VLSI Devices Lecture 5

Sung-Min Hong (smhong@gist.ac.kr)
Semiconductor Device Simulation Laboratory
Department of Electrical Engineering and Computer Science
Gwangju Institute of Science and Technology (GIST)

Surface potential, $\phi_s \equiv \phi(0) - \phi(\infty)$

- A downward bending of bands in the p-type silicon near the surface
 - It is important to note that

$$V_g - V_{fb} = \phi_s + V_{ox}$$

At the silicon-oxide interface,

$$\epsilon_{ox}|\mathbf{E}_{ox}| = \epsilon_{si}|\mathbf{E}_{si}|$$

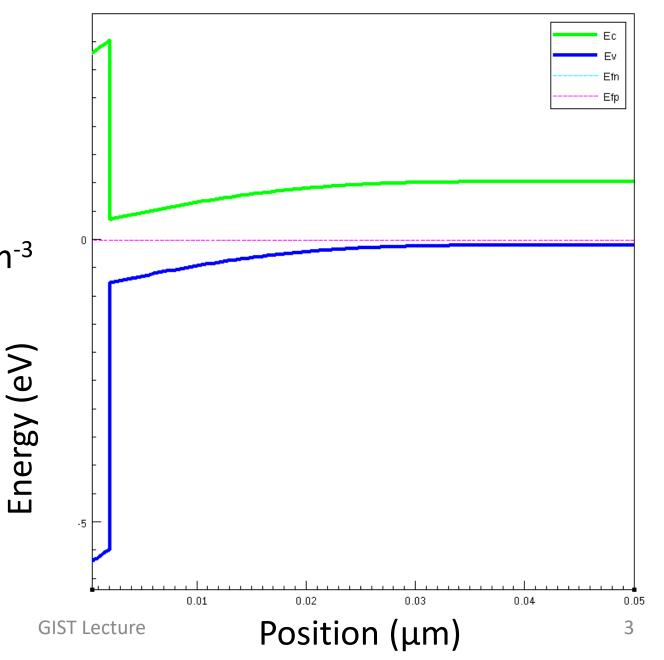
-Since
$$\epsilon_{ox} = 3.9\epsilon_0$$
 and $\epsilon_{si} = 11.7\epsilon_0$, $|\mathbf{E}_{ox}| \approx 3|\mathbf{E}_{si}|$

Taur, Eq. (2.172)

Taur, Eq. (2.173)

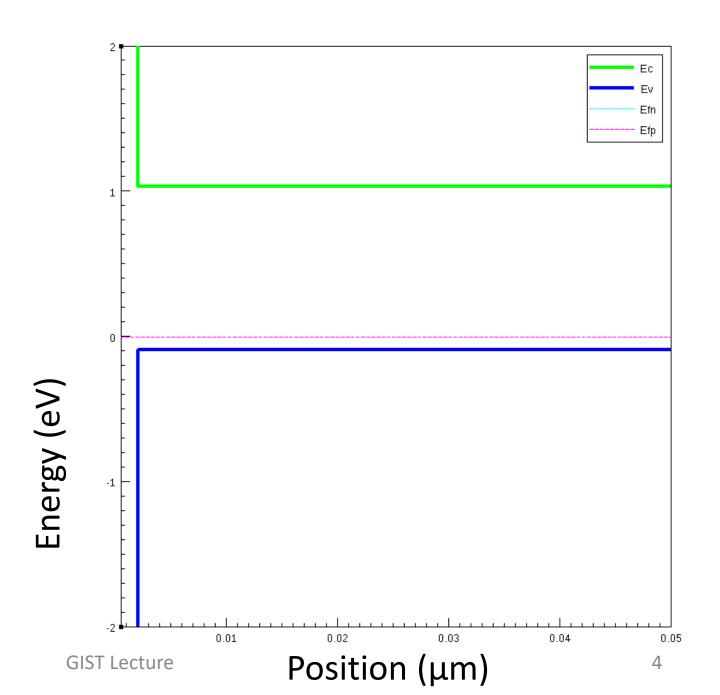
TCAD simulation

- Model parameter
 - -Workfunction of 4.17 eV
 - -Oxide thickness of 20 Å
 - -P-type doping of 1X10¹⁸ cm⁻³

