

VLSI Devices

Lecture 23


Sung-Min Hong (smhong@gist.ac.kr)

Semiconductor Device Simulation Laboratory

Department of Electrical Engineering and Computer Science

Gwangju Institute of Science and Technology (GIST)

Coverage

- Two YouTube lectures reserved for advanced topics
 - L14: ~~Substrate bias, channel mobility~~
 - L15: ~~3.2.1~~
 - L16: ~~3.2.1 (Continued)~~
 - L17: ~~Velocity saturation (3.2.2)~~
 - L18: ~~Channel length modulation and so on (3.2.3, 3.2.4, 3.2.5)~~
 - L19: MOSFET scaling
 - L20: MOSFET scaling (Continued)
 - L21: Quantum effect (4.2.4)
 - L22: Double-gate MOSFETs (10.3)
 -  – L23: FinFETs
 - L24: CFETs

Basic assumptions

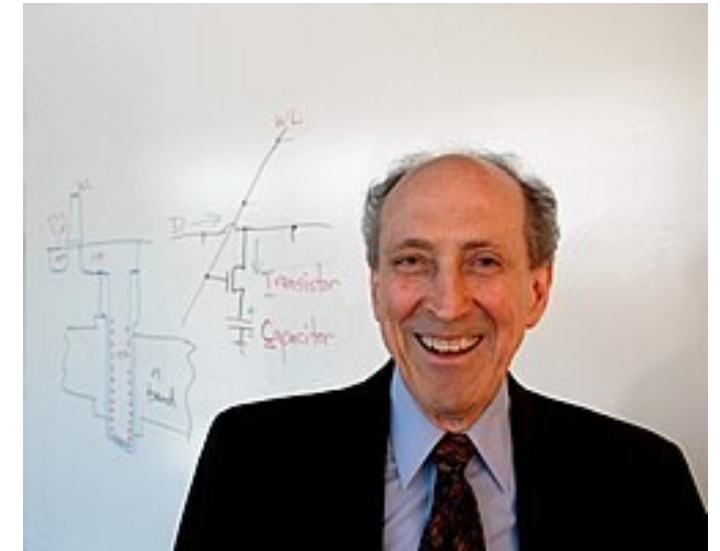
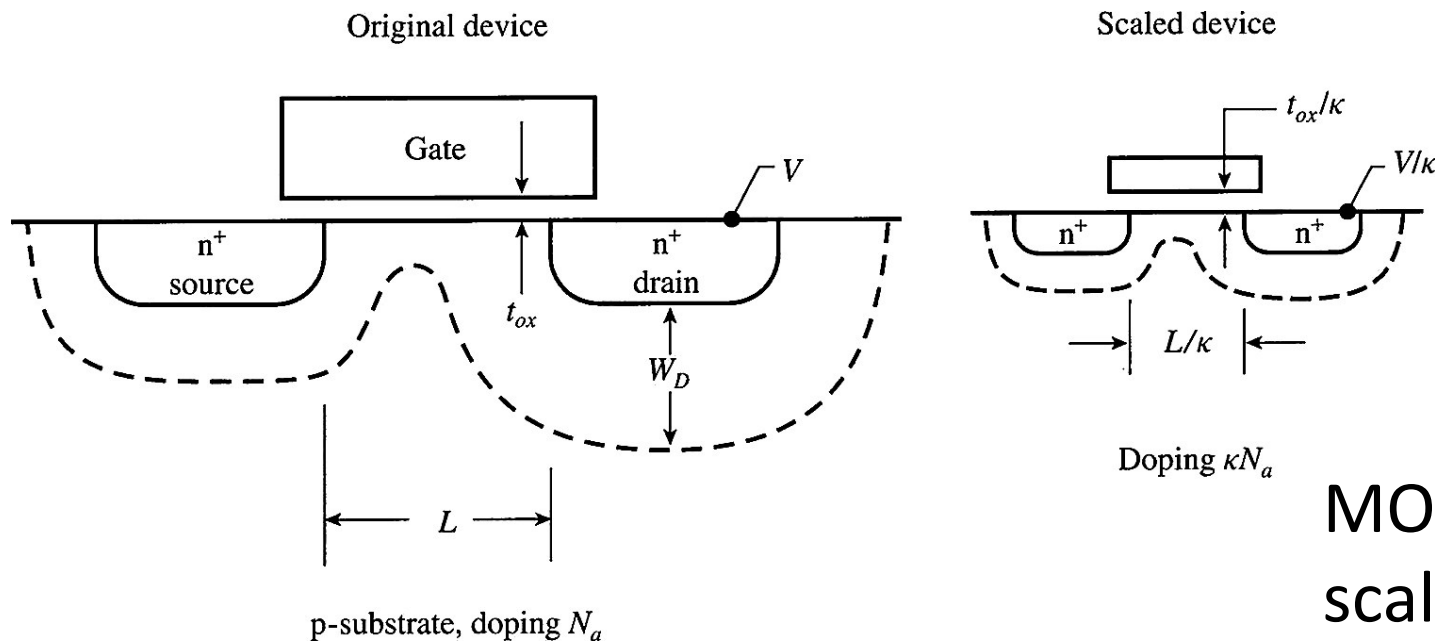
- High-resolution lithographic techniques (Minimum L)
- Technological advancement in ion implantation (Shallow junction)



An architect and a construction worker (Image generated by ChatGPT)

Constant-field scaling (Dennard scaling)

- Keep short-channel effects under control,
 - By scaling down the vertical dimensions along with the horizontal dimensions.
 - Decrease the applied voltage.
 - Increase the substrate doping concentration.



R. H. Dennard
(Inventor of DRAM)

MOSFET constant-electric-field
scaling (Taur, Fig. 4.1)

Rules for constant-field scaling (1)

- Scaling assumption ($\kappa > 1$)
 - Device dimensions (t_{ox} , L , W , and x_j): $1/\kappa$
 - Doping concentration (N_a and N_d): κ
 - Voltage (V): $1/\kappa$
- Maximum drain depletion width

$$W_D = \sqrt{\frac{2\epsilon_{si}(\phi_{bi} + V_{dd})}{qN_a}} \rightarrow \sqrt{\frac{2\epsilon_{si}\left(\phi_{bi} + \frac{1}{\kappa}V_{dd}\right)}{q\kappa N_a}}$$
$$\approx \frac{1}{\kappa} \sqrt{\frac{2\epsilon_{si}(\phi_{bi} + V_{dd})}{qN_a}} = \frac{1}{\kappa} W_D$$

Taur, Eq. (4.1)

Rules for constant-field scaling (2)

- Capacitances
 - They scale down by κ .
- Charge per device ($\sim C \times V$)
 - It scaled down by κ^2 .
- Drain current
 - The original one

$$I_d = \mu_n C_{ox} \frac{W}{L} \left[(V_{gs} - V_t) V_{ds} - \frac{1}{2} V_{ds}^2 \right]$$
$$\mu_n \kappa C_{ox} \frac{\frac{1}{\kappa} W}{\frac{1}{\kappa} L} \left[\left(\frac{1}{\kappa} V_{gs} - V_{t,scaled} \right) \frac{1}{\kappa} V_{ds} - \frac{1}{2} \frac{1}{\kappa^2} V_{ds}^2 \right] \approx \frac{1}{\kappa} I_d$$

