not  
have been possible without a network position analysis (8).

In our attempts to take advantage of the network structures,  
we encounter various challenges owed to the negative weights  
and bipartite sets in our constructed network. Recent work  
of Derr et. al in extending the notions of balance theory to  
bipartite networks using signed butterflies instead of signed  
triads proved especially helpful. We draw on the three sign  
prediction methods created by them: the Signed Caterpillars  
Based Classifier, Random Walk Based Signed Prediction, and  
Matrix Factorization with Balance Theory. They tested and

## Significance Statement

The significance of our study can be understood from two points of view. From a theoretical standpoint, existing work on signed, bipartite networks is limited. Expanding existing network functionalities for such a network is challenging with the presence of negative edge weights and disjoint sets of nodes. At the same time, applications of such a network are ubiquitous — from terrorist-target to buyer-seller networks — making the learning of its construction and analysis important. In this case, we focus on the application of analyzing signed, bipartite networks in e-commerce. We make use of advanced sign prediction methods and extend their application to a product-reviewer network. From an application standpoint then, we better understand consumer preferences and aid in decision making while circumventing the need for any user data.

Z.L., V.C., and H.J. designed research, performed research, analyzed data, and wrote the paper. Z.L. did the data visualization, implemented the SCsc method, co-wrote the Abstract, Introduction, and Background information, and wrote the Data Visualization, SCsc methodology, and Limitation sections in this report; V.C. did the sentiment analysis and data preprocessing, implemented the MFwBT method, wrote the Data Acquisition, Sentiment Analysis, MFwBT Methodology, Results, and Acknowledgements sections in the report; H.J. acquired the data, assisted with the data preprocessing and sentiment analysis, implemented the SBRW method, performed the signed butterfly calculations, co-wrote the Abstract, Introduction, Background information sections, and wrote the Balance Theory, SBRW Methodology, and Conclusion sections in the report

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46 applied these methods to three datasets. One of these is the  
 47 Bonanza dataset belonging to a shopping website similar to  
 48 Amazon, while the other two differ in that they are datasets  
 49 covering vote information for political purposes (9). As de-  
 50 scribed in the work of Derr et al, these methods that receive  
 51 aid from balance theory perform better than their respective  
 52 baseline methods (9). The good performance of these models,  
 53 especially on the Bonanza dataset, motivates our choice to  
 54 apply them in the Amazon setting.

## 55 Background Information

56 We limit the scope of our analysis to the Amazon Fashion  
 57 Products dataset (13). Specifically, we select a 5-core, ran-  
 58 domly sampled reviews dataset. The small size of the subset  
 59 enables our processes to be computationally feasible and its  
 60 density (k-core) provides repeated measures that are crucial  
 61 in making consumer-specific predictions.

62 Prior to creating the network, we perform sentiment anal-  
 63 ysis, which uses natural language processing to determine  
 64 whether the sentiment of a text is positive or negative. Based  
 65 on the results, we create an undirected signed bipartite net-  
 66 work. In the construction of our network, we draw inspiration  
 67 from the work of Wang on Yelp reviews (8). Similarities in-  
 68 clude incorporating a bipartite network with two distinct types  
 69 of nodes. The first group of nodes would be the reviewers  
 70 and the second group of nodes would be the Amazon fashion  
 71 products. An edge represents that a reviewer wrote review for  
 72 that specific product. The network is undirected because this  
 73 relationship is nondirectional by nature. Our work varies from  
 74 Wang's in the assignment of edge weights due to the additional  
 75 component of reviewer sentiment. The network is weighted,  
 76 and the weights are the sentiment values derived from the  
 77 results of sentiment analysis. We restrict the edge weight to  
 78 be either -1 or 1, with 1 representing positive sentiment and  
 79 -1 representing negative sentiment. It would be more reliable  
 80 to have values between -1 and 1 in order to emphasize different  
 81 degrees of sentiment toward the products. However, we opt  
 82 for two discrete values to simplify the sign prediction process.

