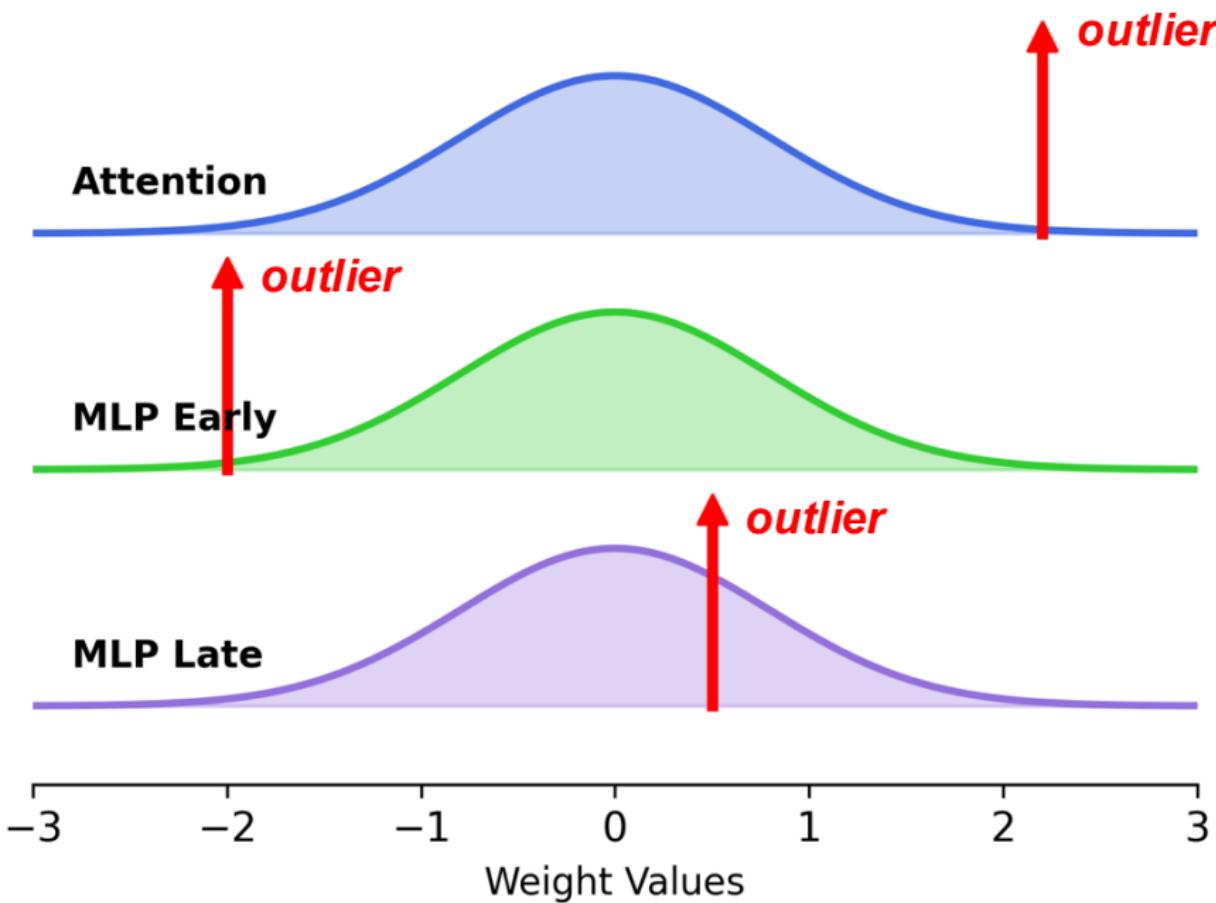
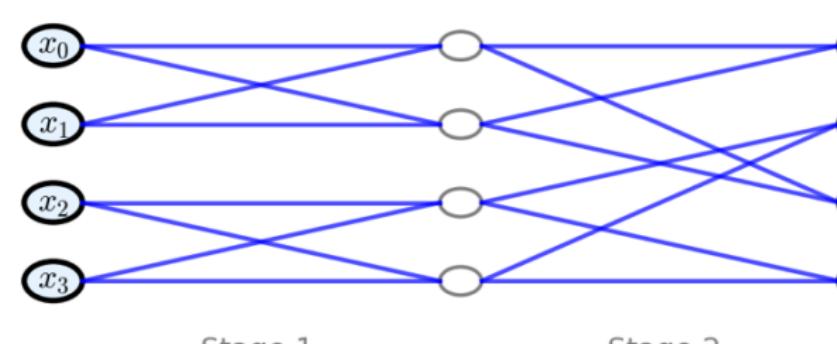


(a) Layer Heterogeneity**(b) Fixed Transform (Hadamard)**

$$\mathbf{H}_1 = [1], \quad \mathbf{H}_{2n} = \frac{1}{\sqrt{2}} \begin{bmatrix} \mathbf{H}_n & \mathbf{H}_n \\ \mathbf{H}_n & -\mathbf{H}_n \end{bmatrix}$$
$$\mathbf{H}_4 = \begin{bmatrix} +1 & +1 & +1 & +1 \\ +1 & -1 & +1 & -1 \\ +1 & +1 & -1 & -1 \\ +1 & -1 & -1 & +1 \end{bmatrix}$$

**(c) Learnable Transform (Butterfly)**

$$\mathbf{B} = \prod_{i=1}^{\log_2 n} \mathbf{B}_i$$
$$\mathbf{B}_1 = \text{diag}(\mathbf{G}(\theta_{1,1}), \mathbf{G}(\theta_{1,2}), \mathbf{G}(\theta_{1,3}), \mathbf{G}(\theta_{1,4}))$$
$$\mathbf{G}(\theta) = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$$

