



# Industrial Computer Vision

## - Boundary Extraction

5<sup>th</sup> lecture, 2022.10.05  
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# Contents

- Edge Detection
- Hough Transform
- Connected Component Labeling

# Image Segmentation

- Image segmentation divides an image into regions that are connected and have some similarity within the region and some difference between adjacent regions.
- The goal is usually to find individual objects in an image.
- For the most part there are fundamentally two kinds of approaches to segmentation: discontinuity and similarity.
  - Similarity may be due to pixel intensity, color or texture.
  - Differences are sudden changes (discontinuities) in any of these, but especially sudden changes in intensity along a boundary line, which is called an edge.

# Detection of Discontinuities

- There are three kinds of discontinuities of intensity: points, lines and edges.
- The most common way to look for discontinuities is to scan a small mask over the image. The mask determines which kind of discontinuity to look for.

$$R = w_1 z_1 + w_2 z_2 + \dots + w_9 z_9 = \sum_{i=1}^9 w_i z_i$$

**FIGURE 10.1** A general  $3 \times 3$  mask.

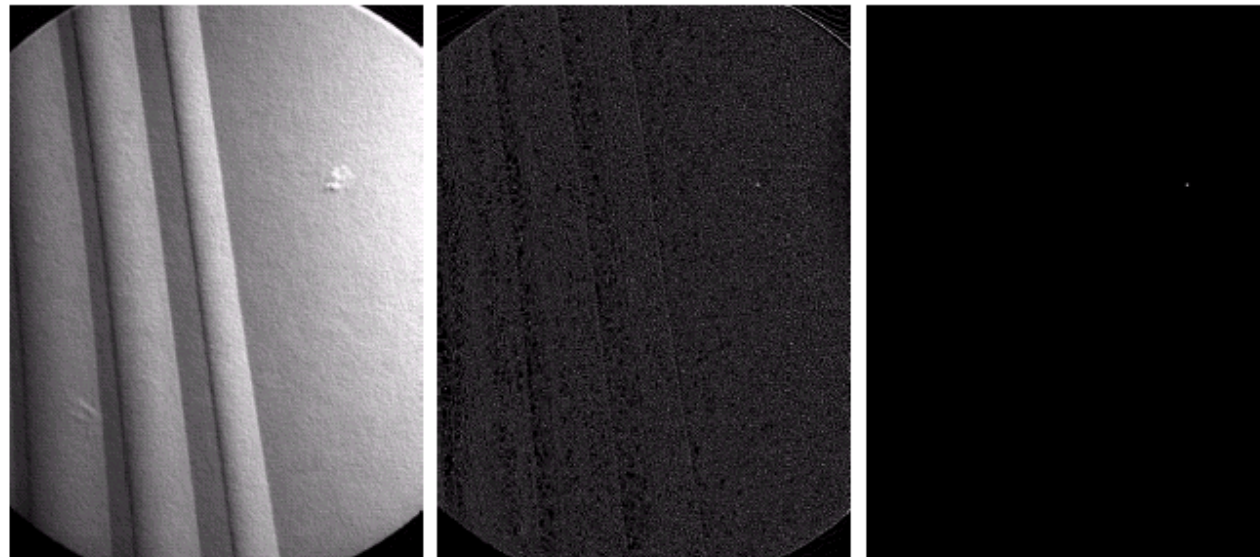
$w_1$	$w_2$	$w_3$
$w_4$	$w_5$	$w_6$
$w_7$	$w_8$	$w_9$

# Detection of Discontinuities: Point Detection

$$|R| \geq T$$

where  $T$  : a nonnegative threshold

-1	-1	-1
-1	8	-1
-1	-1	-1



a  
b c d

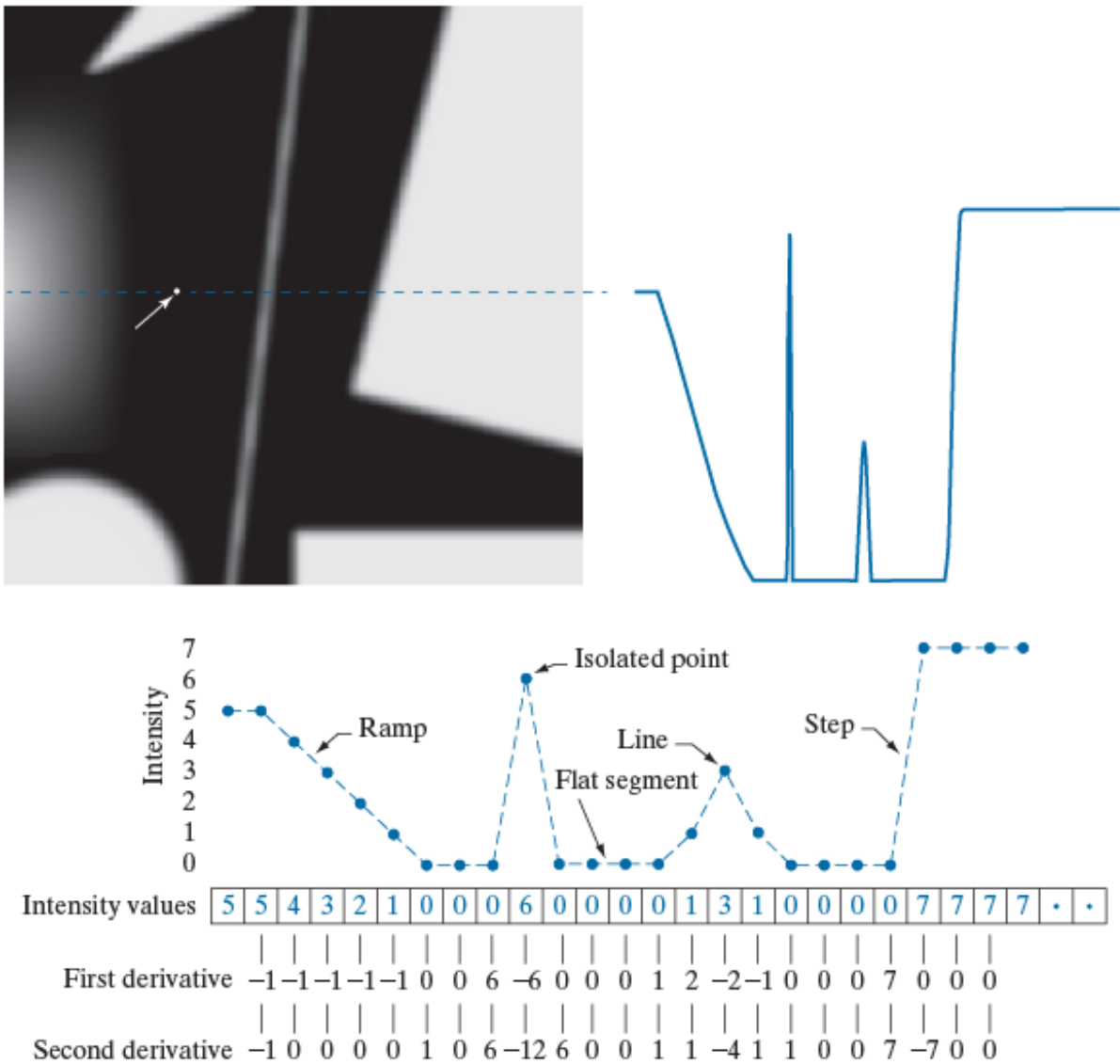
**FIGURE 10.2**

(a) Point detection mask.  
(b) X-ray image of a turbine blade with a porosity.  
(c) Result of point detection.  
(d) Result of using Eq. (10.1-2).  
(Original image courtesy of X-TEK Systems Ltd.)

# Detection of Discontinuities: Line Detection

a b  
c

**FIGURE 10.2**  
(a) Image.  
(b) Horizontal intensity profile that includes the isolated point indicated by the arrow.  
(c) Subsampled profile; the dashes were added for clarity. The numbers in the boxes are the intensity values of the dots shown in the profile. The derivatives were obtained using Eqs. (10-4) for the first derivative and Eq. (10-7) for the second.



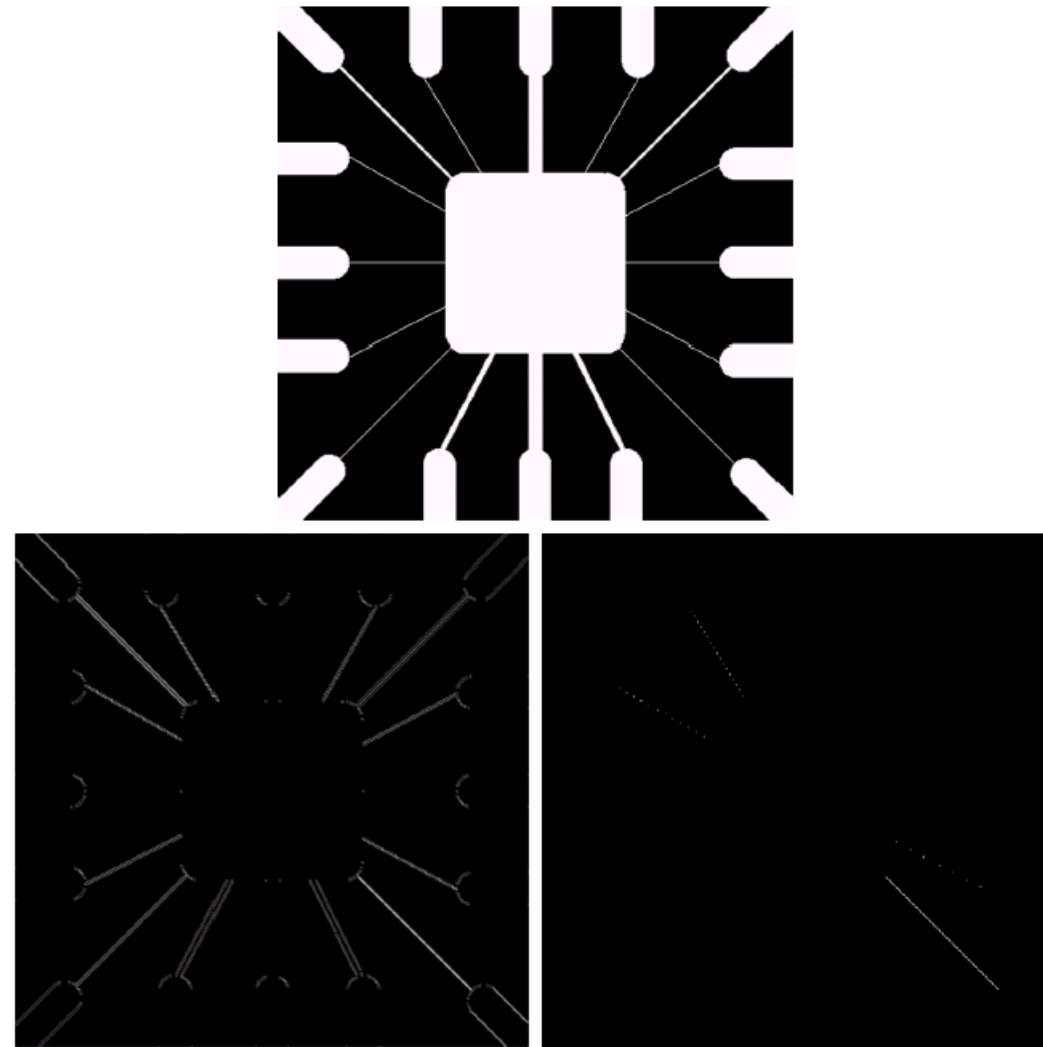
# Detection of Discontinuities: Line Detection

- Only slightly more common than point detection is to find a one pixel wide line in an image.
- For digital images the only three point straight lines are only horizontal, vertical, or diagonal (+ or  $-45^\circ$ ).

**FIGURE 10.3** Line masks.

-1	-1	-1	-1	-1	2	-1	2	-1	2	-1	-1
2	2	2	-1	2	-1	-1	2	-1	-1	2	-1
-1	-1	-1	2	-1	-1	-1	2	-1	-1	-1	2
Horizontal			+45°			Vertical			-45°		

# Detection of Discontinuities: Line Detection



a  
b c

**FIGURE 10.4**

Illustration of line detection.

(a) Binary wire-bond mask.

(b) Absolute value of result after processing with  $-45^\circ$  line detector.

(c) Result of thresholding image (b).

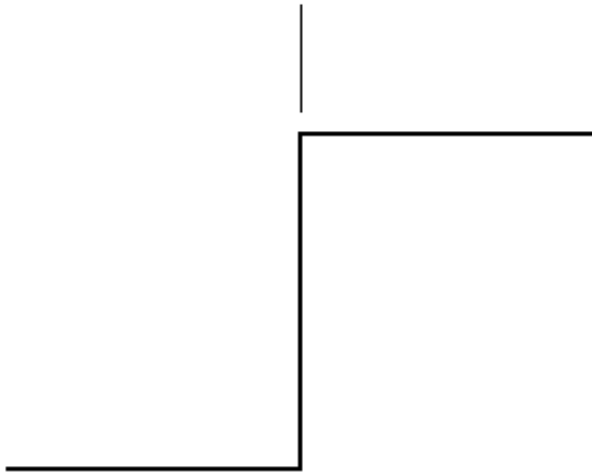


# Detection of Discontinuities: Edge Detection

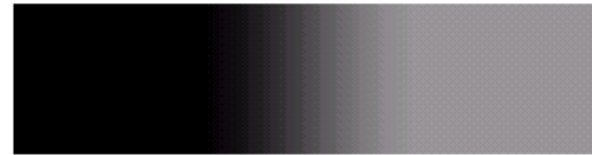
Model of an ideal digital edge



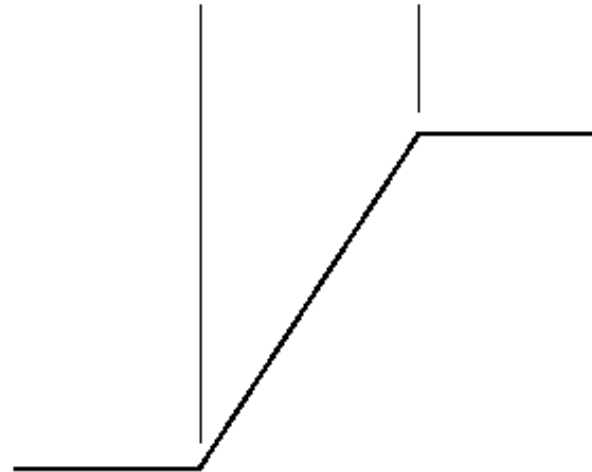
Gray-level profile  
of a horizontal line  
through the image



Model of a ramp digital edge



Gray-level profile  
of a horizontal line  
through the image



a b

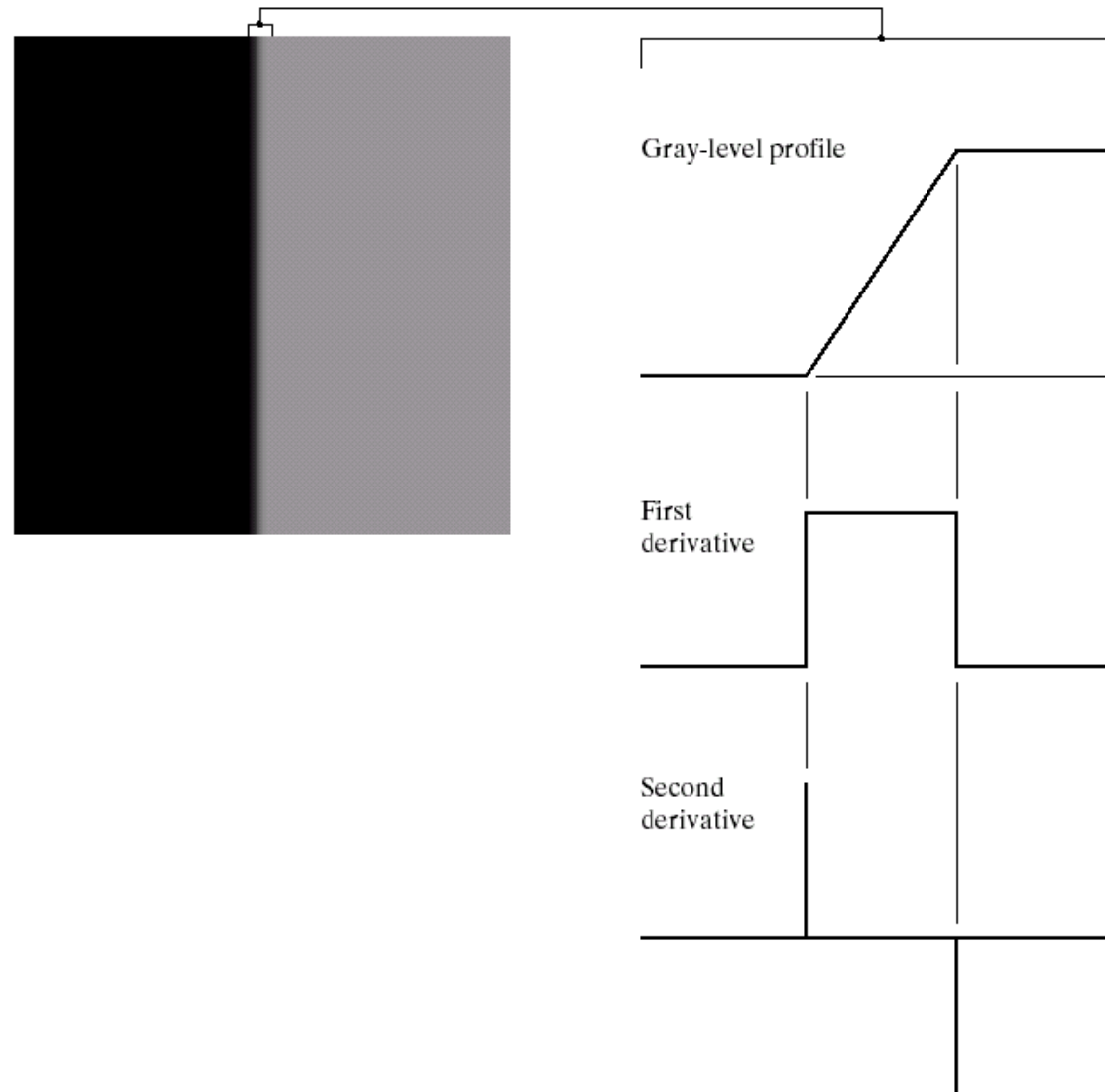
**FIGURE 10.5**  
(a) Model of an ideal digital edge.  
(b) Model of a ramp edge. The slope of the ramp is proportional to the degree of blurring in the edge.

# Detection of Discontinuities: Edge Detection

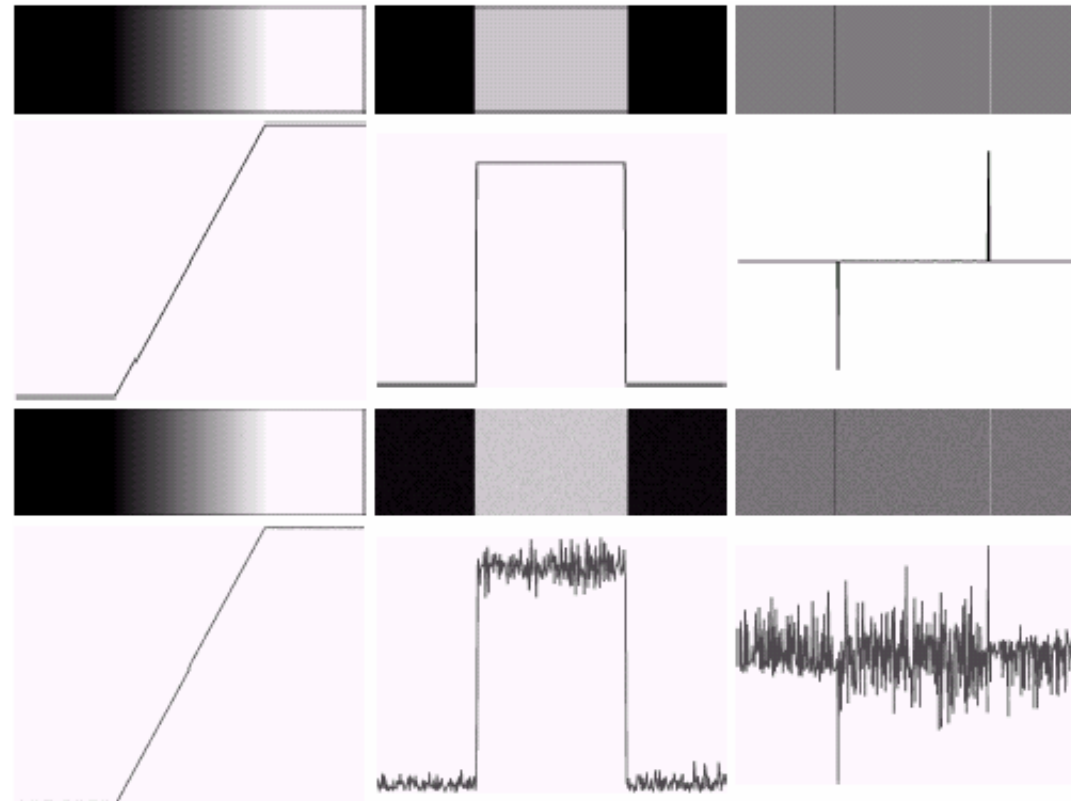
a b

**FIGURE 10.6**

(a) Two regions separated by a vertical edge.  
(b) Detail near the edge, showing a gray-level profile, and the first and second derivatives of the profile.