Effect of scaling on circuit parameters

- Important conclusion of constant-field scaling:
 - Once the device dimensions and the power-supply voltage are scaled down, the circuit speeds up by the same factor.


$$\tau \sim \frac{CV}{I}$$

Scaling factors indicated by red arrows:

- $\frac{1}{\kappa^2}$ points to C
- $\frac{1}{\kappa}$ points to V
- $\frac{1}{\kappa}$ points to I

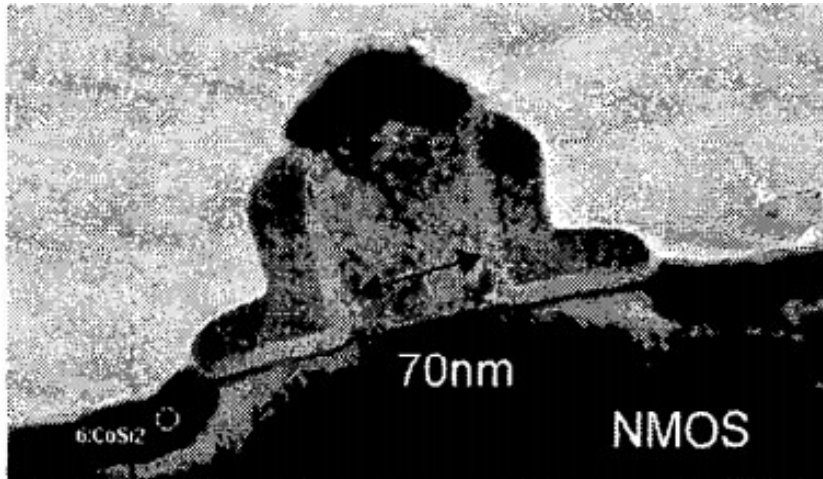
- Moreover, power dissipation per circuit, which is proportional to VI , is reduced by κ^2 .

Chronicles

- Intel and TSMC. IEDM and VLSI papers
 - 130nm: 2000 (Intel, IEDM)
 - 90nm: 2003 (Intel, IEDM)
 - 65nm: 2004 (Intel, IEDM)
 - 45nm: 2007 (Intel, IEDM)
 - 32nm: 2008 (Intel, IEDM)
 - 22nm: 2012 (Intel, VLSI)
 -  – 16nm: 2013 (TSMC, IEDM), 14nm: 2014 (Intel, IEDM)
 - 10nm: 2016 (TSMC, IEDM)
 - 7nm: 2016 (TSMC, IEDM)
 - 5nm: 2019 (TSMC, IEDM)
 - 3nm: 2022 (TSMC, IEDM)
 - 2nm: 2024 (TSMC, IEDM)

Prehistoric(?) MOSFET

- 130-nm MOSFET
 - Major issue: Cu interconnection (Previously, Al)
 - Operation voltage: 1.3 V
 - Oxide thickness: 1.5 nm
 - Poly-silicon gate



SUMMARY OF TRANSISTOR CHARACTERISTICS			
Parameter		180 nm Generation [1]	This Work
V_{DD}	[V]	1.5	1.3
L_{GATE}	[nm]	130	70
T_{OX}	[nm]	2.0	1.5
I_{OFF}	[nA/ μ m]	3	10
$I_{DSAT}(n)$	[mA/ μ m]	1.04	1.02
$I_{DSAT}(p)$	[mA/ μ m]	0.46	0.5
Low V_t I_{OFF}	[nA/ μ m]	-	100
Low V_t $I_{DSAT}(n)$	[mA/ μ m]	-	1.17
Low V_t $I_{DSAT}(p)$	[mA/ μ m]	-	0.6

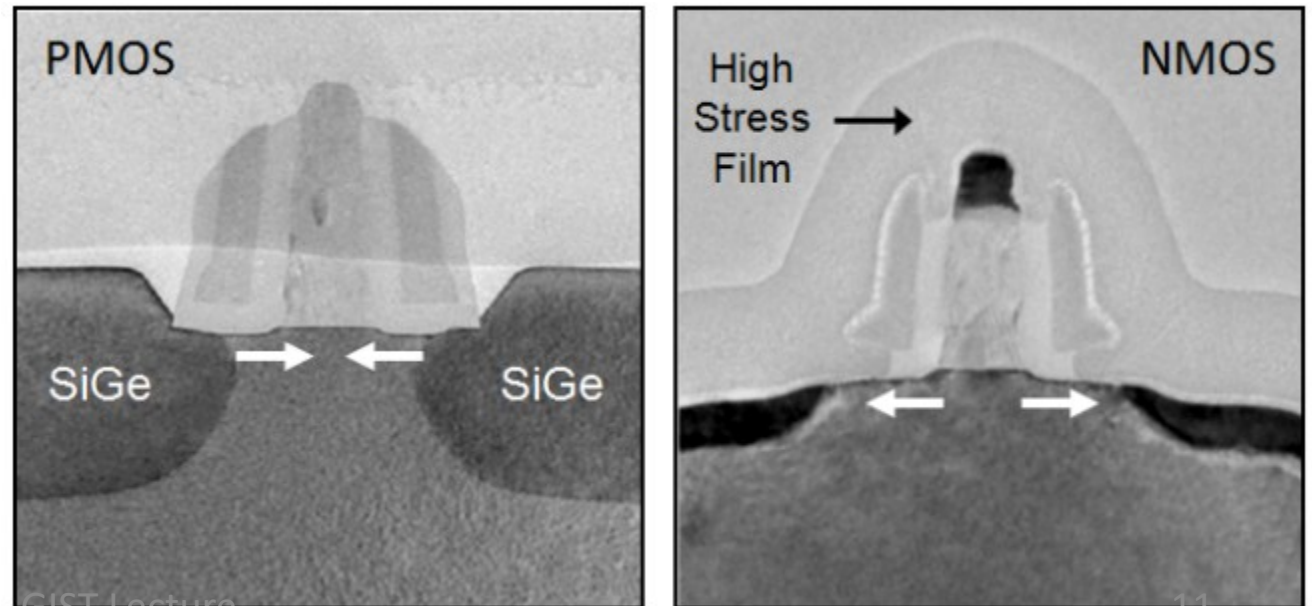
Running out of steam

- In the early 2000s. Why?
 - Due to leakage limitations!
 - The SiO_2 gate oxide had scaled to ~ 1.2 nm at the 90 nm generation.
 - ➔ The gate oxide leakage was increasing exponentially and had become a noticeable percentage of total chip power.
 - Decreasing supply voltage ➔ decreasing threshold voltage ➔ ever-higher subthreshold leakage current
- Increasing transistor leakage
 - Was against the market preferences.
 - The 1980s and 1990s were the era of the home PC.
 - The 2000s was the “mobile” era.

