

Special Topics on Basic EECS I

VLSI Devices

Lecture 15

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Estimation

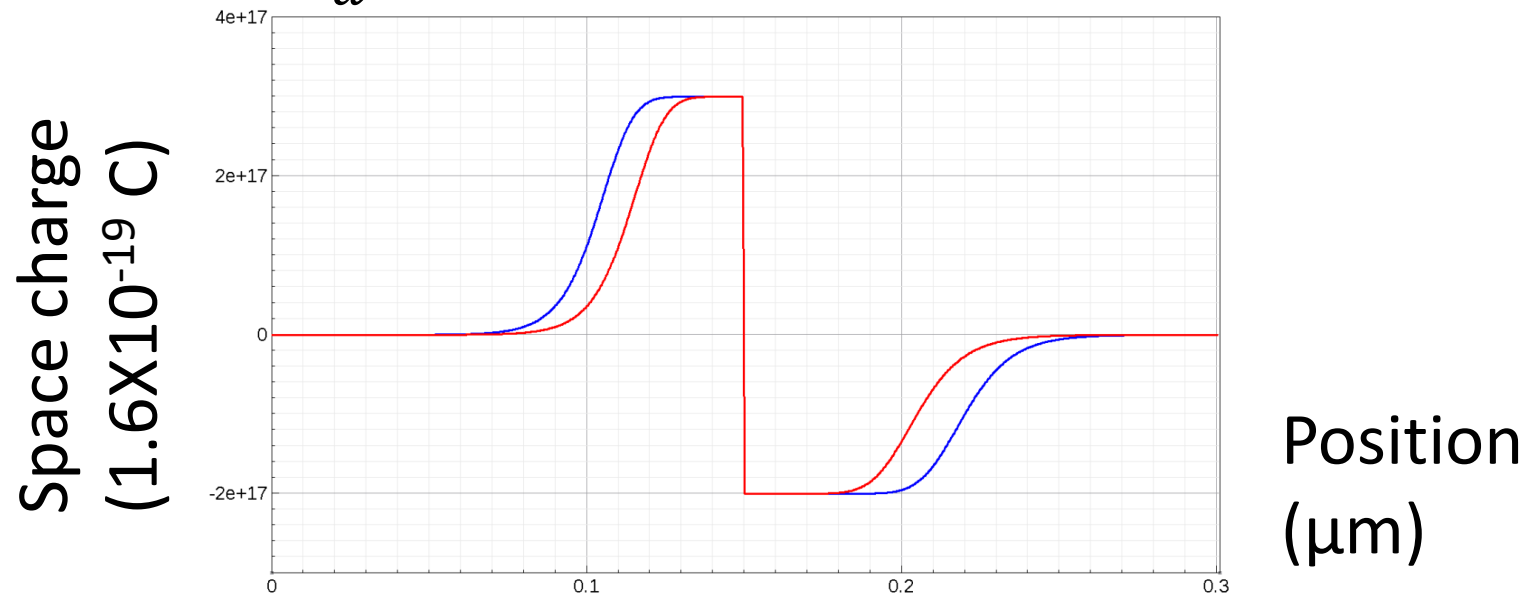
- Distance between two curves: ~ 10 nm (n-type) & ~ 15 nm (p-type)

– Then, for 0.5 V difference,

$$\Delta Q = q \times 4.8 \times 10^{-8} \text{ cm}^{-2}$$

– The capacitance becomes

$$C_d = 9.6 \times 10^{-8} \text{ F cm}^{-2}$$



Bias dependence

- Recall that the depletion width depends on the bias.
 - With the value at equilibrium

$$W_d = W_{d0} \sqrt{1 - \frac{V_{app}}{\phi_{bi}}}$$

- The capacitance becomes

$$C_d = C_{d0} \frac{1}{\sqrt{1 - \frac{V_{app}}{\phi_{bi}}}}$$

Equations in a 1D structure

- Recall the following equations:

- Current densities

$$J_n(x) = -q\mu_n(x)n(x)\frac{d}{dx}\phi_n(x) \quad \text{Taur, Eq. (2.98)}$$

$$J_p(x) = -q\mu_p(x)p(x)\frac{d}{dx}\phi_p(x) \quad \text{Taur, Eq. (2.99)}$$

- At the i -th contacts,

$$\phi_n = \phi_p = V_i$$

Quasi-Fermi potential

- For example, consider $\phi_p(x)$.

