

	\mathfrak{g}	\mathfrak{h}	d_1	d_2	d_3	L_{123}
1	$\mathfrak{so}(k+l+m)$	$\mathfrak{so}(k) \oplus \mathfrak{so}(l) \oplus \mathfrak{so}(m)$	kl	km	lm	$\frac{klm}{2(k+l+m-2)}$
2	$\mathfrak{su}(k+l+m)$	$\mathfrak{s}(\mathfrak{u}(k) \oplus \mathfrak{u}(l) \oplus \mathfrak{u}(m))$	$2kl$	$2km$	$2lm$	$\frac{klm}{k+l+m}$
3	$\mathfrak{sp}(k+l+m)$	$\mathfrak{sp}(k) \oplus \mathfrak{sp}(l) \oplus \mathfrak{sp}(m)$	$4kl$	$4km$	$4lm$	$\frac{2klm}{k+l+m+1}$
4	$\mathfrak{su}(2l), l \geq 2$	$\mathfrak{u}(l)$	$l(l-1)$	$l(l+1)$	l^2-1	$\frac{l(l^2-1)}{4}$
5	$\mathfrak{so}(2l), l \geq 4$	$\mathfrak{u}(1) \oplus \mathfrak{u}(l-1)$	$2(l-1)$	$2(l-1)$	$(l-1)(l-2)$	$\frac{l-1}{2}$
6	\mathfrak{e}_6	$\mathfrak{su}(4) \oplus \mathfrak{sp}(1)^2 \oplus$	16	16	24	4
7	\mathfrak{e}_6	$\mathfrak{so}(8) \oplus^2$	16	16	16	$\frac{8}{3}$
8	\mathfrak{e}_6	$\mathfrak{sp}(3) \oplus \mathfrak{sp}(1)$	14	28	12	$\frac{7}{2}$
9	\mathfrak{e}_7	$\mathfrak{so}(8) \oplus \mathfrak{sp}(1)^3$	32	32	32	$\frac{64}{9}$
10	\mathfrak{e}_7	$\mathfrak{su}(6) \oplus \mathfrak{sp}(1) \oplus$	30	40	24	$\frac{20}{3}$
11	\mathfrak{e}_7	$\mathfrak{so}(8)$	35	35	35	$\frac{175}{18}$
12	\mathfrak{e}_8	$\mathfrak{so}(12) \oplus \mathfrak{sp}(1)^2$	64	64	48	$\frac{64}{5}$
13	\mathfrak{e}_8	$\mathfrak{so}(8) \oplus \mathfrak{so}(8)$	64	64	64	$\frac{256}{15}$
14	\mathfrak{f}_4	$\mathfrak{so}(5) \oplus \mathfrak{sp}(1)^2$	8	8	20	$\frac{20}{9}$
15	\mathfrak{f}_4	$\mathfrak{so}(8)$	8	8	8	$\frac{8}{9}$

Table 1: Generalized Wallach spaces G/\mathbf{H} with G simple, from [?, Table 1].