90-nm node

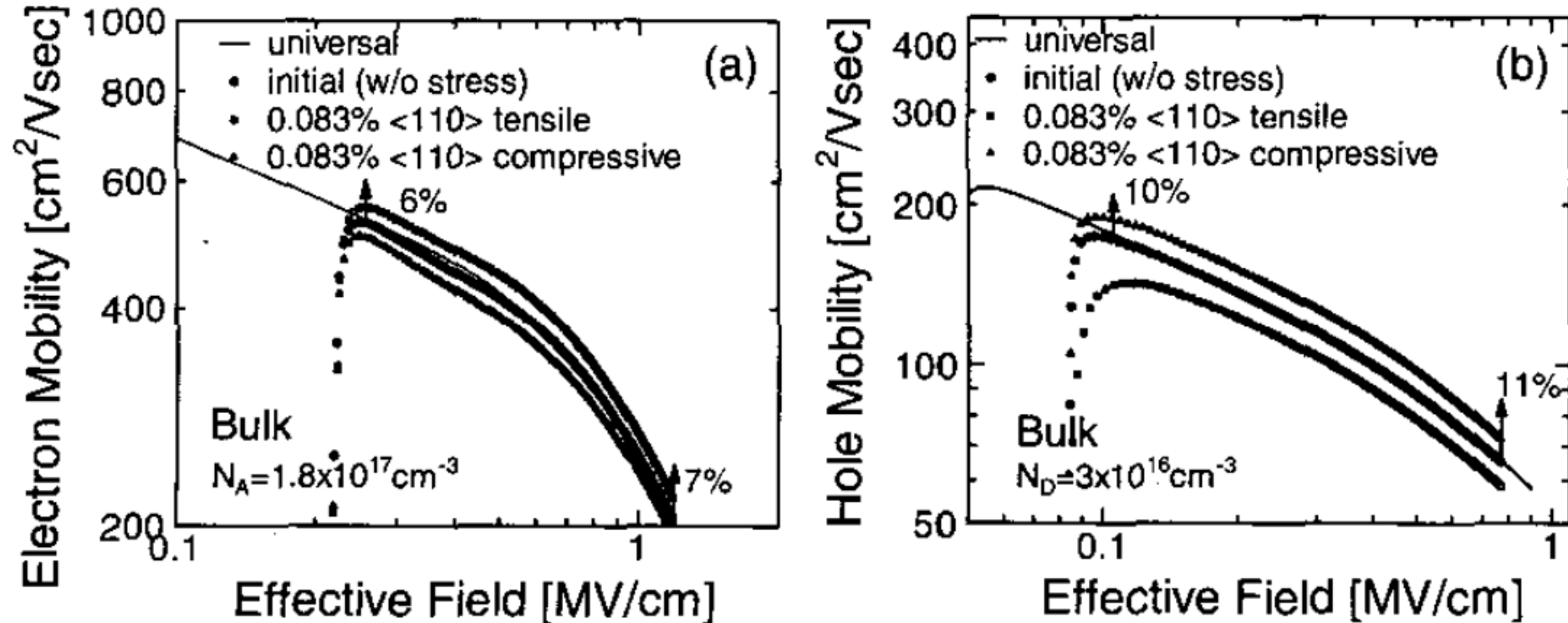
- Oxide thickness: 1.2nm ($\times 0.8$ scaling, not $\times 0.7$)
 - SiGe was selectively deposited in PMOS source-drain regions to provide compressive channel strain.
 - A tensile SiN cap layer was deposited over NMOS transistors to provide tensile channel strain.

90nm uniaxial strained silicon transistors



Impact of stress engineering

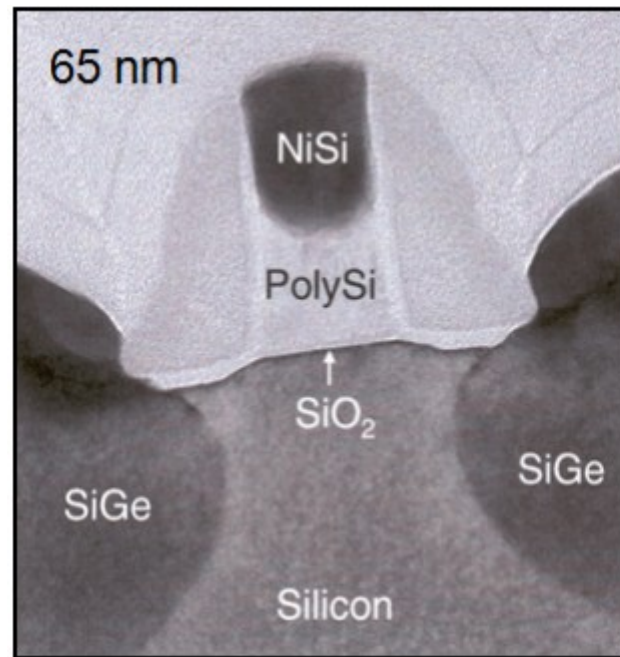
- Mobility enhancement
 - For electrons, tensile strain. For holes, compressive strain



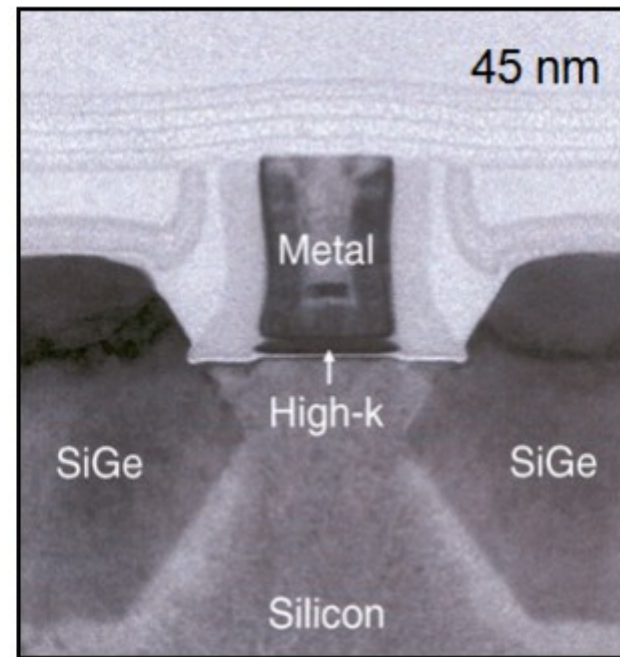
Mobility characteristics under <110> uniaxial strain (K. Uchida, IEDM 2004)

“High-k + metal” gate

- We need to scale the “effective” oxide thickness.
 - Keeping the physical thickness & increasing the oxide capacitance
- Poly depletion effect is now removed.



