
Lecture10: MOSFET, transconductance

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Summary

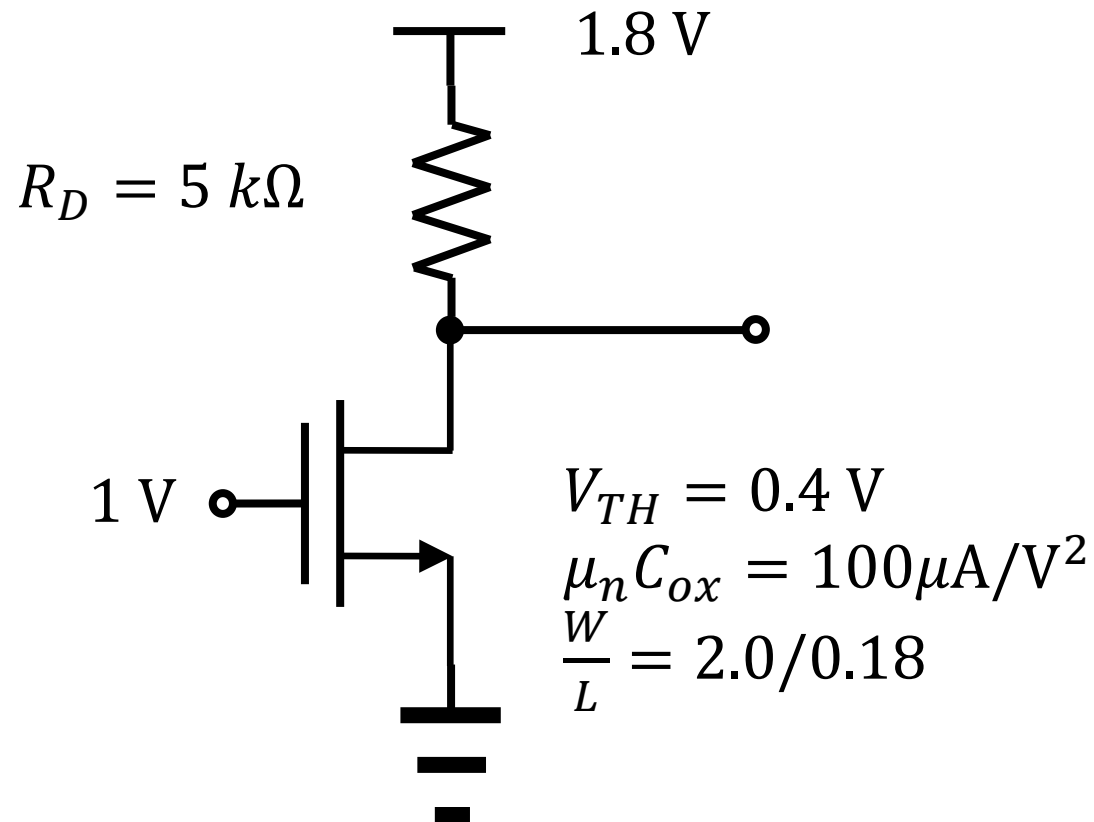
- When $V_G < V_{TH}$,
 - No drain current!

$$I_D = 0$$

- When $V_G > V_{TH}$,
 - Triode mode ($V_{DS} < V_G - V_{TH}$)
$$I_D = \mu_n C_{ox} \frac{W}{L} \left[(V_G - V_{TH}) V_{DS} - \frac{1}{2} V_{DS}^2 \right]$$
 - Saturation mode ($V_{DS} > V_G - V_{TH}$)
$$I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_G - V_{TH})^2$$
 - For a short channel device, I_D increases slightly as V_{DS} increases.

Example 6.6 (Razavi)

- Assume the saturation region.
 - Then, the saturation current becomes $200\ \mu\text{A}$.



