# Discrete Assignment-11.9.1-11

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#### Problem Statement

Write the first five terms in the sequence:

$$a_0 = 3$$
  
 $a_n = 3a_{n-1} + 2$  for  $n > 0$ 

## Solution

Table 1: Input Parameters: First Term and General Formula

Term	Value
x(0)	3
x(n)	3x(n-1) + 2  for  n > 0

Let's find the first 5 terms of the sequence:

$$x(1) = 3x(0) + 2 = 3 \times 3 + 2 = 11 \tag{1}$$

$$x(2) = 3x(1) + 2 = 3 \times 11 + 2 = 35 \tag{2}$$

$$x(3) = 3x(2) + 2 = 3 \times 35 + 2 = 107 \tag{3}$$

$$x(4) = 3x(3) + 2 = 3 \times 107 + 2 = 323 \tag{4}$$

$$x(5) = 3x(4) + 2 = 3 \times 323 + 2 = 971 \tag{5}$$

So, the next 5 terms of the sequence are 11, 35, 107, 323, 971.

## Solution using Z Transform

Let's find the Z transform of the sequence a(n):

$$X(z) = \mathcal{Z}\{x(n)\} = \sum_{n=0}^{\infty} x(n)z^{-n}$$

$$= x(0)z^{0} + x(1)z^{-1} + x(2)z^{-2} + x(3)z^{-3} + \dots$$

$$= 3 + (3x(0) + 2)z^{-1} + (3x(1) + 2)z^{-2} + (3x(2) + 2)z^{-3} + \dots$$

$$= 3 + (3 \cdot 3 + 2)z^{-1} + (3 \cdot (3 \cdot 3 + 2) + 2)z^{-2} + (3 \cdot (3 \cdot (3 \cdot 3 + 2) + 2) + 2)z^{-3} + \dots$$

$$= 3 + 11z^{-1} + 35z^{-2} + 107z^{-3} + \dots$$

So, the Z transform of the sequence x(n) is given by  $X(z)=3+11z^{-1}+35z^{-2}+107z^{-3}+\ldots$ 

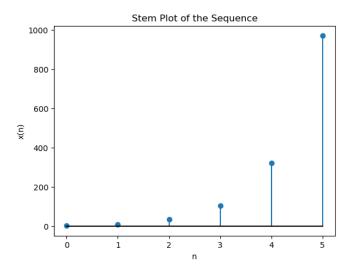


Figure 1: Sequence plot generated from Python script.