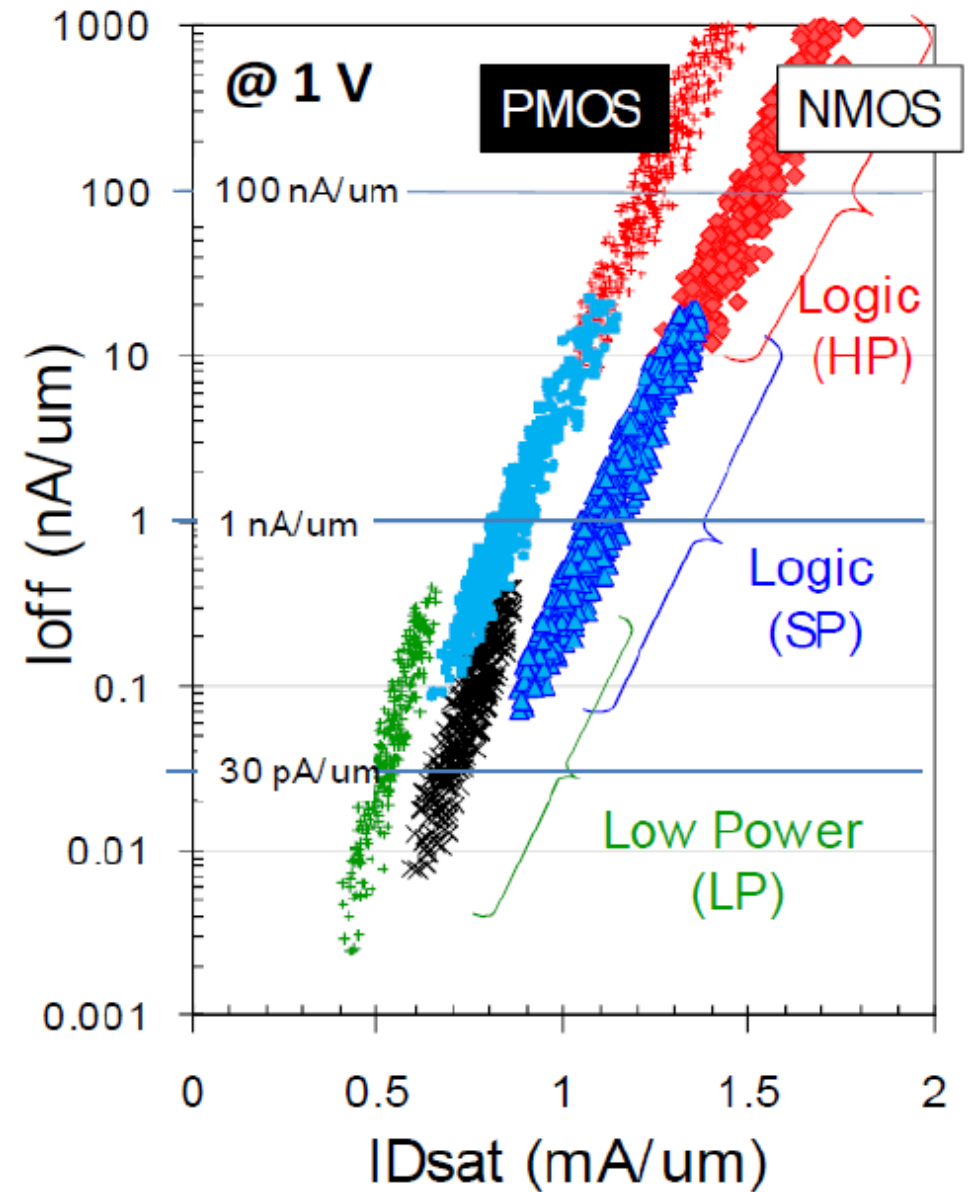
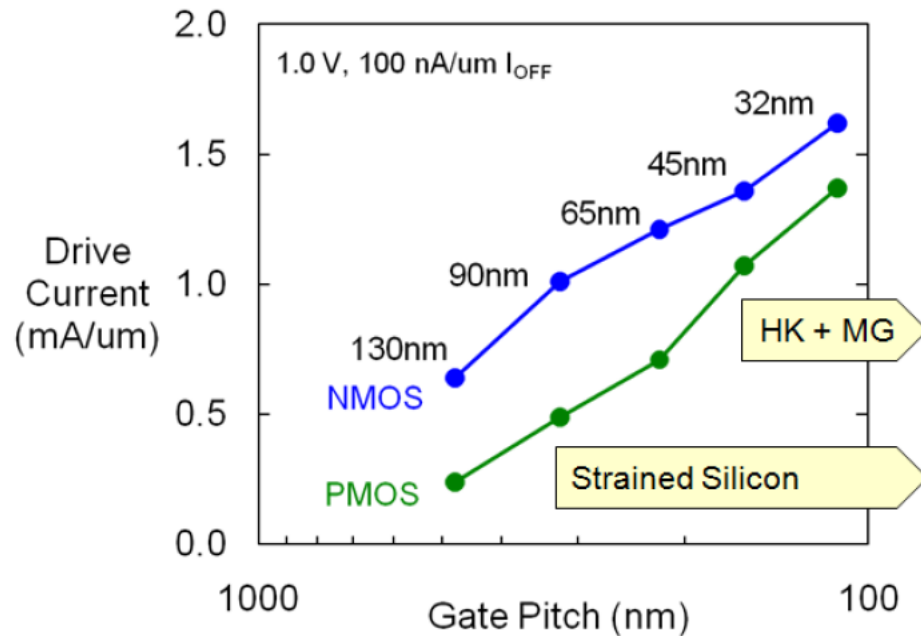
65nm



45nm (high-k metal gate)

Performance

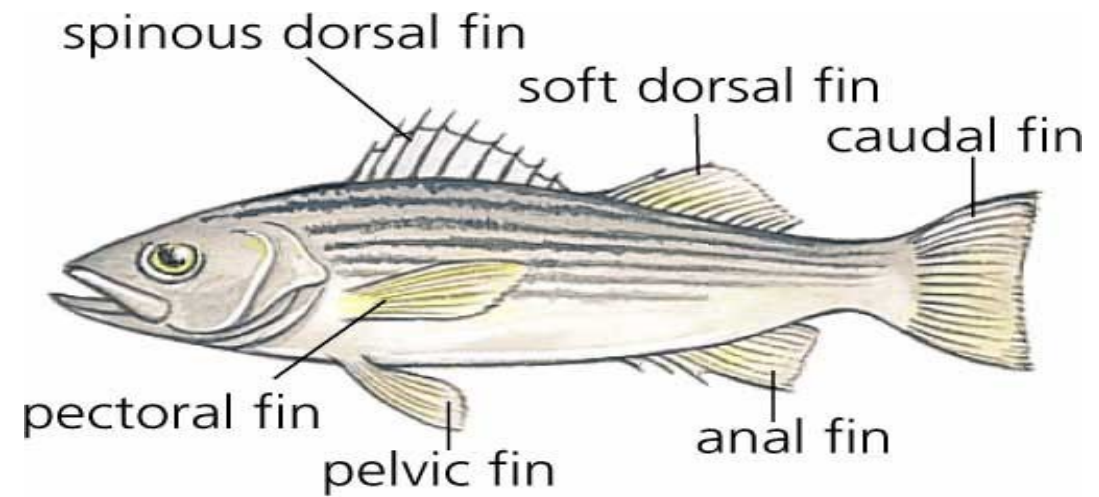
- Drive current improvement
 - Strain engineering
 - High-k + metal gate