83 At the beginning, after constructing such a network, we  
 84 aimed to utilize centrality measures to rank products based  
 85 on reviewer generosity, and identify reviewers with the most  
 86 extreme sentiments. However, since our network involves  
 87 signs and is bipartite, there's no suitable centrality measures  
 88 available for us to use. Thus, we modify our topic to make  
 89 sign predictions which is equally interesting and has existing  
 90 literature.

## 91 Materials and Methods

92 **Data Acquisition.** The dataset used in this project comes from  
 93 Dr. Julian McAuley's research group at UC San Diego (12).  
 94 Professor McAuley is a computer scientist whose research  
 95 focuses on machine learning and recommender systems. His  
 96 website contains a wide variety of datasets spanning from  
 97 Google local reviews to Food recipes. To be allowed to use  
 98 his dataset, he has requested that his works regarding the  
 99 dataset to also be cited. His dataset regarding Amazon product  
 100 reviews contains over 80 million reviews from over 20 million  
 101 users. Professor McAuley et al. has used this data to study  
 102 the evolution of fashion trends using one-class collaborative  
 103 filtering and image-based recommendations (14, 15).

104 The dataset we use is a smaller subset of only 3000 product  
 105 reviews coming from the fashion category (13). The dataset  
 106 contains information such as the style and size of clothing,  
 107 review date, ratings, etc., but the only information we need to  
 108 construct our bipartite network is the product, reviewer, and  
 109 the review sentiment.

110 **A. Sentiment Analysis.** As the product names and reviewers  
 111 are already in the dataset, we still need to find the review  
 112 sentiment for each product review. This is accomplished by  
 113 extracting positive or negative sentiment from the review text,  
 114 also known as sentiment analysis. Sentiment analysis uses  
 115 natural language processing to determine if the sentiment of a  
 116 piece of text is positive or negative. Some of the most common  
 117 sentiment analysis libraries in Python include nltk, textblob,  
 118 bert, etc. This project constructed sentiment bipartite net-  
 119 works using nltk.

120 To construct the bipartite network using nltk, we treat the  
 121 sentiment analysis as a classification task where we build a  
 122 machine learning model to predict whether a given product  
 123 review is positive or negative (17). As sentiment analysis is  
 124 a supervised method, we require target variables. For our  
 125 case, the target variables that the machine learning model  
 126 will be trained on will be based on the ratings of the product  
 127 review. Because most of the ratings rated the products as  
 128 4/5 or 5/5 stars, we decide to categorize ratings of 3 stars or  
 129 below as negative reviews. This decision is made in hopes that  
 130 this will create a more balanced network instead of one that  
 131 is overwhelmingly positive. A possible reason why product  
 132 reviews are generally positive could be that buyers who are  
 133 unsatisfied with their purchase simply requested a return and  
 134 never left a negative feedback.

135 Next, we generated the term document matrix using count  
 136 vectorizer in the scikit learn library. Term document matrix is  
 137 a data frame that counts the occurrences of words across all  
 138 texts and outputs a matrix where the rows are the text it came  
 139 from and the columns are the words that appeared in the text.  
 140 By our construction, we disregard words that appear rarely  
 141 as well as words that appear too frequently. We also ignore  
 142 English "stopwords", which are words that are frequently use  
 143 but don't provide any contextual information such as "the, I,  
 144 and, too, etc." This results in a term document matrix as seem  
 145 below. The matrix contains over 3000 reviews and over 200  
 146 predictor words.

	able	absolutely	actually	amazing	amazon	ankle	arch	arches	area	...	wish	wore	work	worked	working	workout	workouts	worn	years
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
4	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...
3171	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
3172	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
3173	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
3174	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	1	0
3175	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0

Fig. 1. Term Document Matrix

147 We select logistic regression as the machine learning model  
 148 for sentiment analysis. The reason behind choosing logistic  
 149 regression and not support vector machine or neural networks  
 150 is because we are able to easily interpret the sentiment of  
 151 individual words using the coefficients of the logistic model.  
 152 These coefficients are the weights of each individual word used  
 153 in model prediction to determine whether the entire review

is positive or negative. Tables 1 and 2 show the top 5 most positive and top 5 most negative words found after conducting sentiment analysis.