- Everywhere,


$$\frac{d}{dx} \phi_p(x) = -\frac{J_p(x)}{q\mu_p(x)p(x)}$$

Taur, Eq. (2.104)

- In the quasineutral p-region, $p(x) = p_{p0}(x) + \Delta p_p(x)$,

$$\frac{d}{dx} \phi_p(x) \approx -\frac{J_p(x)}{q\mu_p(x)p_{p0}(x)}$$

Small at low
injection

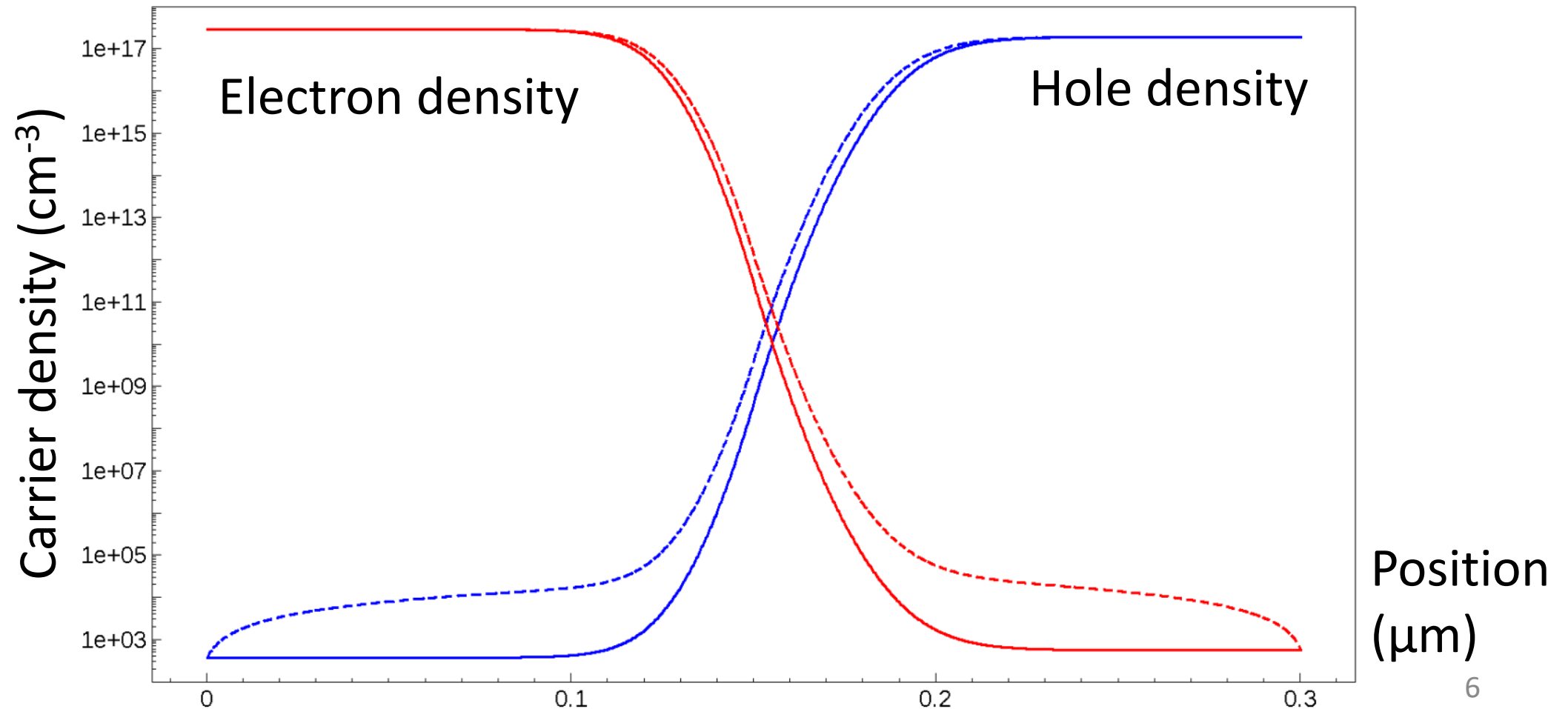


High density



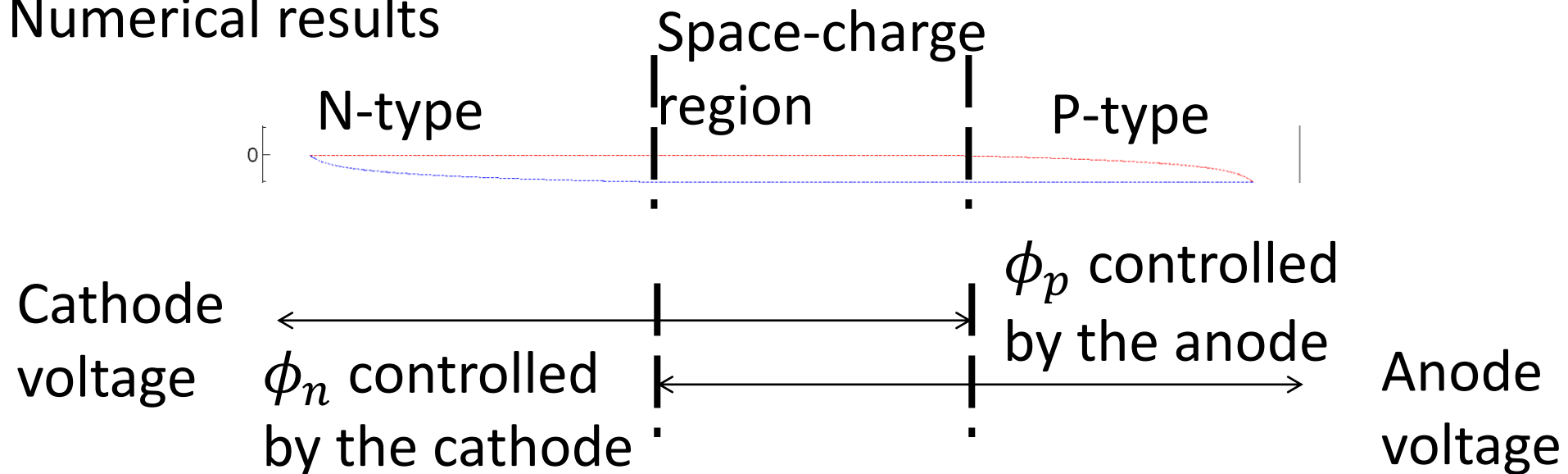
Across the space-charge region

- What is $\frac{d}{dx} \phi_p(x)$? (Solid: 0 V, dash: 0.1 V)