32nm transistor performance and leakage options

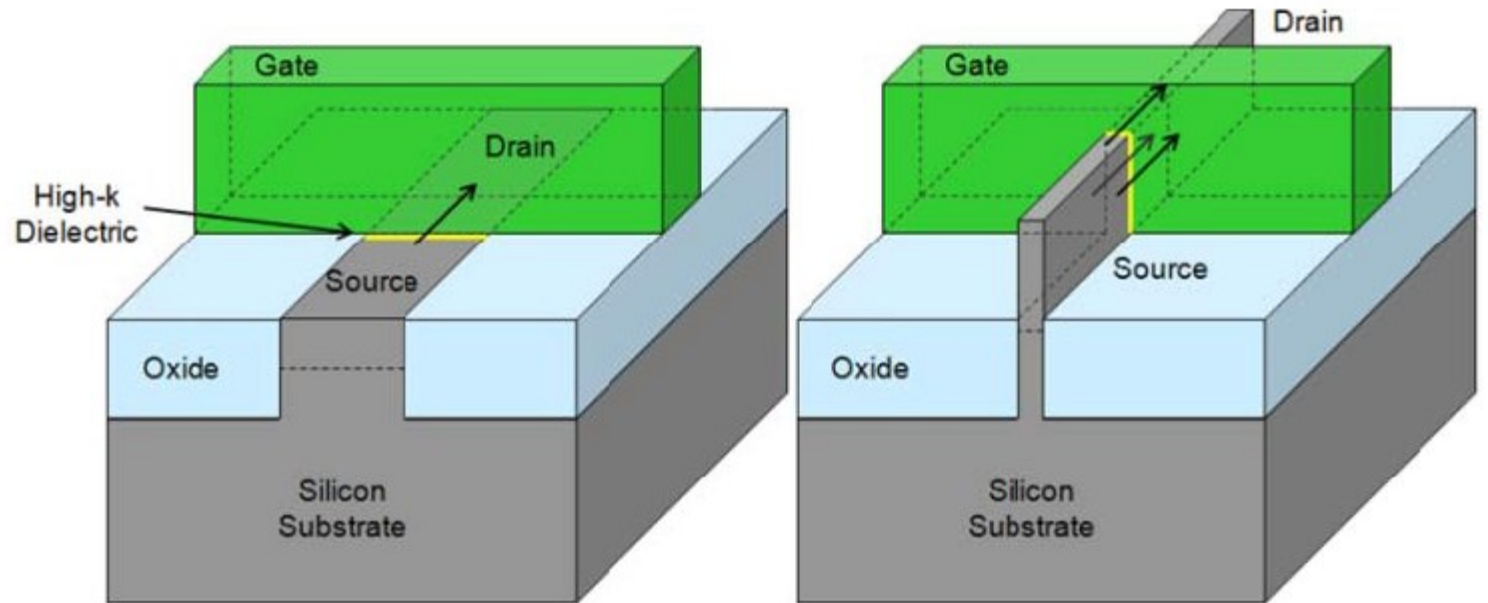
FinFET

- FinFET
 - Following its shape
 - Initially proposed as a SOI FinFET
 - Later, a bulk FinFET



Elizabeth Morales

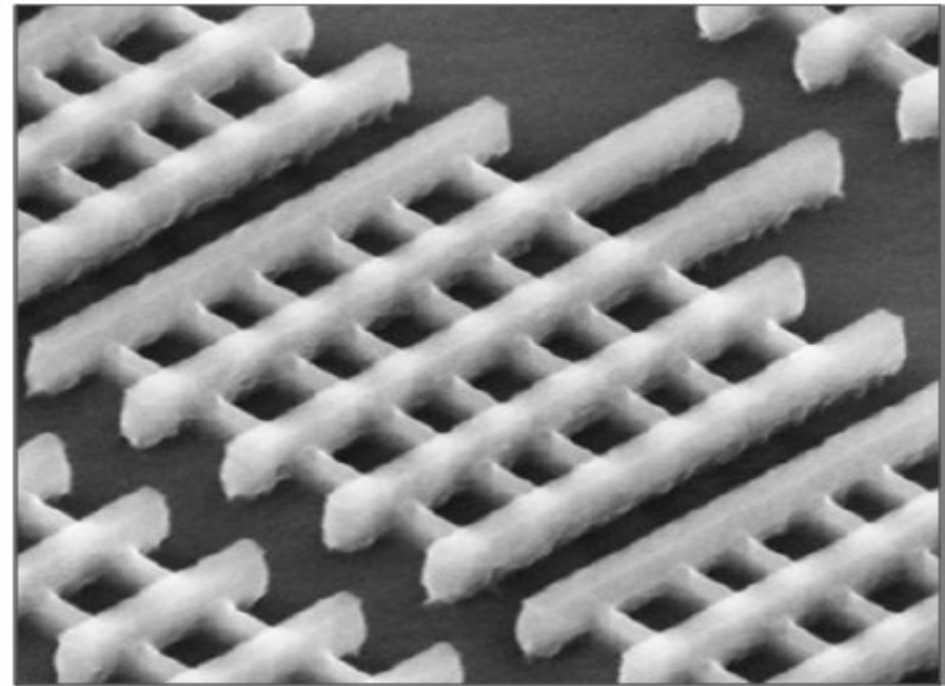
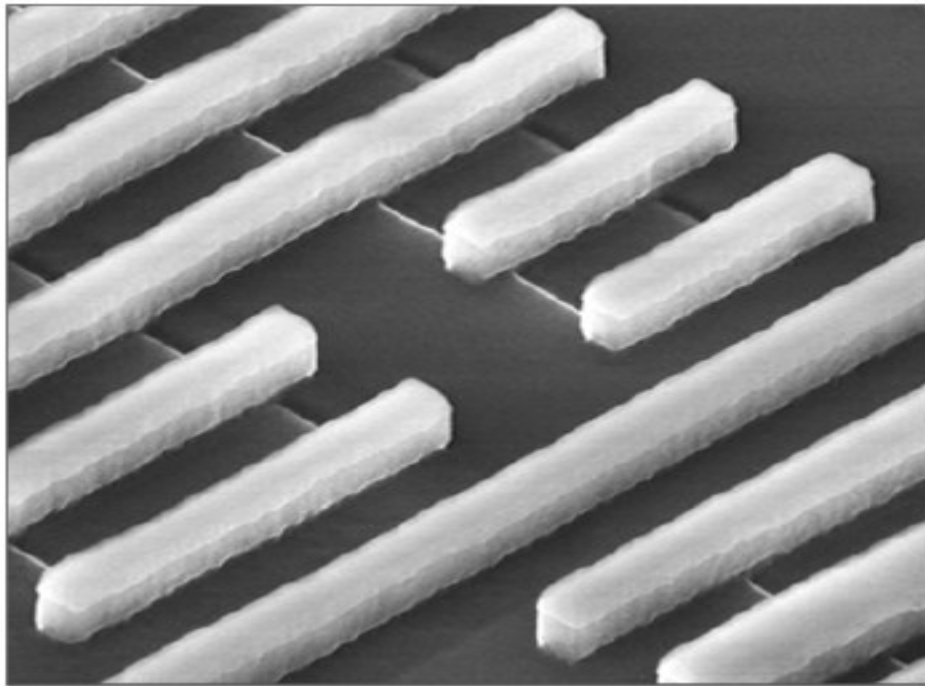
Fins (Google images)



Planar transistor structure (left) and FinFET structure (right)

