

Digital Integrated Circuit

Lecture 12 Delay

Sung-Min Hong (smhong@gist.ac.kr)

Semiconductor Device Simulation Laboratory
School of Electrical Engineering and Computer Science
Gwangju Institute of Science and Technology

Review of Previous Lecture

Lecture 11

- RC model
 - Effective resistance, R
 - Gate capacitance and diffusion capacitances, C
 - Scaling
 - There appears a chain of R and C .

4.3 RC Delay Model

4.3. RC delay model (6)

- Example 4.4
 - Estimate t_{pd} for a “unit” inverter (PMOS width:NMOS width=2:1 & minimum length) driving identical “unit” inverters.
 - Effective resistance is R . (Same for NMOS and PMOS)
 - Capacitance is $(3 + 3m)C$.
- $$t_{pd} = (3 + 3m)RC$$

4.3. RC delay model (7)

- Example 4.5

- The driver is w times unit size.
- The effective resistance is $\frac{R}{w}$ and the diffusion capacitance is wC .
- Estimate t_{pd} .

$$t_{pd} = \left(3 + 3\frac{m}{w}\right)RC$$

- With a fanout of $h = \frac{m}{w}$,

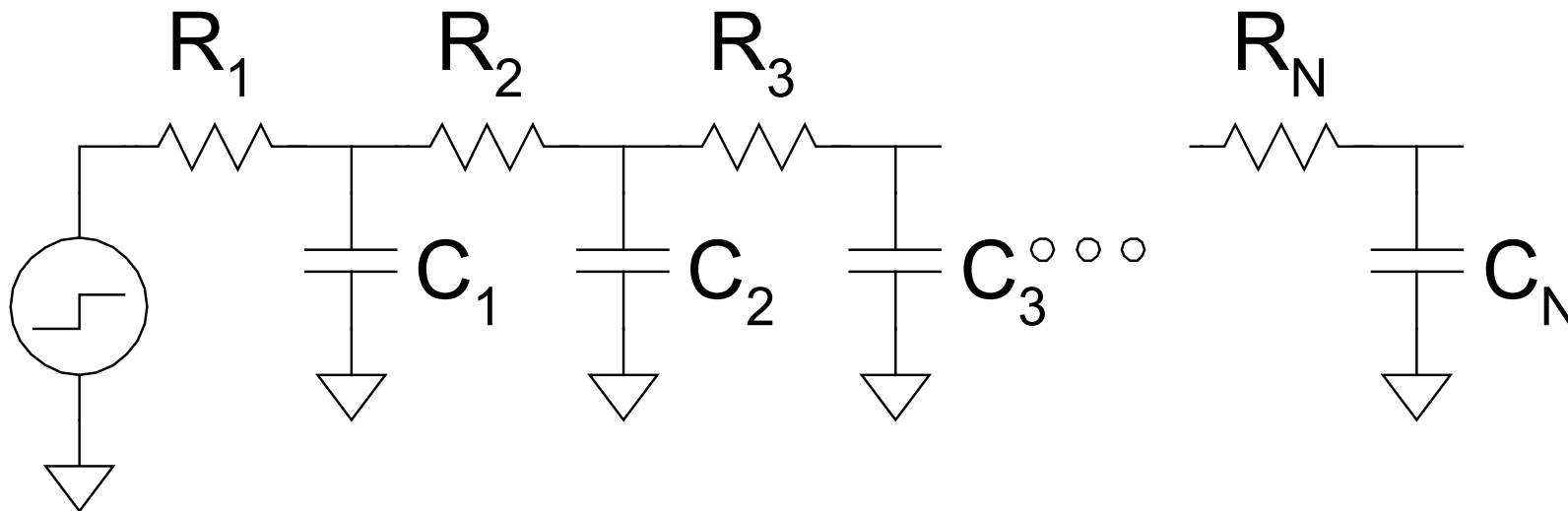
$$t_{pd} = (3 + 3h)RC$$

4.3. RC delay model (8)

- A chain of R and C
 - A simple single time constant approximation

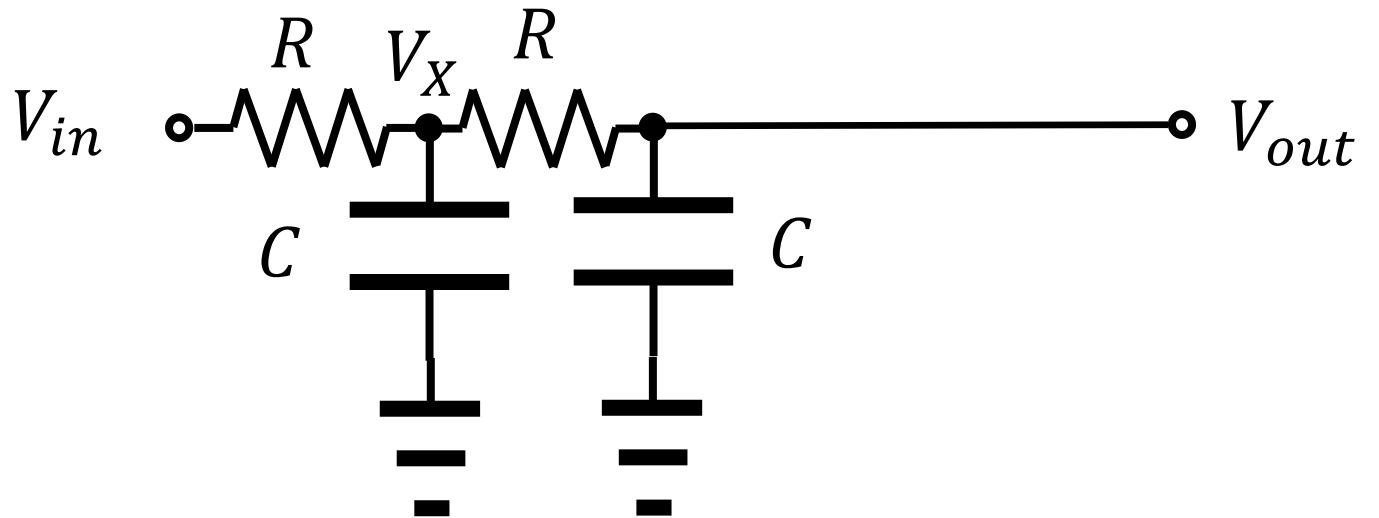
$$t_{pd} \approx \sum_{\text{nodes } i} R_{i\text{-to-source}} C_i$$

$$= R_1 C_1 + (R_1 + R_2) C_2 + \dots + (R_1 + R_2 + \dots + R_N) C_N$$



Homework#4

- Due: AM08:00, October 17
- Problem#1
 - Consider a chain of two RC components. Assume that two resistors are the same and two capacitors are the same. At $t=0$, V_{in} suddenly changes from 1 V to 0 V.
 - Draw the exact response of V_{out} and an approximated one with a single time constant.