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**Table 1. Words in Term Document Matrix with Most Positive Sentiments**

coef	word
2.249833	perfect
2.014510	lightweight
1.667149	smaller
1.655638	make
1.617396	white

**Table 2. Words in Term Document Matrix with Most Negative Sentiments**

coef	word
-2.969220	returned
-2.750874	left
-2.483192	fine
-2.061016	support
-2.008989	large

Notice that while some sentiments determined by the model intuitively make sense, such as "perfect" and "returned" being associated with positive and negative reviews, there are also words whose sentiments aren't very obvious such as "smaller" being positive and "large" being negative. After tuning the complexity and doing 5-fold cross validation, the model is able to achieve a 96.8% accuracy in identifying positive and negative product reviews. We assign the positive reviews with edge weight of 1 and negative reviews with edge weight of -1, combined with the product and reviewer information, we have constructed the bipartite signed network.

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We also conducted sentiment analysis using the textblob library in Python, where we input the review text and the model outputs a polarity score. This however did not provide as much insight as the model we built using nltk, so it was not used in later steps.

**Data Visualization.** The Figure 2 is generated by using Python and NetworkX. It has 368 nodes and 2484 number of edges in total, so the edges are densely distributed in the network. The left group of nodes are the Amazon Fashion Products, and the right group of nodes are the reviewers. Since the network is bipartite, there could only be edges between different types of nodes.

The network is composed of only two colors, red and green. An red edge means that the reviewer wrote a negative review for that product, and a green edge means that the reviewer wrote a positive review for that product. In this network, it can be clearly seen that most of the edges are green with only a few red edges, which means that people prefer to give positive feedback in general for Amazon Fashion Products. This is also true in reality where we can see most people tend to give good comments when writing reviews for the products.

Also, we can see the green tend to be deeper in the left group of nodes because these nodes representing Amazon Fashion

Products have much higher degrees than the reviewers, which means there are much more edges attached to them.

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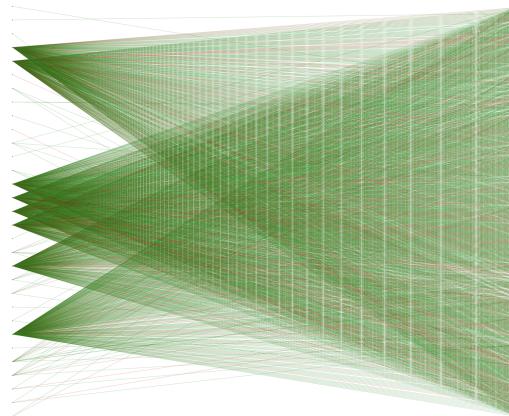
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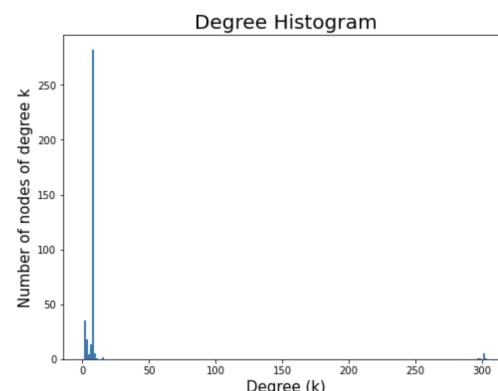
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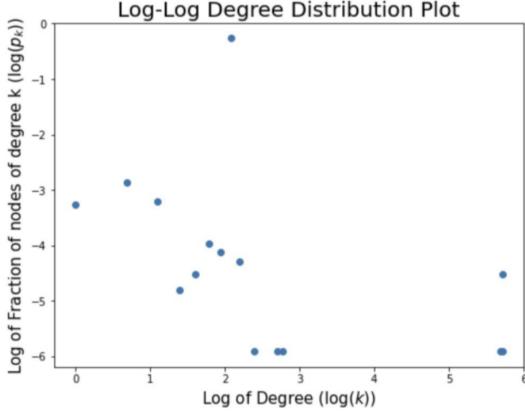
**Fig. 2. Undirected Signed Bipartite Network Visualization**

The Figure 3 is the degree histogram. It is drawn by using Python and NetworkX. We can see that most of the nodes have degree less than 20, and only a very few have degree around 300, so the histogram becomes loosely distributed.