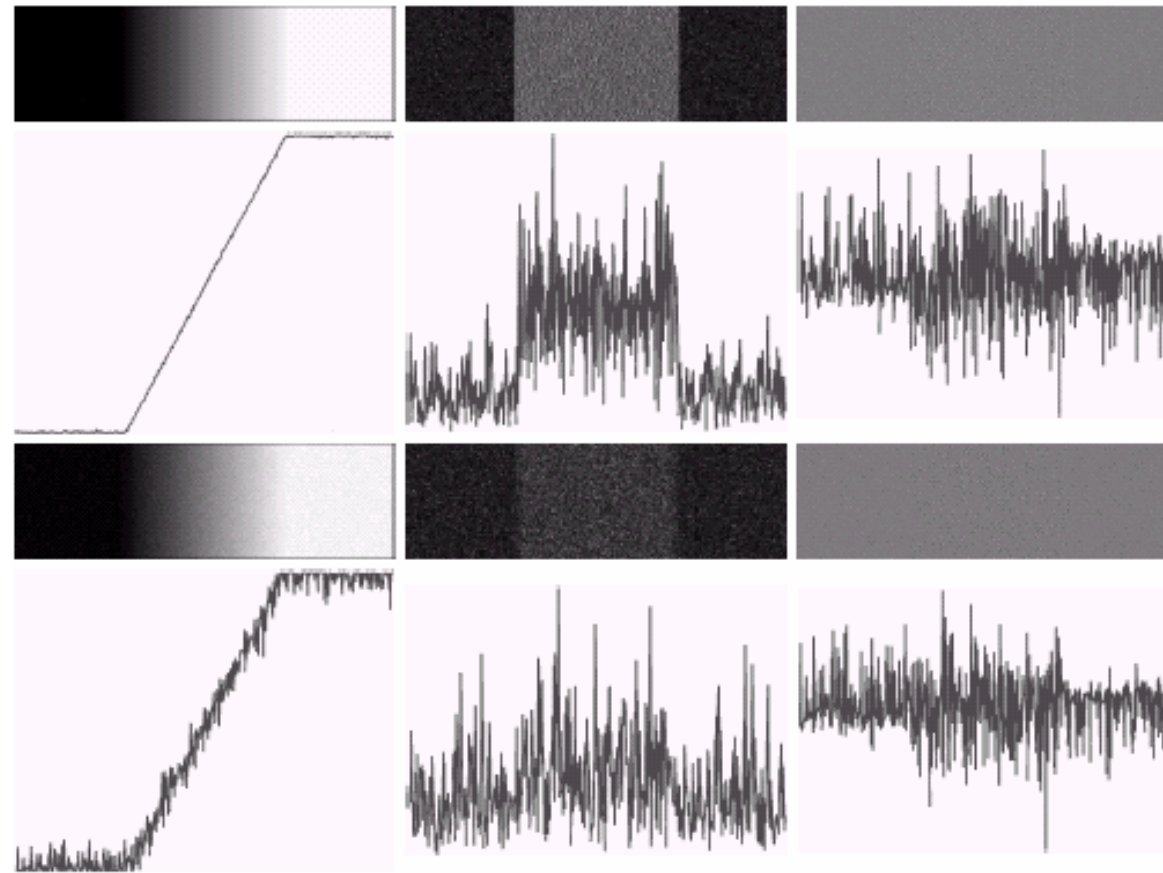
# Detection of Discontinuities: Edge Detection



**FIGURE 10.7** First column: images and gray-level profiles of a ramp edge corrupted by random Gaussian noise of mean 0 and  $\sigma = 0.0, 0.1, 1.0$ , and  $10.0$ , respectively. Second column: first-derivative images and gray-level profiles. Third column: second-derivative images and gray-level profiles.

a  
b  
c  
d

# Detection of Discontinuities: Edge Detection



**FIGURE 10.7** First column: images and gray-level profiles of a ramp edge corrupted by random Gaussian noise of mean 0 and  $\sigma = 0.0, 0.1, 1.0$ , and  $10.0$ , respectively. Second column: first-derivative images and gray-level profiles. Third column: second-derivative images and gray-level profiles.

a  
b  
c  
d

# Detection of Discontinuities: Gradient Operators

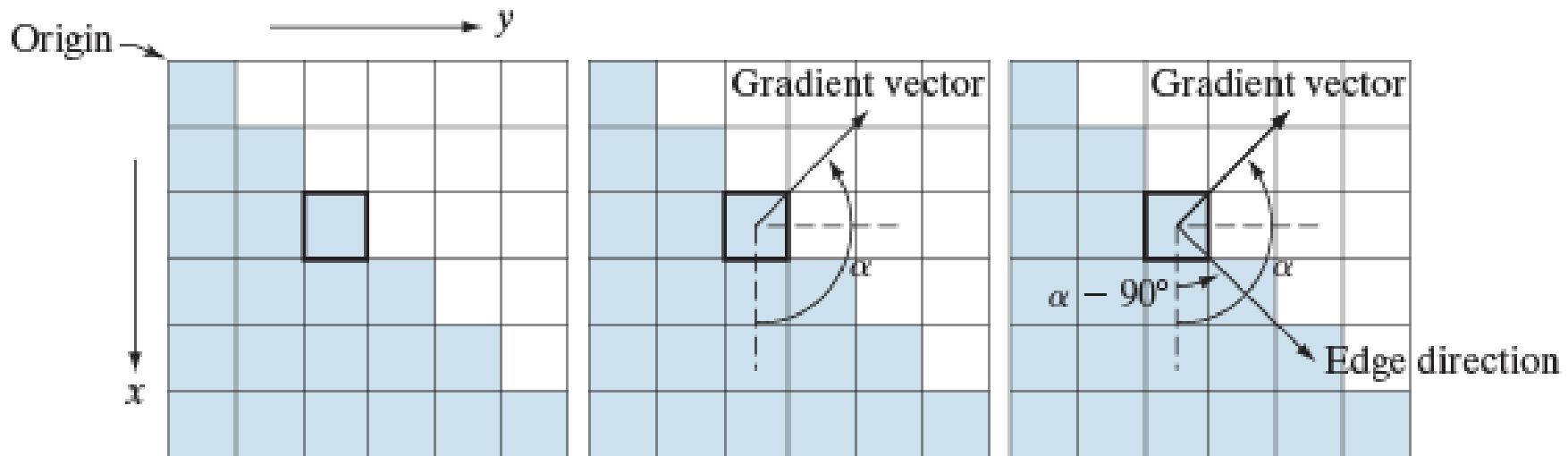
- First-order derivatives:

- The gradient of an image  $f(x,y)$  at location  $(x,y)$  is defined as the vector:

$$\nabla \mathbf{f} = \begin{bmatrix} G_x \\ G_y \end{bmatrix} = \begin{bmatrix} \frac{\partial f}{\partial x} \\ \frac{\partial f}{\partial y} \end{bmatrix}$$

- The magnitude of this vector:  $\alpha(x, y) = \tan^{-1} \left( \frac{G_x}{G_y} \right)$

- The direction of this vector:  $\nabla f = \text{mag}(\nabla \mathbf{f}) = [G_x^2 + G_y^2]^{\frac{1}{2}}$



# Detection of Discontinuities: Gradient Operators

Roberts cross-gradient operators



-1	0	0	-1
0	1	1	0

Roberts

Prewitt operators



-1	-1	-1	-1	0	1
0	0	0	-1	0	1
1	1	1	-1	0	1

Prewitt

Sobel operators



-1	-2	-1	-1	0	1
0	0	0	-2	0	2
1	2	1	-1	0	1

Sobel

# Detection of Discontinuities: Gradient Operators

Prewitt masks for detecting diagonal edges



0	1	1	-1	-1	0
-1	0	1	-1	0	1
-1	-1	0	0	1	1

Prewitt

Sobel masks for detecting diagonal edges



0	1	2	-2	-1	0
-1	0	1	-1	0	1
-2	-1	0	0	1	2

Sobel

a	b
c	d

**FIGURE 10.9** Prewitt and Sobel masks for detecting diagonal edges.



# Detection of Discontinuities: Gradient Operators: Example

a	b
c	d

**FIGURE 10.10**

(a) Original image. (b)  $|G_x|$ , component of the gradient in the  $x$ -direction. (c)  $|G_y|$ , component in the  $y$ -direction. (d) Gradient image,  $|G_x| + |G_y|$ .

$$\nabla f \approx |G_x| + |G_y|$$





# Detection of Discontinuities: Gradient Operators: Example



a	b
c	d

**FIGURE 10.11**  
Same sequence as in Fig. 10.10, but with the original image smoothed with a  $5 \times 5$  averaging filter.

# Detection of Discontinuities: Gradient Operators: Example



a b

**FIGURE 10.12**  
Diagonal edge detection.  
(a) Result of using the mask in Fig. 10.9(c).  
(b) Result of using the mask in Fig. 10.9(d). The input in both cases was Fig. 10.11(a).

0	1	2
-1	0	1
-2	-1	0

-2	-1	0
-1	0	1
0	1	2

# Detection of Discontinuities: Gradient Operators

- Second-order derivatives: (The Laplacian)

- The Laplacian of an 2D function  $f(x,y)$  is defined as

$$\nabla^2 f = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2}$$

- Two forms in practice:

**FIGURE 10.13**  
Laplacian masks  
used to  
implement  
Eqs. (10.1-14) and  
(10.1-15),  
respectively.

---

0	-1	0	-1	-1	-1
-1	4	-1	-1	8	-1
0	-1	0	-1	-1	-1

# Detection of Discontinuities: Gradient Operators

- Consider the function:

$$h(r) = -e^{-\frac{r^2}{2\sigma^2}} \quad \text{where } r^2 = x^2 + y^2$$

and  $\sigma$  : the standard deviation

A Gaussian function

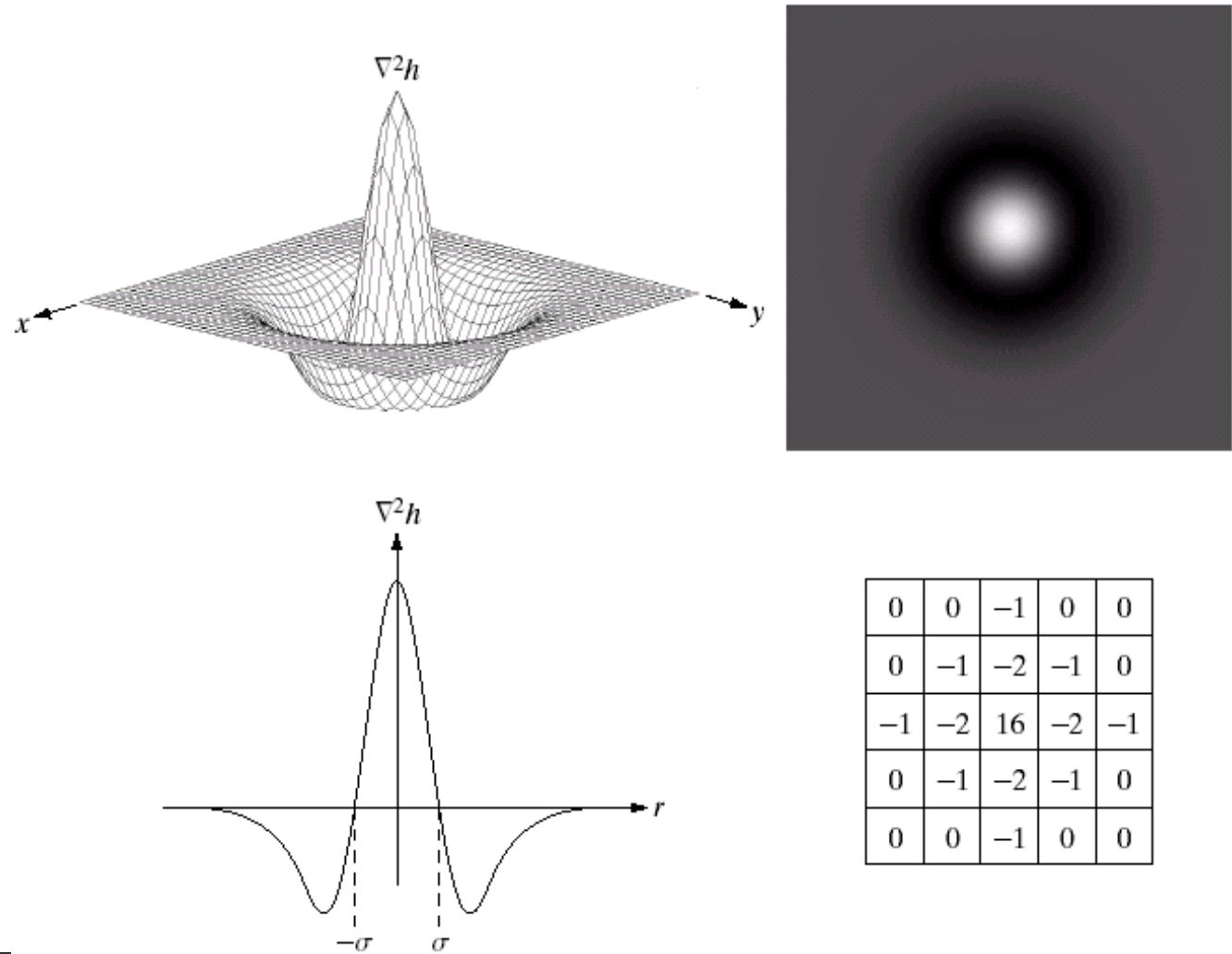
- The Laplacian of h is

$$\nabla^2 h(r) = -\left[ \frac{r^2 - \sigma^2}{\sigma^4} \right] e^{-\frac{r^2}{2\sigma^2}}$$

The Laplacian of a Gaussian  
(LoG)

- The Laplacian of a Gaussian sometimes is called the Mexican hat function. It also can be computed by smoothing the image with the Gaussian smoothing mask, followed by application of the Laplacian mask.

# Detection of Discontinuities: Gradient Operators



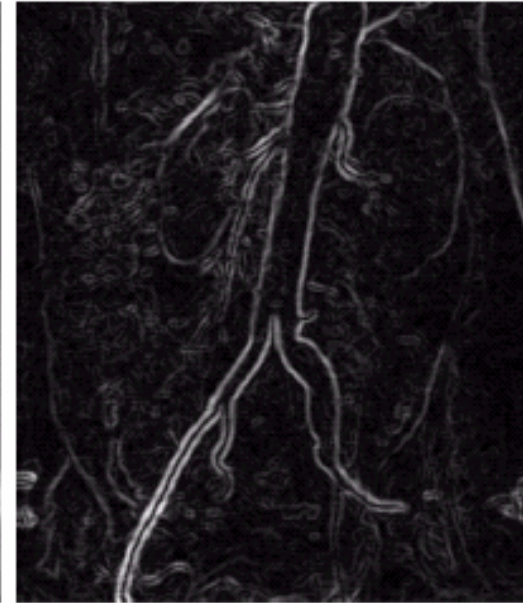
a b  
c d

**FIGURE 10.14**  
Laplacian of a Gaussian (LoG).  
(a) 3-D plot.  
(b) Image (black is negative, gray is the zero plane, and white is positive).  
(c) Cross section showing zero crossings.  
(d)  $5 \times 5$  mask approximation to the shape of (a).

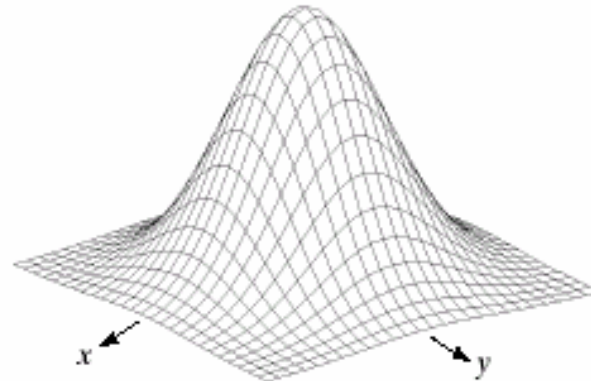
0	0	-1	0	0
0	-1	-2	-1	0
-1	-2	16	-2	-1
0	-1	-2	-1	0
0	0	-1	0	0



# Detection of Discontinuities: Gradient Operators: Example



Sobel gradient



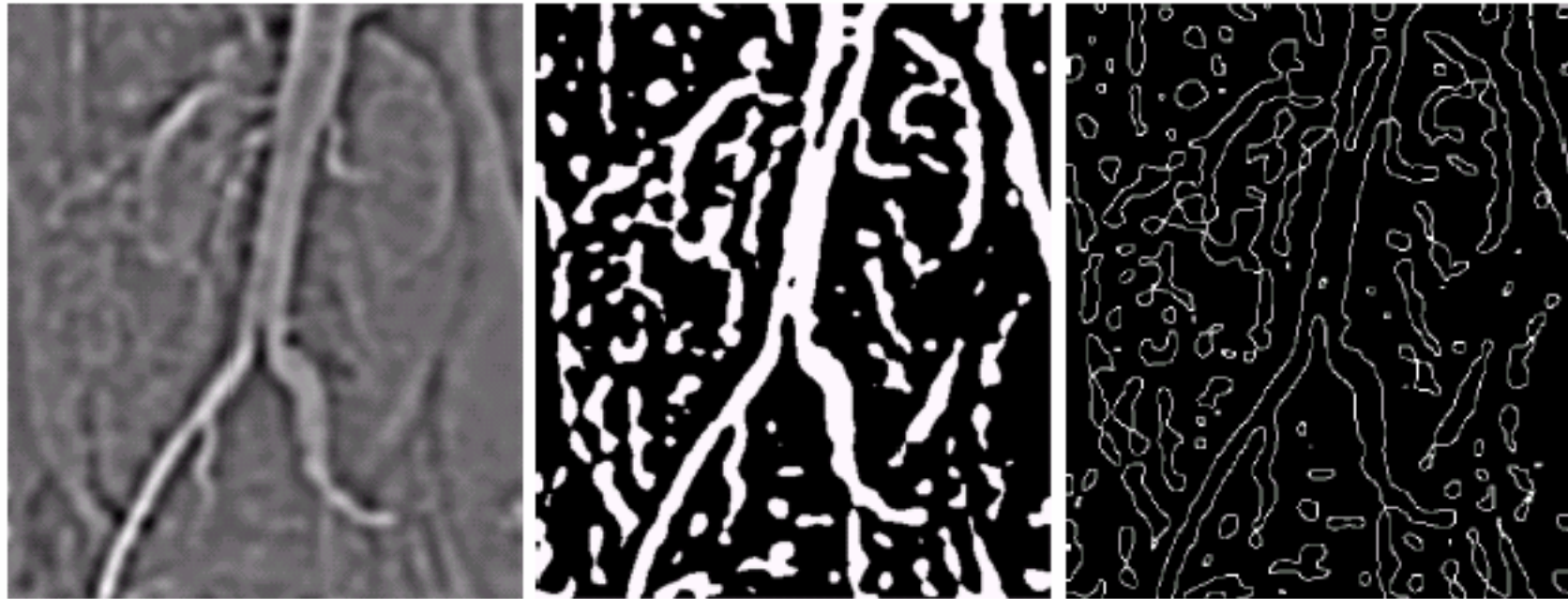
Gaussian smooth function

-1	-1	-1
-1	8	-1
-1	-1	-1

Laplacian mask



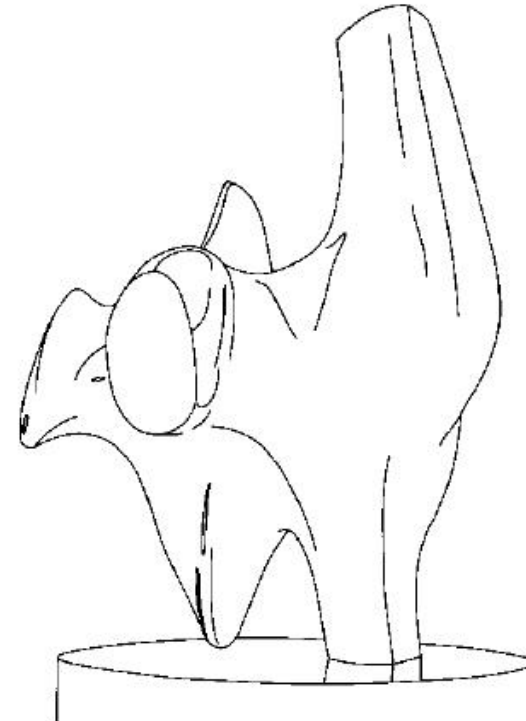
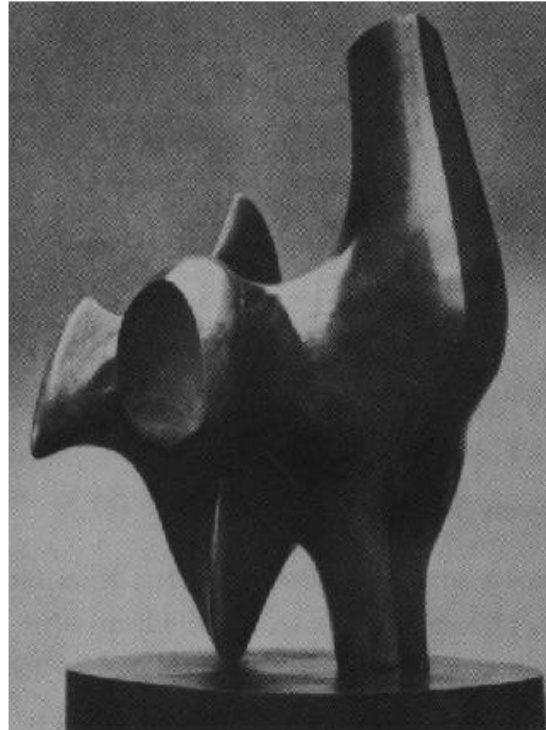
# Detection of Discontinuities Gradient Operators: Example



a b  
c d  
e f g

**FIGURE 10.15** (a) Original image. (b) Sobel gradient (shown for comparison). (c) Spatial Gaussian smoothing function. (d) Laplacian mask. (e) LoG. (f) Thresholded LoG. (g) Zero crossings. (Original image courtesy of Dr. David R. Pickens, Department of Radiology and Radiological Sciences, Vanderbilt University Medical Center.)

