

CptS 451- Introduction to Database Systems

Relational Design Theory (DMS Ch-19)

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Relational Design Theory (topics)

- Motivation & Overview
- Functional Dependencies
- Boyce-Codd Normal Form
- 3NF

Database Design: A 6-Step Program

1. Requirements Analysis: data requirements, critical operations on the data
2. Conceptual DB Design: high-level description of data and constraints - typically using ER model
3. Logical DB Design: conversion into a schema
 - pick a type of DBMS, relational DBMS is most popular and is our focus
4. Schema Refinement: normalization (eliminating redundancy)
5. Physical DB Design: consider workloads, indexes and clustering of data
6. Application/Security Design

Designing/Refining a Database Schema



- Usually many designs possible
 - Often use higher-level design tools.
 - Some designers go straight to relations
 - Useful to understand why tools produce certain schemas
- Some are (much) better than others!
- How do we choose?
 - Theory for relational database design

Designing a Database Schema

Example1: College application info.

- SSN and name
- Colleges applying to
- High schools attended (with city)
- Hobbies

Apply(SSN, sName, cName, HS, HScity, hobby)

Designing a Database Schema

Example1: College application info.

Apply(SSN, sName, cName, HS, HScity, hobby)

Kyle (with SSN 1111) from PHS (Pullman) swims and plays trumpet and he applied to WSU, UW, and OSU.

SSN	sName	cName	HS	HScity	hobby
1111	Kyle	WSU	PHS	Pullman	Swim
1111	Kyle	WSU	PHS	Pullman	Trumpet
1111	Kyle	UW	PHS	Pullman	Swim
1111	Kyle	UW	PHS	Pullman	Trumpet
1111	Kyle	OSU	PHS	Pullman	Swim
1111	Kyle	OSU	PHS	Pullman	Trumpet

Designing a Database Schema

Example1: College application info.

Apply(SSN, sName, cName, HS, HScity, hobby)

Design “anomalies”

1) Redundancy

- Captures information multiple times
 - For example:
 - SSN, sName, HS, Hscity are repeated per (cName, hobby) pair.

SSN	sName	cName	HS	HScity	hobby
1111	Kyle	WSU	PHS	Pullman	Swim
1111	Kyle	WSU	PHS	Pullman	Trumpet
1111	Kyle	UW	PHS	Pullman	Swim
1111	Kyle	UW	PHS	Pullman	Trumpet
1111	Kyle	OSU	PHS	Pullman	Swim
1111	Kyle	OSU	PHS	Pullman	Trumpet

- There is **functional dependency** between SSN and sName, HS and HScity.

Designing a Database Schema

Example1: College application info.

Apply(SSN, sName, cName, HS, HScity, hobby)

Design “anomalies”

1) Redundancy

2) Update anomaly

- if we decide to call the instrument **cornet** (instead of trumpet) we need to modify it in each of the tuples in which it is stored (one per cName). Else, database will be inconsistent.

SSN	sName	cName	HS	HScity	hobby
1111	Kyle	WSU	PHS	Pullman	Swim
1111	Kyle	WSU	PHS	Pullman	Trumpet Cornet
1111	Kyle	UW	PHS	Pullman	Swim
1111	Kyle	UW	PHS	Pullman	Trumpet
1111	Kyle	OSU	PHS	Pullman	Swim
1111	Kyle	OSU	PHS	Pullman	Trumpet

Designing a Database Schema

Example1: College application info.

Apply(SSN, sName, cName, HS, HScity, hobby)

Design “anomalies”

1) Redundancy

2) Update anomaly

3) Deletion anomaly

- How to delete “Trumpet” hoby without deleting applicant information
 - possible solution: use **null** values in the hobby field

SSN	sName	cName	HS	HScity	hobby
1111	Kyle	WSU	PHS	Pullman	Swim
1111	Kyle	WSU	PHS	Pullman	Trumpet -NULL
1111	Kyle	UW	PHS	Pullman	Swim
1111	Kyle	UW	PHS	Pullman	Trumpet -NULL
1111	Kyle	OSU	PHS	Pullman	Trumpet -NULL

Designing a Database Schema

Example: College application info.

- SSN and name
- Colleges applying to
- High schools attended (with city)
- Hobbies

Student(SSN, sName)

Apply(SSN, cName)

HighSchool(SSN, HS)

Located(HS, HScity)

Hobbies(SSN, hobby)

- Decompose the relation into multiple relations
 - No anomalies
 - Can reconstruct the original relations (no loss of information)

Designing a Database Schema

Example: College application info.

- SSN and name
- Colleges applying to
- High schools attended (with city)
- Hobbies

Student(SSN, sName)

Apply(SSN, cName)

HighSchool(SSN, HS)

Located(HS, HScity)

Hobbies(SSN, hobby)

HobbyList(hobby, desc)

CollegeList(cName)

- The best design, for an application for relational databases depend not only on constructing the relations well, but also in what the data is representing in the real world.

Redundancy and Anomalies in Relational Schema – Example2



CptS451 Projects	Student	Proj title	Date	Room#
	Kyle S.	Yelp	04/28/18	EME102A
	Aaron B.	Yelp	04/28/18	EME102A
	Jeromy J.	Yelp	04/28/18	EME102A
	Kelly K.	OODB	04/30/18	ETRL101

Redundancy:

- date of presentation and room# are repeated per member of project group

Redundancy and Anomalies in Relational Schema – Example2 (cont.)



CptS451 Projects	Student	Proj title	Date	Room#
	Kyle S.	Yelp	04/30/14	EME102A
	Aaron B.	Yelp	04/28/14	EME102A
	Jeromy J.	Yelp	04/28/14	EME102A
	Kelly K.	OODB	04/30/14	ETRL101

Error in updating.
Forgot to update all
entries.

Update Anomaly:

- if we modify presentation date for the “yelp” project, we need to modify the date in each of the tuples in which it is stored (one per member). Else, database will be inconsistent.

Redundancy and Anomalies in Relational Schema – Example2 (cont.)



CptS451 Projects	Student	Proj title	Date	Room#
	Kyle S.	Yelp	04/28/18	EME102A
	Aaron B.	Yelp	04/28/18	EME102A
	Jeromy J.	Yelp	04/28/18	EME102A
	Kelly K. NULL	OODB	04/30/18	ETRL101

Deletion Anomaly:

- How to delete the fact that **Kelly K.** dropped out of the project without deleting information about the **OODB** project.
 - possible solution: use **null** values in the student field

Relation Decomposition

CptS451 Projects	Student	Proj title	Date	Room#
	Kyle S.	Yelp	04/28/14	EME102A
	Aaron B.	Yelp	04/28/14	EME102A
	Jeromy J.	Yelp	04/28/14	EME102A
	Kelly K.	OODB	04/30/14	ETRL101
	NULL	dDB	04/24/14	SLOAN123

Student	Proj title	Proj title	Date	Room#
Kyle S.	Yelp	Yelp	04/28/14	EME102A
Aaron B.	Yelp	OODB	04/30/14	ETRL101
Jeromy J.	Yelp	dDB	04/24/14	SLOAN123
Kelly K.	OODB			

Anomalies have gone:

- No more repeated data
- Easy to update project information

Designing a Database Schema

Design by decomposition – how does it work?