MOS transconductance

- “conductance” of a simple resistor
 - It means $\frac{I}{V}$.
- “trans” + “conductance”
 - Between different terminals

$$g_m = \frac{\partial I_D}{\partial V_{GS}} \quad (6.44)$$

- For the saturation region,

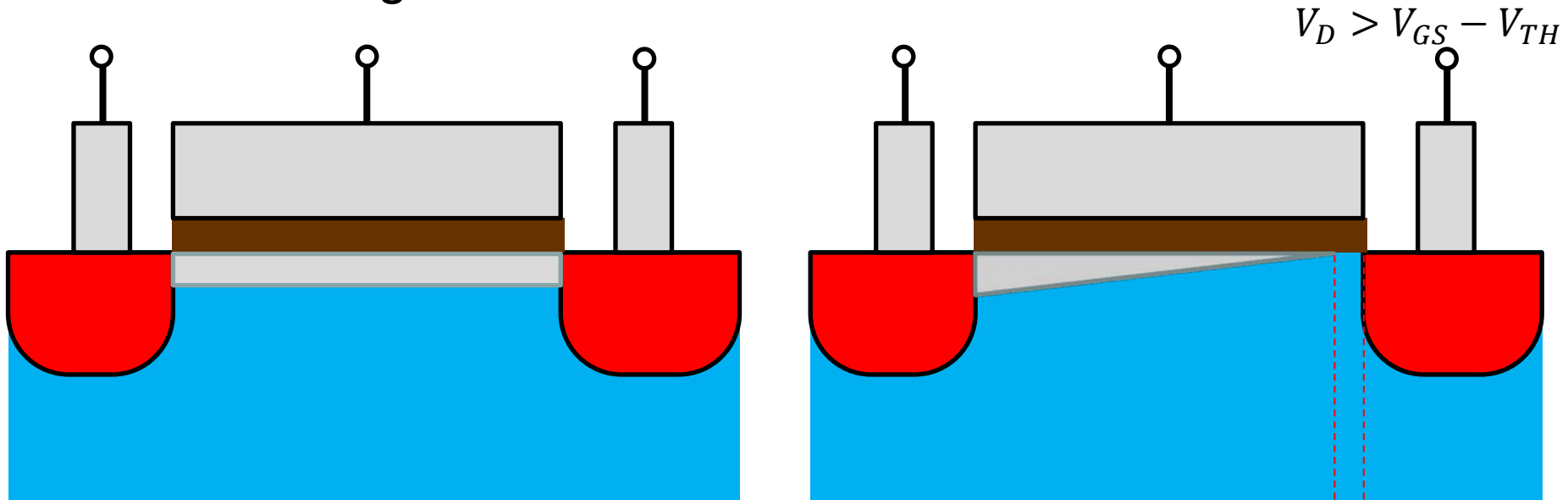
$$g_m = \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})$$

$$g_m = \sqrt{2\mu_n C_{ox} \frac{W}{L} I_D}$$

$$g_m = \frac{2I_D}{V_{GS} - V_{TH}}$$

Channel length modulation

- Channel length modulation



- Output resistance?

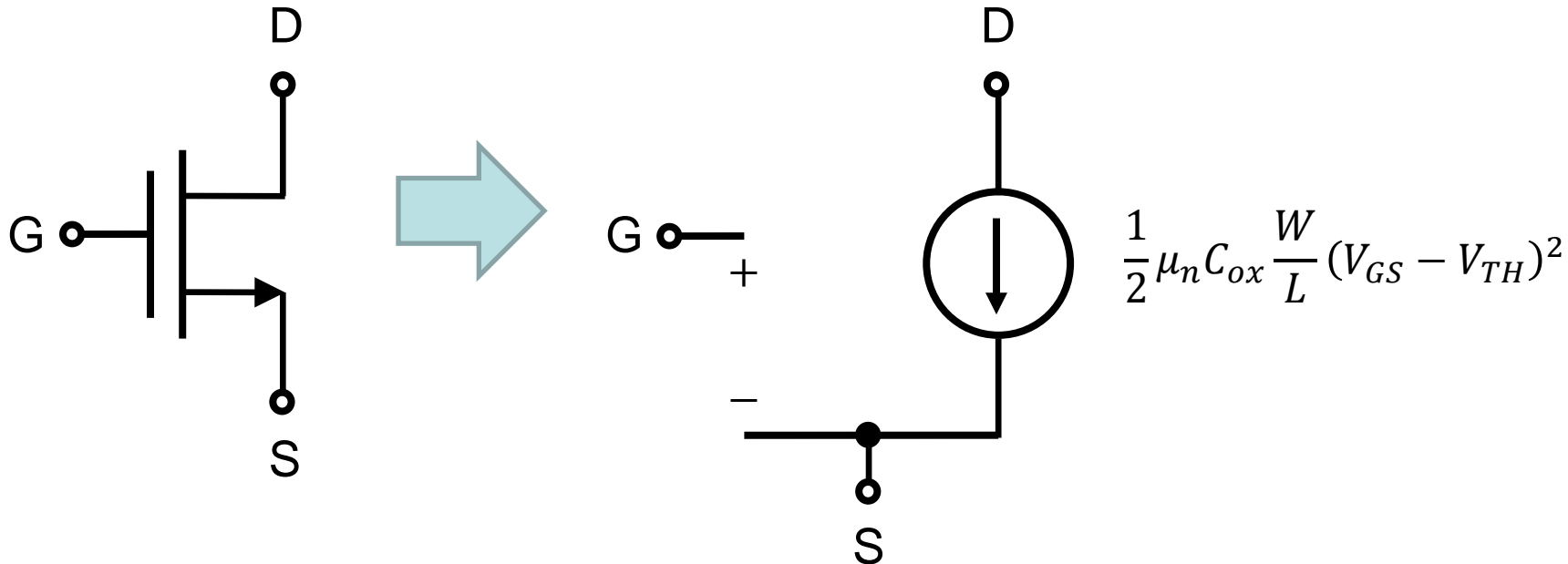
$$r_o = \frac{\Delta V_{DS}}{\Delta I_D}$$

