Discrete Assignment-11.9.1-11

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Problem Statement

Write the first five terms in the sequence:

$$a_0 = 3 \tag{1}$$

$$a_n = 3a_{n-1} + 2 \quad \text{for } n > 0$$
 (2)

Solution

Table 1: Input Parameters: First Term and General Formula

Term	Value
$\mathbf{x}(0)$	3
x(n)	3x(n-1) + 2 for n > 0

So, the first 5 terms of the sequence are (3, 11, 35, 107, 323).

Difference Equation and Z-transform

The given difference equation is:

$$y(n) - 3y(n-1)x(n-1) = -x(n-1) + 3x(n)$$
(3)

where
$$x(n) = u(n)$$
 (4)

$$y(n) - 3y(n-1)u(n-1) = -u(n-1) + 3u(n)$$
(5)

Parameter

Z-transform of the difference equation is:

$$Y(z) = \frac{3z^{-1}Y(z) - z^{-1} + 3}{1 - z^{-1}}$$
(6)

$$Y(z) = \frac{2(1-z^{-1})}{z^{-2} - 2z^{-1} - 2} \tag{7}$$

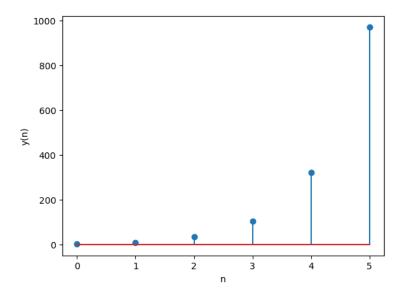


Figure 1: Sequence