- Start with “mega” relations
- Decompose into smaller, better relations with same info.
- Can do decomposition automatically

Automatic decomposition

- “Mega” relations + *properties of the data (functional dependencies)*
- System decomposes based on properties
- Final set of relations satisfy *normal form*
 - *No anomalies, no lost information*

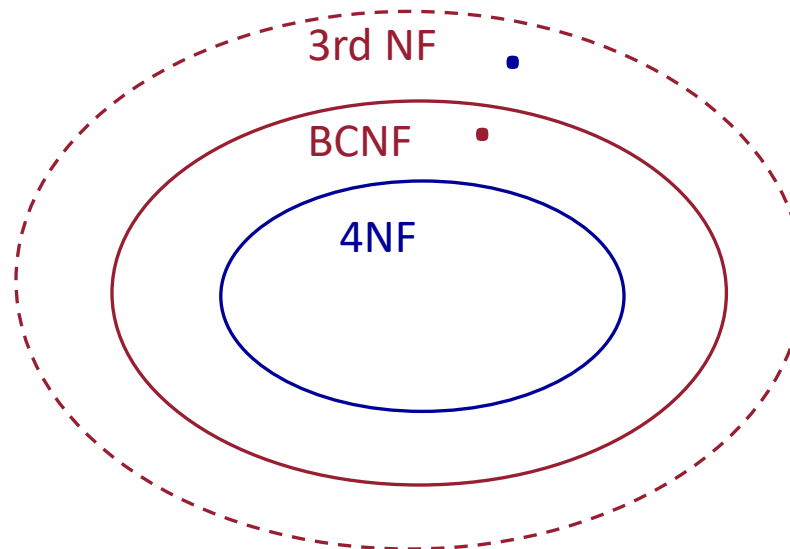
Designing a Database Schema

Normal Forms

Functional dependencies \Rightarrow Boyce-Codd Normal Form

+ Multivalued dependencies \Rightarrow Fourth Normal Form

1st NF
2nd NF
3rd NF



In CptS451, we will only cover BCNF and 3NF

What we will cover:

Functional Dependencies and BCNF



Apply(SSN, SName, cName)

- Redundancy: Storing SSN-sName pair once for each college

Functional Dependency $SSN \rightarrow sName$

- Same SSN always has same sName
- Should store each SSN's sName only once

SSN	sName	cName
1111	Kyle	WSU
1111	Kyle	UW
1111	Kyle	OSU

Boyce-Codd Normal Form If $A \rightarrow B$ then A is a key

Apply(SSN, sName, cName) : SSN is not a key
Apply is not in BCNF

Decompose: Student(SSN, sName) Apply(SSN, cName)
SSN is the key SSN, CName is the key

Functional Dependency

Functional Dependency - Example

Example:

Hourly_Emps (SSN, name, dept, rating, hourly_pay, num_hours)

Assume there is fixed hourly pay rate for each rating.

ssn	name	dept	rating	hourly_pay	num_hours
111-11-1111	Kelly	123	5	18	40
222-11-2222	Kyle	124	4	16	40
333-11-3333	John	124	4	16	20
444-11-4444	Roseanne	123	4	16	20
555-11-5555	Ning	123	5	18	40

Problems????

Key : ssn FDs: ssn \rightarrow name,dept,rating,num_hours
 rating \rightarrow hourly_pay

Functional Dependency - Example

Hourly_Emps(SSN, name, dept, rating, hourly_pay, num_hours)

- Suppose **hourly_pay** is determined by **rating**
 - rating = 4 → hourly_pay = 16
 - rating = 5 → hourly_pay = 18
 - rating = 6 → hourly_pay = 20
 - ...
- Two tuples with same **rating** have same **hourly_pay**
rating → **hourly_pay** (rating functionally determines hourly pay)

Functional Dependency - Definition

For all tuples t, u in R ,

if $t[A] = u[A] \Rightarrow t[B] = u[B]$

then $A \rightarrow B$

Definition: Given Relation $R(A_1, \dots, A_n, B_1, \dots, B_m, C_1, \dots, C_l)$

A_1, \dots, A_n *functionally determine* B_1, \dots, B_m , i.e.,

$$(A_1, \dots, A_n \rightarrow B_1, \dots, B_m)$$

When any two tuples agree on the attributes

A_1, A_2, \dots, A_n

Then they must also agree on the attributes

B_1, B_2, \dots, B_n

Functional Dependency (FD) – Some Terminology



- FDs are based on knowledge of real world. They generalize the concept of a key.
- If we know that an FD holds on all tuples, then we say that **R satisfies the FD**
- If we say that **R satisfies an FD “F”**, we are stating a **constraint** on R

Functional Dependency (FD) - Some Terminology

Let X and Y be set of attributes from relation $R=(A,B,C,...)$

Trivial FD

- Those that are true for every relation
- $X \rightarrow Y$ is **trivial** if Y is a subset of the X , i.e., $Y \subseteq X$
- Example: $AB \rightarrow A$

Nontrivial FD

- $X \rightarrow Y$ is called **nontrivial** if at least one of the attributes in Y is not among the attributes in X , i.e., $Y \not\subseteq X$
- Examples: $AB \rightarrow AC$

Completely nontrivial FD

- Called *completely nontrivial* if none of the attributes in Y is one of the attributes in X , i.e., $Y \cap X = \emptyset$
- Example: $AB \rightarrow C$

FD – Observation

- If both of these FDs are true:

$ssn \rightarrow rating$
 $rating \rightarrow hourly_pay$

- Then this FD also holds:

$ssn \rightarrow hourly_pay$

If we find out from application domain (real world data) that a relation satisfies some FDs, it doesn't mean that we found all the FDs that it satisfies!

There could be more FDs implied by the ones we have.

Reasoning About FDs

- Given some FDs, we can usually infer additional FDs:
 $ssn \rightarrow rating$ and $rating \rightarrow hourly_pay$ implies $ssn \rightarrow hourly_pay$
- An FD f is implied by a set of FDs F , if f holds whenever all FDs in F hold.
 - F^+ = closure of F is the set of all FDs that are implied by F .
- Armstrong's Axioms (X, Y, Z are sets of attributes):
 - Reflexivity: If $X \subseteq Y$, then $Y \rightarrow X$
 - Augmentation: If $X \rightarrow Y$, then $XZ \rightarrow YZ$ for any Z
 - Transitivity: If $X \rightarrow Y$ and $Y \rightarrow Z$, then $X \rightarrow Z$
- These are **sound** and **complete** inference rules for FDs!

Additional Rules for FDs

Additional rules while reasoning about F^+

1. Combining Rule (Union)

Combining Right sides of FDs

$A_1, \dots, A_n \rightarrow B_1$	}	is equivalent to $A_1, \dots, A_n \rightarrow B_1, \dots, B_m$
$A_1, \dots, A_n \rightarrow B_2$		
....		
$A_1, \dots, A_n \rightarrow B_m$		

Example: $A \rightarrow B$ and $A \rightarrow C$ is equivalent to $A \rightarrow BC$.