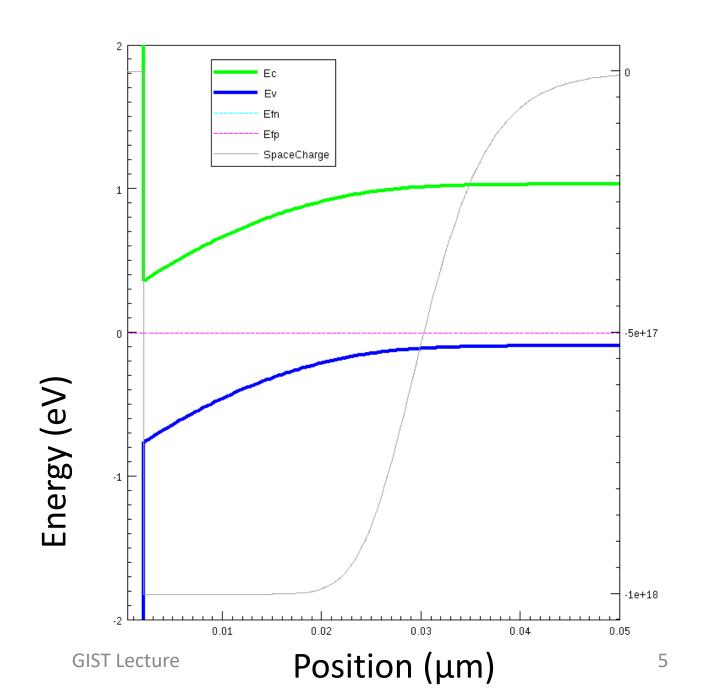


• V_g = -0.94 V

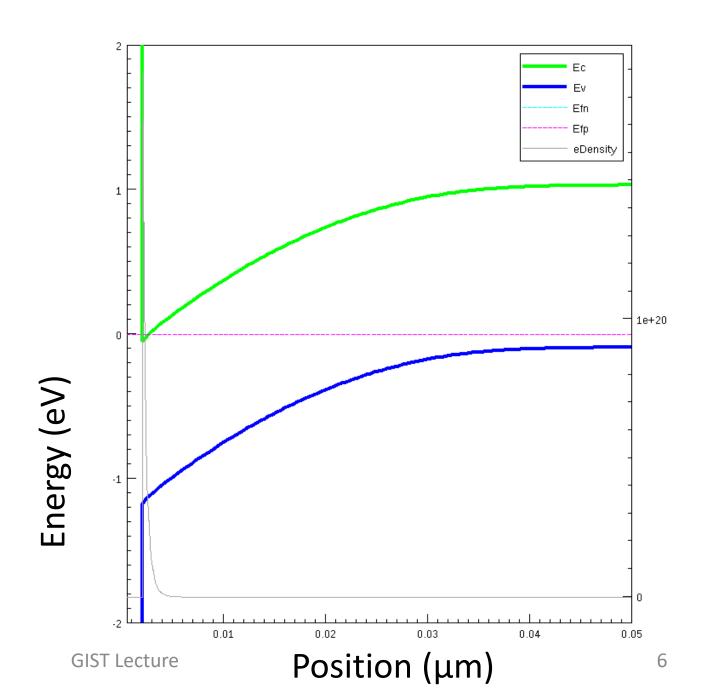
Flatband condition



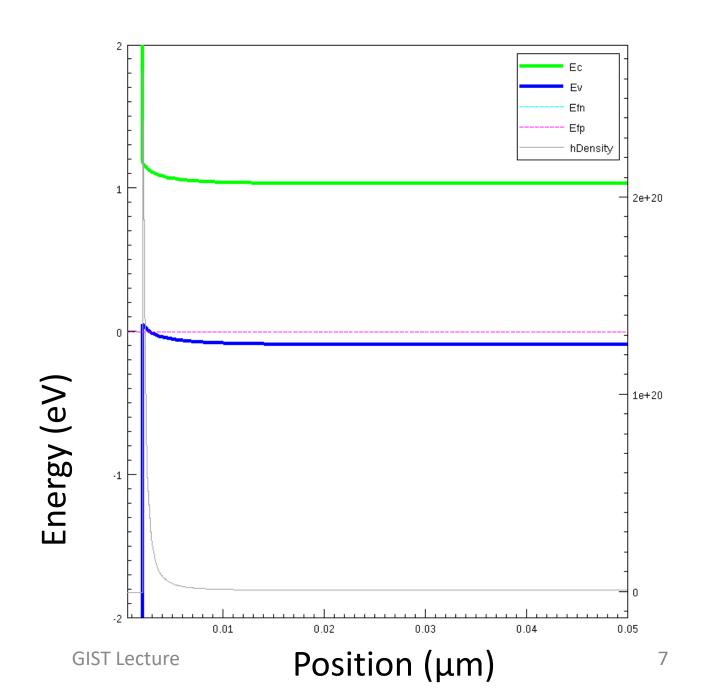
- V_g = 0.0 V - Depletion
- Space charge