Large-signal model (1/2)

- Saturation region

$$I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2$$

- Drain current is determined by gate voltage. (*voltage-controlled current source*)
- Channel-length modulation?

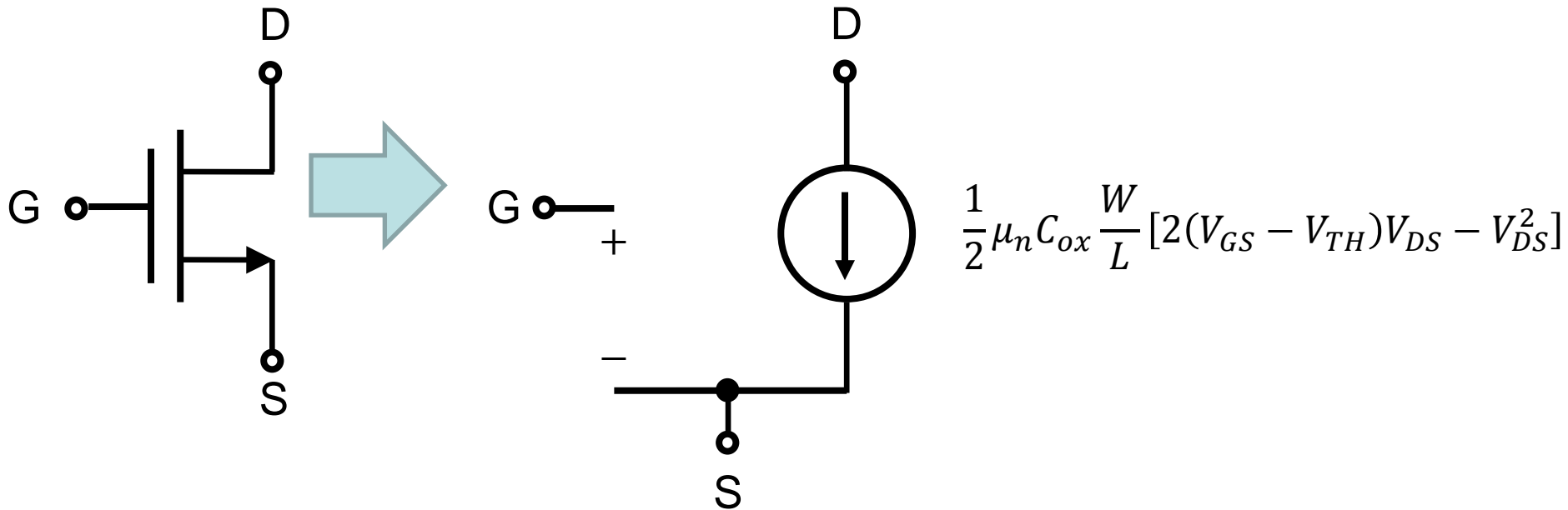


Large-signal model (2/2)