Additional Rules for FDs

2. Splitting Rule (Decomposition)

Splitting right sides of FDs

$A_1, \dots, A_n \rightarrow B_1, \dots, B_m$ is equivalent to

$$\begin{aligned} A_1, \dots, A_n &\rightarrow B_1 \\ A_1, \dots, A_n &\rightarrow B_2 \\ &\dots \\ A_1, \dots, A_n &\rightarrow B_m \end{aligned}$$

Example: $A \rightarrow BC$ is equivalent to $A \rightarrow B$ and $A \rightarrow C$.

Can we also split **left**-hand-side?

- **No.** There is no splitting rule for left sides

Example?

What we talked about so far...

1. Redundancy and Anomalies in Relational Schema
2. Design by decomposition
 - Start with “mega” relations containing everything
 - Decompose into smaller, better relations with same info.
 - Can do decomposition automatically
 - Final set of relations satisfies *normal form*
 - No anomalies, no lost information
 - BCNF (will cover)
 - 1NF, 2NF, 3NF, 4NF (won't cover)
3. Functional dependencies (FDs)
4. Rules for Functional Dependencies
 - Armstrong Axioms,
 - Closure of FDs
5. Closure of Attributes (next)

Closure of Attributes

- Given relation R , FDs F , set of attributes $X=\{A_1,A_2,...A_n\}$
- Find all $Y=\{B_1,...,B_m\}$ such that $X \rightarrow Y$

Closure of X denoted by $X^+ = \{A_1,A_2,...A_n\}^+$

How to calculate $\{A_1,A_2,...A_n\}^+$?

Start with $X=\{A_1,A_2,...A_n\}$

Repeat until no change:

For every FD rule in F $X' \rightarrow Y'$,
if X' is in the closure set
add Y' to the set

Hourly_Emps(SSN,name,dept,
rating,hourly_pay,
num_hours)

ssn \rightarrow name,dept,rating,num_hours
rating \rightarrow hourly_pay

Closure Example

Hourly_Emps(SSN, name, dept, rating, hourly_pay, num_hours)

$ssn \rightarrow name, dept, rating, num_hours$

$rating \rightarrow hourly_pay$

$\{ssn\}^+ = \{ssn, name, dept, rating, num_hours, hourly_pay\}$

Hence:

$ssn \rightarrow ssn, name, dept, rating, num_hours, hourly_pay$

Key : ssn

Armstrong's Axioms

Reflexivity: If $X \subseteq Y$, then $Y \rightarrow X$

Augmentation: If $X \rightarrow Y$, then $XZ \rightarrow YZ$ for any Z

Transitivity: If $X \rightarrow Y$ and $Y \rightarrow Z$, then $X \rightarrow Z$ 38

Closure Example

$R(A, B, C, D, E, F)$

$A, B \rightarrow C$

$A, D \rightarrow E$

$B \rightarrow D$

$A, F \rightarrow B$

- Compute $\{A, B\}^+$ $\{A, B\}^+ = \{A, B, \quad \quad \quad \}$
- Compute $\{A, F\}^+$ $\{A, F\}^+ = \{A, F, \quad \quad \quad \}$

Closure Example

$R(A, B, C, D, E, F)$

$A, B \rightarrow C$

$A, D \rightarrow E$

$B \rightarrow D$

$A, F \rightarrow B$

- Compute $\{A, B\}^+$ $\{A, B\}^+ = \{A, B, C, D, E\}$
- Compute $\{A, F\}^+$ $\{A, F\}^+ = \{A, F, B, C, D, E\}$

What is the key of R?

Closure Example 2

Practice yourselves:

$R(A,B,C,D)$

$A, B \rightarrow C$

$A, D \rightarrow B$

$B \rightarrow D$

- Compute $\{A,B\}^+$ $\{A,B\}^+ = \{A, B, \quad \quad \quad \}$
- Compute $\{A,D\}^+$ $\{A,D\}^+ = \{A, D, \quad \quad \quad \}$
- Compute $\{B,D\}^+$ $\{B,D\}^+ = \{B, D, \quad \quad \quad \}$

What is the key of R?

Functional Dependencies and Keys



- Assume $R=(A_1,...A_n,B_1,...B_m,C_1,...C_k)$ is a relation with no duplicates
- Suppose **$A_1,A_2,...A_n \rightarrow$ all attributes**
 - i.e., **$A_1,A_2,...A_n \rightarrow A_1,...A_n,B_1,...B_m,C_1,...,C_k$**
 - The group of attributes **$A_1,...,A_n$ is a key** that functionally determine the complete tuple.

$R(A,B,C,D)$

$\{A,B\}^+ = \{A, B, C, D\}$

$A, B \rightarrow C$

$A, D \rightarrow B$

$B \rightarrow D$

Keys

- A **superkey** is a set of attributes A_1, \dots, A_n such that they functionally determine the complete tuple.
 - **Ex:** $R(A, B, C, D, E, F)$ with FDs $\{AB \rightarrow C; AD \rightarrow E; B \rightarrow DA; F \rightarrow B\}$
 $\{A, C, F\}$ is a **superkey** for R
- A **key** is a minimal key
 - A superkey and for which no subset is a key
 - **Ex:** $\{A, F\}$ is a **minimal key** for R

Computing (Super)Keys

- Given $R=(A_1,...,A_n,B_1,..B_m,C_1,..C_k)$, let X be a subset of the attributes for R , i.e.,
$$X \subseteq \{A_1,...,A_n,B_1,..B_m,C_1,..C_k\}$$
- For all subsets X , compute X^+
- If X^+ is equal to [all attributes], then X is a **superkey**
- Minimal $X(s)$ is/are the **key(s)**
 - Can we have more than one key ?
 - YES

Computing Keys – Example1

Product(name, price, category, color)

FDs:

name, category \rightarrow price

category \rightarrow color

Closures:

$\{name\}^+ = \{name\}$

$\{price\}^+ = \{price\}$

$\{category\}^+ = \{category, color\}$

$\{color\}^+ = \{color\}$

- What is the key?

Key

$\{name, price\}^+ = \{name, price\}$

$\{name, category\}^+ = \{name, category, price, color\}$

$\{name, color\}^+ = \{name, color\}$

$\{price, category\}^+ = \{price, category, color\}$

$\{price, color\}^+ = \{price, color\}$

$\{category, color\}^+ = \{category, color\}$

Superkey

$\{name, price, category\}^+ = \{name, price, category, color\}$

$\{name, price, color\}^+ = \{name, price, color\}$

Superkey

$\{name, category, color\}^+ = \{name, price, category, color\}$

$\{price, category, color\}^+ = \{price, category, color\}$

Superkey

$\{name, price, category, color\}^+ = \{name, price, category, color\}$

Functional Dependency

- Back to Example:

**Student(SSN, sName, address,
HScode, HSname, HScity, GPA, priority)**

- **Functional dependencies:**

$SSN \rightarrow sName$

$SSN \rightarrow address$

$SSN \rightarrow HScode$

$HScode \rightarrow HSname, HScity$

$HSname, HScity \rightarrow HScode$

$SSN \rightarrow GPA$

$GPA \rightarrow priority$

We assume that each student has one (current) address, and has graduated from one high schools.