- $V_g = 1.0 \text{ V}$ -Inversion
- Electron density



- V_g = -2.0 V -Accumulation
- Hole density



General relation beyond depletion approx. (1)

With the depletion approximation, we obtained

$$Q_d = -qN_aW_d = -\sqrt{2\epsilon_{si}qN_a\phi_s}$$

- We can do much better!
 - -A generation relation for $Q_s = Q_d + Q_i$
 - The Poisson equation

$$\frac{d^2\phi}{dx^2} = -\frac{q}{\epsilon_{si}}[p(x) - n(x) - N_a]$$

Inversion charge

Taur, Eq. (2.175)

General relation beyond depletion approx. (2)

Following Taur's notation,

For a while, $\phi(\infty) = -\phi_B$ is used as the reference value. Therefore,

$$n(x) = n_i \exp\left(\frac{q\phi(x)}{k_B T}\right) \rightarrow n(x) = n(\infty) \exp\left(\frac{q\phi(x)}{k_B T}\right) \qquad \text{Taur, Eq. (2.178)}$$

$$p(x) = n_i \exp\left(-\frac{q\phi(x)}{k_B T}\right) \rightarrow p(x) = p(\infty) \exp\left(-\frac{q\phi(x)}{k_B T}\right) \qquad \text{Taur, Eq. (2.177)}$$

Taur, Eq. (2.178)

-The Poisson equation

$$\frac{d^2\phi}{dx^2} = -\frac{q}{\epsilon_{si}} \left[N_a \left(\exp\left(-\frac{q\phi}{k_B T}\right) - 1 \right) - \frac{n_i^2}{N_a} \left(\exp\left(\frac{q\phi}{k_B T}\right) - 1 \right) \right]$$

Taur, Eq. (2.179)

General relation beyond depletion approx. (3)

- Multiplying $\frac{d\phi}{dx} dx$,
 - -The Poisson equation

$$\frac{d\phi}{dx}d\left(\frac{d\phi}{dx}\right) = -\frac{q}{\epsilon_{si}}\left[N_a\left(\exp\left(-\frac{q\phi}{k_BT}\right) - 1\right) - \frac{n_i^2}{N_a}\left(\exp\left(\frac{q\phi}{k_BT}\right) - 1\right)\right]d\phi$$

- Integrate the above equation.

Integrate the above equation.
$$\int_{0}^{-E_{x}(x)} \frac{d\phi}{dx} d\left(\frac{d\phi}{dx}\right)$$
 Taur, Eq. (2.180)
$$= -\frac{q}{\epsilon_{si}} \int_{0}^{\phi(x)} \left[N_{a} \left(\exp\left(-\frac{q\phi}{k_{B}T}\right) - 1 \right) - \frac{n_{i}^{2}}{N_{a}} \left(\exp\left(\frac{q\phi}{k_{B}T}\right) - 1 \right) \right] d\phi$$

General relation beyond depletion approx. (4)

• (Square of) Electric field

-From
$$\frac{1}{2}E_{\chi}^{2}(x) = -\frac{q}{\epsilon_{si}}\left[-N_{a}\frac{k_{B}T}{q}\exp\left(-\frac{q\phi}{k_{B}T}\right) - N_{a}\phi + N_{a}\frac{k_{B}T}{q} - \frac{n_{i}^{2}}{N_{a}}\frac{k_{B}T}{q}\exp\left(\frac{q\phi}{k_{B}T}\right) + \frac{n_{i}^{2}}{N_{a}}\phi + \frac{n_{i}^{2}}{N_{a}}\frac{k_{B}T}{q}\right], \text{ we get}$$

$$\begin{aligned} &E_{\chi}^{2}(\chi) \\ &= \frac{2k_{B}TN_{a}}{\epsilon_{si}} \left[\left(\exp\left(-\frac{q\phi}{k_{B}T}\right) + \frac{q\phi}{k_{B}T} - 1 \right) \right. \\ &\left. + \frac{n_{i}^{2}}{N_{a}^{2}} \left(\exp\left(\frac{q\phi}{k_{B}T}\right) - \frac{q\phi}{k_{B}T} - 1 \right) \right] \end{aligned}$$

Taur, Eq. (2.181)

General relation beyond depletion approx. (5)

