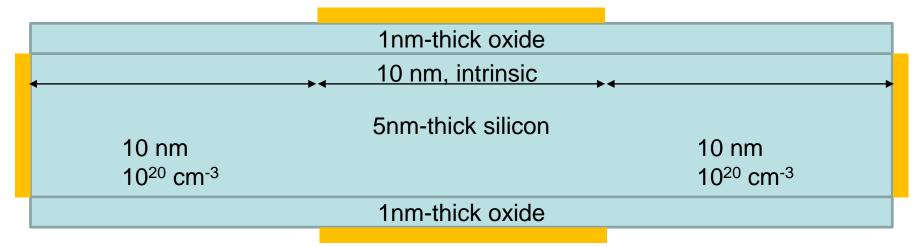
#### Lecture21

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#### Homework#17

- Due: AM08:00, November 23 (Next Monday)
- Problem#1
  - Calculate the I<sub>D</sub>-V<sub>D</sub> curve of the double-gate MOSFET. Consider several gate voltages (0 V ~ 1.1 V).



### Finite volume method

- FEM is <u>NOT</u> used.
- The box method is used.
  - Differential form

$$\nabla \cdot \mathbf{F} = s$$

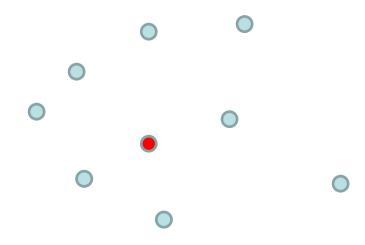
Integrated form

$$\oint_{\partial \Omega} \mathbf{F} \cdot d\mathbf{a} = \int_{\Omega} s d^3 x$$

- $\Omega$  is the Voronoi cell.
- Delaunay mesh is needed!

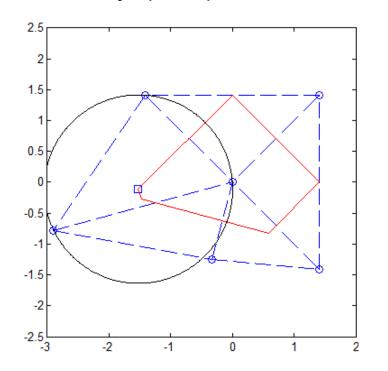
#### Voronoi volume

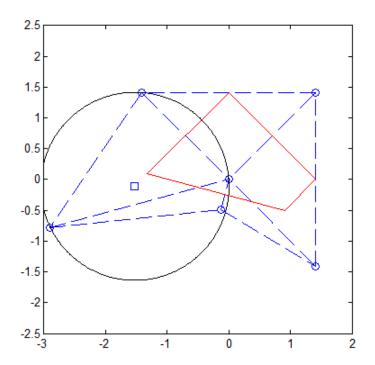
- Within the Voronoi volume of a center node, the closest node is the center node.
  - Calculating the plane (3D) or the line (2D), which is perpendicular to an edge and cross its mid-point



# Pentagon examples

Delaunay (Left) versus non-Delaunay (Right)



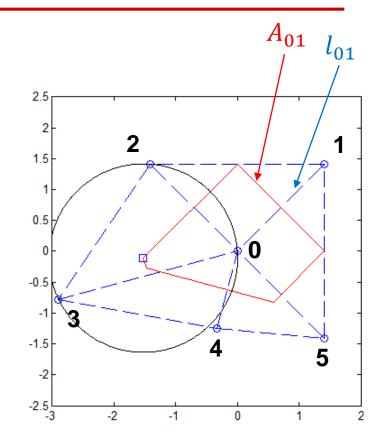


# Poisson equation

- LHS,  $\oint_{\partial\Omega} \mathbf{F} \cdot d\mathbf{a}$ 
  - It can be written as

$$\sum_{i=1}^{5} F_{0i} A_{0i} = -\sum_{i=1}^{5} \epsilon \frac{\phi_i - \phi_0}{l_{0i}} A_{0i}$$

- We must calculate  $l_{0i}$  and  $A_{0i}$ .



## Recipe

- For a 2D structure, it is not very difficult.
  - For each triangle whose side lengths are a, b, and c, calculate the circumradius, R.

$$Area = \frac{abc}{4R}$$

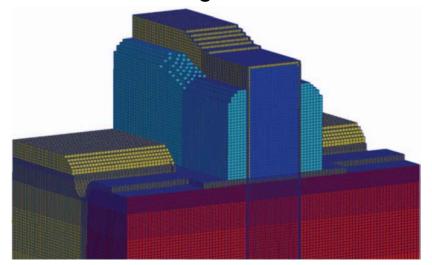
From the circumcenter, by using the Pythagorean theorem,

$$R^2 = \left(A_{01,triangle}\right)^2 + \left(\frac{l_{01}}{2}\right)^2$$

How about an obtuse triangle?

### 3D mesh?

- Tetrahedron-based mesh
  - Difficult to calculate Voronoi cells
  - Structured grid cannot be used.



A structured grid (L. Wang et al., ULIS, 2014)