From the last2 above we can derive $SSN \rightarrow priority$

Computing Keys – Example3

Student(SSN, sName, address, HScode, HSname, HScity, GPA, priority)

- FDs:**

SSN \rightarrow sName, address,
HScode, GPA

HScode \rightarrow HSname, HScity

HSname, HScity \rightarrow HScode

GPA \rightarrow priority

$\{SSN\}^+ = \{SSN, sName, address, HSname, HScity, GPA, priority\}$

$\{sName\}^+ = \{sName\}$

$\{HScode\}^+ = \{HScode, HSname, HScity\}$

$\{HSname\}^+ = \{HSname\}$

$\{HScity\}^+ = \{HScity\}$

$\{GPA\}^+ = \{GPA, priority\}$

$\{priority\}^+ = \{priority\}$

- What is the key?**

$\{SSN, sName\}^+ = \{SSN, sName, address, GPA, priority\}$

$\{SSN, address\}^+ = \{SSN, sName, address, , HScity, GPA, priority\}$

$\{SSN, HScode\}^+ = \{SSN, sName, address, HScode, HSname, HScity, GPA, priority\}$

$\{SSN, HSname\}^+ = \{SSN, sName, address, HSname, GPA, priority\}$

$\{SSN, HScity\}^+ = \{SSN, sName, address, HScity, GPA, priority\}$

$\{SSN, GPA\}^+ = \{SSN, sName, address, GPA, priority\}$

$\{SSN, priority\}^+ = \{SSN, sName, address, GPA, priority\}$

Computing Keys – Example3



$\{sName, address\}^+ = \{sName, address\}$
 $\{sName, HScode\}^+ = \{sName, HScode, HSname, Hscity\}$
 $\{sName, HSname\}^+ = \{sName, HSname\}$
 $\{sName, HScity\}^+ = \{sName, HScity\}$
 $\{sName, GPA\}^+ = \{sName, GPA, priority\}$
 $\{sName, priority\}^+ = \{sName, priority\}$

$\{address, HScode\}^+ = \{address, HScode, HSname, Hscity\}$
 $\{address, HSname\}^+ = \{address, HSname\}$
 $\{address, HScity\}^+ = \{address, HScity\}$
 $\{address, GPA\}^+ = \{address, GPA, priority\}$
 $\{address, priority\}^+ = \{address, priority\}$

$\{HScode, HSname\}^+ = \{HScode, HSname, Hscity\}$
 $\{HScode, HScity\}^+ = \{HScode, HSname, Hscity\}$
 $\{HScode, GPA\}^+ = \{HScode, HSname, Hscity, GPA, priority\}$
 $\{HScode, priority\}^+ = \{HScode, HSname, Hscity, priority\}$

$\{HSname, HScity\}^+ = \{HScode, HSname, Hscity\}$
 $\{HSname, GPA\}^+ = \{HScode, HSname, Hscity, GPA, priority\}$
 $\{HSname, priority\}^+ = \{HScode, HSname, Hscity, priority\}$

$\{HScity, GPA\}^+ = \{HScity, GPA, priority\}$
 $\{HScity, priority\}^+ = \{HScity, priority\}$
 $\{GPA, priority\}^+ = \{GPA, priority\}$

Complete the rest:

- Closures for subsets with three attributes
- Closures for subsets with four attributes
- Closures for subsets with five attributes
- Closures for subsets with six attributes
- Closures for subsets with seven attributes
- Closure for the complete set

Key or Keys?

- Can a relation have more than one key?
— Yes.

- Examples:

For $R(A,B,C)$

$A \rightarrow B,$
 $B \rightarrow C$
 $C \rightarrow A$

3 Keys:
A or B or C

$AB \rightarrow C,$
 $BC \rightarrow A$

2 Keys:
AB or BC

$A \rightarrow BC,$
 $B \rightarrow AC$

2 Keys:
A or B

Back to the main problem...

- Given a relation schema, we need to decide whether it is a good design
 - Such a decision must be guided by an understanding of what problems, if any, arise from the current schema.
 - Redundancy, Update/Insert/Delete anomalies
 - FDs that hold on the relation may cause such problems.
 - Example: `hourly_emp` relation

ssn	name	dept	rating	hourly_pay	num_hours
111-11-1111	Kelly	123	5	18	40
222-11-2222	Kyle	124	4	16	40
333-11-3333	John	124	4	16	20
444-11-4444	Roseanne	123	4	16	20
555-11-5555	Min	123	5	18	40

Key : ssn FDs: $ssn \rightarrow name, dept, rating, num_hours$
 $rating \rightarrow hourly_pay$

Back to the main problem...

- Several “Normal Forms” have been proposed. If a relation is in one of these normal forms, we know that certain kinds of problems does not exist.
 - BCNF (most important normal forms from DB design standpoint)
 - BCNF - Main Idea: We want all attributes in every tuple to be determined by the tuple’s key attributes, i.e. part of a *superkey*
 - $X \rightarrow A$ is OK if X is a (super)key
 - $X \rightarrow A$ is not OK otherwise
- What does this say about redundancy?*

ssn	name	dept	rating	hourly_pay	num_hours
111-11-1111	Kelly	123	5	18	40
222-11-2222	Kyle	124	4	16	40
333-11-3333	John	124	4	16	20
444-11-4444	Roseanne	123	4	16	20
555-11-5555	Min	123	5	18	40

Key : ssn **FDs**: ssn \rightarrow name,dept,rating, num_hours
 rating \rightarrow hourly_pay

Design by Decomposition – Eliminate Anomalies

- Main idea:
 - $X \rightarrow A$ is OK if X is a (super)key
 - $X \rightarrow A$ is not OK otherwise
 - Need to decompose the table, but how?

Decompositions in General

$$R(A_1, \dots, A_n, B_1, \dots, B_m, C_1, \dots, C_p)$$

$$R_1(A_1, \dots, A_n, B_1, \dots, B_m)$$
$$R_2(A_1, \dots, A_n, C_1, \dots, C_p)$$

R_1 = projection of R on $A_1, \dots, A_n, B_1, \dots, B_m$

R_2 = projection of R on $A_1, \dots, A_n, C_1, \dots, C_p$

Lossless Decomposition

$R(A_1, \dots, A_n, B_1, \dots, B_m, C_1, \dots, C_p)$

$R_1(A_1, \dots, A_n, B_1, \dots, B_m)$

$R_2(A_1, \dots, A_n, C_1, \dots, C_p)$

- Decomposition of R into R_1 and R_2 is lossless if,
 1. $\{A_1, \dots, A_n, B_1, \dots, B_m\} \cup \{A_1, \dots, A_n, C_1, \dots, C_p\} = \{A_1, \dots, A_n, B_1, \dots, B_m, C_1, \dots, C_p\}$
 2. $R_1 \bowtie R_2 = R$

Lossless Decomposition

ssn	name	dept	rating	hourly_pay	num_hours
111-11-1111	Kelly	123	5	18	40
222-11-2222	Kyle	124	4	16	40
333-11-3333	John	124	4	16	20
444-11-4444	Roseanne	123	4	16	20
555-11-5555	Min	123	5	18	40