SEM image

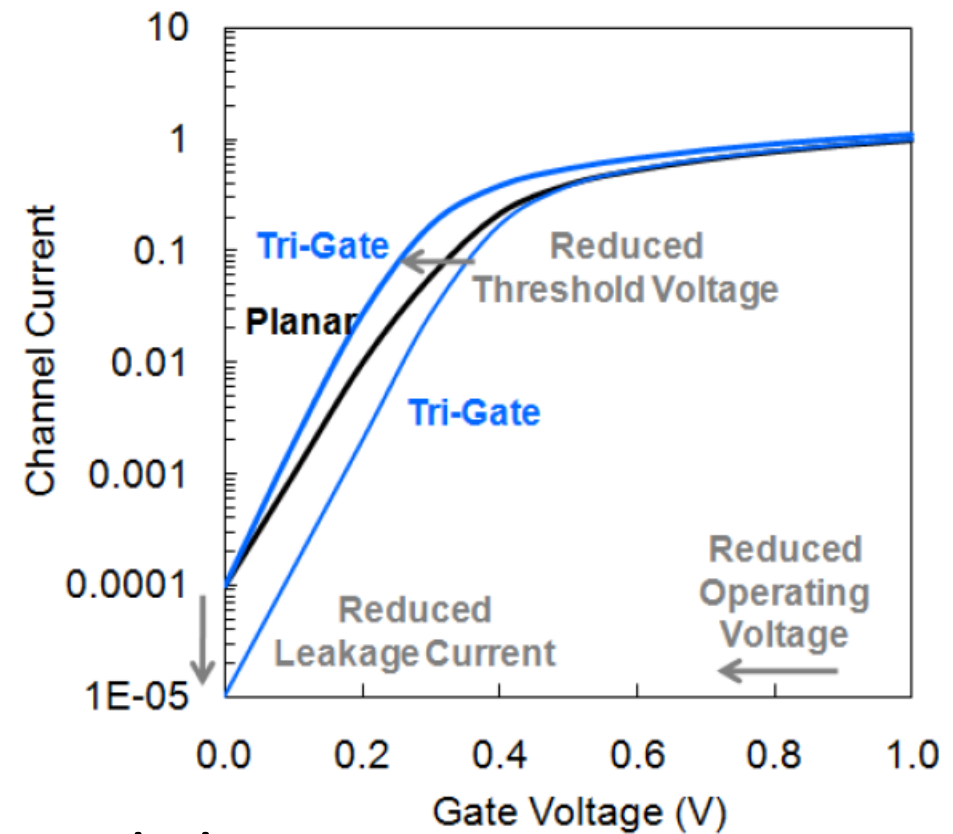
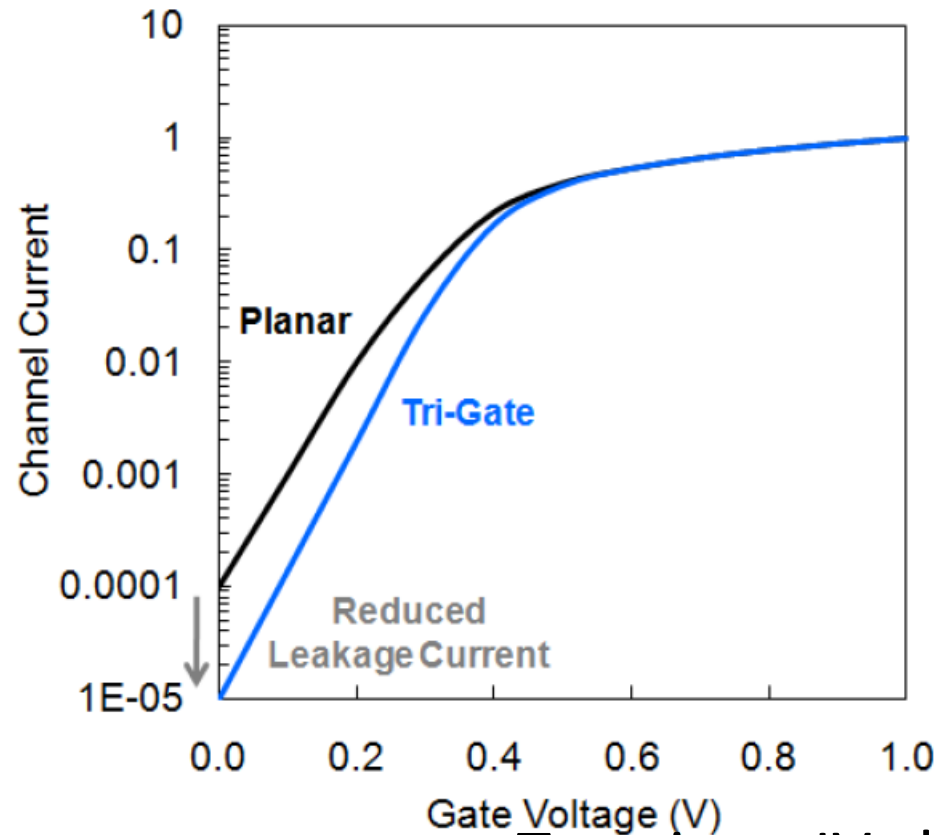
- FinFET
 - Improved electrostatic control of the channel region



32nm planar transistors (left) and 22nm FinFETs (right)

Performance

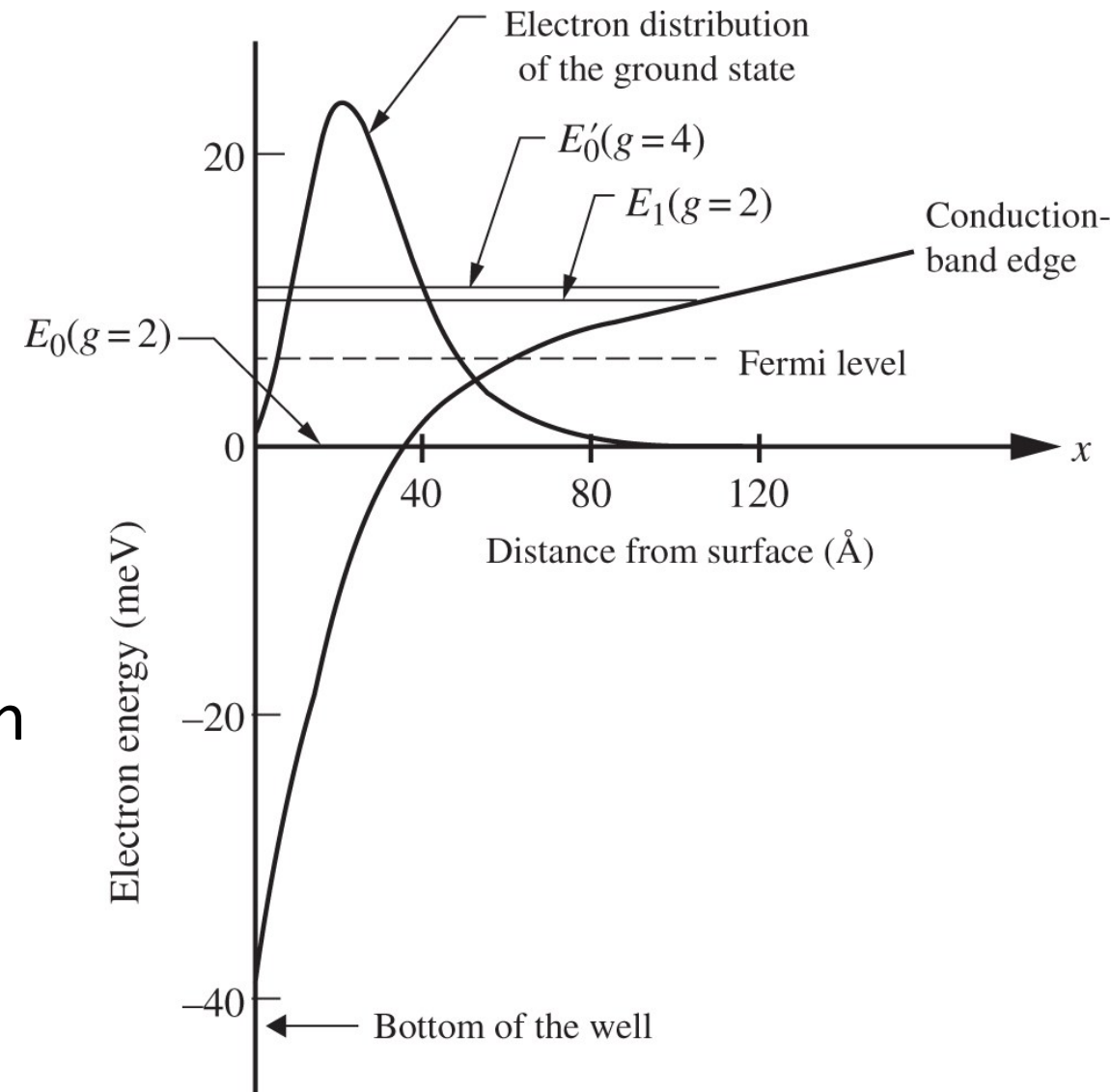
- Steeper sub-threshold slope
 - $\times 10$ off-state leakage reduction



