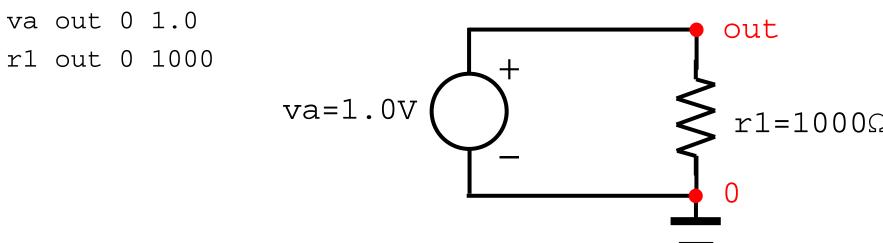
Lecture24

Sung-Min Hong (smhong@gist.ac.kr)

Semiconductor Device Simulation Lab.
School of Electrical Engineering and Computer Science
Gwangju Institute of Science and Technology

How to describe a circuit

- Of course, we can draw a circuit schematic. What else?
- A netlist for this circuit looks like:



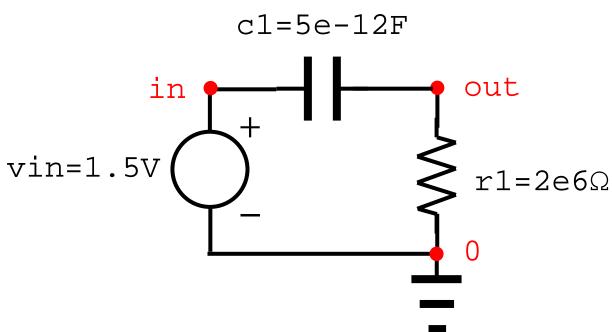
Format for two-terminal devices

elementlabel node1 node2 value

RC filter

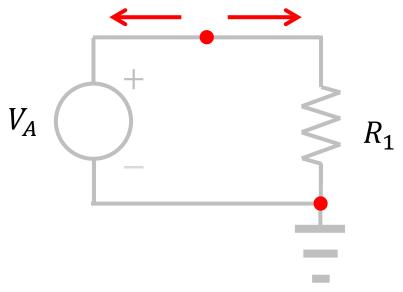
A netlist for this circuit looks like:

c1 in out 5e-12 r1 out 0 2e6 vin in 0 1.5



Circuit analysis (1)

- Kirchhoff's current law (KCL)!
 - At any node in an electrical circuit, the sum of currents flowing into that node is equal to the sum of currents flowing out of that node.



Circuit analysis (2)

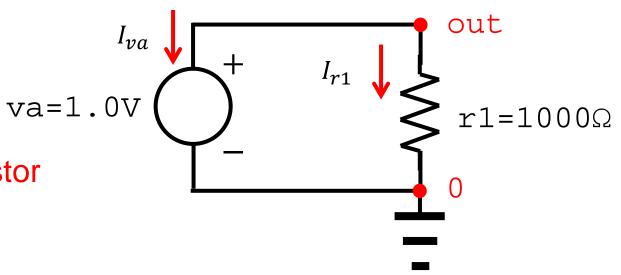
- Our simple problem
 - Three equations:

Voltage source

$$V(out) - 0.0 = 1.0$$

$$V_{r1} = \frac{V(out)}{1000}$$
 Resistor

$$I_{va} + I_{r1} = 0$$
 KCL



Implementation?

- Solution vector, $[I_{va} \quad I_{r1} \quad V(out)]^T$
 - Then, the system is written as

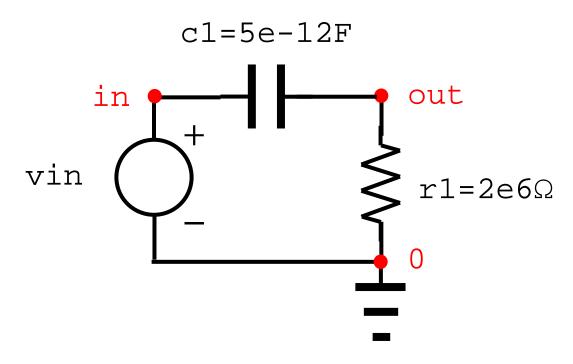
$$\begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & -0.001 \\ 1 & 1 & 0 \end{bmatrix} \begin{vmatrix} I_{va} \\ I_{r1} \\ V(out) \end{vmatrix} = \begin{bmatrix} 1.0 \\ 0 \\ 0 \end{bmatrix}$$

The solution is

$$\begin{bmatrix} I_{va} \\ I_{r1} \\ V(out) \end{bmatrix} = \begin{bmatrix} -0.001 \\ +0.001 \\ 1.0 \end{bmatrix}$$

RC circuit

Solve a simple transient problem by a numerical means.