Key : ssn

FDs: ssn → name,dept,rating,num_hours
rating → hourly_pay

Hourly_Emps

H1

ssn	name	dept	rating	num_hours
111-11-1111	Kelly	123	5	40
222-11-2222	Kyle	124	4	40
333-11-3333	John	124	4	20
444-11-4444	Roseanne	123	4	20
555-11-5555	Min	123	5	40

H2

rating	hourly_pay
4	16
5	18

- $\{ssn, name, dept, rating, num_hours\} \cup \{rating_hourly_pay\} = \{ssn, name, dept, rating, num_hours, rating_hourly_pay\}$
- $H1 \bowtie H2 = \text{Hourly_Emps}$

Boyce-Codd Normal Form

Definition. A relation R is in BCNF if:
Whenever $X \rightarrow B$ is a non-trivial dependency,
then X is a key or superkey.
– i.e., $X^+ = \{\text{all attributes}\}$

There are no
“bad” FDs

Boyce-Codd Normal Form

Definition. A relation R is in BCNF if:
 Whenever $X \rightarrow B$ is a non-trivial dependency,
 then X is a key or superkey.
 — i.e., $X^+ = \{\text{all attributes}\}$

hourly_emp (SSN, name, dept, rating, hourly_pay, num_hours)

Key: {SSN}

$\text{ssn} \rightarrow \text{name, dept, rating, num_hours}$
 $\text{rating} \rightarrow \text{hourly_pay}$

hourly_emp is not in BCNF.

Not every FD has a key on the left hand side

Student(SSN, sName, address, HScore, HSname, HScity, GPA, priority)

Key: {SSN, HScore}

$\text{SSN} \rightarrow \text{sName, address, GPA}$
 $\text{HScore} \rightarrow \text{HSname, HScity}$
 $\text{HSname, HScity} \rightarrow \text{Hscore}$
 $\text{GPA} \rightarrow \text{priority}$

Student is not in BCNF.

Not every FD has a key on the left hand side

Boyce-Codd Normal Form – Example1

Given $R(A,B,C,D)$

$AB \rightarrow C$

$BC \rightarrow D$

$CD \rightarrow A$

$AD \rightarrow B$

Calculate:

$\{A,B\}^+ = \{A,B,C,D\}$ **key**

$\{B,C\}^+ = \{B,C,D,A\}$ **key**

$\{C,D\}^+ = \{C,D,A, B\}$ **key**

$\{A,D\}^+ = \{A,D,B,C\}$ **key**

In BCNF

Boyce-Codd Normal Form – Example2

Given $R(A,B,C,D,E)$

$AB \rightarrow C$

$DE \rightarrow C$

$B \rightarrow D$

~~$BC \rightarrow B$~~ trivial FD

Calculate:

$\{A,B\}^+ = \{A,B,C,D\}$ X

$\{D,E\}^+ = \{D,E,C\}$ X

$\{B\}^+ = \{B,D\}$ X

Not in BCNF

Boyce-Codd Normal Form – Example3

Given $R(A,B,C,D)$

$AB \rightarrow C$

$AB \rightarrow D$

$C \rightarrow A$

$D \rightarrow B$

Calculate:

$\{A,B\}^+ = \{A,B,C,D\}$ **key**

Not in BCNF

$\{C\}^+ = \{C,A\}$ **X**

$\{D\}^+ = \{D,B\}$ **X**

Lossless BCNF Decomposition

- Next we will study algorithm to decompose a relational schema into sub-schemas which are in BCNF such that the decomposition is lossless

- **Setting:**

Given relation **R**, and

F, FDs for **R**

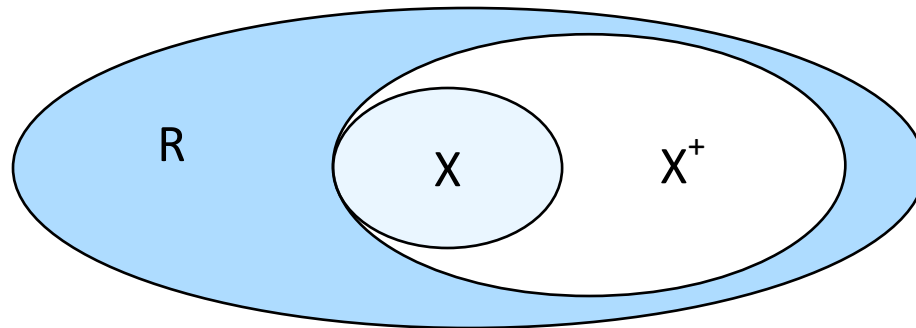
Suppose relation **R** has BCNF violation **X** \rightarrow **Y**.

Decomposition to Reach BCNF (II)



The FD $X \rightarrow Y$ violates BCNF.

1. Expand X to include X^+ . (Cannot be all attributes - why?)
2. Decompose R into $R_1(X^+)$ and $R_2(X, \text{rest})$, i.e., $X \cup (R - X^+)$.



3. Find the FD's for the decomposed relations.
 - Project the FD's from F^+ on R_1 and R_2 :
 - calculate all consequents of F that involve only attributes from R_1 and R_2
4. Iterate over all the resulting sub schemes until all in BCNF

Note: Any table with only 2 attributes is always in BCNF!!!

BCNF Decomposition Algorithm

Input: relation R and F (FDs for R)

Output: decomposition of R into BCNF relations with “lossless join”

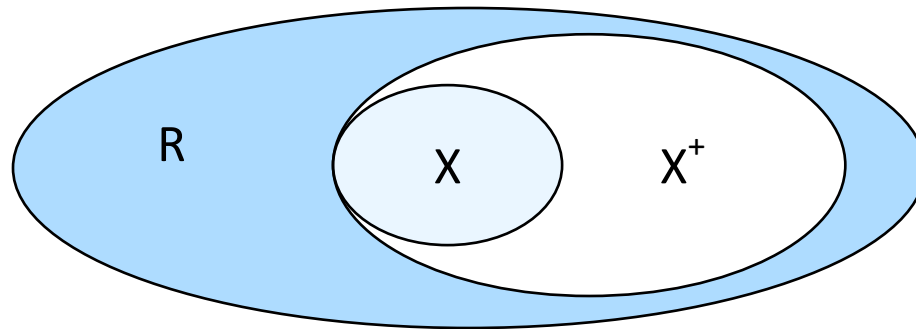
- Compute keys for R
- Repeat until all relations are in BCNF:
 - Pick any R' with $X \rightarrow Y$ that violates BCNF
 - Decompose R' into $R_1(X^+)$ and $R_2(X, \text{rest})$
 - Compute FDs for R_1 and R_2
 - Compute keys for R_1 and R_2

Decomposition to Reach BCNF (II)



The FD $X \rightarrow Y$ violates BCNF.

1. Expand X to include X^+ .
 - Cannot be all attributes - why?
2. Decompose R into $R_1(X^+)$ and $R_2(X, \text{rest})$, i.e., $X \cup (R - X^+)$.



How do we
calculate this?

3. Find the FD's for the decomposed relations.
 - Project the FD's from F on R_1 and R_2 :
 - calculate all consequents of F that involve only attributes from R_1 and R_2
4. Iterate over all the resulting sub schemes until all in BCNF

How to find the FD's for the decomposed relations?

