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# Lecture11: MOSFET, small-signal model

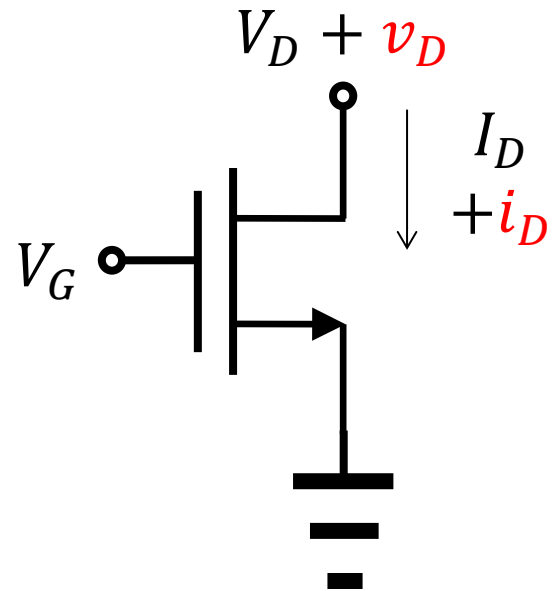
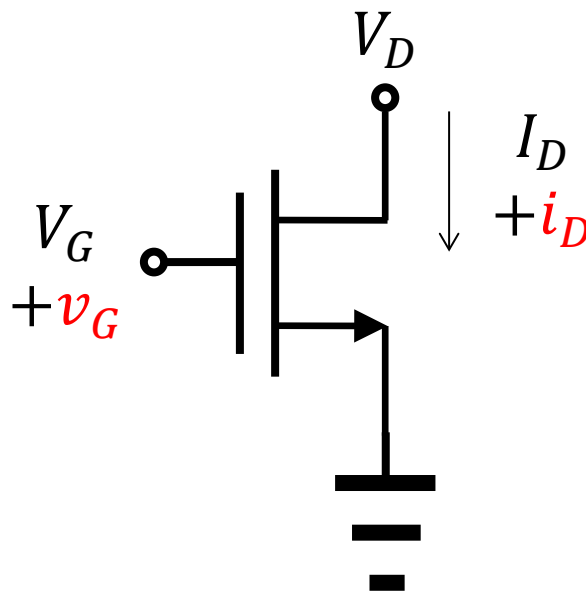
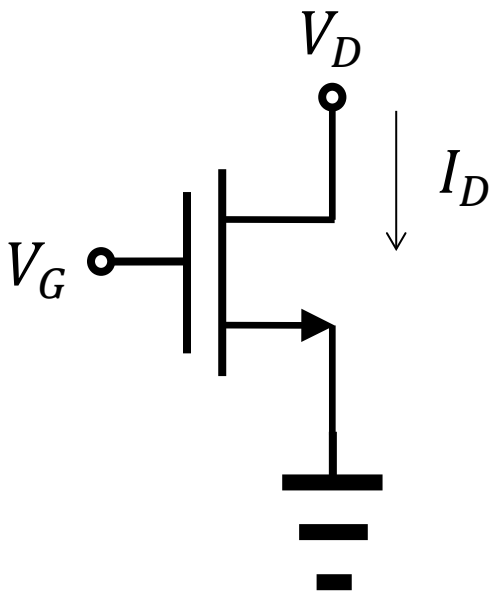
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# Summary

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- We can define two derivatives.
  - First,  $\frac{\partial I_D}{\partial V_{GS}}$ . It is the transconductance.
  - Second,  $\frac{\partial I_D}{\partial V_{DS}}$ . It is the inverse of the output resistance,  $r_O$ .