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Frequency domain

• At a frequency, f, the impedance of the RC part is $Z(\omega) = R + \frac{1}{i\omega C}$ ($\omega = 2\pi f$)

- Therefore,

$$I(\omega) = \frac{V(\omega)}{Z(\omega)} = \frac{V(\omega)}{R + \frac{1}{i\omega C}} = \frac{j\omega C + \omega^2 R C^2}{1 + (\omega R C)^2} V(\omega)$$

- For example, when $V(t) = V_0 \cos \omega t$,

$$I(t) = \frac{\omega^2 R C^2}{1 + (\omega R C)^2} V_0 \cos \omega t - \frac{\omega C}{1 + (\omega R C)^2} V_0 \sin \omega t$$

Circuit analysis

Five equations

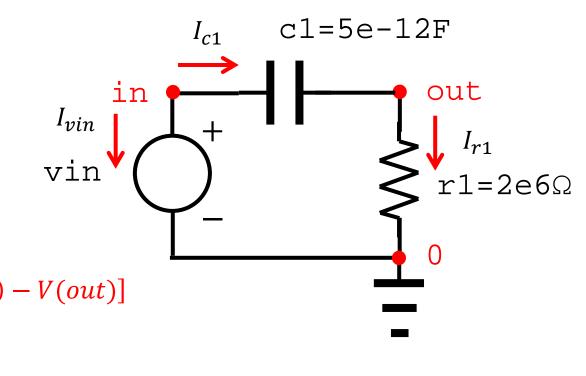
- Two KCL's
$$I_{vin} + I_{c1} = 0$$
 $-I_{c1} + I_{r1} = 0$

Three equations

$$V(in) - 0.0 = \cos \omega t$$

$$I_{c1} = 5 \times 10^{-12} \frac{d}{dt} [V(in) - V(out)]$$

$$I_{r1} = \frac{V(out) - 0.0}{2 \times 10^6}$$



Implementation?

- Solution vector, $[I_{vin} \ I_{c1} \ I_{r1} \ V(in) \ V(out)]^T$
 - Then, the system is written as

$$= \begin{bmatrix} \cos \omega t \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

Backward Euler

- An implicit method
 - Uniform time discretization, $t_i = i\Delta t$
 - The time derivative at t_i is assumed to be

$$\frac{d}{dt} \begin{bmatrix} I_{vin} \\ I_{c1} \\ I_{r1} \\ V(in) \\ V(out) \end{bmatrix}_{t=t_i} = \frac{1}{\Delta t} \begin{bmatrix} I_{vin} \\ I_{c1} \\ I_{r1} \\ V(in) \\ V(out) \end{bmatrix}_{t=t_i} - \frac{1}{\Delta t} \begin{bmatrix} I_{vin} \\ I_{c1} \\ I_{r1} \\ V(in) \\ V(out) \end{bmatrix}_{t=t_{i-1}}$$

Discretized form

- By using the backward Euler method,
 - Then, the system is written as

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MATLAB (1)

RC filter

First, define some constants.

```
R = 2e6; % Ohm
C = 5e-12; % F
freq = 1e0; % Hz
deltat = 1/\text{freg}/100; % 0.01 of a period

    The system matrix

A = zeros(5,5);
A(1,:) = [0 \ 0 \ 0 \ 1 \ 0];
A(2,:) = [0 \ 1 \ 0 \ -C/deltat \ C/deltat];
A(3,:) = [0 \ 0 \ 1 \ 0 \ -1/R];
A(4,:) = [1 1 0 0 0];
A(5,:) = [0 -1 1 0 0];
```

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MATLAB (2)

RC filter (Continued)

```
b = zeros(5,1);
solution = [0 0 0 1 0]';
N = 1000;
for ii=1:N
    t = ii*deltat;
    solution old = solution;
    b(1,1) = cos(2*pi*freq*t);
    b(2,1) = -C/deltat*(solution old(4,1)-solution old(5,1));
    solution = A \setminus b;
end
```