Transistor IV characteristics

Quantum effect

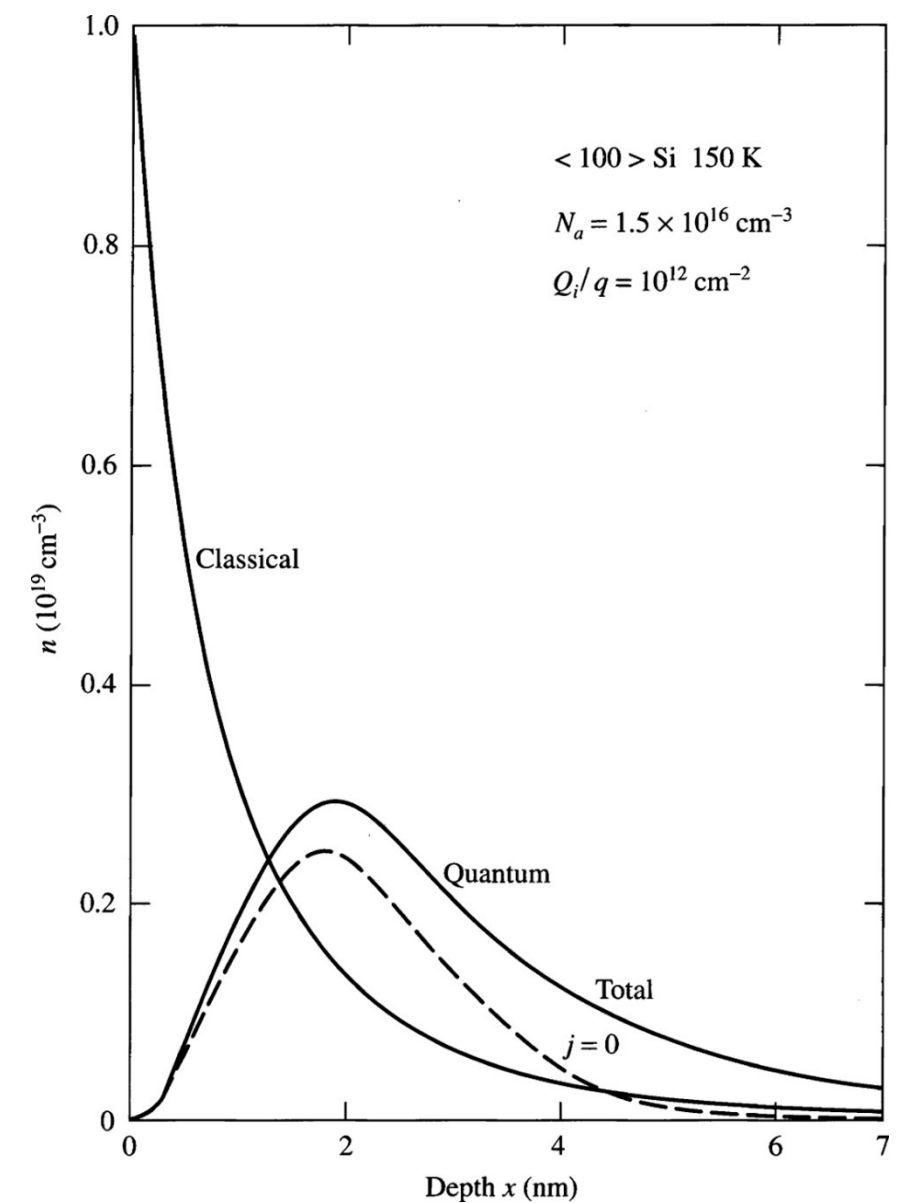
- Potential well formed by
 - The oxide barrier
 - The silicon conduction band
- Subbands
 - Quantized levels
 - Solutions of the Schrödinger equation
- Nearly zero n at the interface



Energy levels of inversion-layer electrons (Taur, Fig. 4.18) 18

Electron profile

- Classical vs. quantum-mechanical
 - Maximum n at the interface
- Quantum mechanical effects
 - At high fields, V_t becomes higher.
 - Effective gate oxide thickness is larger.



Classical and quantum-mechanical
electron density (Taur, Fig. 4.19)5

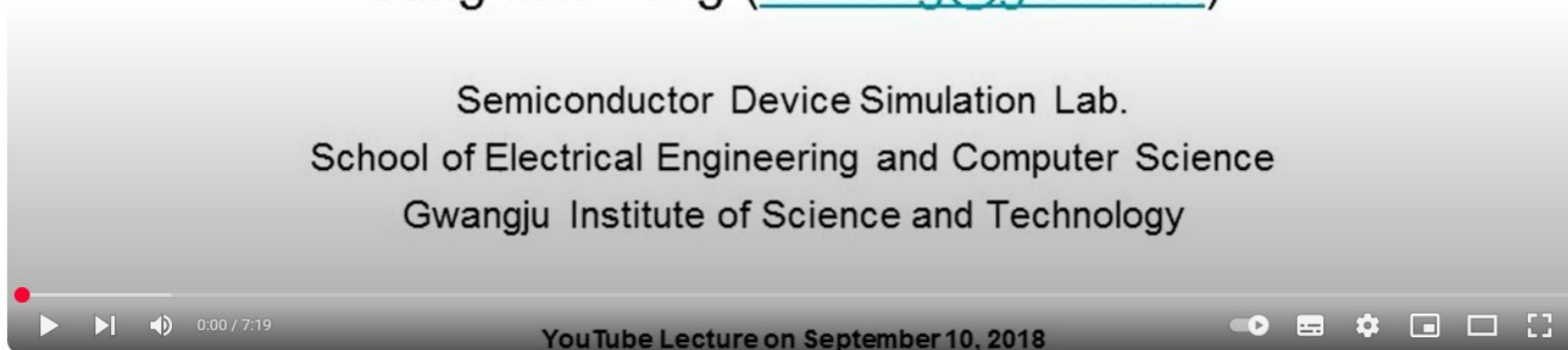
Poisson-Schrödinger solver

- General way to calculate the subband structure
 - It requires numerical analysis...
 - Interested? Watch my YouTube videos. (They are recorded in Korean.)