- Triode region

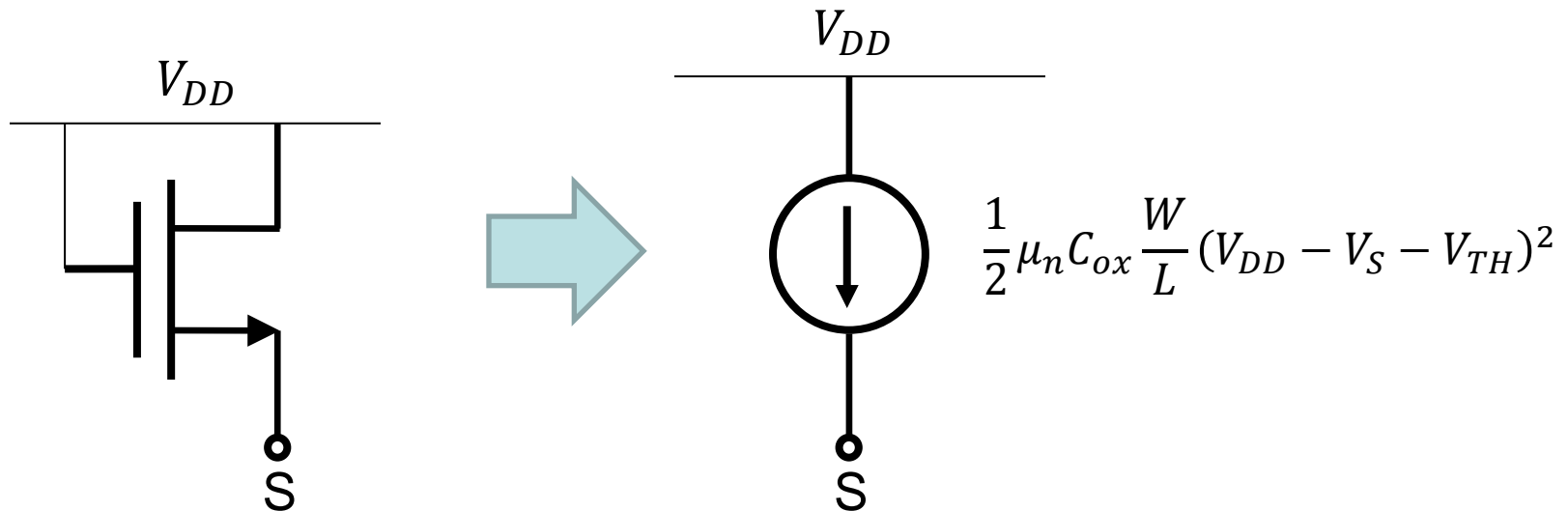
$$I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} [2(V_{GS} - V_{TH})V_{DS} - V_{DS}^2]$$

- Still, it can be described by a *voltage-controlled current source*.



Example 6.13 (Razavi)

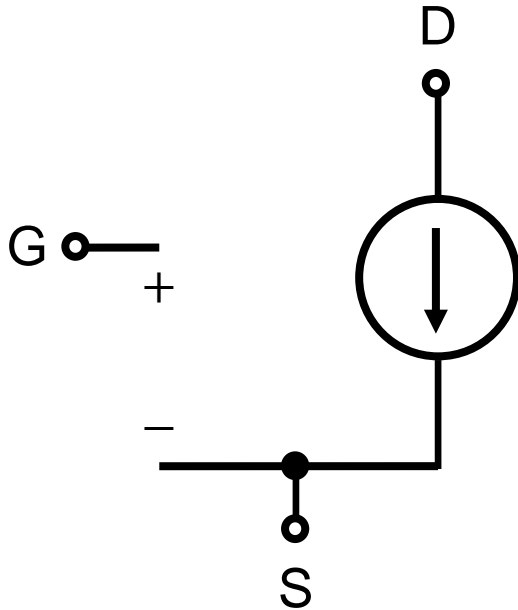
- Always in the saturation region!
 - Any necessary condition?