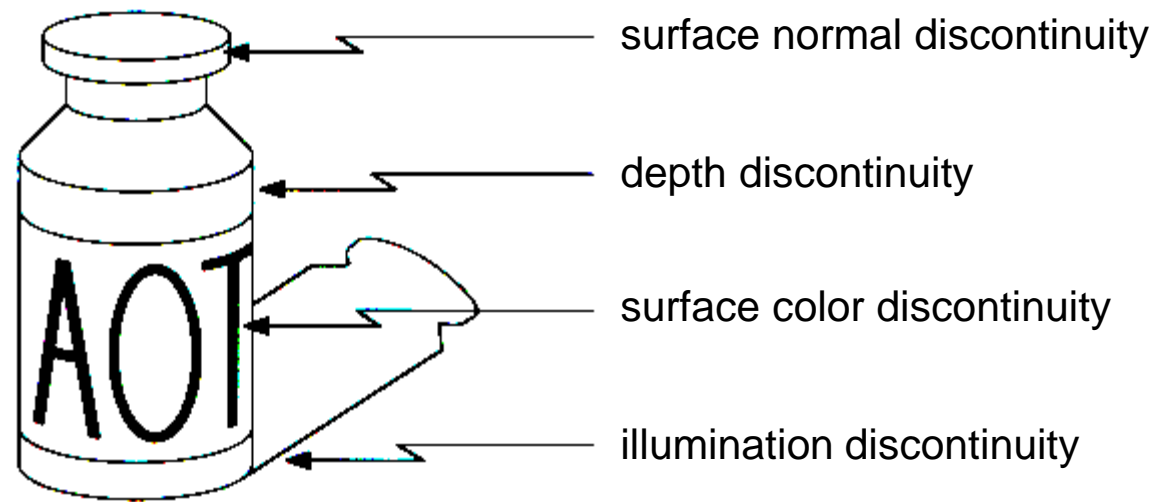
# Edge detection



- Convert a 2D image into a set of curves
  - Extracts salient features of the scene
  - More compact than pixels

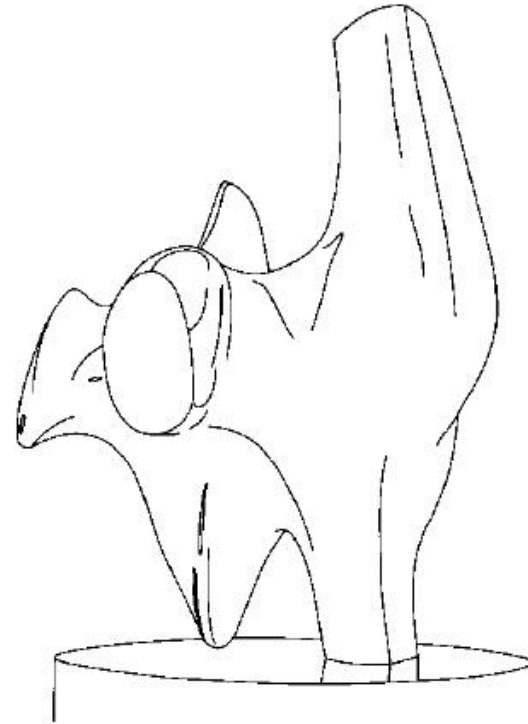
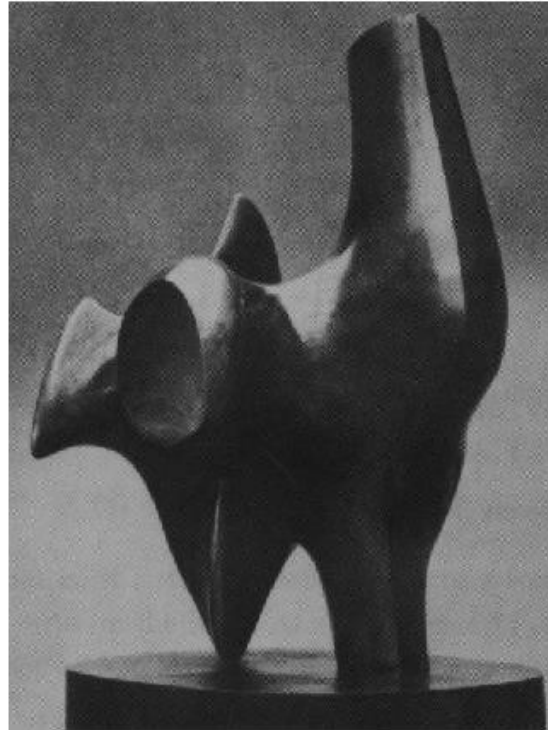


# Origin of Edges



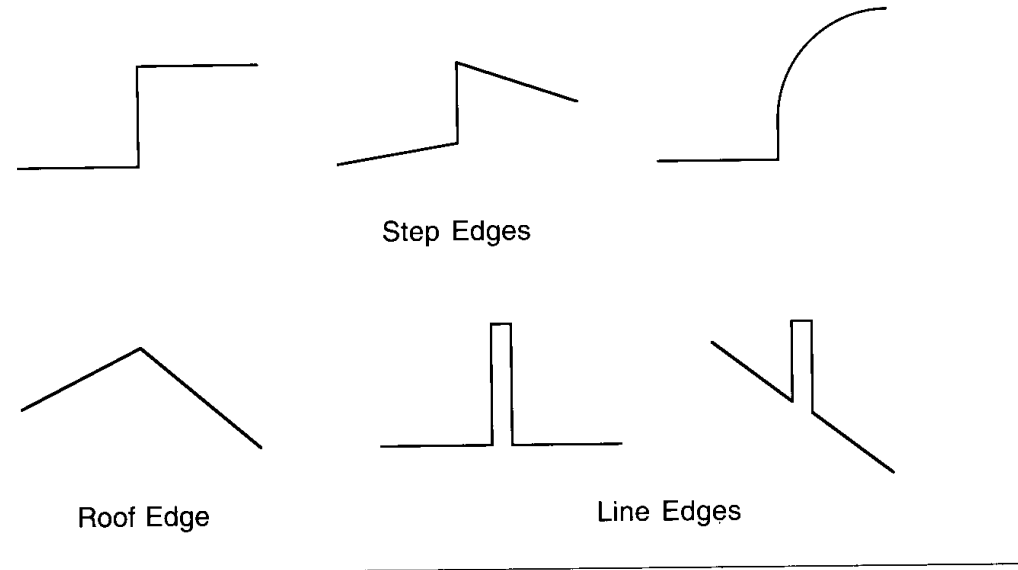
- Edges are caused by a variety of factors

# Edge detection



- How can you tell that a pixel is on an edge?

# Profiles of image intensity edges



# Edge detection

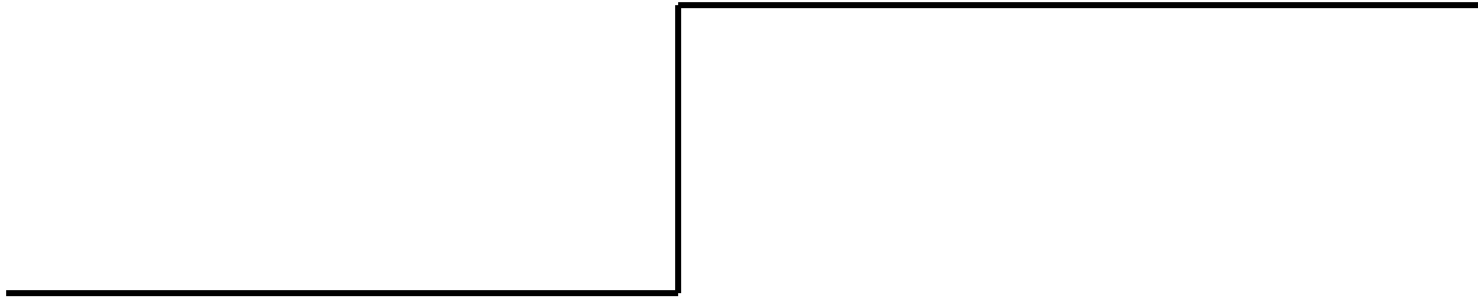
1. Detection of short linear edge segments (edgels)
2. Aggregation of edgels into extended edges
  - (maybe parametric description)

# Edgel detection

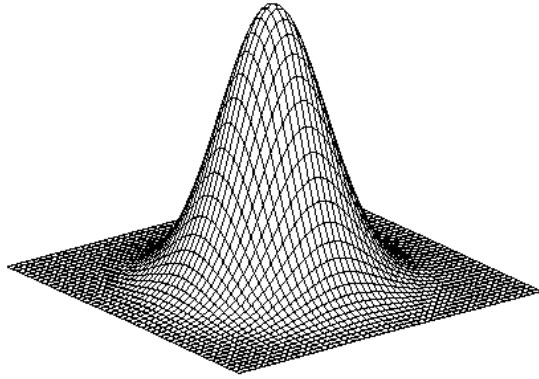
- Difference operators
- Parametric-model matchers

# Edge is Where Change Occurs

- Change is measured by derivative in 1D
- Biggest change, derivative has maximum magnitude
- Or 2<sup>nd</sup> derivative is zero.

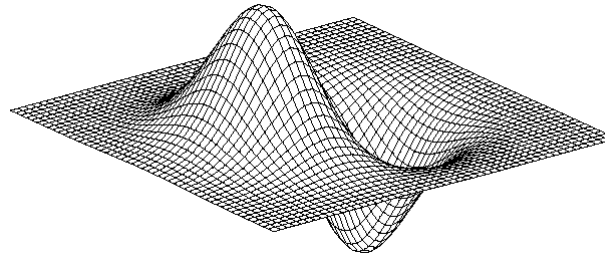


# 2D edge detection filters



Gaussian

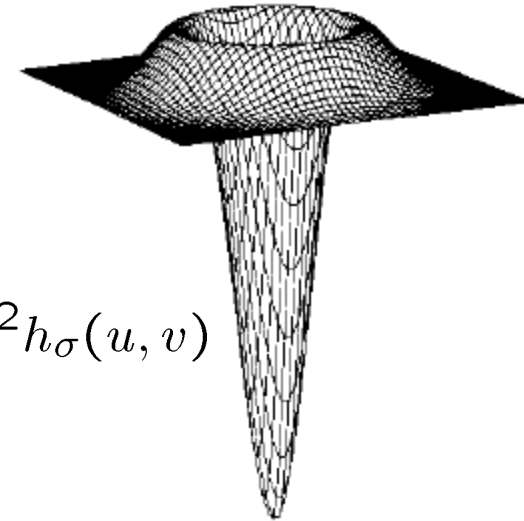
$$h_{\sigma}(u, v) = \frac{1}{2\pi\sigma^2} e^{-\frac{u^2+v^2}{2\sigma^2}}$$



derivative of Gaussian

$$\frac{\partial}{\partial x} h_{\sigma}(u, v)$$

Laplacian of Gaussian



$$\nabla^2 h_{\sigma}(u, v)$$

$\nabla^2$  is the **Laplacian** operator:

$$\nabla^2 f = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2}$$

# Optimal Edge Detection: Canny

- Assume:
  - Linear filtering
  - Additive iid Gaussian noise
- Edge detector should have:
  - Good Detection. Filter responds to edge, not noise.
  - Good Localization: detected edge near true edge.
  - Single Response: one per edge.



# Optimal Edge Detection: Canny (continued)

- Optimal Detector is approximately Derivative of Gaussian.
- Detection/Localization trade-off
  - More smoothing improves detection
  - And hurts localization.
- This is what you might guess from (detect change) + (remove noise)

# The Canny edge detector



- original image (Lena)

# The Canny edge detector



norm of the gradient

# The Canny edge detector



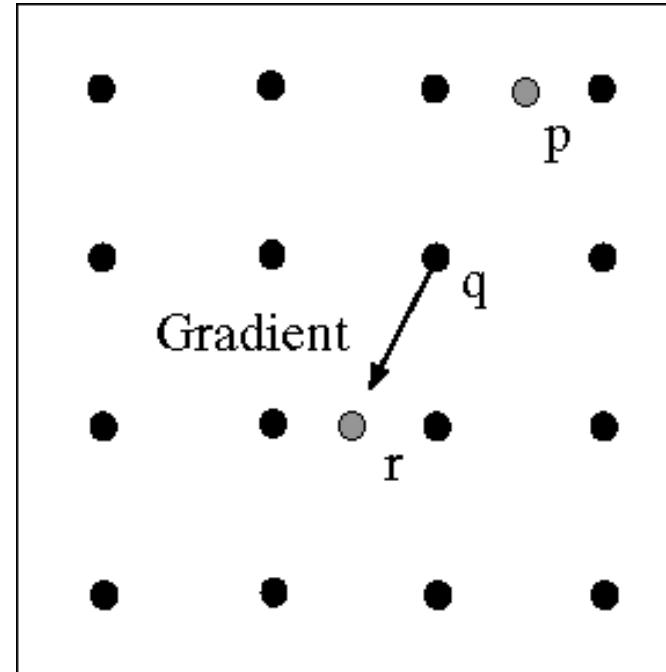
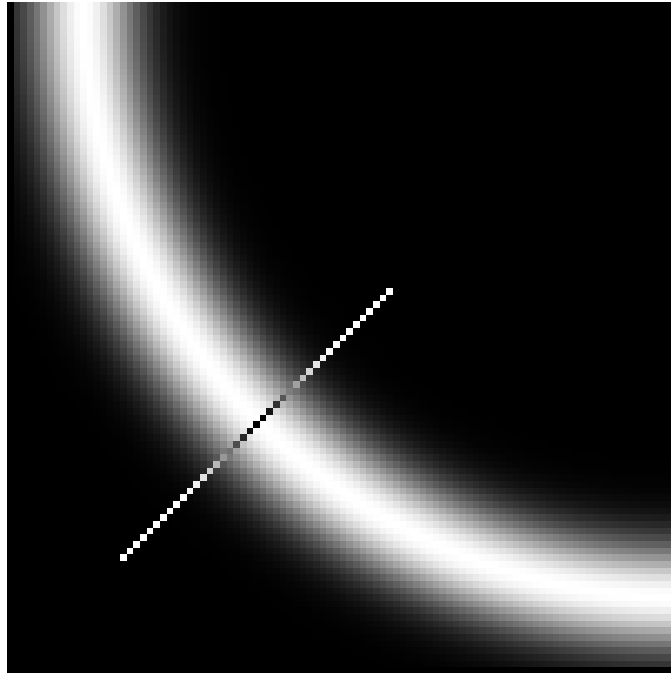
thresholding

# The Canny edge detector



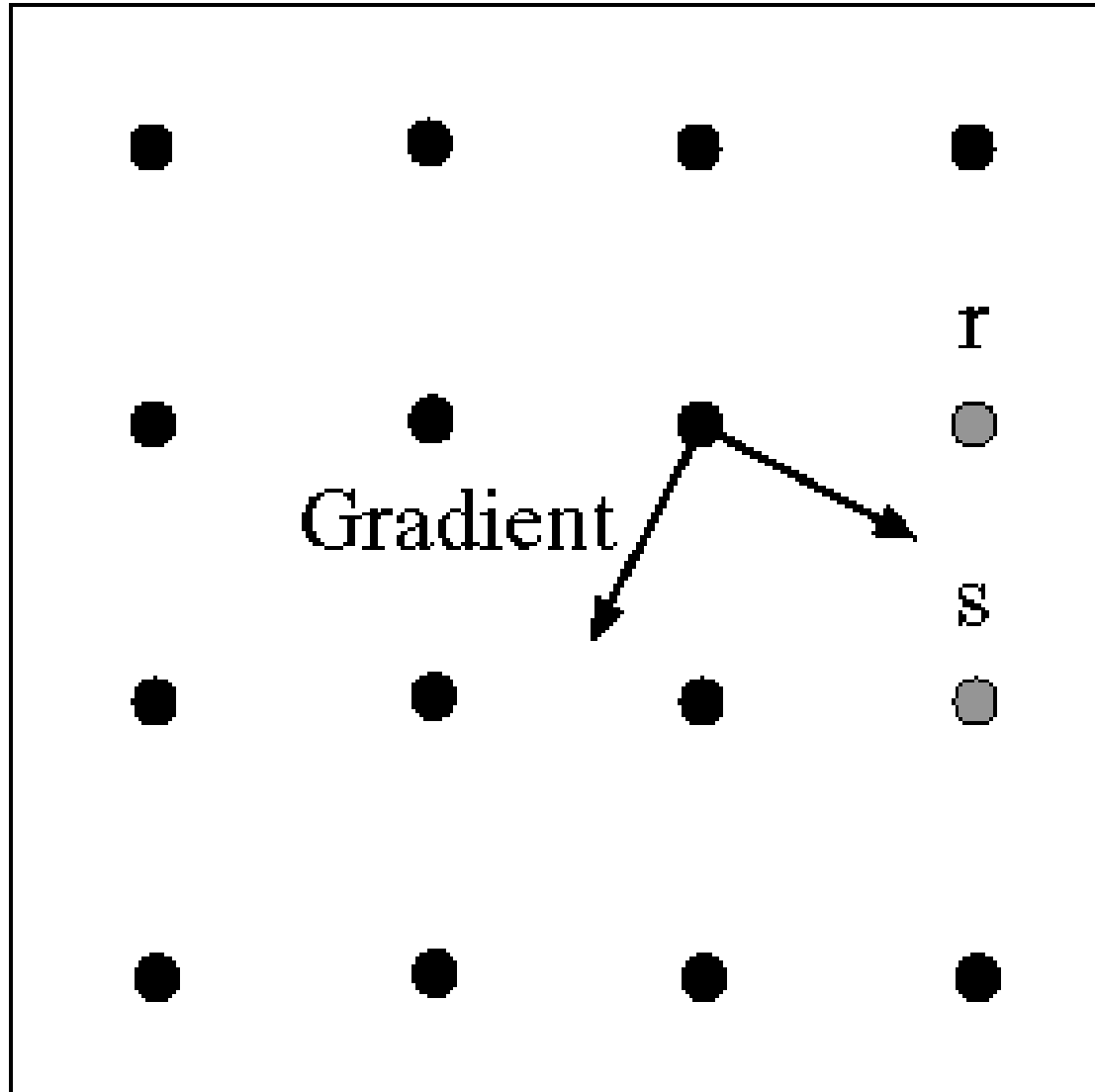
thinning  
(non-maximum suppression)

# Non-maximum suppression



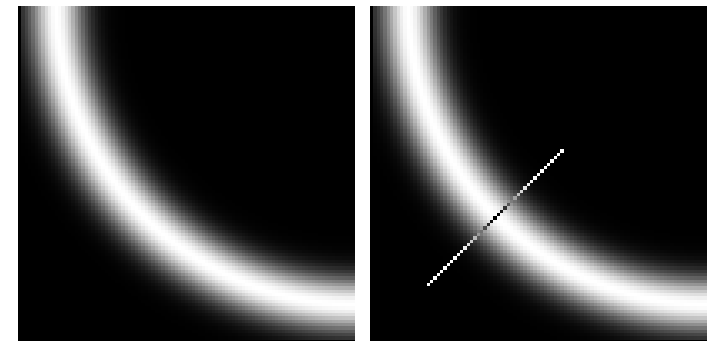
- Check if pixel is local maximum along gradient direction
  - requires checking interpolated pixels  $p$  and  $r$

# Non-maximum suppression



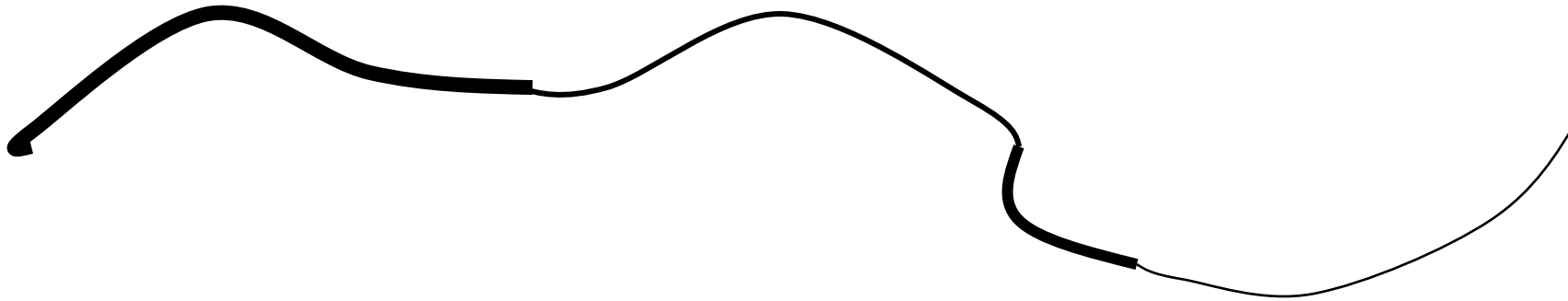
Predicting  
the next  
edge point

Assume the marked point  
is an edge point. Then we  
construct the tangent to the  
edge curve (which is  
normal to the gradient at  
that point) and use this to  
predict the next points  
(here either r or s).