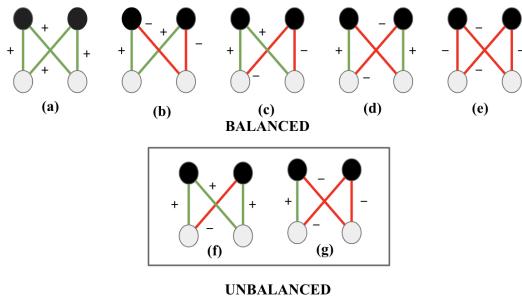
**Fig. 3. Degree Histogram**

The Figure 4 is the log-log degree distribution plot. Most of the nodes in this network have degree less than 20. However, some of the nodes have degree around 300 that are Amazon Fashion Products which receive high amount of reviews from customers. Thus, there can be a really large gap between these degree values, so it would be more reasonable to use a log-log plot instead of the original one.



**Fig. 4.** Log-Log Degree Distribution Plot

**Balance Theory.** The study of signed networks is challenging because we lose access to otherwise useful tools such as centrality measures. We utilize balance theory because it is designed for signed networks and is the most advanced technique in their study (11). Balance theory uses the notion of tension in social systems to classify these systems as either balanced – which are less likely to change – or unbalanced. Applying lessons from traditional balance theory to bipartite networks, however, is not straightforward. Bipartite networks have two key hindrances in that they have two different types of nodes and do not have triads. Derr et. al expand the functionality of balance theory to bipartite networks with the creation of signed butterflies as illustrated in Fig. 5. In 5(a), the structure with all positive signs represents that both the reviewers reviewed the two products positively. Unbalanced structures in 5(f) and 5(g) represent unstable scenarios where two reviewers possess opposing views on the same products. In real-life, we expect unbalanced structures to occur less frequently due to their unstable nature (1). We count the instances of different classes of balanced and unbalanced signed butterflies in our dataset. Table 3 verifies that for the Amazon fashion products dataset, we observe a significantly greater proportion of balanced scenarios. We show that the dataset adheres to balance theory defined in terms of signed butterflies, making balance theory based sign prediction methods viable in this context.



**Fig. 5.** The Seven Signed Butterfly Structures

**Table 3. Signed Butterfly Distribution in the Amazon Products Dataset**

Signed Butterfly Class	Count	%
(a) (+,+,+,+)	3,573,088	83.3
(b) (+,-,-,+)	609,556	14.2
(c) (+,+,-,-)	16	3.73e-04
(d) (+,-,+,-)	0	0
(e) (-,-,-,-)	101,196	2.34
<b>Balanced</b>	<b>4,283,856</b>	<b>85.6</b>
(f) (+,+,-,-)	4072	0.09
(g) (+,-,-,-)	682	0.02
<b>Unbalanced</b>	<b>4,754</b>	<b>0.11</b>

**A.1. Signed Caterpillars Based Classifier Method.** The first sign prediction method that will be covered in this project is the SCsc method, which is short for Sign Caterpillars Based Classifier. A signed caterpillar is paths of length 3 that are missing just one link to become a signed butterfly that's covered above in balance theory, and it can either have balance path or unbalanced path (9). A balanced path means presence of even number of negative links among those three, while an unbalanced path means presence of odd number of negative links among those three. In this method, the signs are predicted by extracting features from either the individuals (i.e. their positive or negative degrees) or local neighborhood features based on balance theory (i.e. signed caterpillars), and Logistic regression machine learning model is built to make final predictions (9). This method is successfully implemented by modifying the existing coding template provided in the work of Derr et al (16). We applied this method by first dividing the original Amazon Fashion dataset into two different sets, with 90 percent as the training set and the rest 10 percent as the test set, so we can check the performance of our model based on the test set.