Let R have a schema **R(A,B,C,D)**

R1 have a schema **R1(A,C)**

FD over R be:

$A \rightarrow B$ and $B \rightarrow C$

How to find the FD's for the decomposed relations?



Algorithm to compute the set of FD's that hold on R1

Input: Relation R

R1, a sub-schema of R.

Set of FDs, F that hold in R

Output: The set of FDs that hold in R1.

Method:

Let T be the set of FDs that hold in $R1$ (initially empty).

- For each X that is a subset of $R1$, do
 - Compute X^+
 - For each attribute B in X^+ in such that:
 - $\Rightarrow B$ is in $R1$
 - $\Rightarrow B$ is not in X
 - Add $X \rightarrow B$ to T (i.e., the functional dependency $X \rightarrow B$ holds in $R1$)
- Eliminate trivial dependencies from T

Example - 1

Let R have a schema $R(A,B,C,D)$

R1 have a schema $R1(A,C)$

FD over R be:

$A \rightarrow B$ and $B \rightarrow C$

- Compute $\{A\}^+ = \{A,B,C\}$
 - hence dependency $A \rightarrow C$ holds in R1
- Compute $\{C\}^+ = \{C\}$
 - no new dependency gets added.
- Compute $\{AC\}^+ = \{ABC\}$
 - $AC \rightarrow AC$ holds, but it is a trivial dependency. Therefore, no new dependency gets added.

In general you can limit search as follows:

1. It is not necessary to consider the closure of the set of **all attributes**
 - For example, $\{AC\}^+$ need not have been considered in the above example
2. Not necessary to consider a set of attributes that does not contain the “left hand side” of any dependency.
 - $\{C\}^+$ need not have been considered in the above example
3. Not necessary to consider a set that contains an attribute that is not in the “left hand side” of any functional dependency
 - $\{AC\}^+$ need not have been considered in the above example.

Example - 2

Consider $R(A,B,C,D,E)$ and $R1(A,B,C)$

FD on R be $A \rightarrow D$, $B \rightarrow E$, $DE \rightarrow C$

- Compute $\{A\}^+ == \{A,D\}$
 - no dependency gets added.
- Compute $\{B\}^+ == \{B,E\}$
 - no dependency gets added
- $\{C\}^+$ does not need to be considered since $\{C\}$ not in the left hand side of any FD
- Compute $\{AB\}^+ == \{A,B,C,D,E\}$
 - add dependency $AB \rightarrow C$
- $\{AC\}^+$ and $\{BC\}^+$ do not need to be considered since $\{C\}$ not in the left hand side of any FD
- Since $\{AB\}^+ ==$ all attributes in R, $\{ABC\}$ need not be considered.
- Hence, the only dependency on R1 is: $AB \rightarrow C$

Example - 2



Consider $R(A,B,C,D,E)$ and $R1(A,B,C)$

FD on R be $A \rightarrow D$, $B \rightarrow E$, $DE \rightarrow C$

BCNF Decomposition – Example1

Given $R(A,B,C,D,E)$

with functional dependencies:

$D \rightarrow B$

$CE \rightarrow A$

a. In BCNF?

$\{D\}^+ = \{D,B\}$ D is not a key and $D \rightarrow B$ violates BCNF.

$\{CE\}^+ = \{C,E,A\}$ CE is not a key and $CE \rightarrow A$ violates BCNF.

The Key for R is $\{CDE\}$

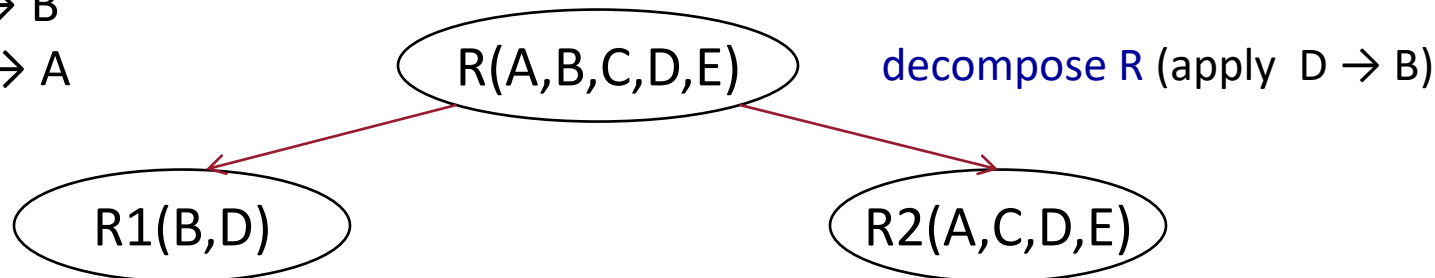
BCNF Decomposition – Example1 (cont.)



Given $R(A,B,C,D,E)$ with functional dependencies:

$D \rightarrow B$

$CE \rightarrow A$



Compute FDs for $R1$: $D \rightarrow B$

Compute key for $R1$: D

(see next slide)

(in BCNF)

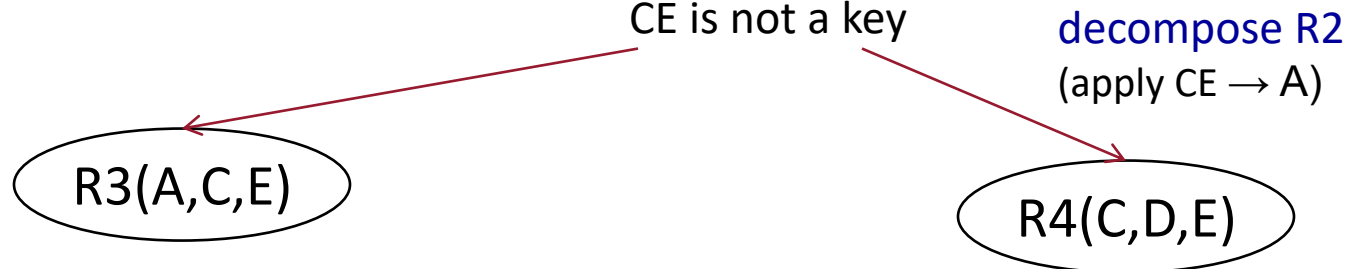
Any table with only 2 attributes is always in BCNF!!!

Compute FDs for $R2$: $CE \rightarrow A, CDE \rightarrow A$ (see next slide)

Compute keys for $R2$: CDE (see next slide)

(not in BCNF) : $CE \rightarrow A$ violates BCNF,

CE is not a key



Compute FDs for $R3$: $CE \rightarrow A$

Compute keys for $R3$: CE

(see next-next slide)

(in BCNF)

Compute FDs for $R4$: None

Compute keys for $R4$: CDE

(see next-next slide)

(in BCNF)

$R(A,B,C,D,E)$ is decomposed into $R1(B,D)$, $R3(A,C,E)$, and $R4(C,D,E)$

The decomposition is **dependency-preserving**. Why?

BCNF Decomposition – Example1(cont.)