# Hysteresis

- Check that maximum value of gradient value is sufficiently large
  - drop-outs? use **hysteresis**
    - use a high threshold to start edge curves and a low threshold to continue them.





# Effect of $\sigma$ (Gaussian kernel size)



original



Canny with  $\sigma = 1$



Canny with  $\sigma = 2$

The choice of  $\sigma$  depends on desired behavior

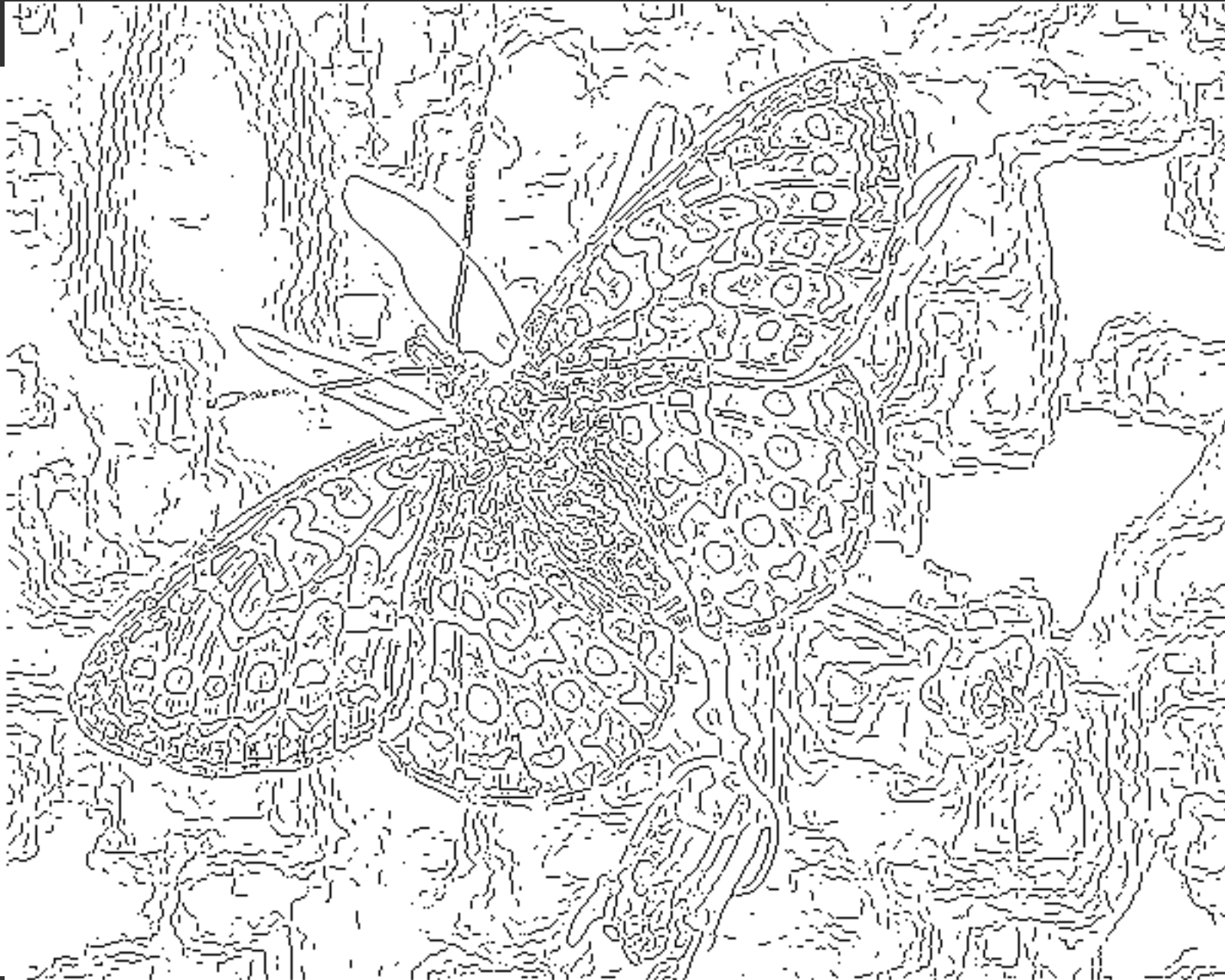
- large  $\sigma$  detects large scale edges
- small  $\sigma$  detects fine features

# Scale



- Smoothing
- Eliminates noise edges.
- Makes edges smoother.
- Removes fine detail.





fine scale  
high  
threshold



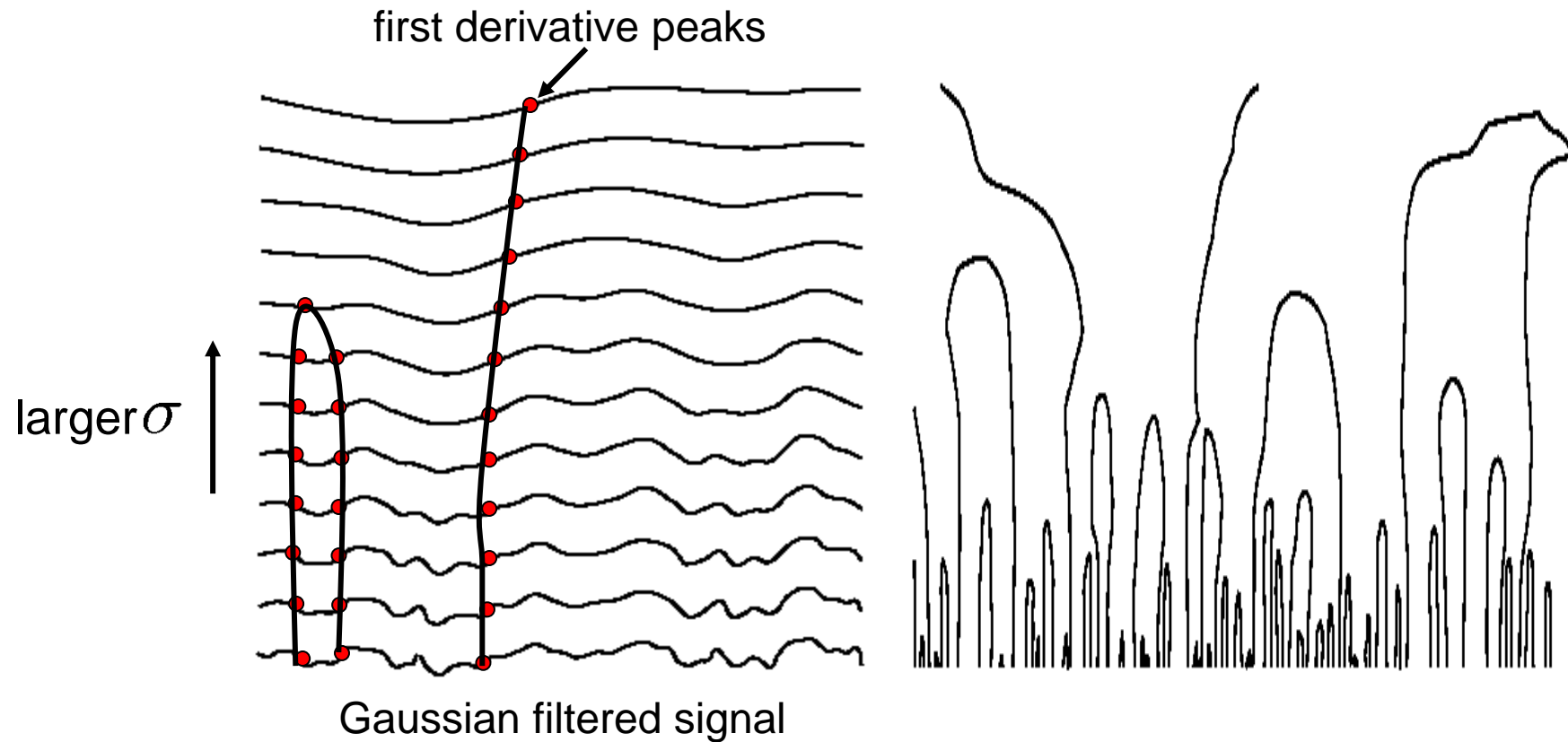
coarse  
scale,  
high  
threshold





coarse  
scale  
low  
threshold

# Scale space (Witkin 83)



- Properties of scale space (w/ Gaussian smoothing)
  - edge position may shift with increasing scale ( $\sigma$ )
  - two edges may merge with increasing scale
  - an edge may **not** split into two with increasing scale

# Edge detection by subtraction



original



# Edge detection by subtraction



smoothed (5x5 Gaussian)

# Edge detection by subtraction

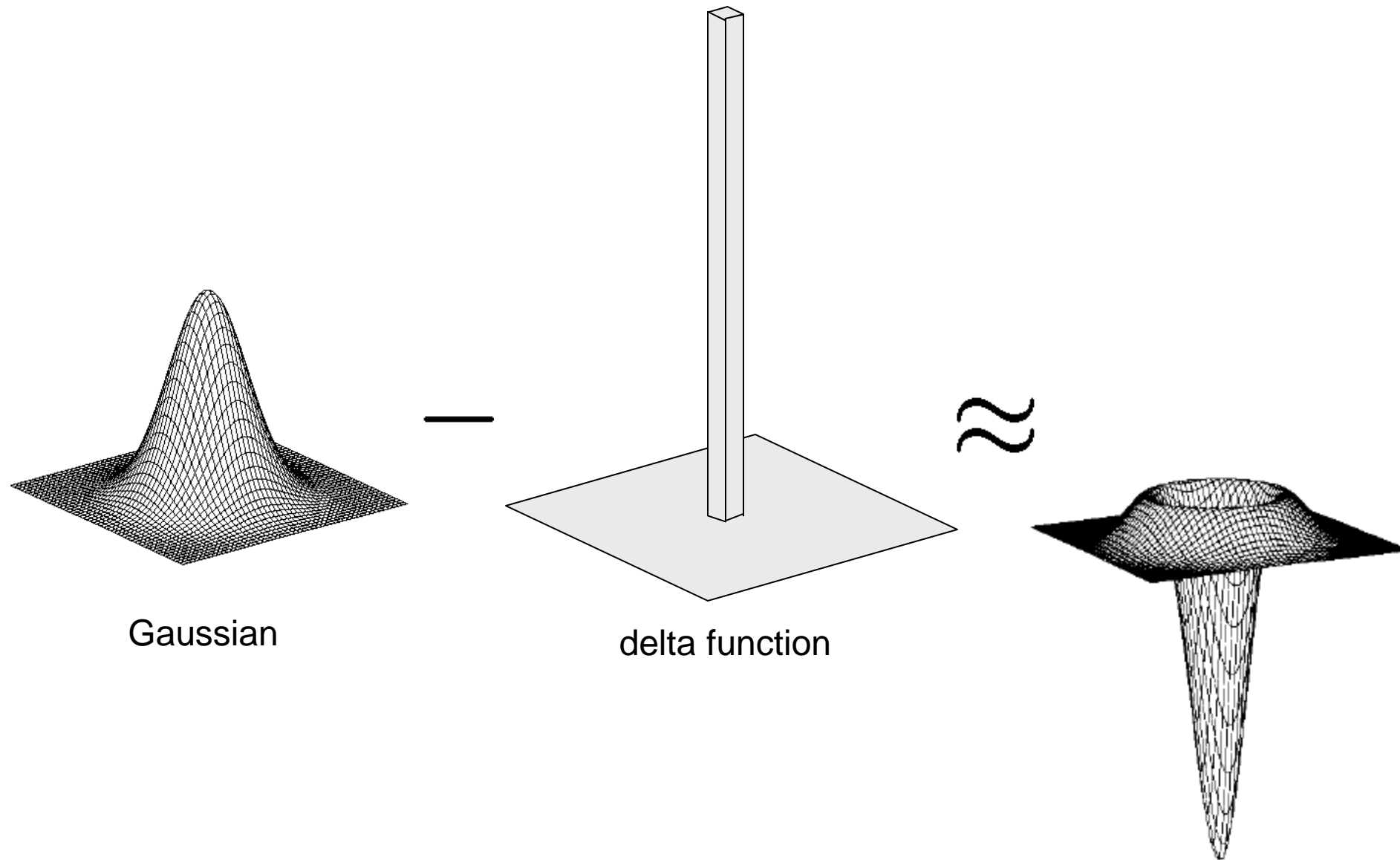


smoothed – original  
(scaled by 4, offset +128)

Why does  
this work?

filter demo

# Gaussian - image filter



# An edge is not a line...



How can we detect *lines* ?

# Edge Linking and Boundary Detection: Local Processing

- Two properties of edge points are useful for edge linking:
  - the strength (or magnitude) of the detected edge points
  - their directions (determined from gradient directions)
- This is usually done in local neighborhoods.
- Adjacent edge points with similar magnitude and direction are linked.
- For example, an edge pixel with coordinates  $(x_0, y_0)$  in a predefined neighborhood of  $(x, y)$  is similar to the pixel at  $(x, y)$  if

$$|\nabla f(x, y) - \nabla f(x_0, y_0)| \leq E, \quad E: \text{a nonnegative threshold}$$

$$|\alpha(x, y) - \alpha(x_0, y_0)| < A, \quad A: \text{a nonnegative angle threshold}$$



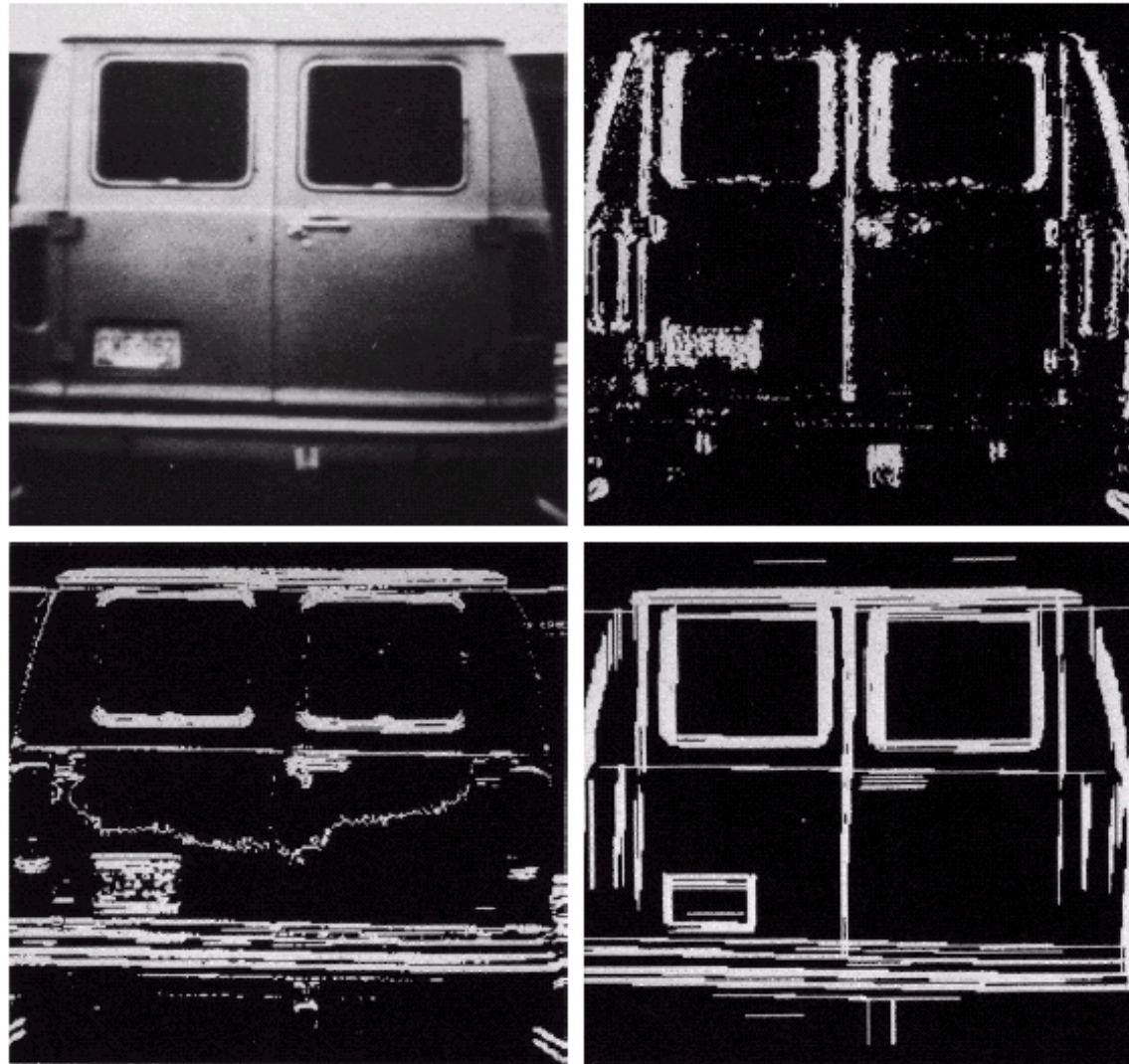
# Edge Linking and Boundary Detection: Local Processing: Example

a b  
c d

**FIGURE 10.16**

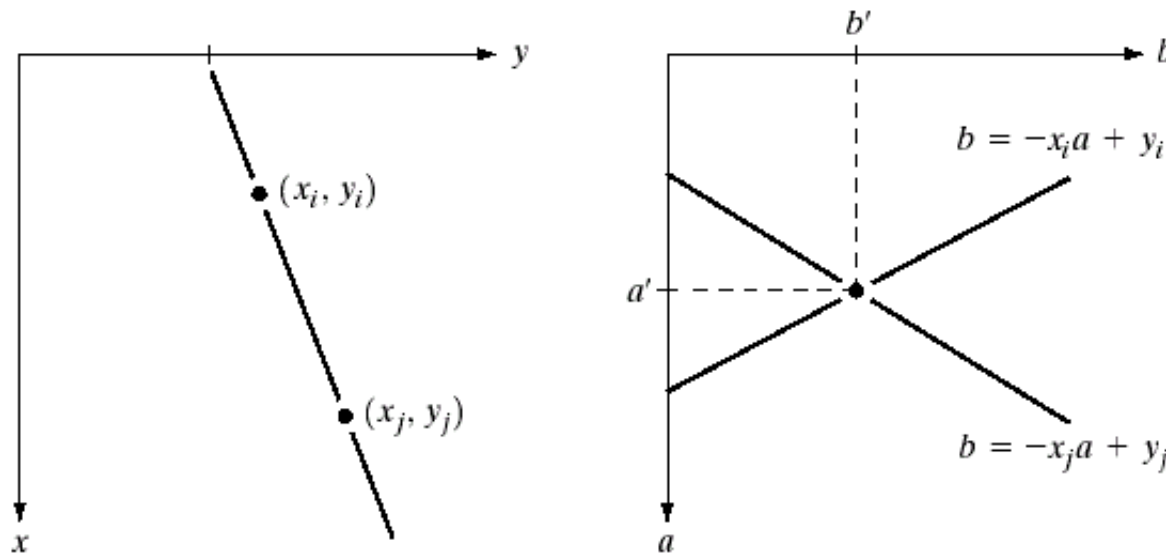
(a) Input image.  
(b)  $G_y$  component  
of the gradient.  
(c)  $G_x$  component  
of the gradient.  
(d) Result of edge  
linking. (Courtesy  
of Perceptics  
Corporation.)

In this example,  
we can find the  
license plate  
candidate after  
edge linking  
process.