**A.2. Random Walk Based Signed Prediction Method.** Random-walk-based methods are a ubiquitous solution for various purposes including link prediction. Previous applications of these methods have been limited to link prediction in unsigned unipartite networks. Derr et al. extend their application to sign prediction and incorporate balance theory (9). We reproduce their method for the Amazon dataset and detail the corresponding process below.

To make use of the random-walk-based models, the bipartite network  $\mathbf{B}$  is first converted into a unipartite one  $\mathbf{A}$ . This is achieved by creating one-mode projection matrices for  $\mathbf{U}_P$  and  $\mathbf{U}_R$ , which are the sets of product and reviewer nodes respectively. Then, the projection matrices are converted into an adjacency matrix  $\mathbf{A}$ . To create the one-mode projection matrices, Derr et al. use balance theory to form signed triangles. Let  $ns_{ij}^A$  be the number of products that reviewers  $i$  and  $j$  agree on. Conversely, let  $ns_{ij}^D$  be the number of products they disagree on. Then  $\mathbf{P}_{Rij} = \mathbf{P}_{Rji} = ns_{ij}^A - ns_{ij}^D$  where  $\mathbf{P}_R$  is the reviewer projection matrix. In words,  $\mathbf{P}_R$  represents the degree of agreement between different reviewers. We can construct a products projection matrix  $\mathbf{P}_P$  in a similar manner. The real-life interpretation of such a matrix is not as straightforward as that of reviewers, but it can be understood to represent the degree of similarity in being liked or disliked between different products. To avoid adding trivial connections,

## 229 Sign Prediction Methods.

we bound  $ns_{ij}^A - ns_{ij}^D$  using the following definition:

$$P_{Rij} = \begin{cases} 0 & \text{if } \delta_{low} < ns_{ij}^A - ns_{ij}^D < \delta_{high} \\ ns_{ij}^A - ns_{ij}^D & \text{otherwise} \end{cases} \quad [1]$$

where we arbitrarily pick  $\delta_{low} = -10$  and  $\delta_{high} = 10$ .

The projection matrices  $\mathbf{P}_R$  and  $\mathbf{P}_P$  are converted into adjacency matrix  $\mathbf{A}$  according to the following definition:

$$\mathbf{P}_{Rij} = \begin{bmatrix} \hat{\mathbf{B}}_B & \omega\hat{\mathbf{B}} \\ \omega\hat{\mathbf{B}}^T & \hat{\mathbf{B}}_S \end{bmatrix} \quad [2]$$

where  $\hat{\mathbf{B}}$  is the row normalized version of  $\mathbf{B}$ , defined as  $\hat{\mathbf{B}}_{ij} = \mathbf{B}_{ij} / \sum_k |\mathbf{B}_{ik}|$  and  $\omega$  is a parameter created to favor the real, existing links rather than those inferred using balance theory. Finally, we use a random-walk-based model and define  $\mathbf{Y}$ :

$$\mathbf{Y}_{ij} = \sum_k \hat{\mathbf{A}}_{ik} \mathbf{Y}_{kj} \quad [3]$$

We obtain the link sign predictions from the upper right corner of  $\mathbf{Y}$ .

**A.3. Matrix Factorization with Balance Theory Method.** Matrix Factorization with Balance Theory, or MFwBT, is a method that expands on the Basic Matrix Factorization model by incorporating Balance Theory (9).