Given $R(A,B,C,D,E)$

$D \rightarrow B$

$CE \rightarrow A$

Compute FD's for $R_1(B,D)$:

$\{B\}^+$
 $\{D\}^+$
 $\{B,D\}^+$

$\{D\}$ is the key

Compute FD's for $R_2(A,C,D,E)$:

$\{A\}^+$	$\{A,C,D\}^+$
$\{C\}^+$	$\{A,C,E\}^+$
$\{D\}^+$	$\{A,D,E\}^+$
$\{E\}^+$	$\{C,D,E\}^+$
$\{A,C\}^+$	$\{A,C,D,E\}^+$
$\{A,D\}^+$	
$\{A,E\}^+$	
$\{C,D\}^+$	
$\{C,E\}^+$	
$\{D,E\}^+$	

$\{CDE\}$ is the key

BCNF Decomposition – Example1(cont.)

Given $R(A,B,C,D,E)$

$D \rightarrow B$

$CE \rightarrow A$

Compute FD's for $R_1(B,D)$:

$\{B\}^+$	
$\{D\}^+ = \{B,D\}$	$D \rightarrow B$ added
$\{B,D\}^+$	

$\{D\}$ is the key

Compute FD's for $R_2(A,C,D,E)$:

$\{A\}^+$	$\{A,C,D\}^+$
$\{C\}^+ = \{C\}$	$\{A,C,E\}^+$
$\{D\}^+ = \{B,D\}$	$\{A,D,E\}^+$
$\{E\}^+ = \{E\}$	$\{C,D,E\}^+ = \{C,D,E,B,A\}$ $CDE \rightarrow A$ added
$\{A,C\}^+$	$\{A,C,D,E\}^+$
$\{A,D\}^+$	
$\{A,E\}^+$	
$\{C,D\}^+ = \{C,D,B\}$	
$\{C,E\}^+ = \{C,E,A\}$ $CE \rightarrow A$ added	
$\{D,E\}^+ = \{D,E,B\}$	

$\{CDE\}$ is the key

BCNF Decomposition – Example1(cont.)

Given $R_2(A,C,D,E)$

$CE \rightarrow A$

$CDE \rightarrow A$

Compute FD's for $R_3(A,C,E)$:

$\{A\}^+$
 $\{C\}^+$
 $\{E\}^+$
 $\{A,C\}^+$
 $\{A,E\}^+$
 $\{C,E\}^+$
 $\{A,C,E\}^+$

$\{CE\}$ is the key

Compute FD's for $R_4(C,D,E)$:

$\{C\}^+$
 $\{D\}^+$
 $\{E\}^+$
 $\{C,D\}^+$
 $\{C,E\}^+$
 $\{D,E\}^+$
 $\{C,D,E\}^+$

BCNF Decomposition – Example1(cont.)

Given $R_2(A,C,D,E)$

$CE \rightarrow A$

$CDE \rightarrow A$

Compute FD's for $R_3(A,C,E)$:

~~$\{A\}^+$~~
 $\{C\}^+ = \{C\}$
 $\{E\}^+ = \{E\}$
 ~~$\{A,C\}^+$~~
 ~~$\{A,E\}^+$~~
 $\{C,E\}^+ = \{C,E,A\}$ $CE \rightarrow A$ added
 ~~$\{A,C,E\}^+$~~

$\{CE\}$ is the key

Compute FD's for $R_4(C,D,E)$:

$\{C\}^+ = \{C\}$
 $\{D\}^+ = \{D\}$
 $\{E\}^+ = \{E\}$
 $\{C,D\}^+ = \{C,D\}$
 $\{C,E\}^+ = \{C,E,A\}$
 $\{D,E\}^+ = \{D,E\}$
 ~~$\{C,D,E\}^+$~~

$\{CDE\}$ is the key

BCNF Decomposition – Example3

- Consider a relation with schema **R(A,B,C,D)** and **FD's**:
 $BC \rightarrow D$,
 $BC \rightarrow A$,
 $D \rightarrow B$,
 $A \rightarrow C$
 - Find the minimal key(s) for this relation.
 - Is R in BCNF?
 - If not in BCNF, decompose the relation into collections of relations that are in BCNF.
 - Are the functional dependencies preserved in the BCNF decomposition?

BCNF Decomposition – Example2

Given **Hourly_Emps**(ssn, name,dept,rating,num_hours,rating_hourly_pay)
with functional dependencies:

ssn \rightarrow name,dept,rating,num_hours

rating \rightarrow hourly_pay

a. In BCNF?

{ssn}⁺ = {ssn,name,dept,rating,num_hours}

ssn is a key and first functional dependency doesn't violate BCNF.

{rating}⁺ = {rating,hourly_pay}

rating is not a key and second functional dependency violates BCNF.

Therefore, Hourly_Emps is not in BCNF.

BCNF Decomposition – Example2 (cont.)



Hourly_Emps(ssn,name,dept,rating,num_hours,rating,hourly_pay)

ssn \rightarrow name,dept,rating,num_hours

rating \rightarrow hourly_pay

Hourly_Emps(ssn,name,dept,rating,num_hours,rating,hourly_pay)

decompose Hourly_Emps
(rating \rightarrow hourly_pay)

H2(rating,hourly_pay)

Compute FDs for H2: rating \rightarrow hourly_pay

Compute key for H2: rating

(in BCNF)

H1(ssn,name,dept,rating,num_hours,rating)

Compute FDs for H1: ssn \rightarrow name,dept,rating,num_hours

Compute key for H1: ssn

(in BCNF)

Hourly_Emps is decomposed into:

H1(ssn,name,dept,rating,num_hours,rating) and H2(rating,hourly_pay)

The BCNF decomposition is dependency-preserving.

BCNF Decomposition – Example4



Student(SSN, sName, address, HScore, HSname, HScity, GPA, priority)

FDs:

SSN \rightarrow sName, address, GPA

GPA \rightarrow priority

HScode \rightarrow HSname, HScity

HSname, HScity \rightarrow Hscore

Key : SSN, HScore

a. In BCNF?

No. Several violations.

For example:

$\{HSCode\}^+ = \{HSCode, HSname, HScity\}$

HSCode is not a key , $HSCode \rightarrow HSname, HScity$ violates BCNF.

$\{SSN\}^+ = \{SSN, sName, address, GPA, priority\}$

SSN is not a key , $SSN \rightarrow sName$ and $SSN \rightarrow address$ violates BCNF.

BCNF Decomposition – Example2 (cont.)

Student(SSN, sName, address, HScore, HSname, HScity, GPA, priority)

SSN \rightarrow sName, address, GPA

GPA \rightarrow priority

HScore \rightarrow HSname, Hscity

HSname, HScity \rightarrow Hscore

- b. Decompose Student (use HScore \rightarrow HSname, HScity)

S1(HScore, HSname, HScity)

FDs: HScore \rightarrow HSname, Hscity ; HSname, HScity \rightarrow Hscore

Keys: {HScore} and {HSname, Hscity}

(in BCNF)

S2(SSN, sName, address, HScore, GPA, priority)

FDs: SSN \rightarrow sName, address, GPA, priority ; GPA \rightarrow priority

Key: {SSN, HScore}

(not in BCNF)

Decompose S2 (use GPA \rightarrow priority)

S3(GPA, priority) (in BCNF)

S4(SSN, sName, address, HScore, GPA) (not in BCNF)

(next slide)

BCNF Decomposition – Example2 (cont.)