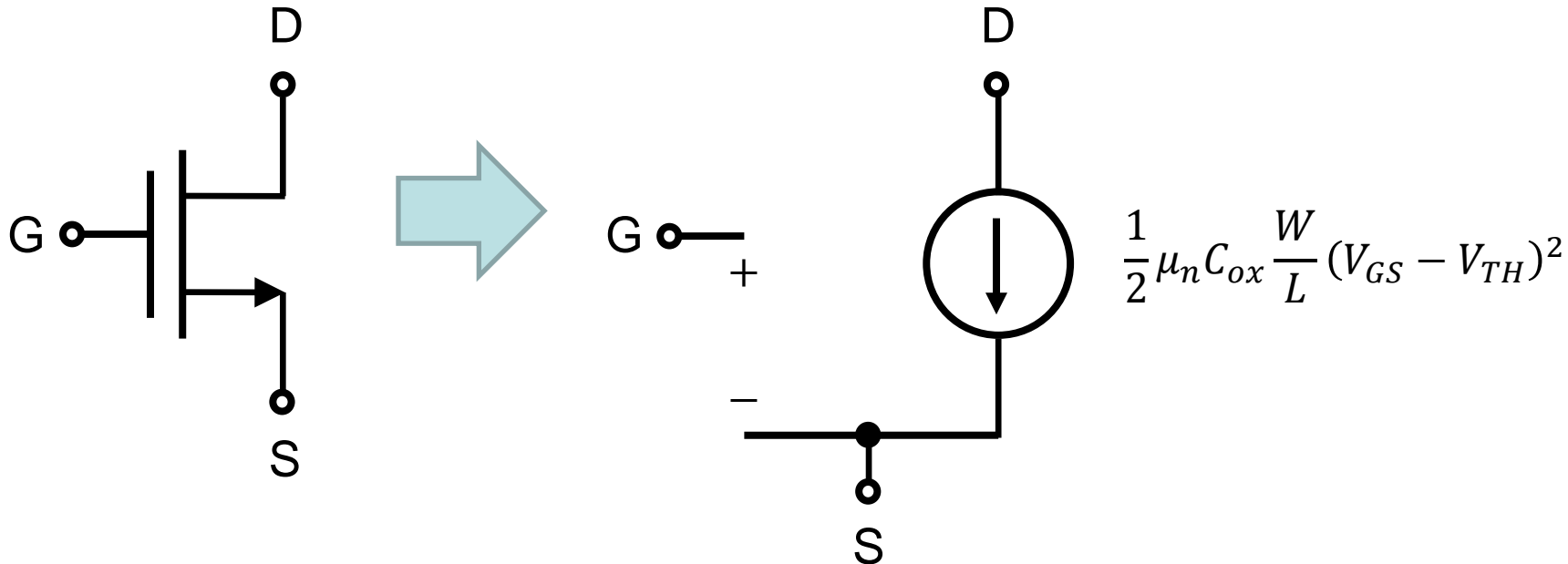


# Large-signal model (1/2)

- Saturation region

$$I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2$$

- Drain current is determined by gate voltage. (*voltage-controlled current source*)
- Channel-length modulation?