- At x=0, we have $\phi(0)=\phi_{s}$.
 - -Then,

$$E_s^2$$

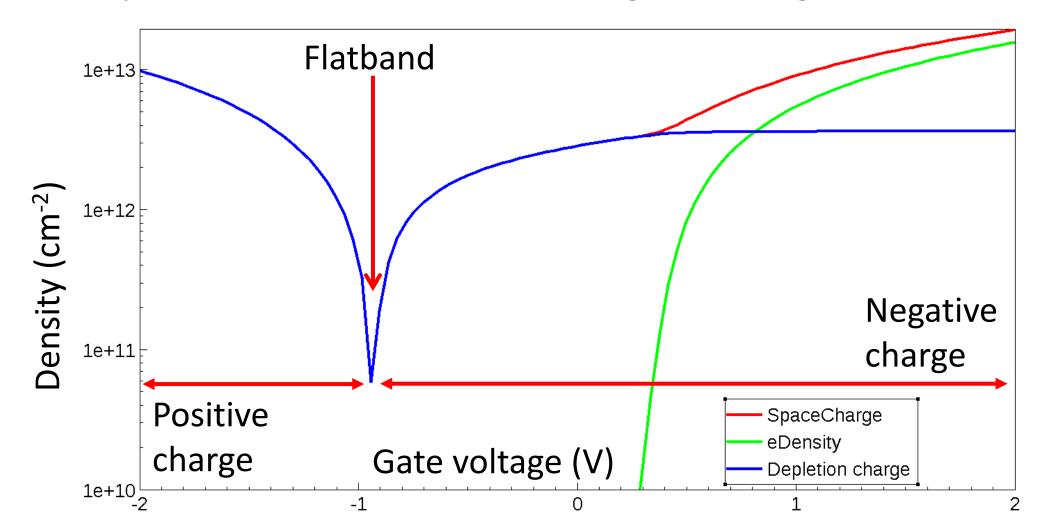
$$= \frac{2k_B T N_a}{\epsilon_{si}} \left[\left(\exp\left(-\frac{q\phi_s}{k_B T}\right) + \frac{q\phi_s}{k_B T} - 1 \right) + \frac{n_i^2}{N_a^2} \left(\exp\left(\frac{q\phi_s}{k_B T}\right) - \frac{q\phi_s}{k_B T} - 1 \right) \right]$$

General relation beyond depletion approx. (6)

$$\begin{split} \bullet & \text{ At } x=0 \text{, we have } \phi(0)=\phi_{S}. \\ & -\text{From } Q_{S}=-\epsilon_{si}E_{S}, \\ & Q_{S} \\ & =\pm\sqrt{2\epsilon_{si}k_{B}TN_{a}}\left[\left(\exp\left(-\frac{q\phi_{S}}{k_{B}T}\right)+\frac{q\phi_{S}}{k_{B}T}-1\right)\right. \\ & \left. +\frac{n_{i}^{2}}{N_{a}^{2}}\left(\exp\left(\frac{q\phi_{S}}{k_{B}T}\right)-\frac{q\phi_{S}}{k_{B}T}-1\right)\right]^{1/2} \end{split}$$
 Taur, Eq. (2.182)

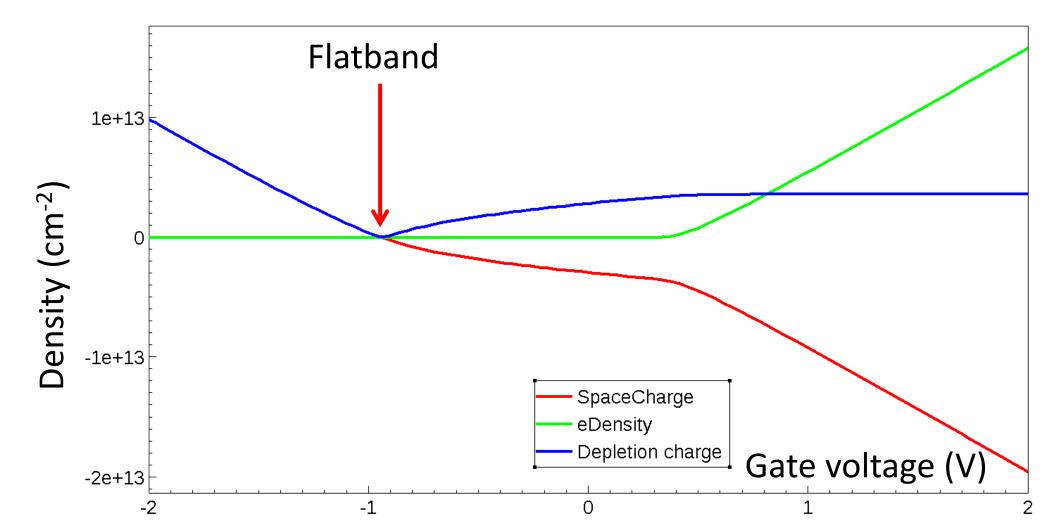
Threshold voltage (1)

Draw quantities as functions of the gate voltage.