The matrix factorization model approach considers the following optimization problem:

$$\min_{U,V} \sum_{(p_i,r_j) \in \mathcal{E}} \max(0, 1 - \mathbf{B}_{ij}(\mathbf{u}_i^\top \mathbf{v}_j))^2 + \lambda(|\mathbf{U}|_F^2 + |\mathbf{V}|_F^2) \quad [4]$$

Where the objective is to discover the latent matrices of the set of products and reviewers,  $\mathbf{U} = [\mathbf{u}_1, \mathbf{u}_2, \dots, \mathbf{u}_{n_P}] \in \mathbb{R}^{d \times n_P}$  and  $\mathbf{V} = [\mathbf{v}_1, \mathbf{v}_2, \dots, \mathbf{v}_{n_R}] \in \mathbb{R}^{d \times n_R}$  for dimension  $d$ . Given  $\mathbf{u}_i^\top \mathbf{v}_j$  is the predicted link sign between product  $p_i$  and reviewer  $r_j$ , and  $\mathbf{B}_{ij}$  is the real link sign between product  $p_i$  and reviewer  $r_j$ , summed over  $\mathcal{E}$  the set of edges in the bi-adjacency matrix  $\mathbf{B}$ . If the predicted link and the real link are of the same sign and greater than 1, there is no loss. If the predicted link and the real link have different signs, then the loss value will drive the minimization during the training process. This minimization can be achieved using Stochastic Gradient Descent (SGD) following the works of (18).

The shortfall of matrix factorization is that it focuses on minimizing the errors of predicting existing link signs, by incorporating balance theory, it can convert many signed caterpillars into balanced signed butterflies to encourage the learning of link signs of product and reviewer pairs that previously did not exist.

The Matrix Factorization with Balance Theory method is given by:

$$\begin{aligned} \min_{U,V} \sum_{(p_i,r_j) \in \mathcal{E}} & \max(0, 1 - \mathbf{B}_{ij}(\mathbf{u}_i^\top \mathbf{v}_j))^2 + \lambda(|\mathbf{U}|_F^2 + |\mathbf{V}|_F^2) \\ & + \alpha \sum_{(p_i,r_j) \in \mathcal{E}_i^+} \max(0, 1 - \hat{\mathbf{S}}_{ij}(\mathbf{u}_i^\top \mathbf{v}_j))^2 \\ & + \beta \sum_{(p_i,r_j) \in \mathcal{E}_i^-} \max(0, 1 - \hat{\mathbf{S}}_{ij}(\mathbf{u}_i^\top \mathbf{v}_j))^2 \end{aligned} \quad [5]$$

Where  $\alpha, \beta$  are weights used to control the incorporation of signed butterflies  $\hat{\mathbf{S}}$  using implicit positive and negative links  $\mathcal{E}_i^+$  and  $\mathcal{E}_i^-$  as defined by the balance theory.

The implementation of MFwBT ran into trouble because the code implementation provided by Derr et al. requires an "extra\_links\_from\_B\_balance\_theory.txt" file (16). Based on inference, we presume these extra link files are the implicit positive and negative links  $\mathcal{E}_i^+$  and  $\mathcal{E}_i^-$ . However, the authors did not explain how these extra links are generated and there is no example of how such a link file would be formatted. Had I, Vincent, noticed this missing detail earlier, we might have had enough time to generate some form of extra link file through pure trial and error to get some result. As a result, we failed to implement this method with our signed bipartite network.

## Results

The results are given by two metrics, the AUC score and F1 score. AUC, or the "Area Under the ROC Curve," measures the two-dimensional area under the ROC (receiver operating characteristic) curve. The ROC curve plots True Positive Rate (TPR) vs. False Positive Rate (FPR) on a scale from 0 to 1 for different classification thresholds (19). True Positive Rate and False Positive Rate are given by the formulas:

$$\begin{aligned} \text{TPR} &= \frac{\text{True Positive}}{\text{True Positive} + \text{False Negative}} \\ \text{FPR} &= \frac{\text{False Positive}}{\text{False Positive} + \text{True Negative}} \end{aligned} \quad [6]$$

In simplest terms, if AUC is 0.0, the classifier is misclassifying all positives as negatives, and all negatives as positives; if AUC is 0.5, the classifier is classifying values at a rate no better than a coin flip; if AUC is greater than 0.5, the classifier is classifying most values correctly, and if AUC is exactly 1, it is classifying all values correctly (21).