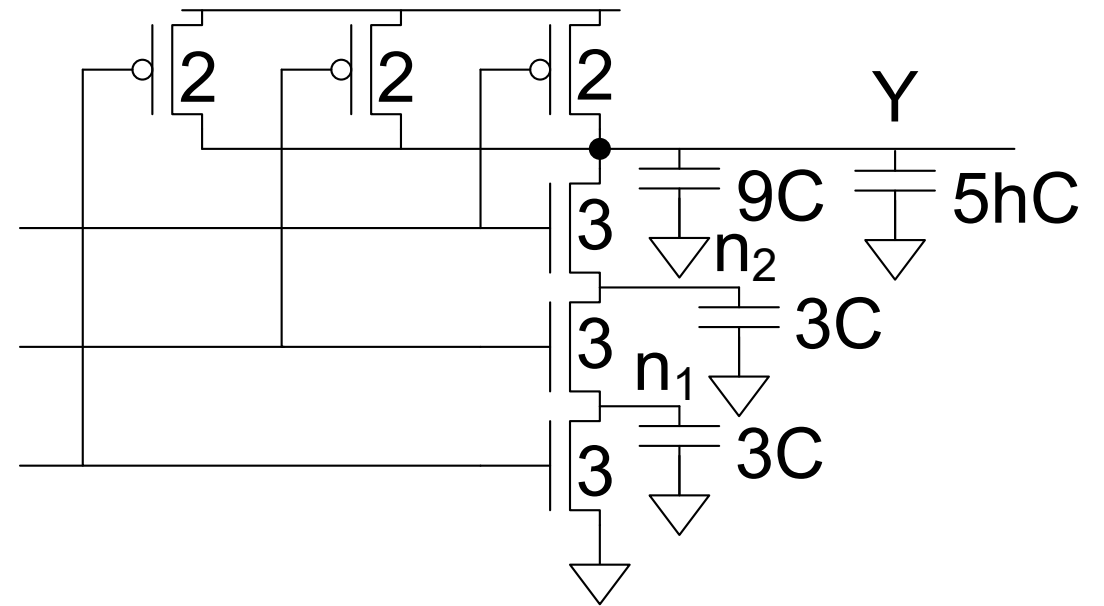
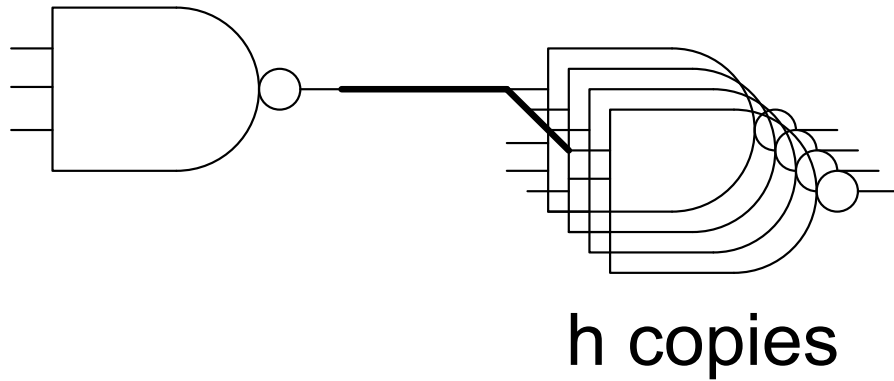


Homework#4

- Problem#2
 - Draw the exact response of V_X and an approximated one with a single time constant.

4.3. RC delay model (9)

- Example 4.7 (h identical NANDs)
 - We studied it in Example 4.2.



4.3. RC delay model (10)

- For the falling transition
 - Estimate t_{pdf} .
- For the rising transition (in the worst case)
 - Estimate t_{pdr} .

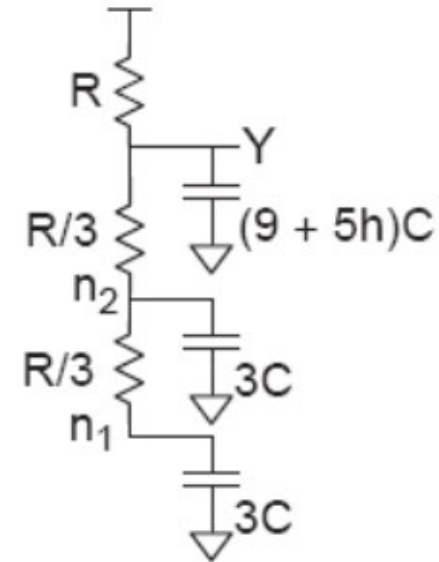
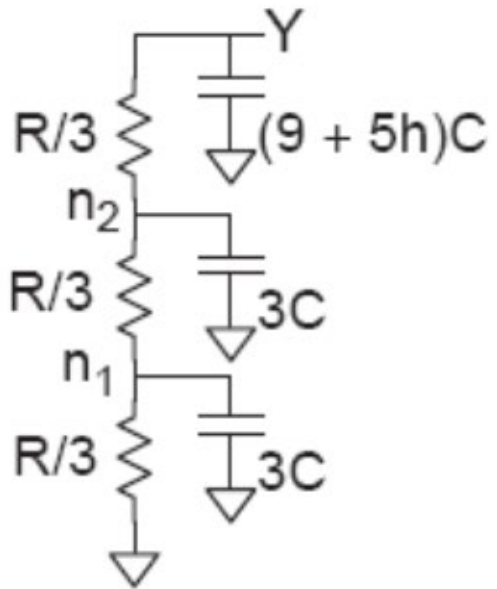


Fig. 4.15

4.3. RC delay model (11)

- Delay components
 - *Parastic delay*: Time for a gate to drive its own internal diffusion capacitance
 - *Effort delay*: It depends on the ratio of external load capacitance to input capacitance.
 - The normalized delay, $d = \frac{t_{pd}}{3RC}$, can be written as

$$d = \text{parastic delay} + \text{effort delay}$$

4.3. RC delay model (12)

- Layout dependence of capacitance
 - A good layout minimizes the diffusion area.

