

# Discrete Assignment-11.9.1-11

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## Problem Statement

Write the first five terms in the sequence:

$$\begin{aligned}a(0) &= 3 \\a(n) &= 3a_{n-1} + 2 \quad \text{for } n > 0\end{aligned}$$

## Solution

Table 1: Input Parameters: First Term and General Formula

Term	Value
$a(0)$	3
$a(n)$	$3a(n-1) + 2$ for $n > 0$

Let's find the first 5 terms of the sequence:

$$x(1) = 3x(0) + 2 = 3 \times 3 + 2 = 11 \quad (1)$$

$$x(2) = 3x(1) + 2 = 3 \times 11 + 2 = 35 \quad (2)$$

$$x(3) = 3x(2) + 2 = 3 \times 35 + 2 = 107 \quad (3)$$

$$x(4) = 3x(3) + 2 = 3 \times 107 + 2 = 323 \quad (4)$$

$$x(5) = 3x(4) + 2 = 3 \times 323 + 2 = 971 \quad (5)$$

So, the next 5 terms of the sequence are 11, 35, 107, 323, 971.

The common difference of this arithmetic progression is  $d = 3$ , and the general term  $x(n)$  for an arithmetic progression is given by:

$$x(n) = x(0) + nd$$

Substitute the values:

$$x(n) = 3 + 3n$$

## Solution using Z Transform

Let's find the Z transform of the sequence  $a(n)$ :

$$\begin{aligned} X(z) &= \mathcal{Z}\{x(n)\} = \sum_{n=0}^{\infty} x(n)z^{-n} \\ &= x(0)z^0 + x(1)z^{-1} + x(2)z^{-2} + x(3)z^{-3} + \dots \\ &= 3 + (3x(0) + 2)z^{-1} + (3x(1) + 2)z^{-2} + (3x(2) + 2)z^{-3} + \dots \\ &= 3 + (3 \cdot 3 + 2)z^{-1} + (3 \cdot (3 \cdot 3 + 2) + 2)z^{-2} + (3 \cdot (3 \cdot (3 \cdot 3 + 2) + 2) + 2)z^{-3} + \dots \\ &= 3 + 11z^{-1} + 35z^{-2} + 107z^{-3} + \dots \end{aligned}$$

So, the Z transform of the sequence  $x(n)$  is given by  $X(z) = 3 + 11z^{-1} + 35z^{-2} + 107z^{-3} + \dots$

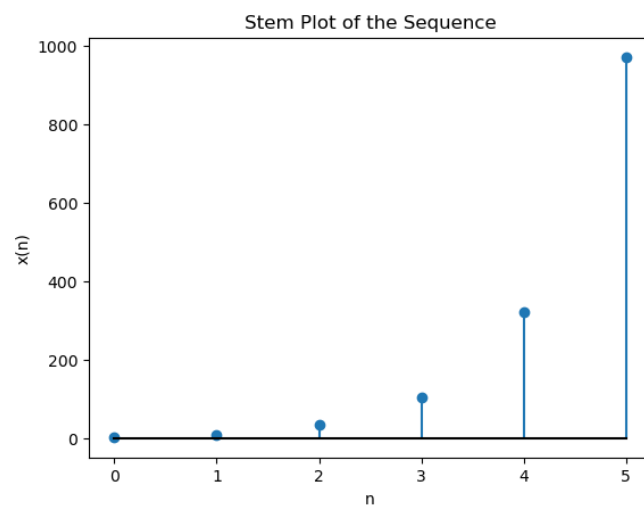


Figure 1: Sequence plot generated from Python script.