Threshold voltage (2)

• The same graph, in the linear scale,



Depletion approximation

- Electric field (V/cm) Position (µm) W_d
- Consider a depleted MOS structure.
 - With the depletion width, W_d ,

$$\phi_s = \frac{1}{2} W_d \left(q \frac{N_a}{\epsilon_{si}} W_d \right)$$

-Then,

$$W_d = \sqrt{\frac{2\epsilon_{si}\phi_s}{qN_a}}$$

0 (No field)

Oxide

P-type substrate

Taur, Eq. (2.188)

-Total depletion charge in silicon, Q_d , is

$$Q_d = -qN_aW_d = -\sqrt{2\epsilon_{si}qN_a\phi_s}$$

Taur, Eq. (2.189)

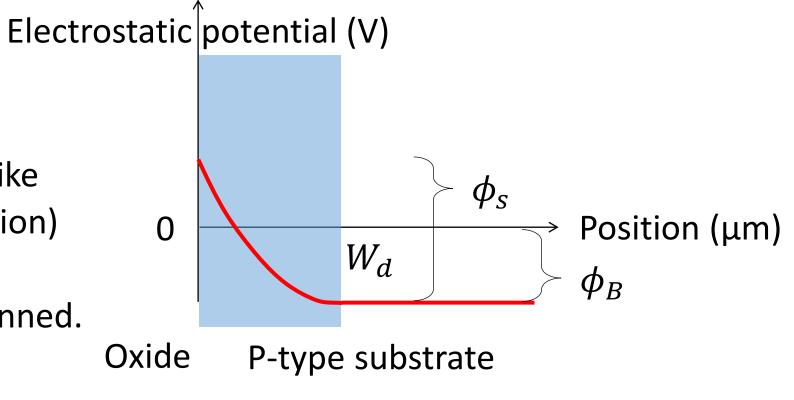
Potential profile

- A parabolic potential profile
 - -The depletion region cannot grow indefinitely.

-When $\phi_S = 2\phi_B$, $n(0) = p(\infty)$

The surface behaves liken-type material. (Inversion)

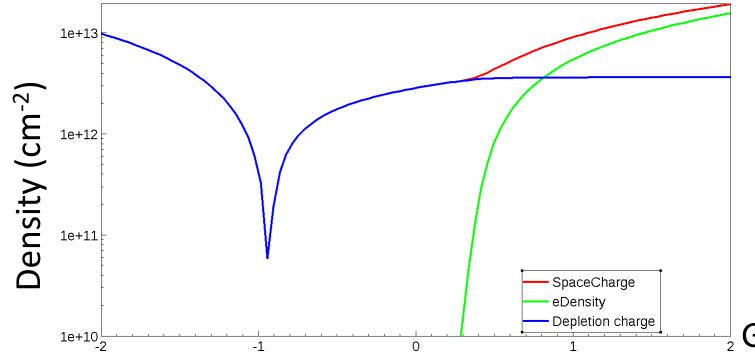
 $-\phi_s$ is approximately pinned.



Maximum depletion width

Therefore, maximum depletion width becomes

$$W_d = \sqrt{\frac{4\epsilon_{si}\phi_B}{qN_a}} = \sqrt{\frac{4\epsilon_{si}k_BT \ln(N_a/n_i)}{q^2N_a}}$$
 Taur, Eq. (2.190)



← Depletion charge does not increase.

Gate voltage (V)

Beyond threshold voltage

It's not perfectly fixed.

- The surface potential is <u>almost</u> fixed. (Surface potential pinning)
 - –Small additional change in $\phi_{\scriptscriptstyle S}$ induces an exponential increase of the electron density.
 - Remember that $n = n_i \exp\left(\frac{q\phi}{k_B T}\right)$.
 - When $\phi_S=2\phi_B$,

$$n(0) = n_i \exp\left(\frac{q\phi_B}{k_B T}\right) = p(\infty)$$

–Additional potential ($\Delta\phi$) yields

$$n(0) = p(\infty) \exp\left(\frac{q\Delta\phi}{k_B T}\right)$$

It's a high density.

Thank you!