# Edge Linking and Boundary Detection : Hough Transform

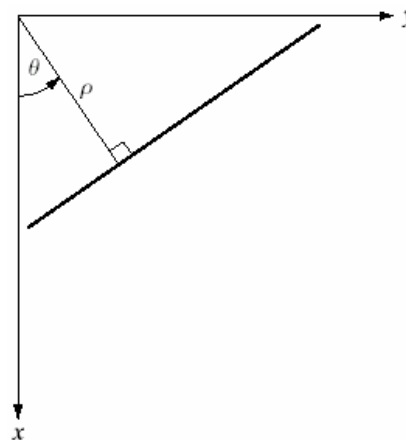
- Hough transform: a way of finding edge points in an image that lie along a straight line.  $y_i = ax_i + b$
- Example: xy-plane v.s. ab-plane (parameter space)



**FIGURE 10.17**  
(a)  $xy$ -plane.  
(b) Parameter space.

# Edge Linking and Boundary Detection : Hough Transform

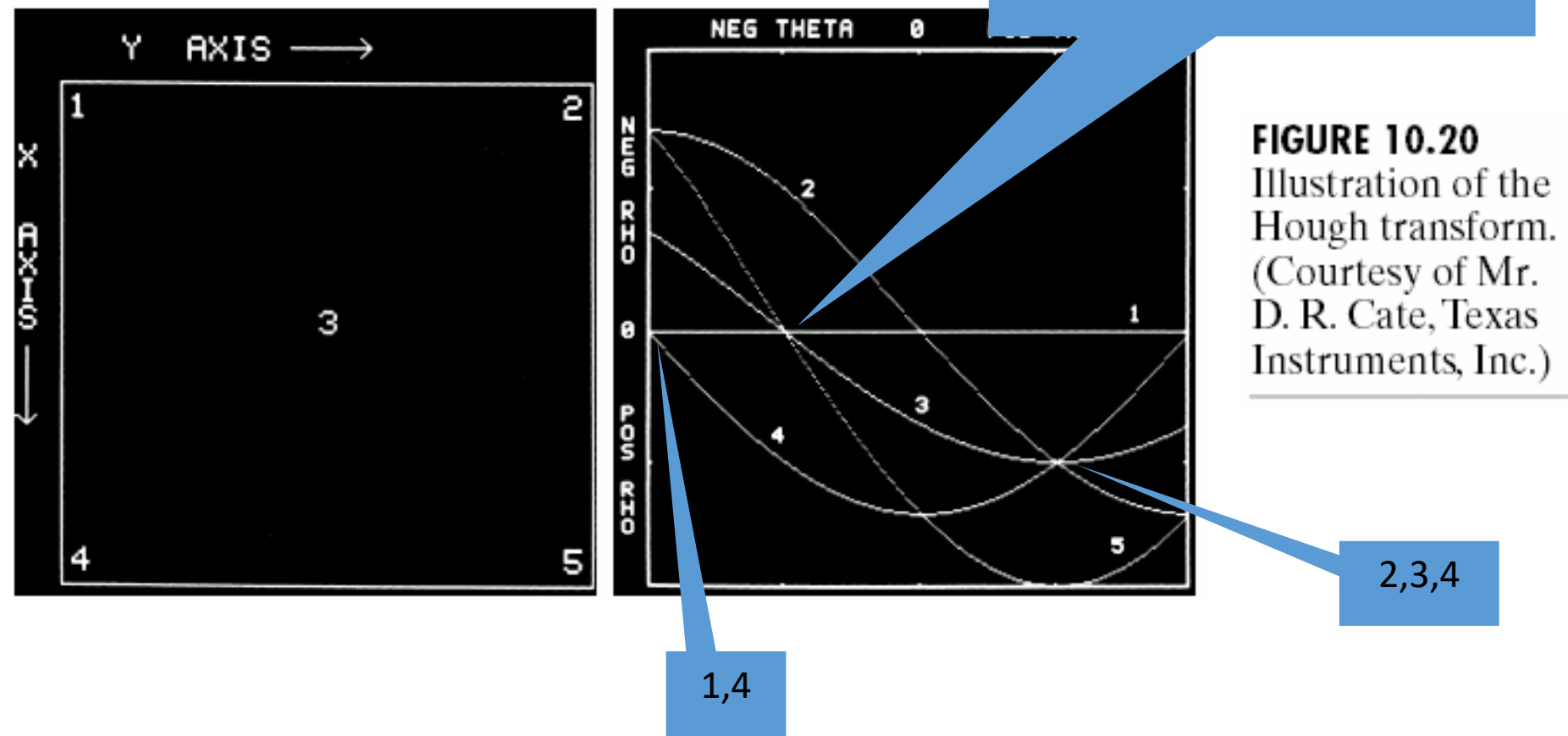
- The Hough transform consists of finding all pairs of values of  $\theta$  and  $\rho$  which satisfy the equations that pass through  $(x,y)$ .
- These are accumulated in what is basically a 2-dimensional histogram.
- When plotted these pairs of  $\theta$  and  $\rho$  will look like a sine wave. The process is repeated for all appropriate  $(x,y)$  locations.



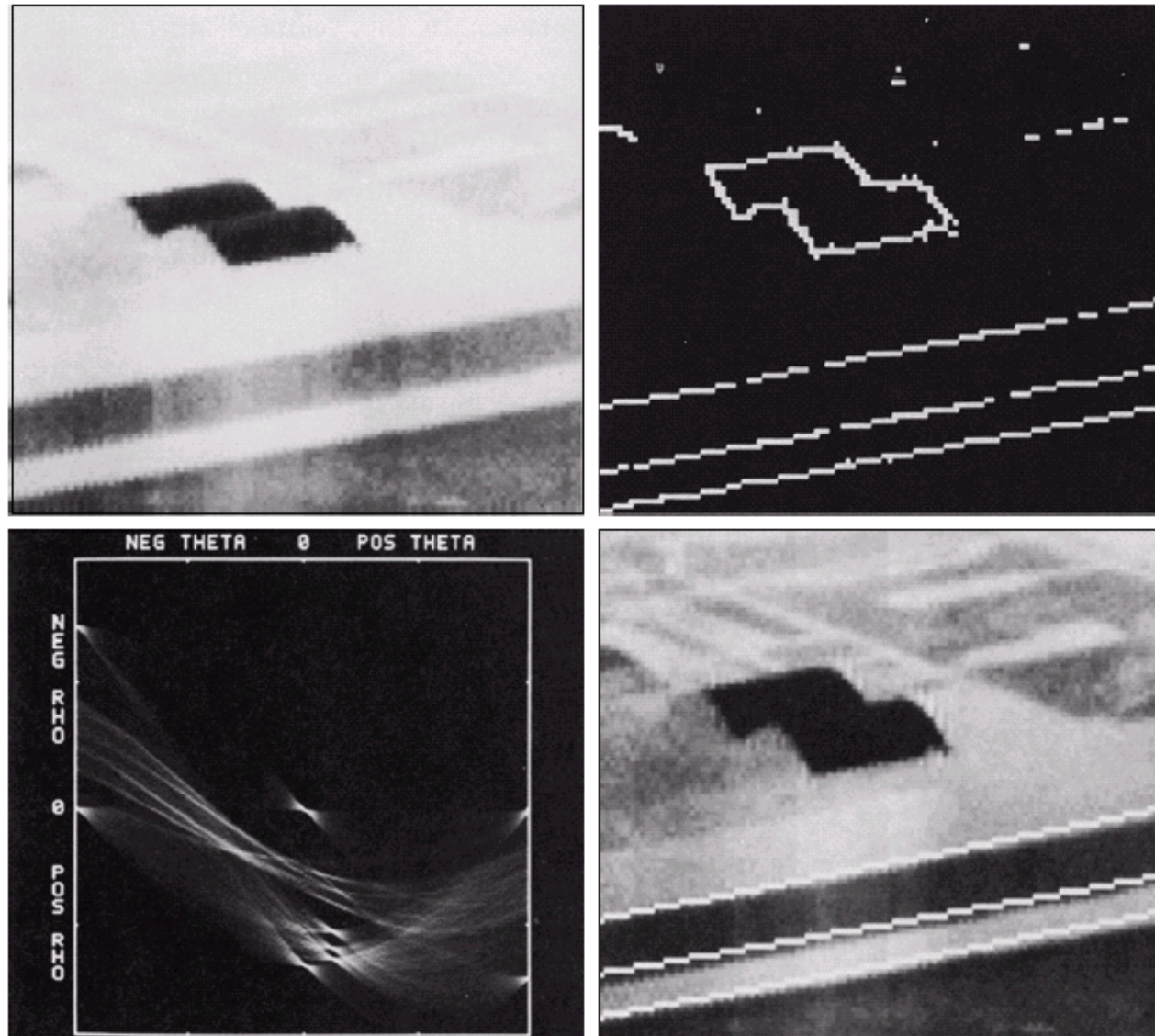
$$x \cos \theta + y \sin \theta = \rho$$



# Edge Linking and Boundary Detection: Hough Transform Example



# Edge Linking and Boundary Detection: Hough Transform Example



a	b
c	d

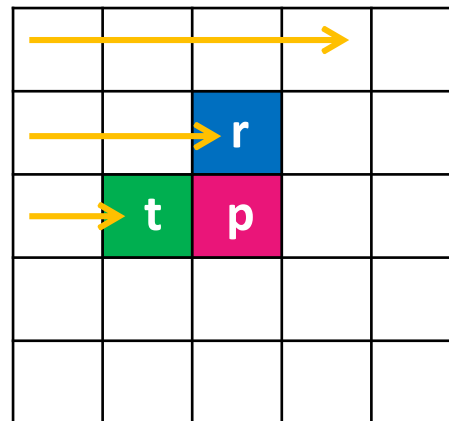
**FIGURE 10.21**  
(a) Infrared image.  
(b) Thresholded gradient image.  
(c) Hough transform.  
(d) Linked pixels.  
(Courtesy of Mr. D. R. Cate, Texas Instruments, Inc.)

# Connected Component Labeling

- Ability to assign different labels to various disjoint component of an image is called connected component labeling.
- This labeling is a fundamental step in
  - a) Shape
  - b) Area
  - c) Boundary

# Basic Scanning Method

- Scan the image from left to right and top to bottom.
- Assume 4-adjacency.
- Let  $p$  be a pixel at any step in the scanning process.
- Before  $p$  the pixel  $r$  and  $t$  are scanned.



# Labeling Algorithm

- This algorithm makes two passes over the image:
  - The first pass to assign temporary labels and record equivalence classes.
  - The second pass to replace each temporary label by the smallest label of its equivalence class.

# Steps in First Pass

- Conditions to check:
  - Does the pixel to the left (West) have the same value as the current pixel?
    - Yes – We are in the same region. Assign the same label to the current pixel
    - No – Check next condition
  - Do both pixels to the North and West of the current pixel have the same value as the current pixel but not the same label?
    - Yes –Assign the current pixel the minimum of the North and West labels, and record their equivalence relationship
    - No – Check next condition

# Steps in First Pass..

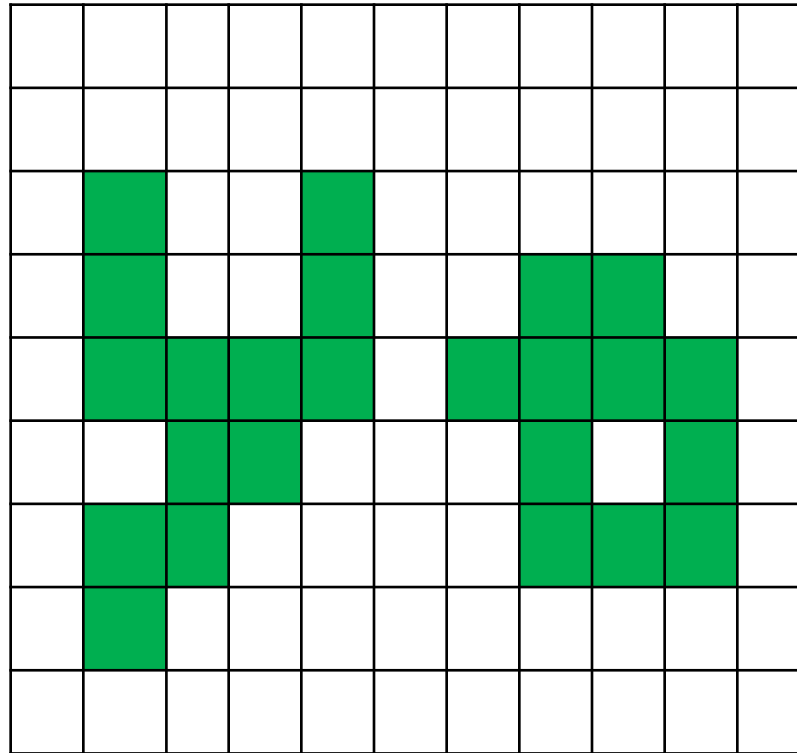
- Does the pixel to the left (West) have a different value and the one to the North the same value as the current pixel?
  - Yes – Assign the label of the North pixel to the current pixel
  - No – Check next condition
- Do the pixel's North and West neighbors have different pixel values than current pixel?
  - Yes – Create a new label id and assign it to the current pixel

# Steps in Second Pass

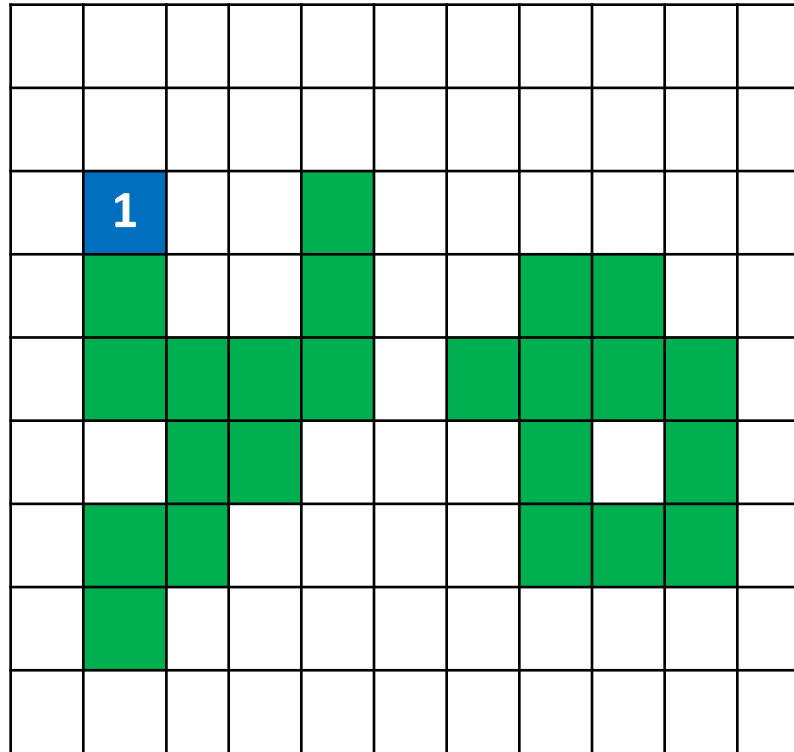
- In the First pass we record some equivalence relationships.
- In Second Pass:
  - Process Equivalence pairs to form equivalent classes.
  - Re-label the element with the label assigned to its equivalent classes.



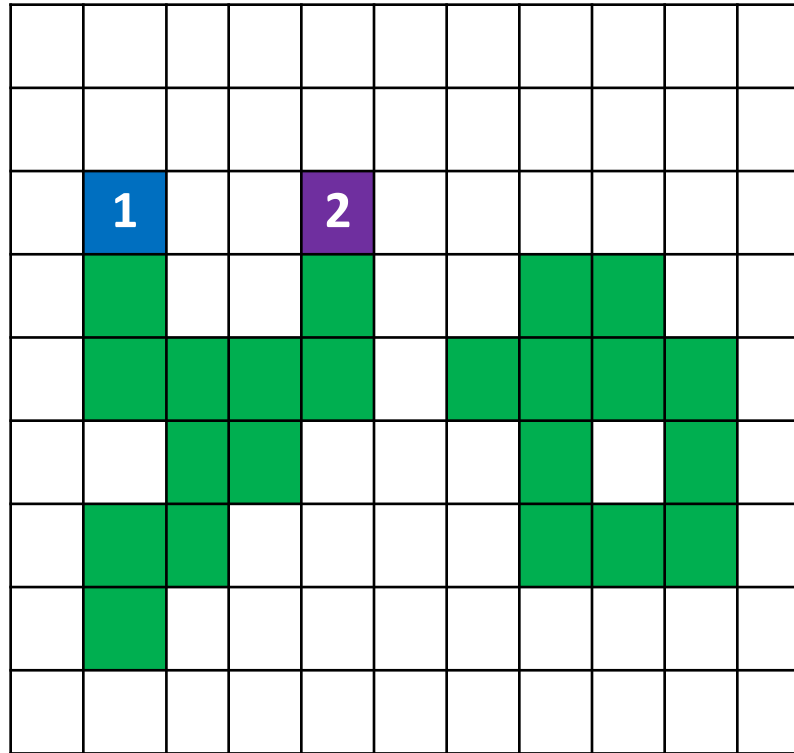
# Connected Component Labeling (example)



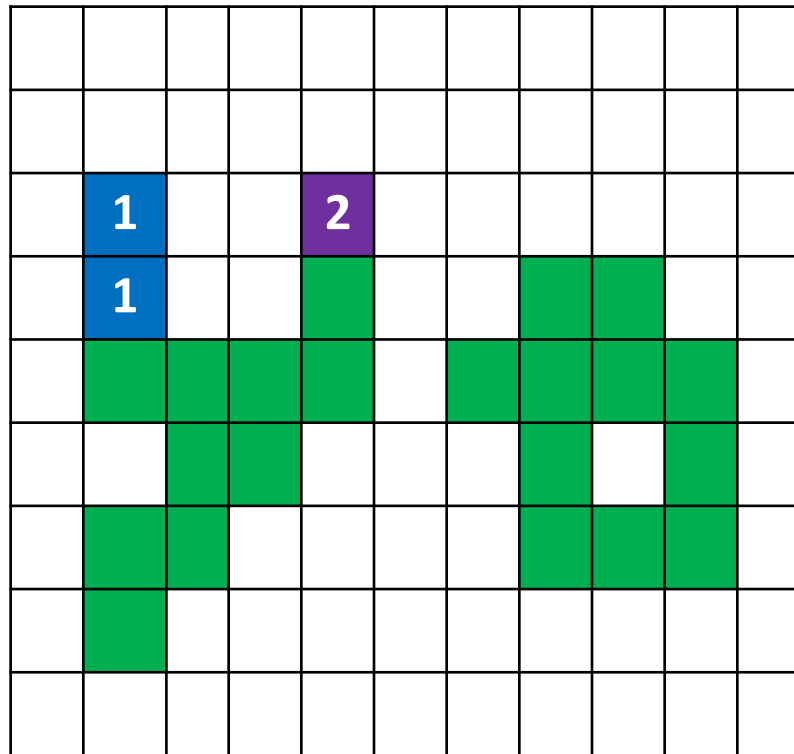
# Connected Component Labeling (example)



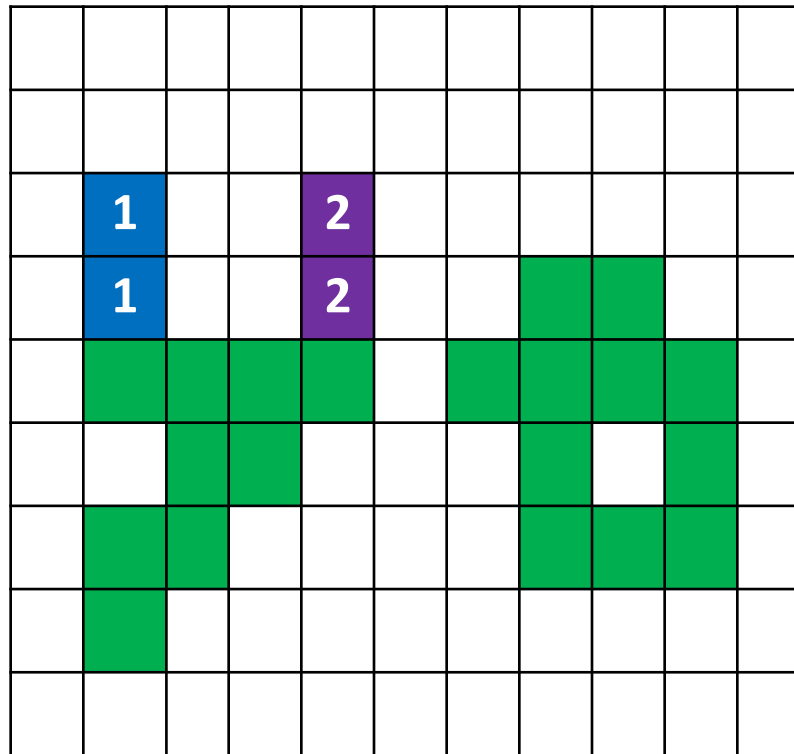
# Connected Component Labeling (example)



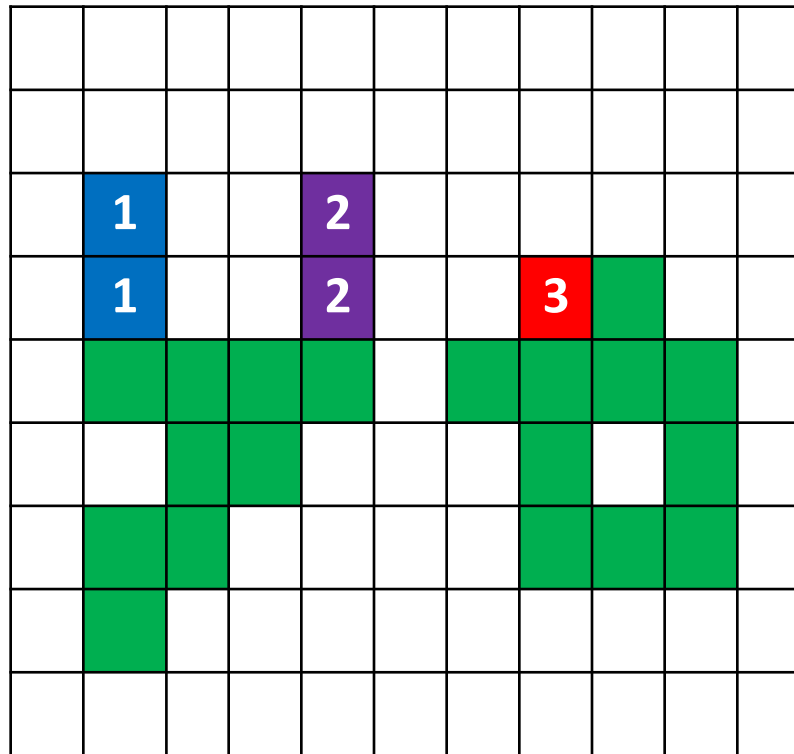
# Connected Component Labeling (example)



