Let 90% residents of i commute back and forth to their workplace at j. Residents start travelling from i between t_1 and t_2 , and arrive at j between t_{c1} and t_{c2} . Let $T_{ij}(t)$ be a commuter pulse that is non-zero between t_1 and t_2 that satisfies

$$\int_{t_1}^{t_2} T_{ij} \ dt = 0.9 N_i(t_1)$$

where $N_i(t)$ is the population of node i at time t. The transport is then

$$\dot{S}_i = \dots - \frac{S_i(t)}{N_i(t)} T_{ij}$$

$$\dot{I}_i = \dots - \frac{I_i(t)}{N_i(t)} T_{ij}$$

$$\dot{R}_i = \dots - \frac{R_i(t)}{N_i(t)} T_{ij}$$

where ... refers to the standard SIR terms. The total number of people leaving i between t_1 and t_2 is then

$$-\int_{t_1}^{t_2} \left(\dot{S}_i + \dot{I}_i + \dot{R}_i \right) dt = \int_{t_1}^{t_2} T_{ij} dt = 0.9 N_i(t_1)$$

If we disallow I(t) to leave home, we get

$$\dot{S}_{i} = \cdots - \frac{S_{i}(t)}{N_{i}(t)} T_{ij}$$

$$\dot{I}_{i} = \cdots$$

$$\dot{R}_{i} = \cdots - \frac{R_{i}(t)}{N_{i}(t)} T_{ij}$$

and the total number of people leaving is

$$0.9N_i(t_1) - \int_{t_1}^{t_2} \dot{I}_i dt$$
 (1)

which is in general a difficult integral to compute, but we are guaranted that (1) has a lower and upper bound of 0 and $0.9N_i(t_1)$ respectively.