# MATH 601 (DUE 11/22)

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### 1. THE THEOREM ON SYMMETRIC POLYNOMIALS

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**Exercise.** (Problem 1) By substituting  $u_4 = 0$ , we get  $u_1^2 u_2 u_3 + u_1 u_2^2 u_3 + u_1 u_2 u_3^2 = s_3 s_1$ .  $s_3 s_1$  with 4 variables expands to  $u_1^2 u_2 u_3 + u_1^2 u_2 u_4 + u_1^2 u_3 u_4 + u_1 u_2^2 u_3 + u_1 u_2^2 u_4 + u_1 u_2 u_3^2 + 4 u_1 u_2 u_3^2 u_4 + u_1 u_2 u_4^2 + u_1 u_3^2 u_4 + u_1 u_3 u_4^2 + u_2^2 u_3 u_4 + u_2 u_3^2 u_4 + u_2 u_3 u_4^2$ . Then  $s_3 s_1 - f$  where f is the original polynomial gives us  $4 u_1 u_2 u_3 u_4 = 4 s_4$ . Therefore,  $f = s_3 s_1 - 4 s_4$ .