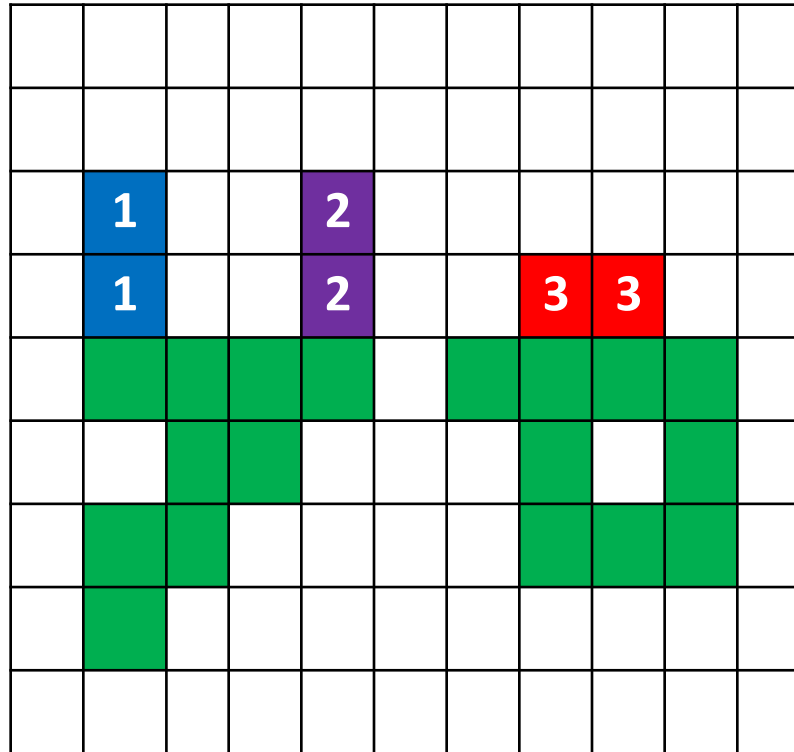
# Connected Component Labeling (example)



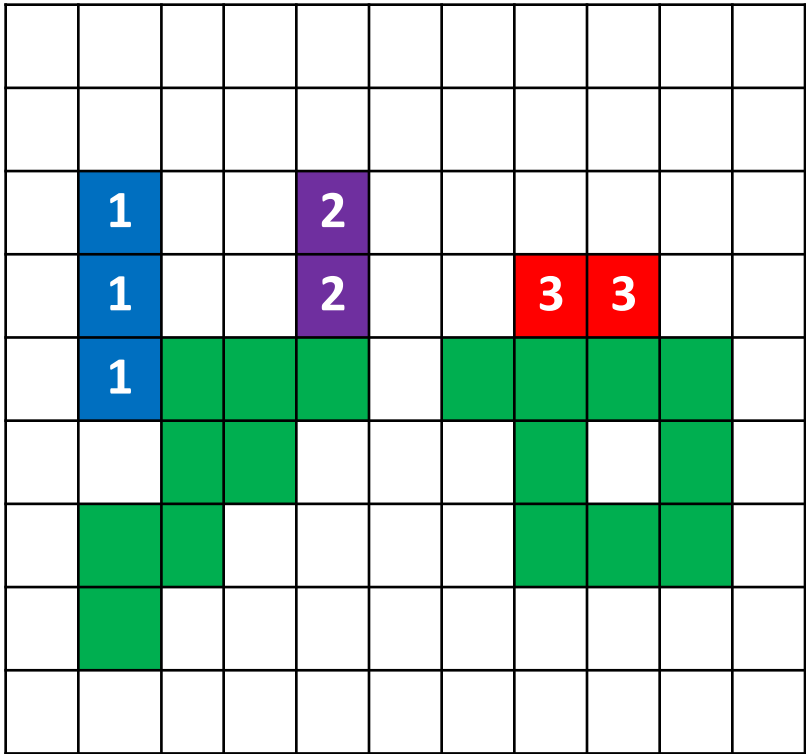
# Connected Component Labeling (example)



# Connected Component Labeling (example)

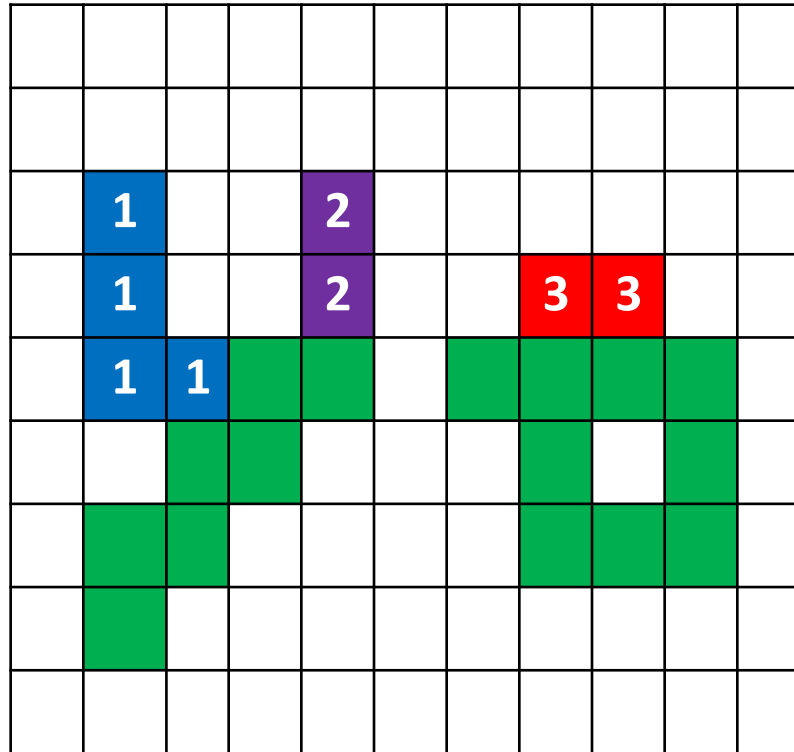


# Connected Component Labeling (example)

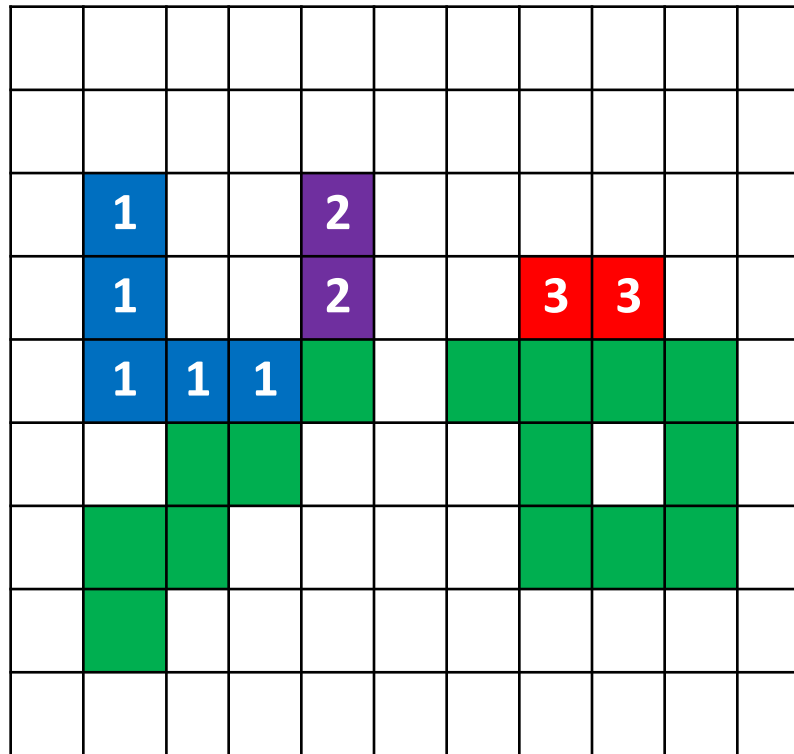




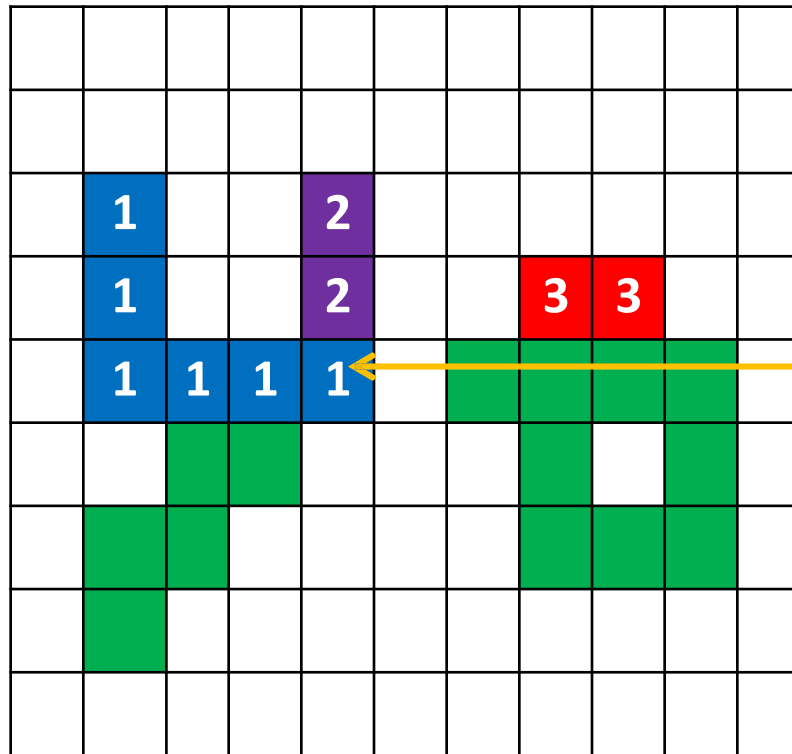
# Connected Component Labeling (example)



# Connected Component Labeling (example)

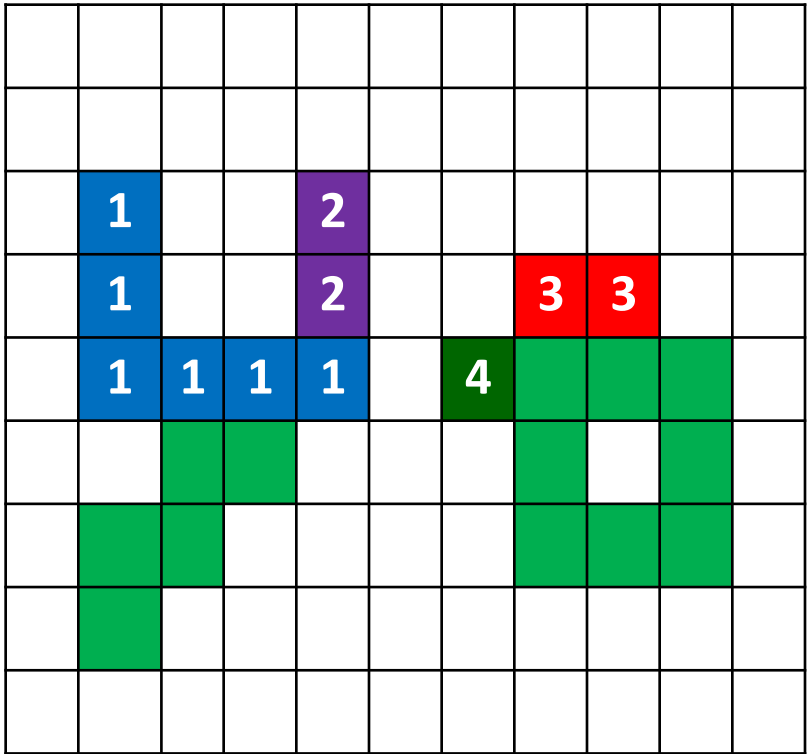


# Connected Component Labeling (example)

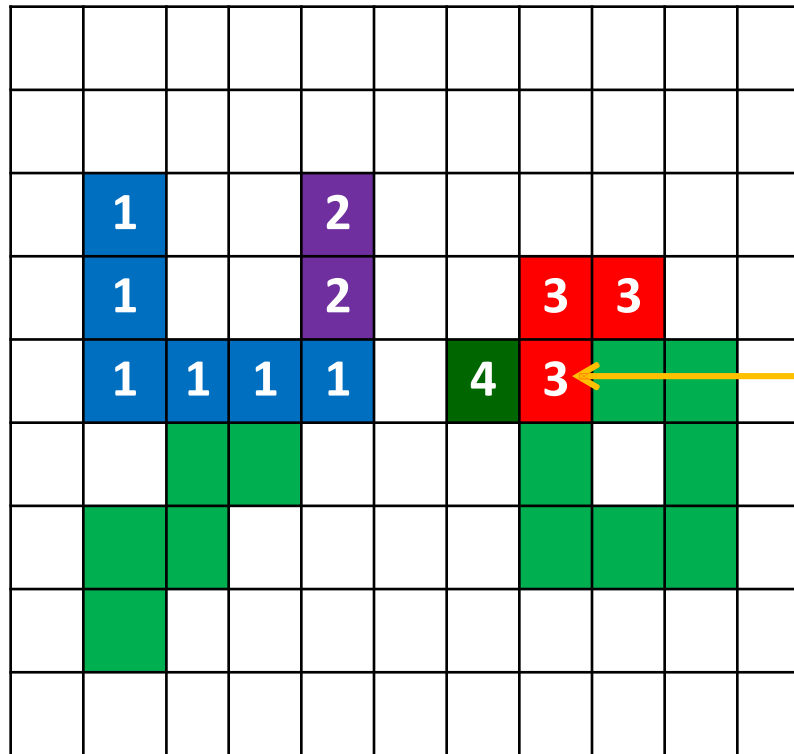


**(1,2) equivalent  
relation**

# Connected Component Labeling (example)

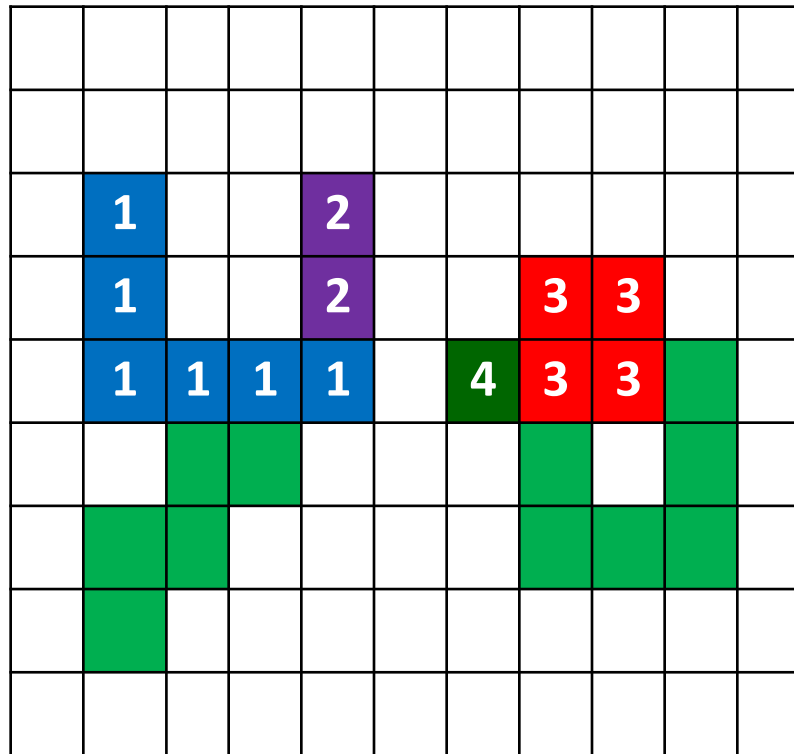


# Connected Component Labeling (example)

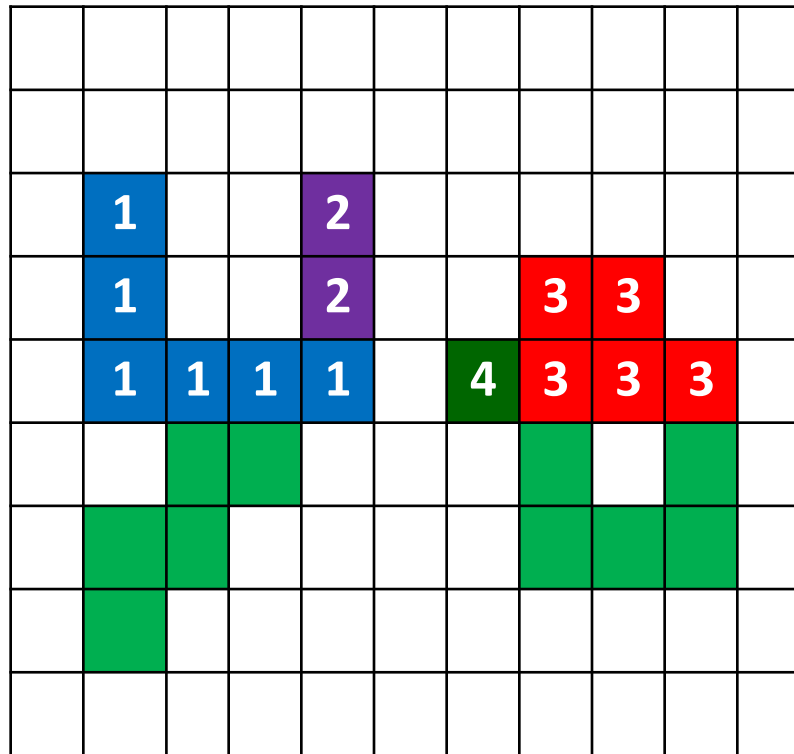


**(3,4) equivalent  
relation**

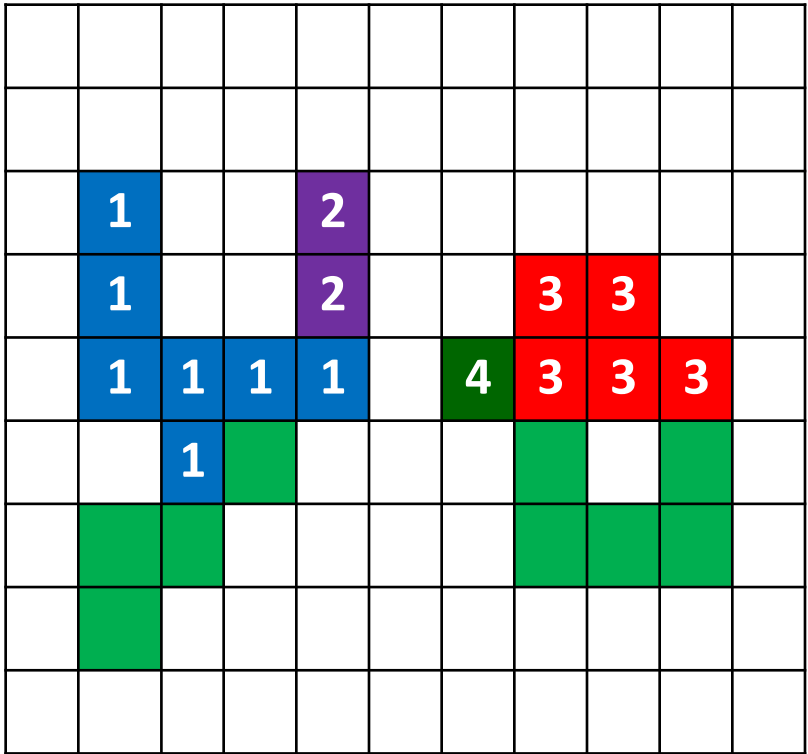
# Connected Component Labeling (example)