The other metric is the F1 score, which is the harmonic mean of precision (P) and recall (R) (20):

$$\frac{1}{F_1} = \frac{\frac{1}{P} + \frac{1}{R}}{2} \quad [7]$$

Note precision is the percentage of positively classified that are actually positive:

$$\text{Precision} = \frac{\text{True Positive}}{\text{True Positive} + \text{False Positive}} \quad [8]$$

And recall is the percentage of actual positives that are correctly classified:

$$\text{Recall} = \frac{\text{True Positive}}{\text{True Positive} + \text{False Negative}} \quad [9]$$

F1 score is useful for imbalanced data because it is a better metric than plain accuracy.

The result of the code implementation of our sign prediction method is given by Table 4.

Observe that the Signed Bipartite Random Walk Method (SBRW) performed better than the Signed Caterpillar based Classifier Method (SCsc) on both metrics. This is different from the result of the paper where the methods are based on (9), where no one single method outperformed others across all datasets and metrics. However, considering that we only

**Table 4. Link Sign Prediction Results in terms of (AUC, F1)**

Metric	SCsc	SBRW	MFwBT
AUC	0.864	0.970	-
F1	0.877	0.993	-

367 have one dataset and implemented two of the three methods,  
368 it is probably not out of the ordinary.

369 Also notice that F1 score tends to be higher than AUC  
370 score. This confirms the results from Derr et al.'s paper where  
371 the F1 scores are much higher than AUC in the Bonanza  
372 dataset (9). In the paper, the Bonanza dataset has a heavy  
373 positive imbalance where 98% of the links are positive. This is  
374 similar to our dataset where 85% of the links are positive. In  
375 cases like these, the AUC is a more accurate metric than F1.  
376 We can see that to better detect negative links, some positive  
377 links are misclassified.

378 According to the literature, the Matrix Factorization with  
379 Balance Theory method (MFwBT) is supposedly better at  
380 balancing the ratio of positive and negative implicit links  
381 depending on the choice of  $\alpha$  and  $\beta$  (9). However, this is hard to  
382 confirm because we did not successfully implement the method  
383 and the paper itself fixed  $\alpha = \beta$  for their experimentations.

## 384 Conclusion

385 In conclusion, the outcomes of this paper are illuminating on  
386 multiple fronts. Firstly, we devise a method to study reviewer  
387 sentiments in a way that utilizes network features. Specifically,  
388 we construct an undirected, signed, bipartite product-reviewer  
389 network where the signs represent discrete values of reviewer  
390 sentiment. We also carefully extract sentiment values using  
391 natural language processing. Secondly, we conduct exploratory  
392 analysis of the network, generating insights on the degree dis-  
393 tribution, sentiment (sign) distribution, and adherence to bal-  
394 ance theory. Finally, we explore three sign prediction methods  
395 and successfully implement two with more than 85% accuracy.  
396 The accuracy and effectiveness of Amazon's prediction systems  
397 likely remain confidential, making comparison of our models  
398 with theirs difficult. We are also not aware of any other aca-  
399 demic work in predicting consumer sentiment that our results  
400 can be compared with. Nonetheless, with a limited number  
401 of features and an avoided risk of privacy issues, our models  
402 obtain an objectively reliable accuracy. The code materials  
403 and data to reproduce our results can be found at [this link](#).

## 404 Limitations

405 The first limitation of our project is that the edges weights of  
406 our undirected signed bipartite network are constrained to be  
407 either 1 or -1. In reality, there should be values between -1  
408 and 1 to represent different levels of positive sentiment and  
409 negative sentiment. In our case, a reviewer could extremely  
410 like a product or just kind of like the product which make a  
411 huge difference. However, we only use 1 and -1 in this project  
412 in order to simplify our sign prediction process.

413 The second limitation is that we only use a small subset  
414 for experimentation with only thousands of product reviews.  
415 In reality, there would be much larger dataset which cannot  
416 be tested in our own computer. The machine learning models

417 would be more accurate if we can apply sign prediction to a  
418 larger dataset.

419 The third limitation is that when a person rates a product  
420 multiple times, we only keep the first sentiment value in order  
421 to avoid multi-edges.

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