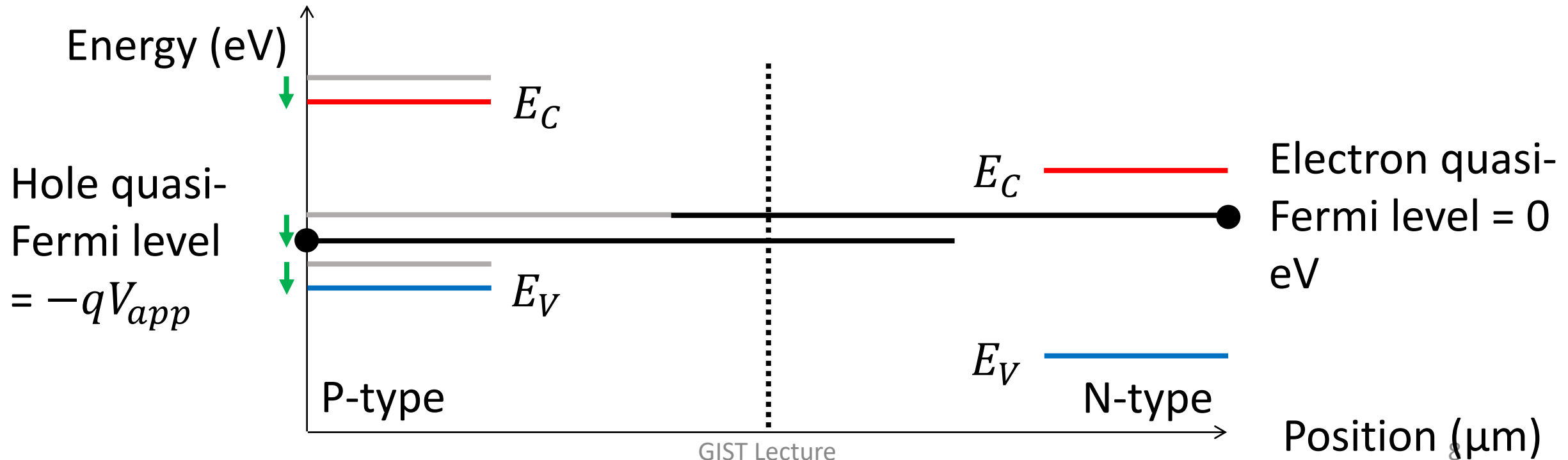
Simply speaking,

- In the forward-biased diode, ϕ_p and ϕ_n are essentially constant across the space-charge region.
 - ϕ_p and ϕ_n are also relatively constant across the space-charge region for the case of small reverse bias.
 - Numerical results



Energy band diagram, revisited

- Separation of quasi-Fermi levels
 - Then, what will happen to the minority carrier density?