# Connected Component Labeling (example)

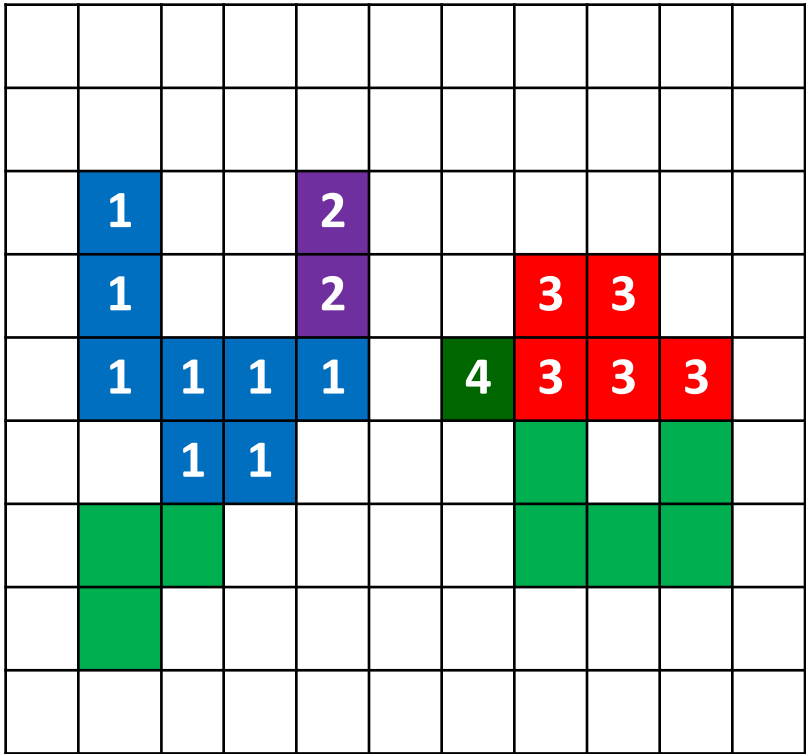


# Connected Component Labeling (example)

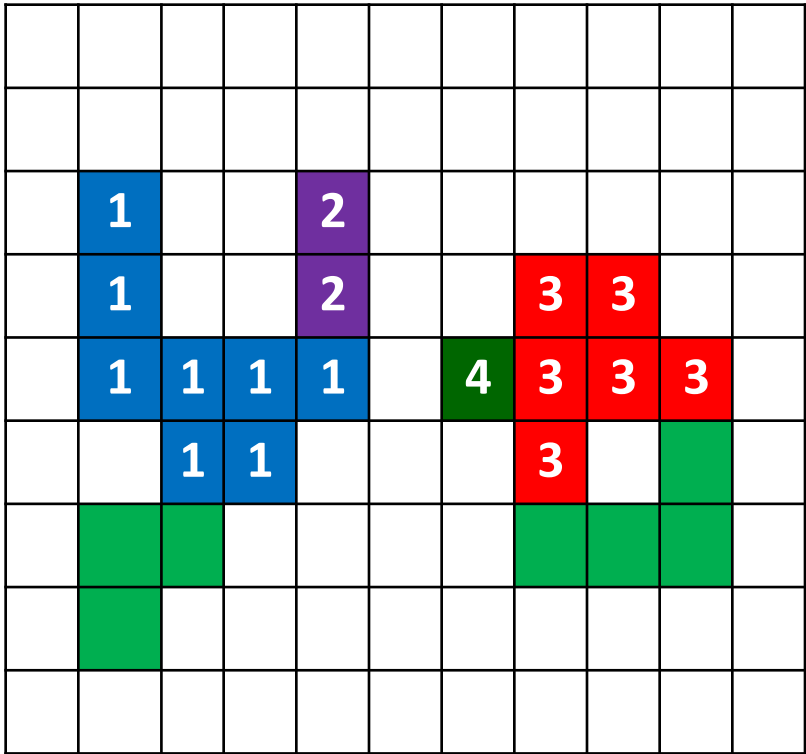




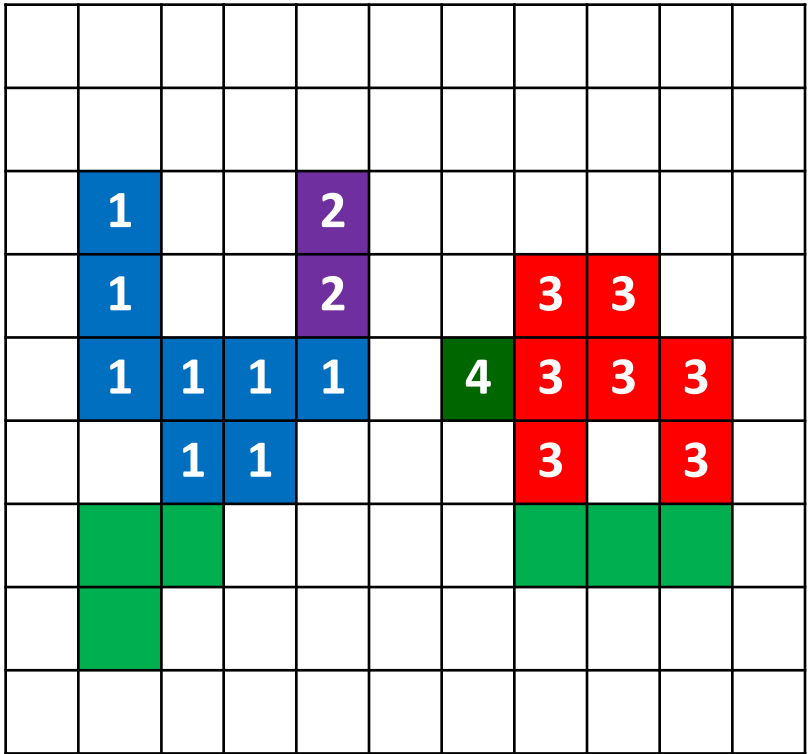
# Connected Component Labeling (example)



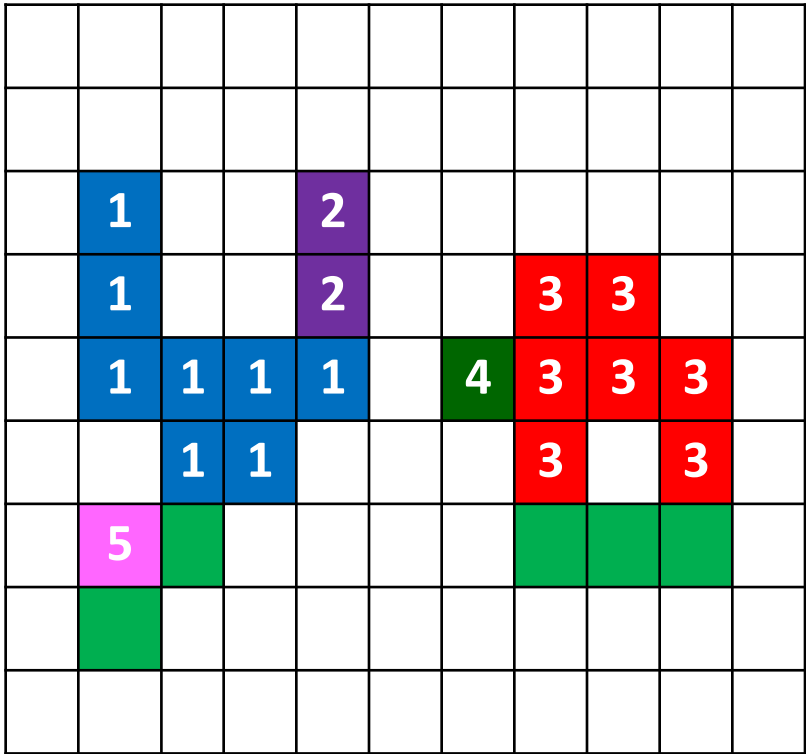
# Connected Component Labeling (example)



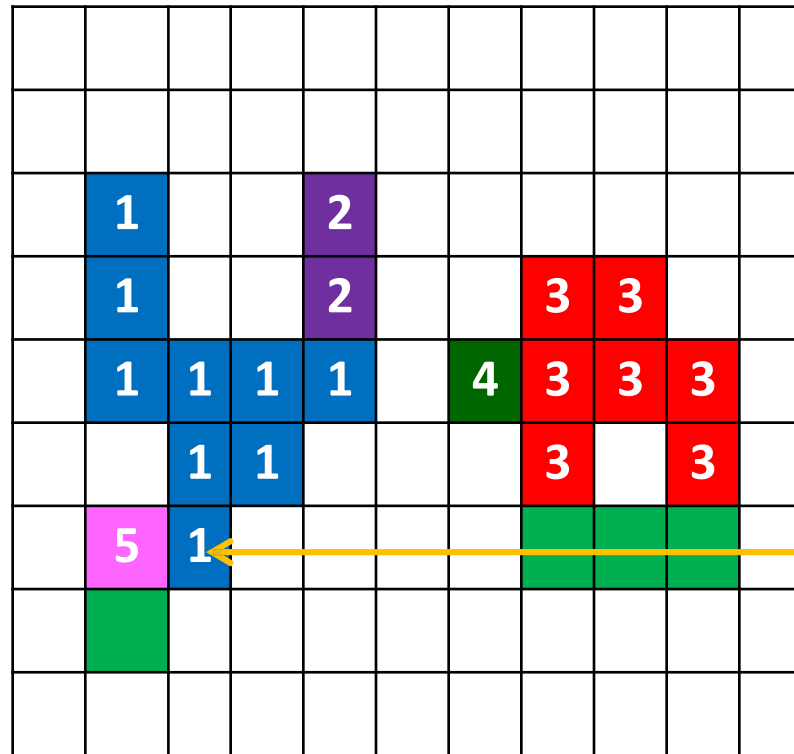
# Connected Component Labeling (example)



# Connected Component Labeling (example)

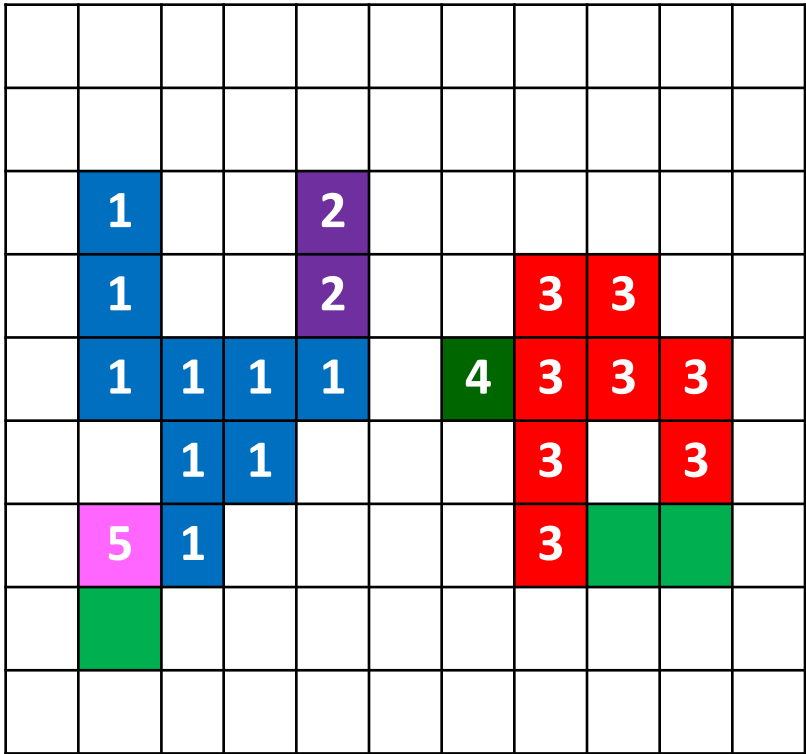


# Connected Component Labeling (example)

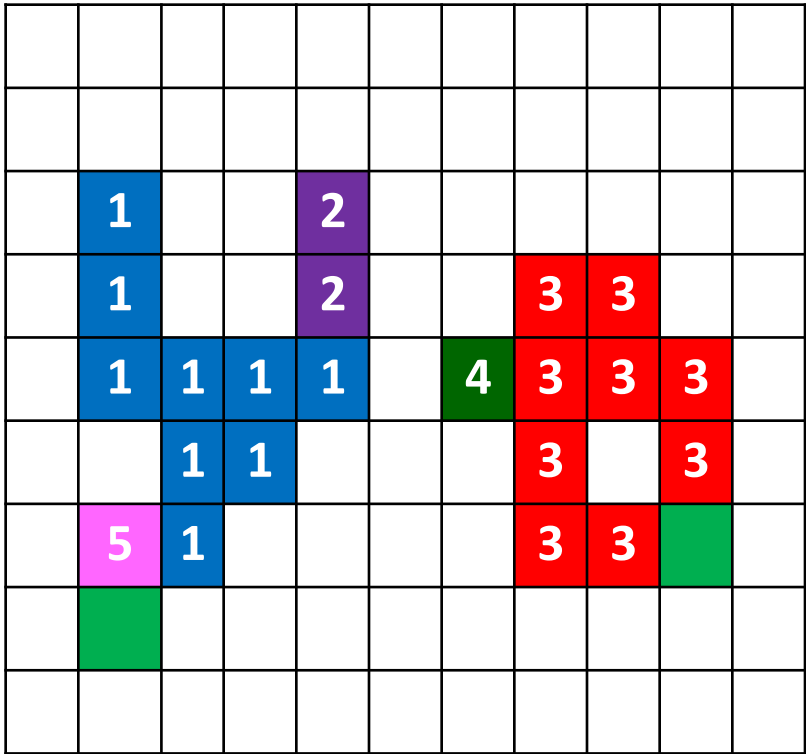


(1,5) equivalent relation

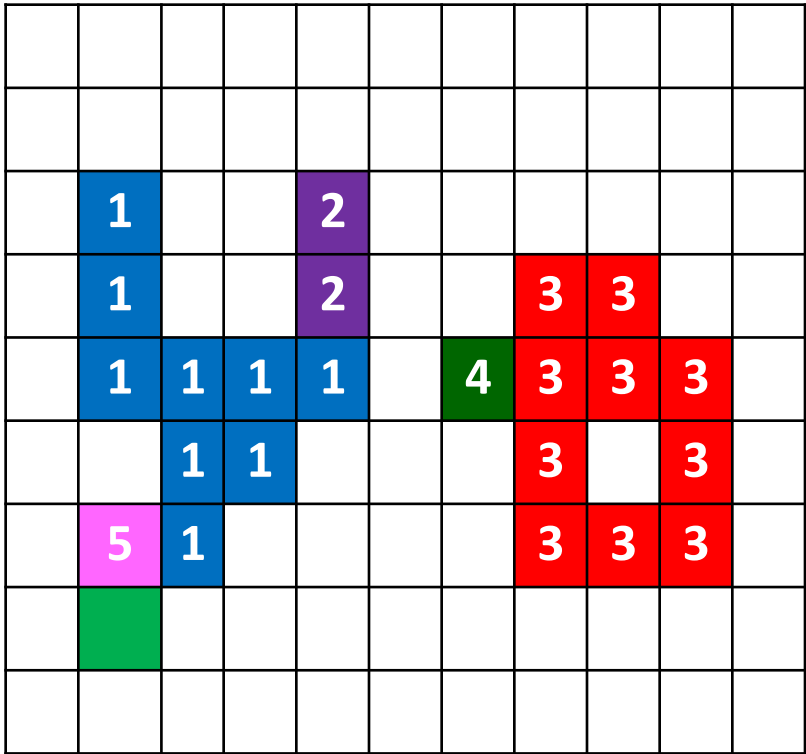
# Connected Component Labeling (example)



# Connected Component Labeling (example)

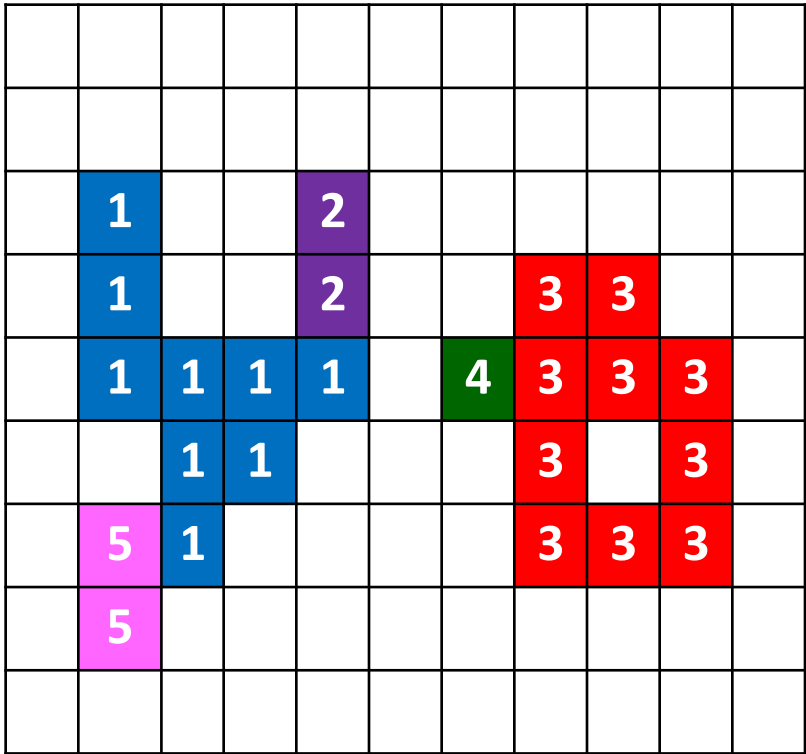


# Connected Component Labeling (example)

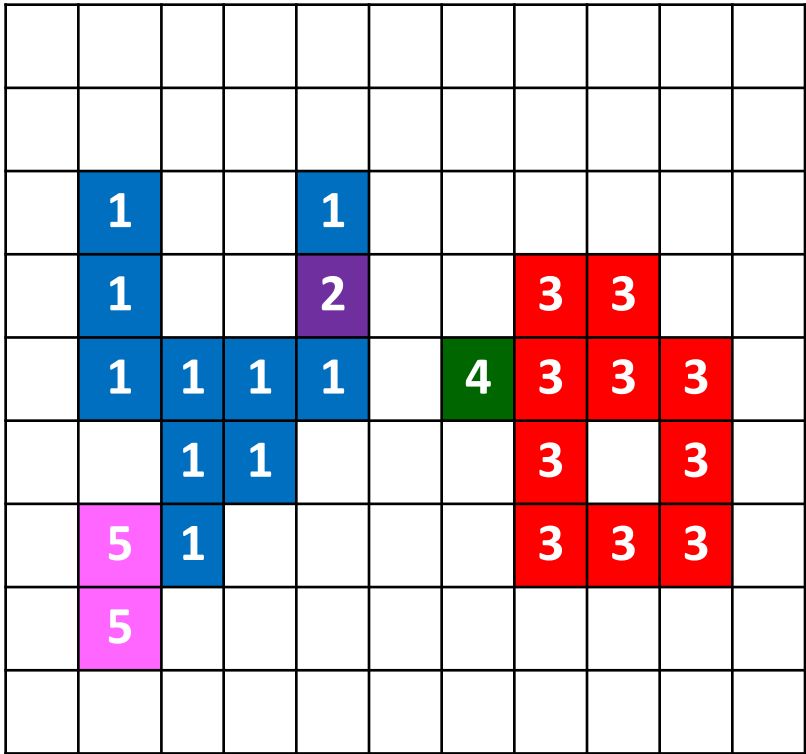




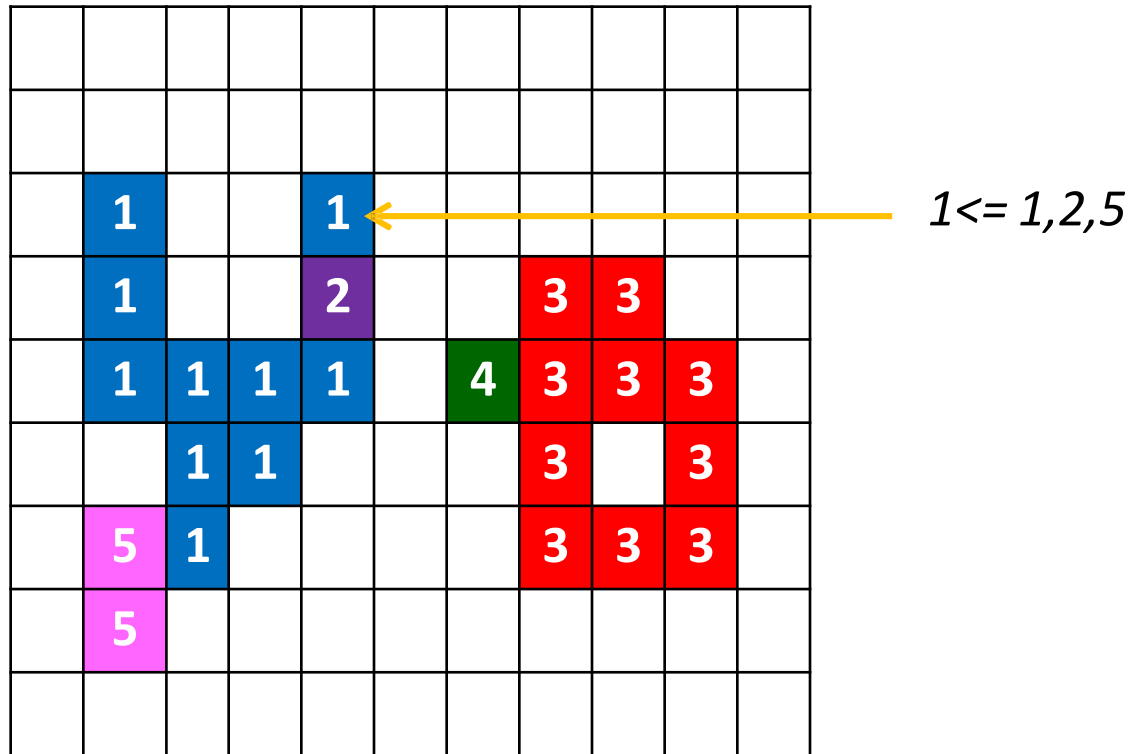
# Connected Component Labeling (example)