Schrödinger-Poisson solver – 1. Potential energy

Sung-Min Hong (smhong@gist.ac.kr)

Semiconductor Device Simulation Lab.
School of Electrical Engineering and Computer Science
Gwangju Institute of Science and Technology



Triangular potential approximation

- Parabolic potential profile

- However, it is further approximated as a linear potential. →
Triangular potential well

- Then, the Schrödinger equation reads

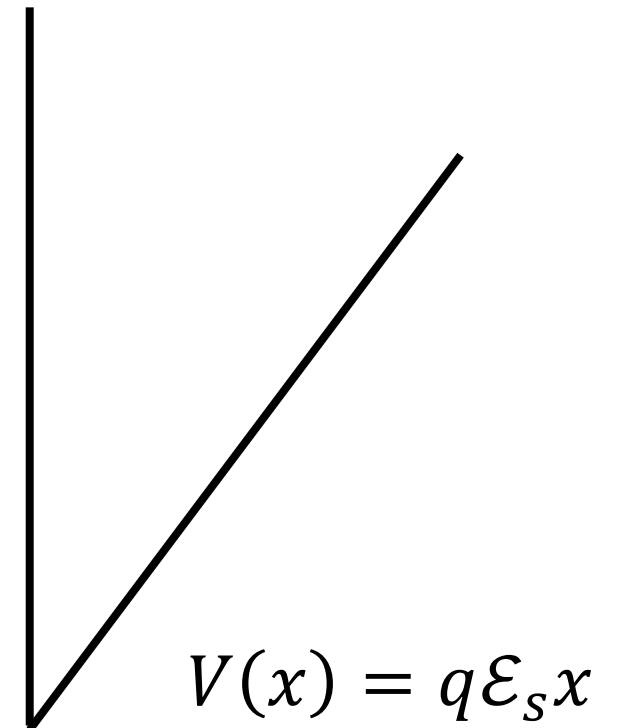
$$\left[-\frac{\hbar^2}{2m_{xx}} \frac{d^2}{dx^2} + q\mathcal{E}_s x \right] \psi(x) = E\psi(x)$$

- Airy function

$$Ai(x) = \frac{1}{\pi} \int_0^\infty \cos\left(\frac{t^3}{3} + xt\right) dt$$

- Its second derivative is

$$\frac{d^2}{dx^2} Ai(x) =$$



Its solution

- Airy function

$$Ai(x) = \frac{1}{\pi} \int_0^{\infty} \cos\left(\frac{t^3}{3} + xt\right) dt$$

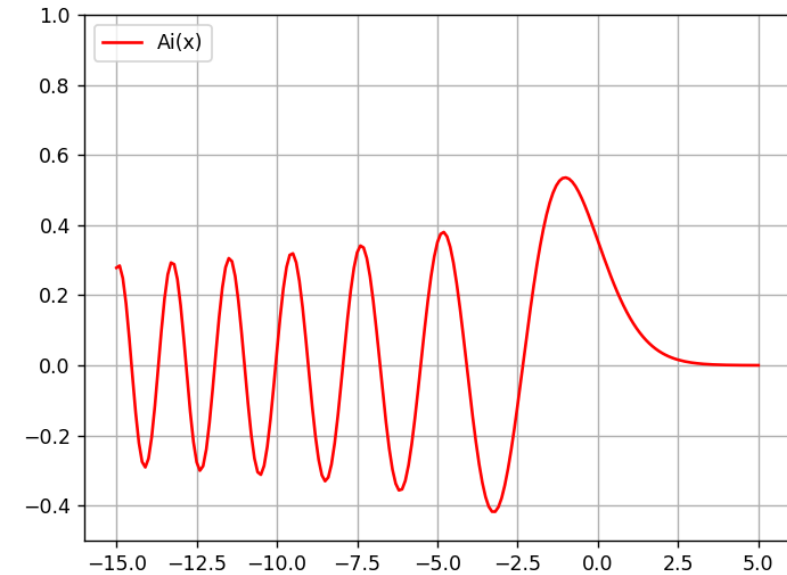
– Its second derivative is

$$\frac{d^2}{dx^2} Ai(x) = -\frac{1}{\pi} \int_0^{\infty} t^2 \cos\left(\frac{t^3}{3} + xt\right) dt$$

– Note that $\frac{d}{dt} \sin\left(\frac{t^3}{3} + xt\right) = (t^2 + x) \cos\left(\frac{t^3}{3} + xt\right)$.

– Therefore,

$$-xAi(x) + \frac{d^2}{dx^2} Ai(x) = -\frac{1}{\pi} \int_0^{\infty} \frac{d}{dt} \sin\left(\frac{t^3}{3} + xt\right) dt = 0$$



Simple manipulation

- The Schrödinger equation is written as

$$\left[\frac{d^2}{dx^2} - \frac{2m_{xx}}{\hbar^2} (q\mathcal{E}_s x - E) \right] \psi = \left[\frac{d^2}{dx^2} - \alpha^3 \left(x - \frac{1}{q\mathcal{E}_s} E \right) \right] \psi = 0$$

- With a new variable, $\xi = \alpha \left(x - \frac{1}{q\mathcal{E}_s} E \right)$, it becomes

$$\left[\frac{d^2}{d\xi^2} - \xi \right] \psi = 0$$

- The solution is $\psi(x) \sim Ai(\xi) = Ai \left(\alpha \left(x - \frac{1}{q\mathcal{E}_s} E \right) \right)$.

- At $x = 0$, the wavefunction must vanish:

$$-\alpha \frac{1}{q\mathcal{E}_s} E_j = a_j$$

Zeros of the Airy function

$$a_0 \approx -2.3381$$

$$a_1 \approx -4.0879$$

Eigenenergy

- Zeros are well approximated as $a_j \approx -\left[\frac{3\pi}{2}\left(j + \frac{3}{4}\right)\right]^{2/3}$.

– Then, the eigenenergy becomes

$$E_j = \frac{q\mathcal{E}_s}{\alpha} \left[\frac{3\pi}{2}\left(j + \frac{3}{4}\right)\right]^{2/3} = \left[\frac{3\hbar q\mathcal{E}_s}{4\sqrt{2m_{xx}}}\left(j + \frac{3}{4}\right)\right]^{2/3} \quad \text{Taur, Eq. (4.46)}$$

- There are two different m_{xx} values: $0.91m_0$ (degeneracy of 2) and $0.19m_0$ (degeneracy of 4)

Thank you!