Minority carrier densities

- We know that the potential difference across the space-charge region is $\phi_{bi} - V_{app}$.
 - However, the quasi-Fermi potential is constant.
 - For holes,

$$p_p(-x_p) = n_i \exp\left(-\frac{\phi(-x_p) - V_{anode}}{k_B T / q}\right)$$

- Now, the potential becomes $\phi(-x_p) + \phi_{bi} - V_{app}$ at x_n . Still, $\phi_p(x_n) = V_{anode}$.

$$p_n(x_n) = p_p(-x_p) \exp\left(-\frac{\phi_{bi} - V_{app}}{k_B T / q}\right) = p_{n0}(x_n) \exp\left(\frac{V_{app}}{k_B T / q}\right)$$

Taur, Eq. (2.108)

Shockley diode equations (Law of junction)

- A similar expression holds for electrons.

- For electrons,

$$n_p(-x_p) = n_n(x_n) \exp\left(-\frac{\phi_{bi} - V_{app}}{k_B T / q}\right) = n_{p0}(-x_p) \exp\left(\frac{V_{app}}{k_B T / q}\right)$$

Taur, Eq. (2.107)

- For holes,

$$p_n(x_n) = p_p(-x_p) \exp\left(-\frac{\phi_{bi} - V_{app}}{k_B T / q}\right) = p_{n0}(x_n) \exp\left(\frac{V_{app}}{k_B T / q}\right)$$

Taur, Eq. (2.108)

- For a forward(/reverse)-biased diode, we have an excess(/a depletion) of minority carriers at the boundaries of the quasineutral regions.

Band diagram, again

- A similar expression holds for electrons.

- For electrons,

$$n_p(-x_p) = n_n(x_n) \exp\left(-\frac{\phi_{bi} - V_{app}}{k_B T / q}\right) = n_{p0}(-x_p) \exp\left(\frac{V_{app}}{k_B T / q}\right)$$

Taur, Eq. (2.107)

- For holes,

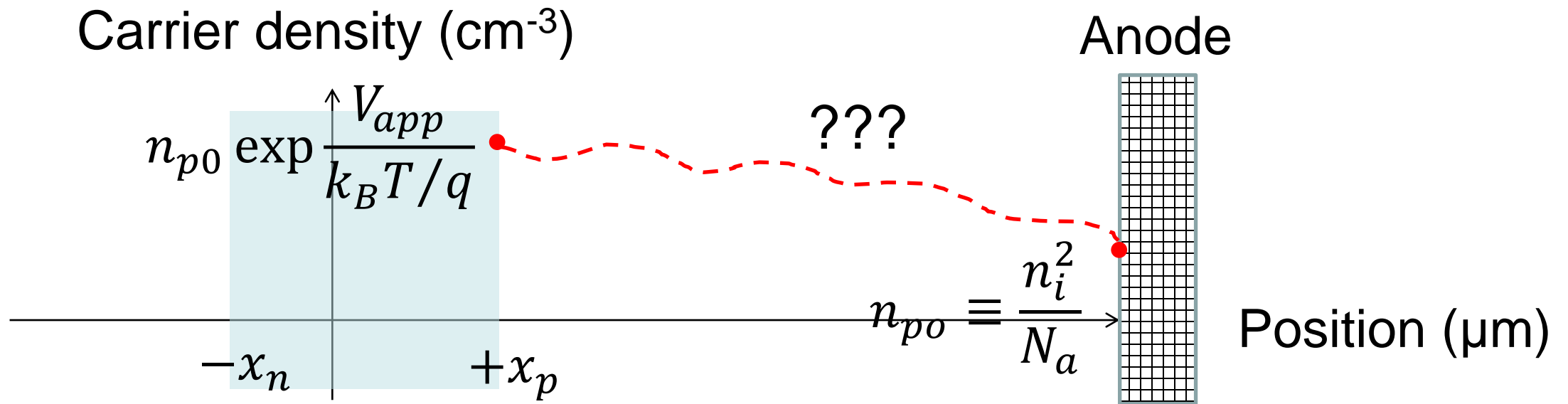
$$p_n(x_n) = p_p(-x_p) \exp\left(-\frac{\phi_{bi} - V_{app}}{k_B T / q}\right) = p_{n0}(x_n) \exp\left(\frac{V_{app}}{k_B T / q}\right)$$

Taur, Eq. (2.108)

- For a forward(/reverse)-biased diode, we have an excess(/a depletion) of minority carriers at the boundaries of the quasineutral regions.