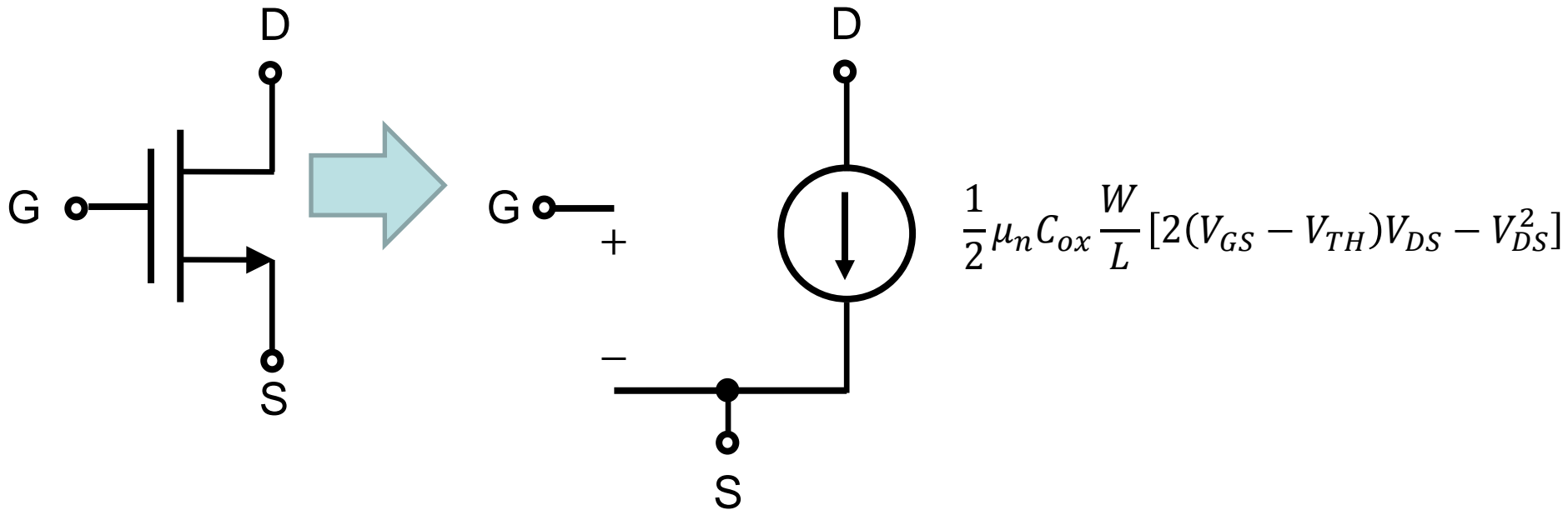


# Large-signal model (2/2)

- Triode region

$$I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} [2(V_{GS} - V_{TH})V_{DS} - V_{DS}^2]$$

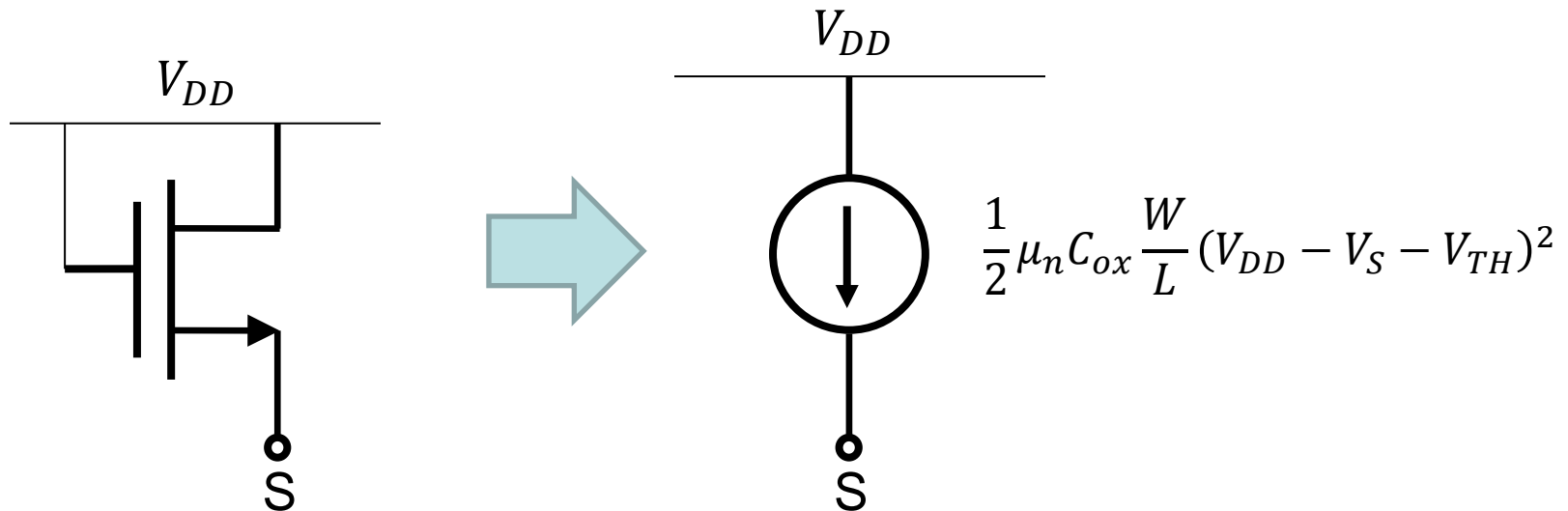
- Still, it can be described by a *voltage-controlled current source*.



# Example 6.13 (Razavi)

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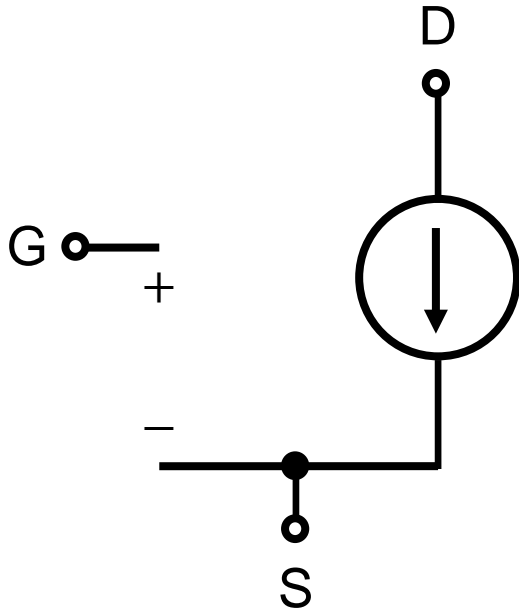
- Always in the saturation region!
  - Any necessary condition?