Student(SSN, sName, address, HScore, HSname, HScity, GPA, priority)

SSN \rightarrow sName, address, GPA

GPA \rightarrow priority

HScore \rightarrow HSname, Hscity

HSname, HScity \rightarrow Hscore

S4(SSN, sName, address, HScore, GPA) (not in BCNF)

FDs: SSN \rightarrow sName, address, GPA, priority

Key: {SSN, HScore}

Decompose (use SSN \rightarrow sName, address, GPA, priority)

S5(SSN, sName, address, GPA, priority) (in BCNF)

FDs: SSN \rightarrow sName, address, GPA, priority

Key: {SSN, HScore}

S6(SSN, HScore) (in BCNF)

Student is decomposed into S1, S3, S5, and S6

BCNF Decomposition for Student

Student

SSN	sName	address	HSCode	HSname	HScity	GPA	Priority
1111	Kyle	Everett	PHS	Pullman High School	Pullman	3.4	2
1111	Kyle	Everett	EHS	Everett High School	Everett	3.4	2
2222	John	Pullman	POHS	Potlatch High School	Potlatch	3.0	3
2222	John	Pullman	MHS	Moscow High School	Moscow	3.0	3
2222	John	Pullman	PHS	Pullman High School	Pullman	3.0	3

S1

HSCode	HSname	HScity
PHS	Pullman High School	Pullman
EHS	Everett High School	Everett
POHS	Potlatch High School	Potlatch
MHS	Moscow High School	Moscow

In BCNF

S2

SSN	sName	address	HSCode	GPA	Priority
1111	Kyle	Everett	PHS	3.4	2
1111	Kyle	Everett	EHS	3.4	2
2222	John	Pullman	POHS	3.0	3
2222	John	Pullman	MHS	3.0	3
2222	John	Pullman	PHS	3.0	3

Not in BCNF

BCNF Decomposition for Student

S2

SSN	sName	address	HSCode	GPA	Priority
1111	Kyle	Everett	PHS	3.4	2
1111	Kyle	Everett	EHS	3.4	2
2222	John	Pullman	POHS	3.0	3
2222	John	Pullman	MHS	3.0	3
2222	John	Pullman	PHS	3.0	3

S3

GPA	Priority
3.4	2
3.0	3

In BCNF

S4

SSN	sName	address	HSCode	GPA
1111	Kyle	Everett	PHS	3.4
1111	Kyle	Everett	EHS	3.4
2222	John	Pullman	POHS	3.0
2222	John	Pullman	MHS	3.0
2222	John	Pullman	PHS	3.0

Not in BCNF

BCNF Decomposition for Student

S4

SSN	sName	address	HSCode	GPA
1111	Kyle	Everett	PHS	3.4
1111	Kyle	Everett	EHS	3.4
2222	John	Pullman	POHS	3.0
2222	John	Pullman	MHS	3.0
2222	John	Pullman	PHS	3.0

S5

SSN	sName	address	GPA
1111	Kyle	Everett	3.4
2222	John	Pullman	3.0

In BCNF

S6

SSN	HSCode
1111	PHS
1111	EHS
2222	POHS
2222	MHS
2222	PHS

In BCNF

BCNF Decomposition for Student

S1

HSCode	HSname	HScity
PHS	Pullman High School	Pullman
EHS	Everett High School	Everett
POHS	Potlatch High School	Potlatch
MHS	Moscow High School	Moscow

S3

GPA	Priority
3.4	2
3.0	3

S5

SSN	sName	address	GPA
1111	Kyle	Everett	3.4
2222	John	Pullman	3.0

S6

SSN	HSCode
1111	PHS
1111	EHS
2222	POHS
2222	MHS
2222	PHS

BCNF Decomposition

- **Claim:** The BCNF decomposition algorithm described results in lossless decompositions (i.e., the original can be reconstructed by joining decomposed relations).
- **Proof.** We will not cover. Check the book (section 19.5) for a detailed discussion on lossless decompositions.

Schema Normalization



- So we have learnt that, if a relation R contains redundancy, we need to decompose it into sub-relations R_1, R_2, \dots, R_n such that
 - each R_i is in BCNF, and
 - the decomposition of R into R_1, R_2, \dots, R_n is a lossless decomposition.
- We also learnt an algorithm for BCNF decomposition that is guaranteed to be lossless.
- **Does this also guarantee dependency preservation???**
- **Not exactly....**
 - In some cases it is not possible to decompose a relation into BCNF relations that have both the lossless-join and the dependency preservation.
 - **Example:** see next-next slide

Example of a Non-Dependency Preserving Decomposition



street	city	zip
1025 S Main	Pullman	91163
925 S Main	Pullman	99163
925 N Main	Pullman	99164

FD:

street,city \rightarrow zip

zip \rightarrow city

There are 2 keys :

{street,city} and {street,zip}

zip \rightarrow city is a BCNF violation, so we must decompose into:

R1(street,zip) and **R2(city,zip)**



R1

street	zip
1025 S Main	91163
925 S Main	99163
925 N Main	99164

FD: none

Key: street,zip

R2

city	zip
Pullman	91163
Pullman	99164

FD: zip \rightarrow city

Key: zip

- Decomposition of address into R1 and R2 is lossless.
- Furthermore, R1 and R2 are in BCNF and doesn't contain any redundancy
- However, the decomposition does not preserve FD **street,city \rightarrow zip**.
 - we cannot enforce the FD **street,city \rightarrow zip** by checking FD's in these decomposed relations.

Third Normal Form (3NF)

- The solution to the problem in the previous slide is to relax the BCNF requirement slightly and allow for **some** redundancy.
- This relaxed condition is called Third Normal Form - 3NF.
 - Disadvantage: storage overhead, anomalies.
 - Advantage: preserve dependencies

Third Normal Form (3NF)

- Relation R with FDs F is in **3NF** if, for all $X \rightarrow A$ in F , one of the following is true:
 - $A \in X$ (it is a *trivial* FD), or
 - X is a superkey, or
 - A is part of some (minimal candidate) key for R .
- *Minimality* of a key is crucial in third condition above!
- If R is in BCNF, obviously in 3NF.
- If R is in 3NF, some redundancy is possible. It is a compromise, used when BCNF not achievable (e.g., no “good” decomposition, or performance considerations).
 - *Lossless-join, dependency-preserving decomposition of R into a collection of 3NF relations always possible.*

Third Normal Form (3NF) - Example

street	city	zip
1025 S Main	Pullman	91163
925 S Main	Pullman	99163
925 N Main	Pullman	99164

FD:

street,city \rightarrow zip

zip \rightarrow city

There are 2 keys :

{street,city} and {street,zip}

Not in BCNF

But in 3NF

Summary of Schema Refinement

- If a relation is in BCNF, it is free of redundancies that can be detected using FDs. Thus, trying to ensure that all relations are in BCNF is a good heuristic.
- If a relation is not in BCNF, we can try to decompose it into a collection of BCNF relations.
 - Must consider whether all FDs are preserved. If a lossless-join, dependency preserving decomposition into BCNF is not possible (or unsuitable, given typical queries), should consider decomposition into 3NF.
 - Decompositions should be carried out and/or re-examined while keeping *performance requirements* in mind.