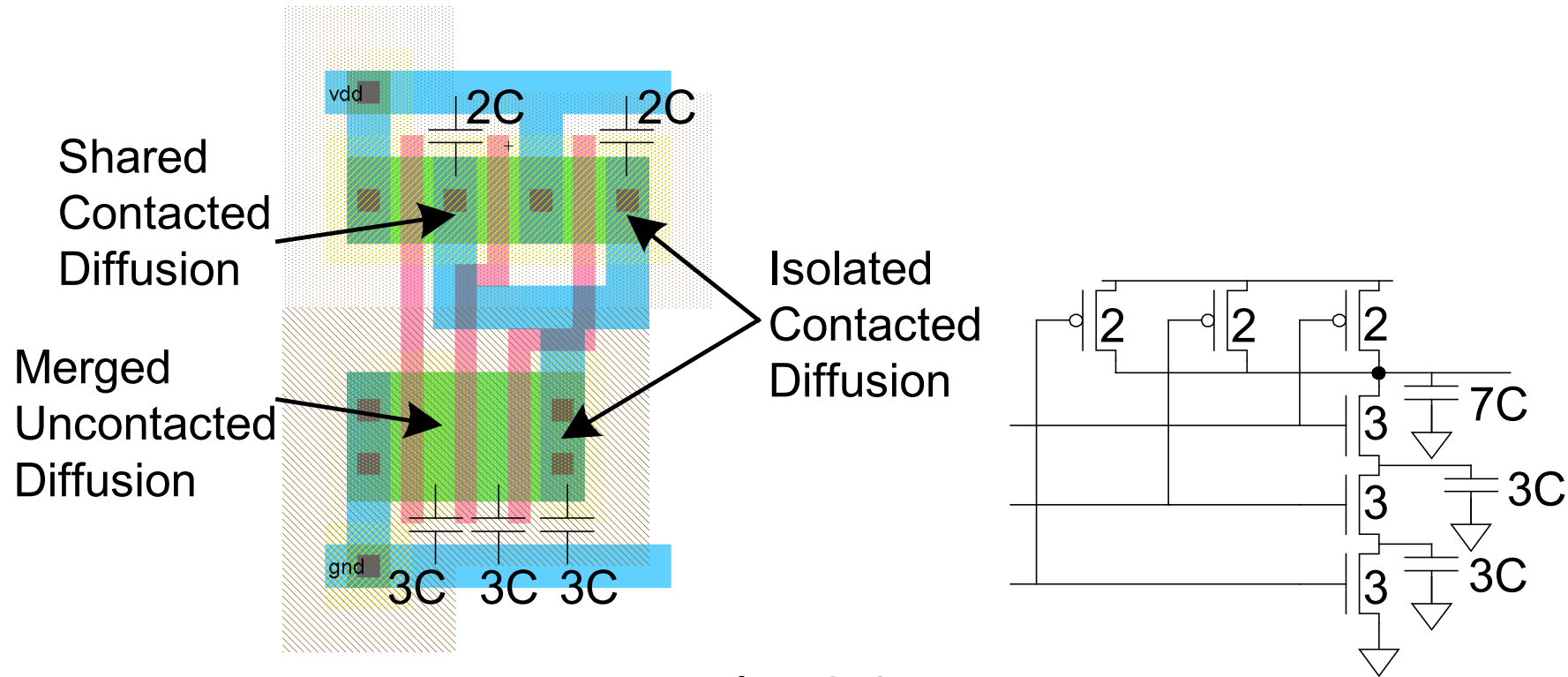


Fig. 4.17

4.4 Linear Delay Model

4.4. Linear delay model (1)

- Delay in a logic gate
 - Normalized delay

$$d = \frac{t_{pd}}{3RC}$$

- Delay has two components:

$$d = f + p = gh + p$$

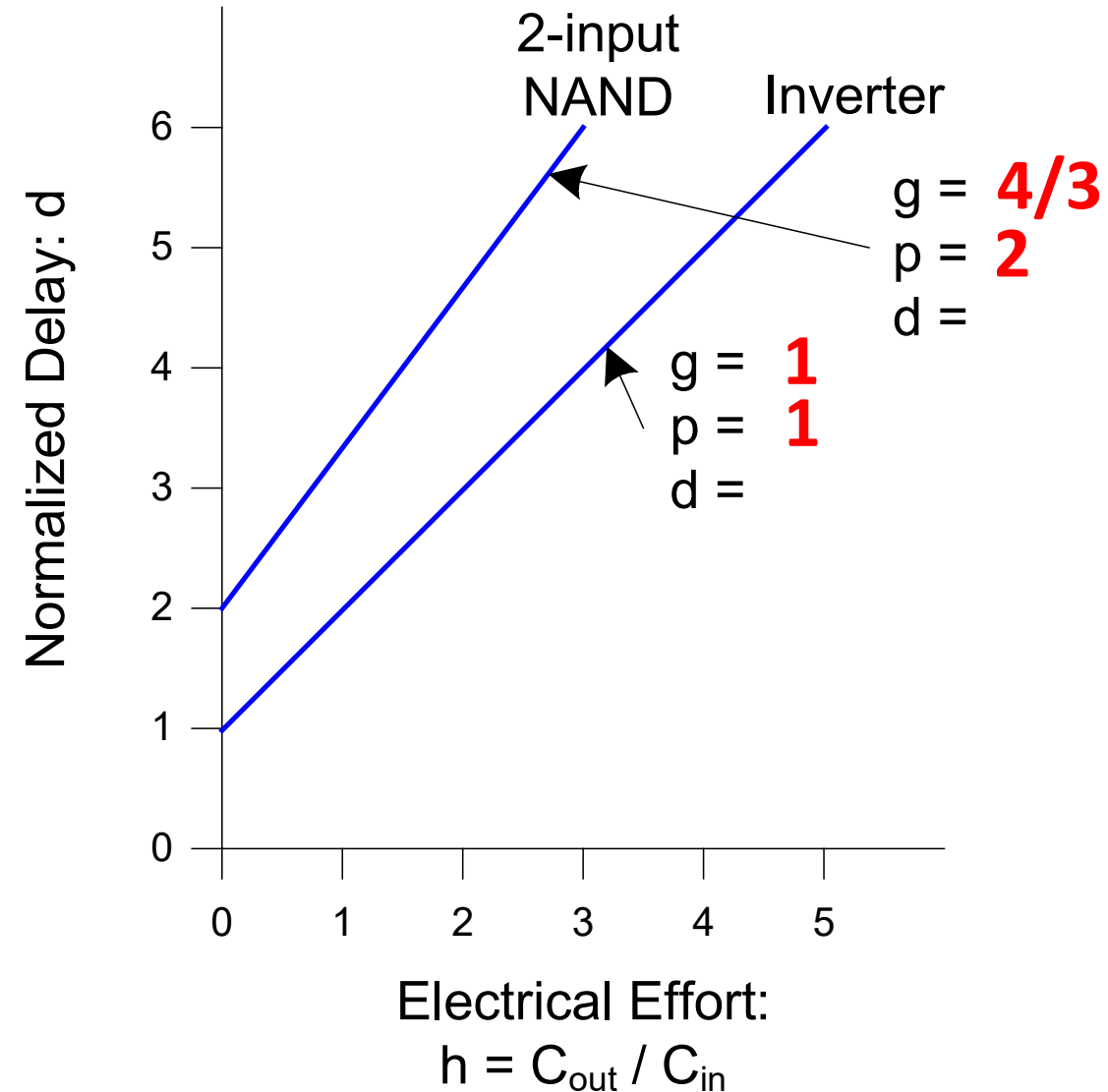
- Effort delay:

$$f = gh$$

(g is the logical effort.)

4.4. Linear delay model (2)

- Delay in a logic gate
 - Fanout (or electrical effort)
$$h = \frac{C_{out}}{C_{in}}$$
(Ratio of output to input capacitance)
 - Parasitic delay, p , represents delay of gate driving no load.
 - p is set by internal parasitic capacitance.



Thank you!