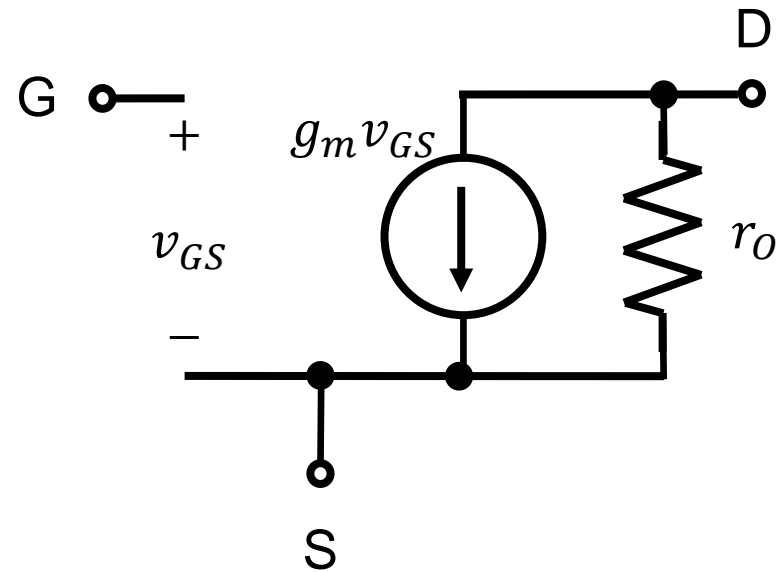
Gate and drain are tied.  
They are connected to  $V_{DD}$ .

# Small-signal model

- The large-signal model is complete (within its accuracy limitation).
  - But, for small-signal analysis, it is convenient to have the small-signal model.



$$I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2 (1 + \lambda V_{DS})$$

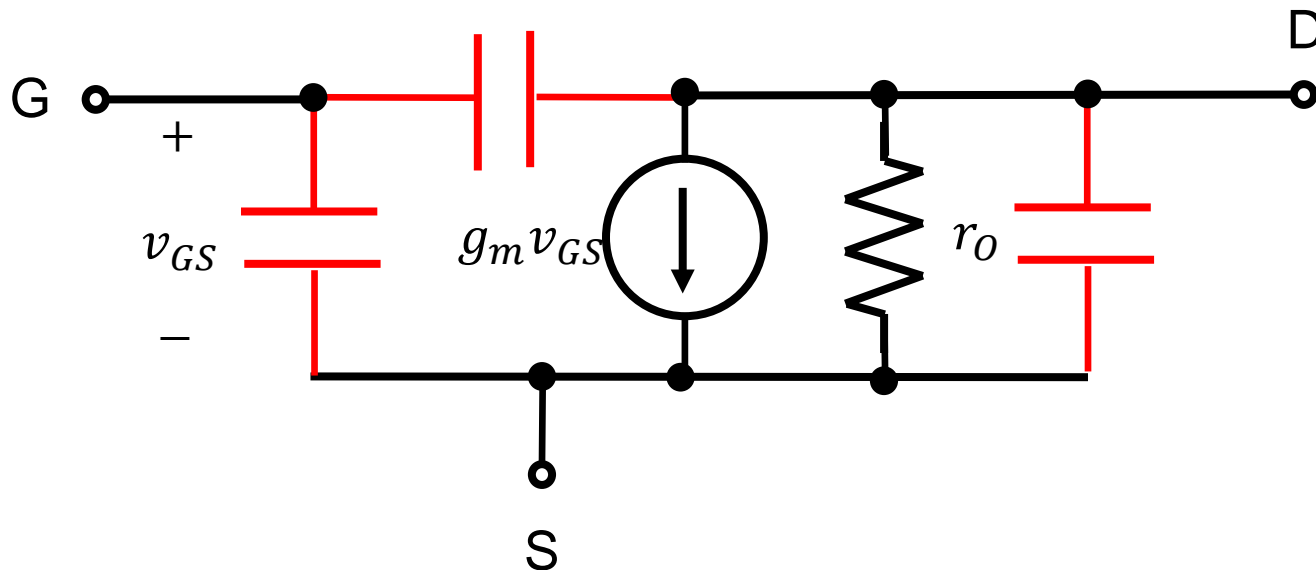


What is  $g_m$  and  $r_o$ ?