Problem simplified

- With the law of junction, we have a simplified problem.
 - Boundary densities are fixed.
 - Electron density profile in the p-type region?



Electron continuity in p-type

- We must solve the electron continuity equation.

$$\frac{\partial n}{\partial t} = \frac{1}{q} \frac{\partial}{\partial x} J_n - R_n + G_n \quad \text{Taur, Eq. (2.109)}$$

- In the p-type region, the electric field is weak.

$$\frac{\partial n}{\partial t} = D_n \frac{\partial^2}{\partial x^2} n - \frac{n - n_{p0}}{\tau_n} \quad \text{Taur, Eq. (2.113)}$$

- At steady state,

$$\frac{d^2}{dx^2} n = \frac{n - n_{p0}}{D_n \tau_n} = \frac{n - n_{p0}}{L_n^2} \quad \text{Taur, Eq. (2.115)}$$



Electron diffusion
length

Solution of diffusion equation

- Boundary values

$$n(x_p) = n_{p0} \exp \frac{V_{app}}{k_B T / q}$$
$$n(\infty) = n_{p0}$$

- The solution is obtained as

$$n(x) = n_{p0} \left(\exp \frac{V_{app}}{V_T} - 1 \right) \exp \left(- \frac{x - x_p}{L_n} \right) + n_{p0}$$

(Our textbook considers a finite thickness of the quasineutral region.)

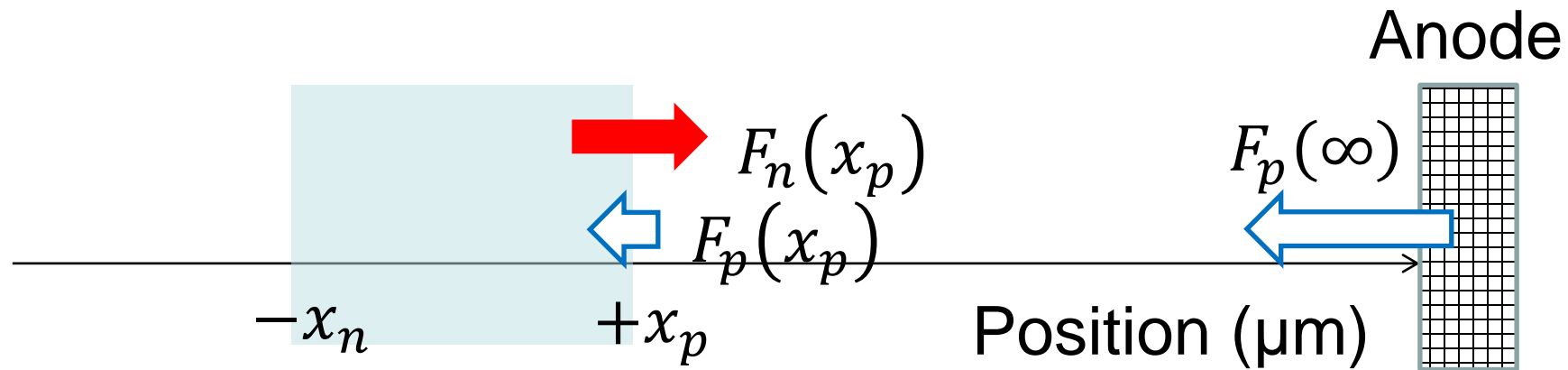
Electron flux

- The electron flux, $F_n(x)$, is found as

$$F_n(x) = -D_n \frac{dn}{dx} = \frac{D_n}{L_n} n_{p0} \left(\exp \frac{V_{app}}{k_B T / q} - 1 \right) \exp \left(-\frac{x - x_p}{L_n} \right)$$

- $-F_n(x)$ is non-uniform. The electron flux decreases as x increases.
- $-F_n(\infty)$ vanishes. All injected electrons are recombined.

$$F_p(\infty) = F_n(x_p) + F_p(x_p)$$



Thank you!