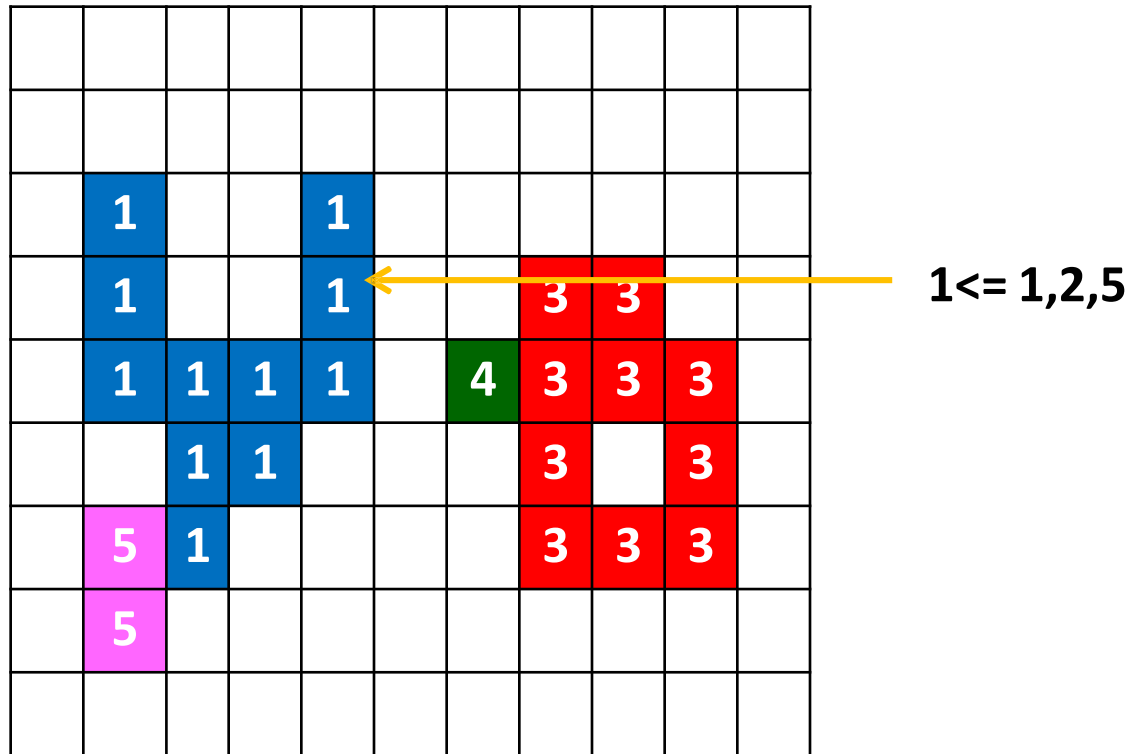
# Connected Component Labeling (example)



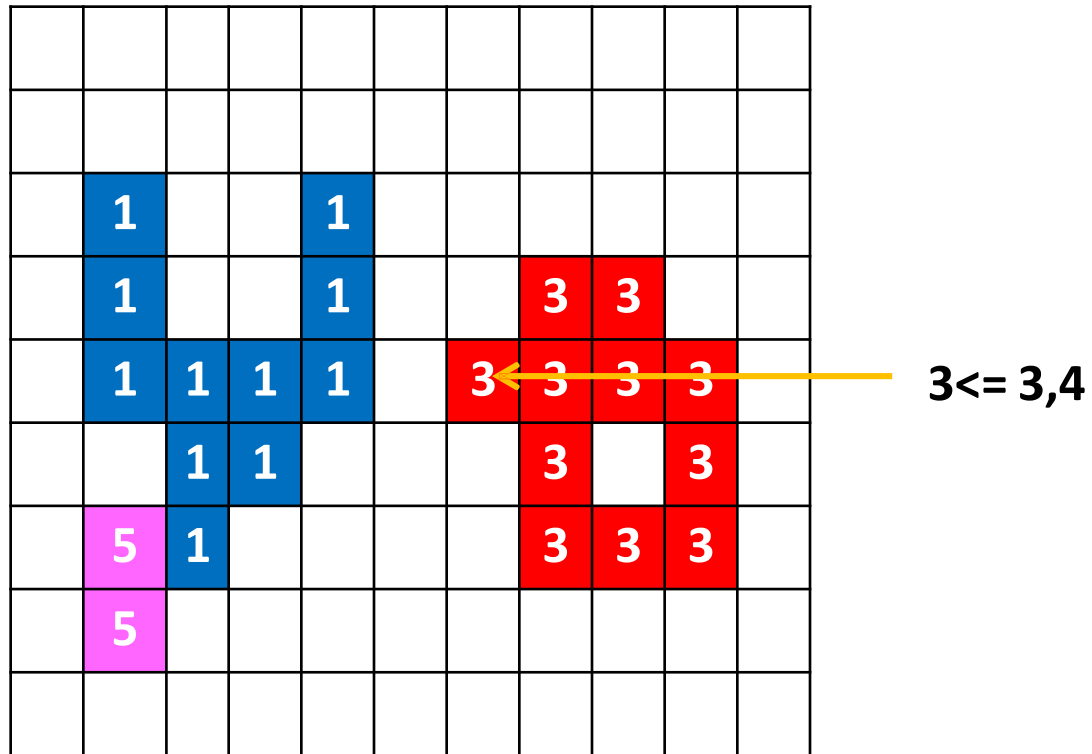
# Connected Component Labeling (example)



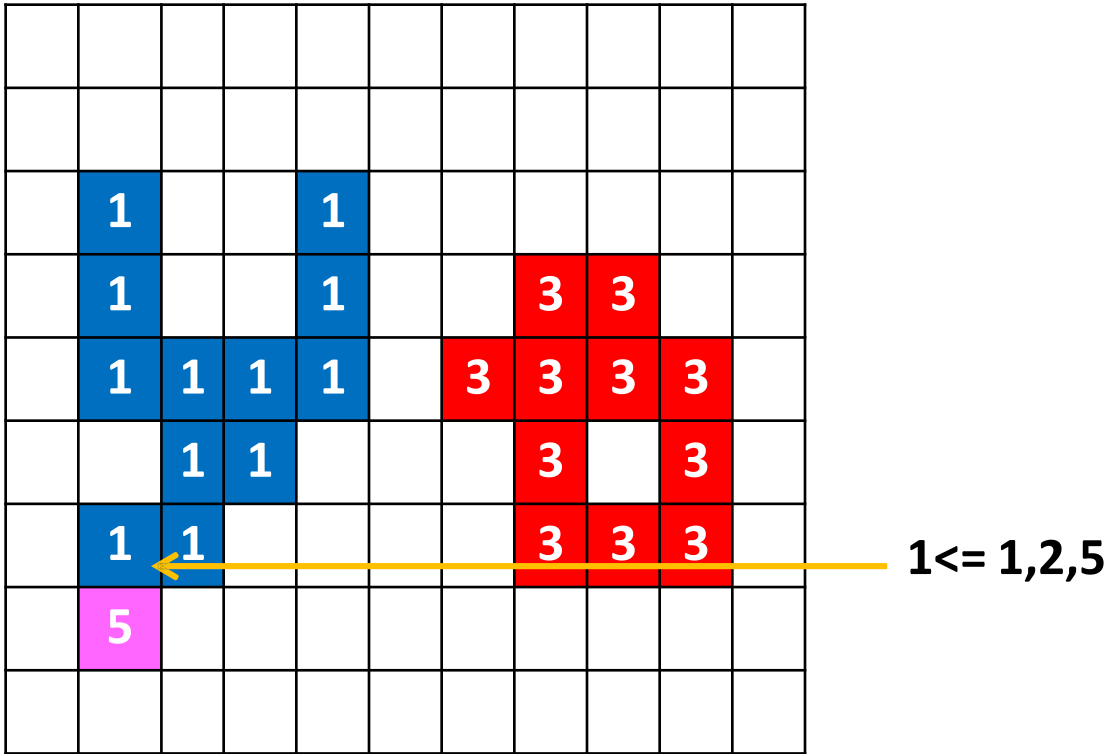
# Connected Component Labeling (example)



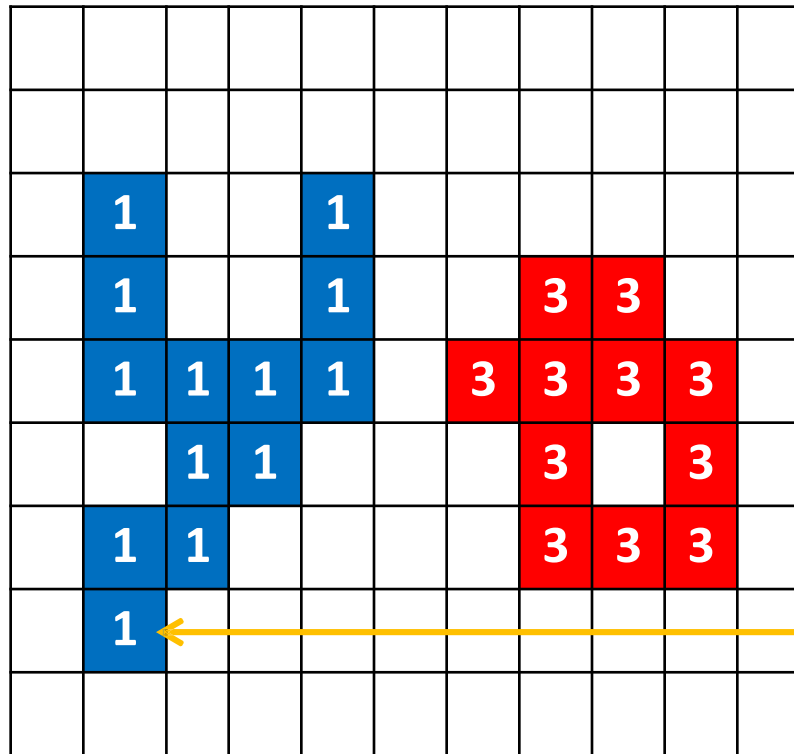
# Connected Component Labeling (example)



# Connected Component Labeling (example)

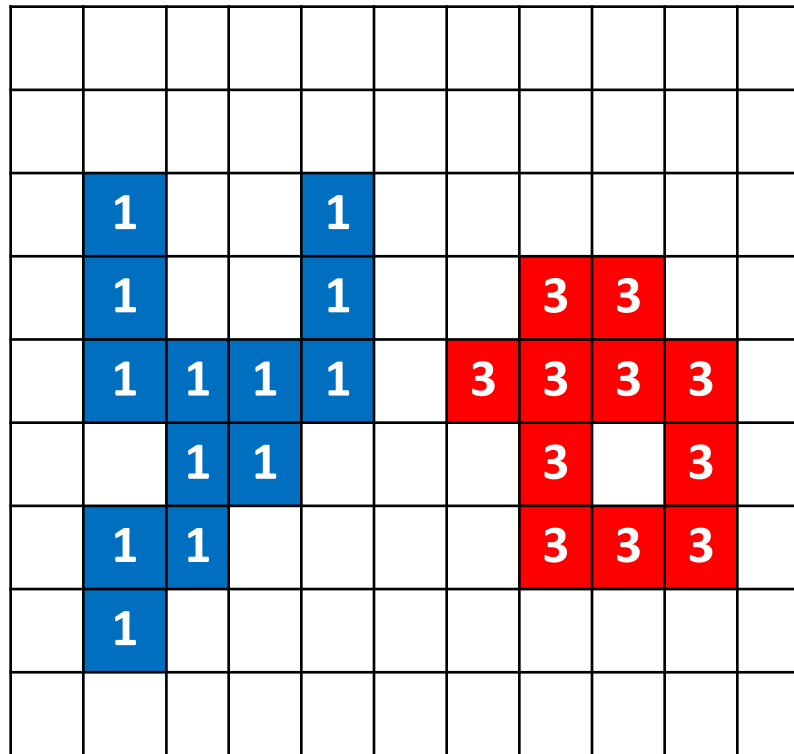


# Connected Component Labeling (example)



$1 \leq 1,2,5$

# Connected Component Labeling (example)



Here we observed that the image contain two distinct class of regions



# Binarization using Otsu algorithm

```
import cv2
import numpy as np
import matplotlib.pyplot as plt

image = cv2.imread('../data/Lena.png', 0)

otsu_thr, otsu_mask = cv2.threshold(image, -1, 1, cv2.THRESH_BINARY | cv2.THRESH_OTSU)
print('Estimated threshold (Otsu):', otsu_thr)

plt.figure(figsize=(6,3))
plt.subplot(121)
plt.axis('off')
plt.title('original')
plt.imshow(image, cmap='gray')
plt.subplot(122)
plt.axis('off')
plt.title('Otsu threshold')
plt.imshow(otsu_mask, cmap='gray')
plt.tight_layout()
plt.show()
```

# Finding external and internal contours

```
import cv2
import numpy as np
import matplotlib.pyplot as plt

image = cv2.imread('../data/BnW.png', 0)

contours, hierarchy = cv2.findContours(image, cv2.RETR_CCOMP, cv2.CHAIN_APPROX_SIMPLE)

image_external = np.zeros(image.shape, image.dtype)
for i in range(len(contours)):
    if hierarchy[0][i][3] == -1:
        cv2.drawContours(image_external, contours, i, 255, -1)

image_internal = np.zeros(image.shape, image.dtype)
for i in range(len(contours)):
    if hierarchy[0][i][3] != -1:
        cv2.drawContours(image_internal, contours, i, 255, -1)

plt.figure(figsize=(10,3))
plt.subplot(131)
plt.axis('off')
plt.title('original')
plt.imshow(image, cmap='gray')
plt.subplot(132)
plt.axis('off')
plt.title('external')
plt.imshow(image_external, cmap='gray')
plt.subplot(133)
plt.axis('off')
plt.title('internal')
plt.imshow(image_internal, cmap='gray')
plt.tight_layout()
plt.show()
```

# Extracting connected component

```
import cv2
import numpy as np

img = cv2.imread('../data/BnW.png', cv2.IMREAD_GRAYSCALE)

connectivity = 8
num_labels, labelmap = cv2.connectedComponents(img, connectivity, cv2.CV_32S)

img = np.hstack((img, labelmap.astype(np.float32)/(num_labels - 1)))
cv2.imshow('Connected components', img)
cv2.waitKey()
cv2.destroyAllWindows()

img = cv2.imread('../data/Lena.png', cv2.IMREAD_GRAYSCALE)
otsu_thr, otsu_mask = cv2.threshold(img, -1, 1, cv2.THRESH_BINARY | cv2.THRESH_OTSU)

output = cv2.connectedComponentsWithStats(otsu_mask, connectivity, cv2.CV_32S)

num_labels, labelmap, stats, centers = output

colored = np.full((img.shape[0], img.shape[1], 3), 0, np.uint8)

for l in range(1, num_labels):
    if stats[l][4] > 200:
        colored[labelmap == l] = (0, 255*l/num_labels, 255*(num_labels-l)/num_labels)
        cv2.circle(colored,
                    (int(centers[l][0]), int(centers[l][1])), 5, (255, 0, 0), cv2.FILLED)

img = cv2.cvtColor(otsu_mask*255, cv2.COLOR_GRAY2BGR)

cv2.imshow('Connected components', np.hstack((img, colored)))
cv2.waitKey()
cv2.destroyAllWindows()
```



# Fitting lines and circles

```
import cv2
import numpy as np
import random

img = np.full((512, 512, 3), 255, np.uint8)

axes = (int(256*random.uniform(0, 1)), int(256*random.uniform(0, 1)))
angle = int(180*random.uniform(0, 1))
center = (256, 256)

pts = cv2.ellipse2Poly(center, axes, angle, 0, 360, 1)
pts += np.random.uniform(-10, 10, pts.shape).astype(np.int32)

cv2.ellipse(img, center, axes, angle, 0, 360, (0, 255, 0), 3)

for pt in pts:
    cv2.circle(img, (int(pt[0]), int(pt[1])), 3, (0, 0, 255))

cv2.imshow('Fit ellipse', img)
cv2.waitKey()
cv2.destroyAllWindows()

ellipse = cv2.fitEllipse(pts)
cv2.ellipse(img, ellipse, (0, 0, 0), 3)

cv2.imshow('Fit ellipse', img)
cv2.waitKey()
cv2.destroyAllWindows()
```

```
img = np.full((512, 512, 3), 255, np.uint8)

pts = np.arange(512).reshape(-1, 1)
pts = np.hstack((pts, pts))
pts += np.random.uniform(-10, 10, pts.shape).astype(np.int32)

cv2.line(img, (0, 0), (512, 512), (0, 255, 0), 3)

for pt in pts:
    cv2.circle(img, (int(pt[0]), int(pt[1])), 3, (0, 0, 255))

cv2.imshow('Fit line', img)
cv2.waitKey()
cv2.destroyAllWindows()

vx, vy, x0, y = cv2.fitLine(pts, cv2.DIST_L2, 0, 0.01, 0.01)
y0 = int(y - x*vy/vx)
y1 = int((512 - x)*vy/vx + y)
cv2.line(img, (0, y0), (512, y1), (0, 0, 0), 3)

cv2.imshow('Fit line', img)
cv2.waitKey()
cv2.destroyAllWindows()
```



# Calculating image moments

```
import cv2
import numpy as np
import matplotlib.pyplot as plt

image = np.zeros((480, 640), np.uint8)
cv2.ellipse(image, (320, 240), (200, 100), 0, 0, 360, 255, -1)

m = cv2.moments(image)
for name, val in m.items():
    print(name, '\t', val)

print('Center X estimated:', m['m10'] / m['m00'])
print('Center Y estimated:', m['m01'] / m['m00'])
```

# Working with curves

```
import cv2, random
import numpy as np

img = cv2.imread('../data/bw.png', cv2.IMREAD_GRAYSCALE)

contours, hierarchy = cv2.findContours(img, cv2.RETR_TREE, cv2.CHAIN_APPROX_SIMPLE)

color = cv2.cvtColor(img, cv2.COLOR_GRAY2BGR)
cv2.drawContours(color, contours, -1, (0,255,0), 3)

cv2.imshow('contours', color)
cv2.waitKey()
cv2.destroyAllWindows()

contour = contours[0]

print('Area of contour is %.2f' % cv2.contourArea(contour))
print('Signed area of contour is %.2f' % cv2.contourArea(contour, True))
print('Signed area of contour is %.2f' % cv2.contourArea(contour[::-1], True))

print('Length of closed contour is %.2f' % cv2.arcLength(contour, True))
print('Length of open contour is %.2f' % cv2.arcLength(contour, False))

hull = cv2.convexHull(contour)
cv2.drawContours(color, [hull], -1, (0,0,255), 3)

cv2.imshow('contours', color)
cv2.waitKey()
cv2.destroyAllWindows()

print('Convex status of contour is %s' % cv2.isContourConvex(contour))
print('Convex status of its hull is %s' % cv2.isContourConvex(hull))

cv2.namedWindow('contours')

img = np.copy(color)

def trackbar_callback(value):
    global img
    epsilon = value*cv2.arcLength(contour, True)*0.1/255
    approx = cv2.approxPolyDP(contour, epsilon, True)
    img = np.copy(color)
    cv2.drawContours(img, [approx], -1, (255,0,255), 3)

cv2.createTrackbar('Epsilon', 'contours', 1, 255, lambda v: trackbar_callback(v))
while True:
    cv2.imshow('contours', img)
    key = cv2.waitKey(3)
    if key == 27:
        break

cv2.destroyAllWindows()
```

# Checking the location of points

```
import cv2, random
import numpy as np

img = cv2.imread('../data/bw.png', cv2.IMREAD_GRAYSCALE)

contours, hierarchy = cv2.findContours(img, cv2.RETR_TREE, cv2.CHAIN_APPROX_SIMPLE)

color = cv2.cvtColor(img, cv2.COLOR_GRAY2BGR)
cv2.drawContours(color, contours, -1, (0,255,0), 3)

cv2.imshow('contours', color)
cv2.waitKey()
cv2.destroyAllWindows()

contour = contours[0]
image_to_show = np.copy(color)
measure = True

def mouse_callback(event, x, y, flags, param):
    global contour, image_to_show

    if event == cv2.EVENT_LBUTTONDOWN:
        distance = cv2.pointPolygonTest(contour, (x,y), measure)
        image_to_show = np.copy(color)
        if distance > 0:
            pt_color = (0, 255, 0)
        elif distance < 0:
            pt_color = (0, 0, 255)
        else:
            pt_color = (128, 0, 128)
        cv2.circle(image_to_show, (x,y), 5, pt_color, -1)
        cv2.putText(image_to_show, '%.2f' % distance, (0, image_to_show.shape[1] - 5),
                    cv2.FONT_HERSHEY_SIMPLEX, 1, (255, 255, 255))

cv2.namedWindow('contours')
cv2.setMouseCallback('contours', mouse_callback)
```

```
while(True):
    cv2.imshow('contours', image_to_show)
    k = cv2.waitKey(1)

    if k == ord('m'):
        measure = not measure
    elif k == 27:
        break

cv2.destroyAllWindows()
```

# Computing distance to 2d point set

```
import cv2
import numpy as np
import matplotlib.pyplot as plt

image = np.full((480, 640), 255, np.uint8)
cv2.circle(image, (320, 240), 100, 0)

distmap = cv2.distanceTransform(image, cv2.DIST_L2, cv2.DIST_MASK_PRECISE)

plt.figure()
plt.imshow(distmap, cmap='gray')
plt.show()
```



# 실습 문제

- 영상을 열고 아래의 내용을 수행하시오.
  - Otsu 의 알고리즘을 통해 thresholding 하시오. (1)
  - (1)의 영상에 대해서 External/Internal Contour을 찾으시오.
  - (1)의 영상에 대해서 Connected Component를 찾고 스페이스를 누를 때마다 random 하게 5개의 component를 보여주시오. (각 component의 색은 random하게 정하시오)
  - (1)의 영상에 대해서 Distance Transform을 계산해서 보여주시오.