# Time-dependent one?

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- Everything was in the dc steady-state...
  - How about the frequency-dependent case?
  - Capacitive components can be seen.
  - Their physical origin?

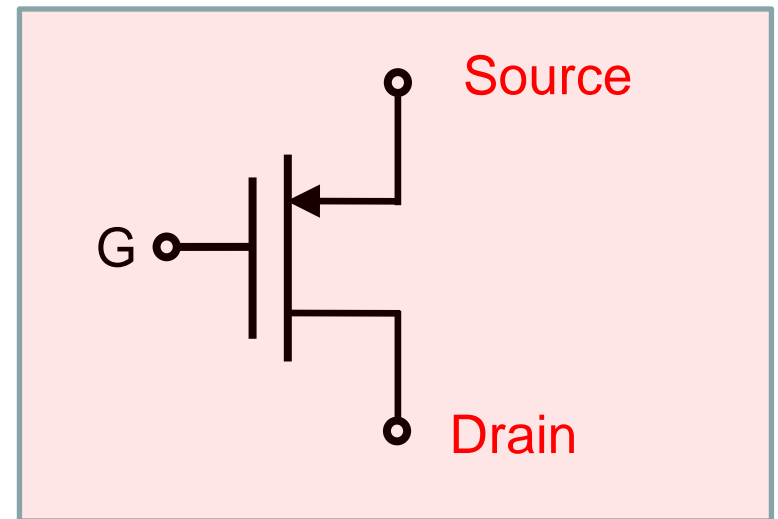
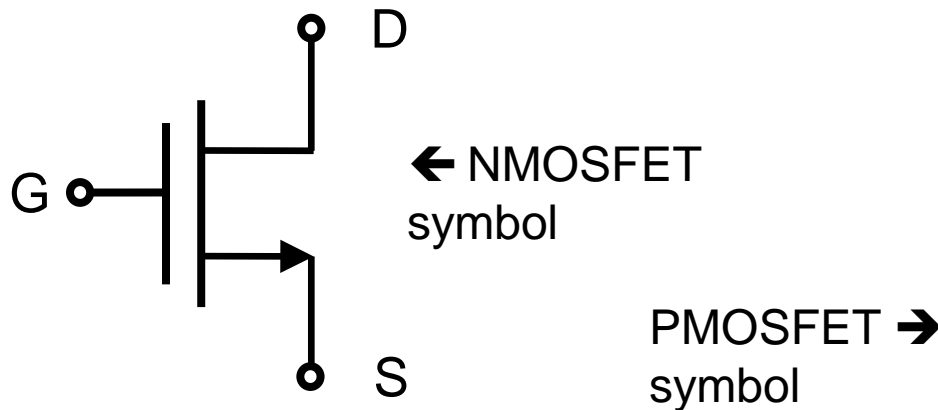


High-frequency, equivalent-circuit model for the case in which the source is connected to the substrate

# CMOS

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- 9's complementary of 123?
  - 876
- Complementary MOS
  - Here we have an NMOSFET.
  - A device where the transport is dominated by holes



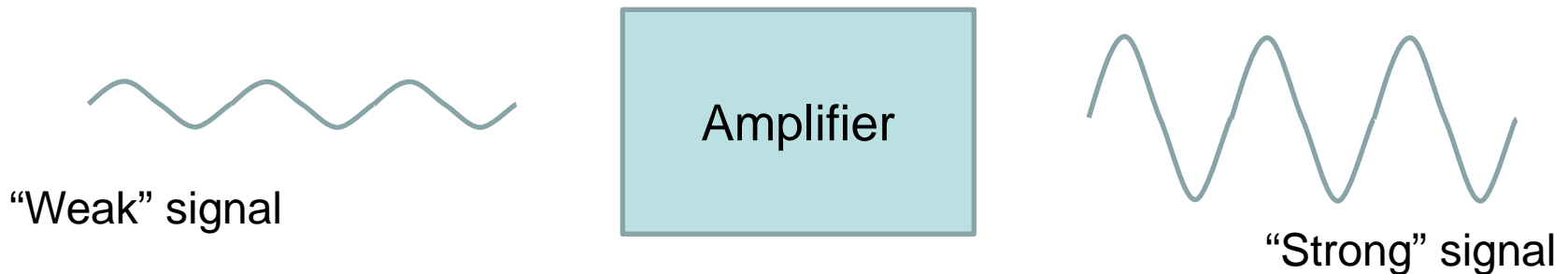
- Why is it important?