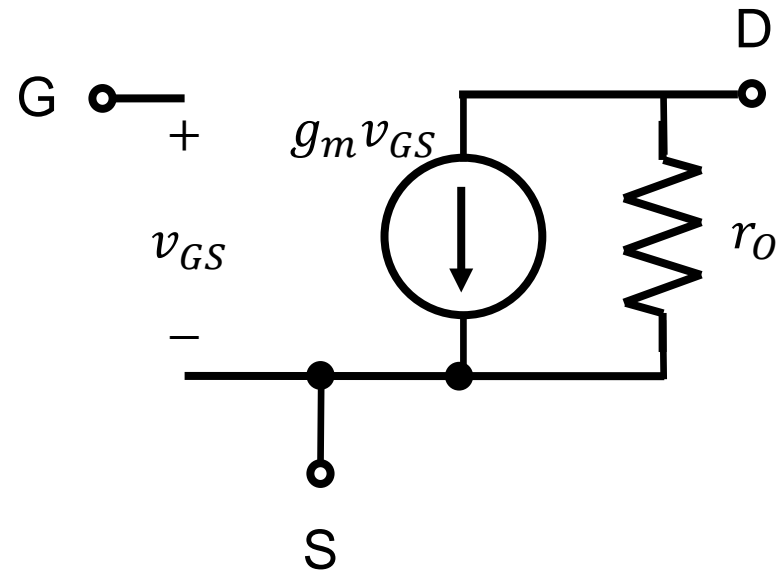
Gate and drain are tied.
They are connected to V_{DD} .

Small-signal model

- The large-signal model is complete (within its accuracy limitation).
 - But, for small-signal analysis, it is convenient to have the small-signal model.



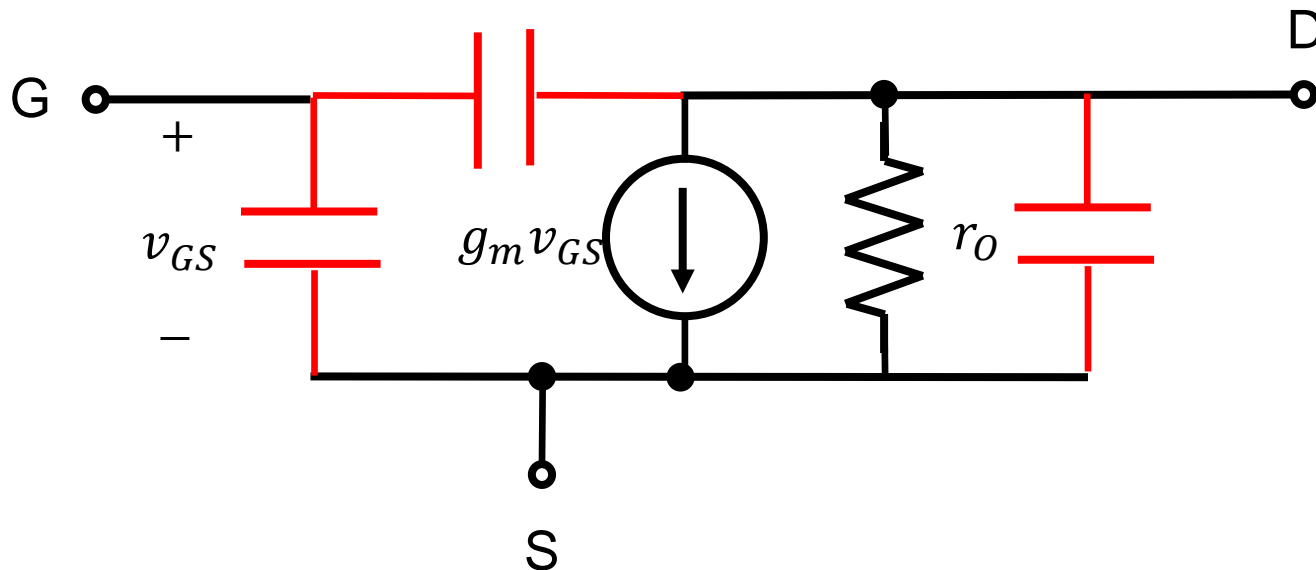
$$I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2 (1 + \lambda V_{DS})$$



What is g_m and r_o ?

Time-dependent one?

- Everything was in the dc steady-state...
 - How about the frequency-dependent case?
 - Capacitive components can be seen.
 - Their physical origin?



High-frequency, equivalent-circuit model for the case in which the source is connected to the substrate