# Why amplifiers?

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- Signal amplification
  - Usually, signals are “weak.” (in the  $\mu\text{V}$  or  $\text{mV}$  range)
  - It is too small for reliable processing.
  - If the signal magnitude is made larger, processing is much easier.

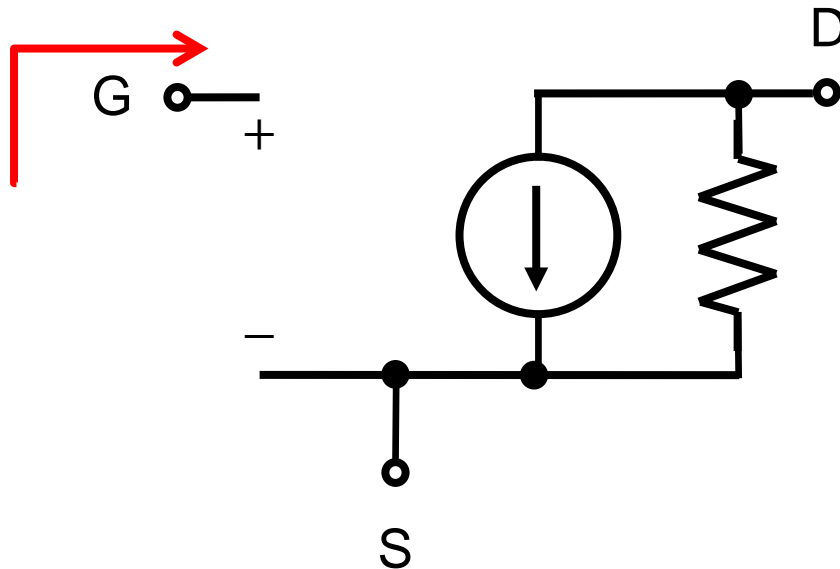


- Desirable properties
  - Low power consumption
  - High speed operation
  - Low noise

# Impedances (1/3)

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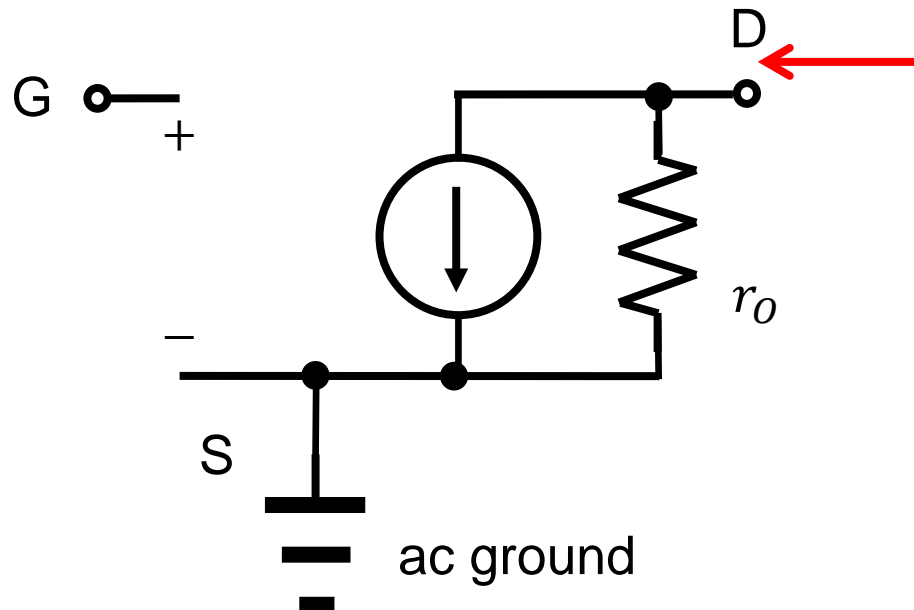
- A MOSFET with three terminals
  - Looking into the gate, we see the infinite impedance.
  - (Strictly valid at the low-frequency range)



# Impedances (2/3)

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- A MOSFET with three terminals
  - Looking into the drain, we see  $r_o$  if the source is ac grounded.



# Impedances (3/3)

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- A MOSFET with three terminals
  - Looking into the source, we see  $1/g_m$  if the gate is ac grounded and channel-length modulation is neglected.

