



Text Classification and Naïve Bayes

Multinomial Naïve Bayes: A Worked Example



$$\hat{P}(c) = \frac{N_c}{N}$$

$$\hat{P}(w|c) = \frac{\text{count}(w,c)+1}{\text{count}(c)+|V|}$$

| | Doc | Words | Class |
|----------|-----|-------------------------------------|-------|
| Training | 1 | Chinese Beijing Chinese | c |
| | 2 | Chinese Chinese Shanghai | c |
| | 3 | Chinese Macao | c |
| | 4 | Tokyo Japan Chinese | j |
| Test | 5 | Chinese Chinese Chinese Tokyo Japan | ? |

Priors:

$$P(c) = \frac{3}{4}$$

$$P(j) = \frac{1}{4}$$

Choosing a class:

$$P(c|d5) \propto \frac{3}{4} * \left(\frac{3}{7}\right)^3 * \frac{1}{14} * \frac{1}{14} \approx 0.0003$$

Conditional Probabilities:

$$P(\text{Chinese}|c) = (5+1) / (8+6) = 6/14 = 3/7$$

$$P(\text{Tokyo}|c) = (0+1) / (8+6) = 1/14$$

$$P(\text{Japan}|c) = (0+1) / (8+6) = 1/14$$

$$P(\text{Chinese}|j) = (1+1) / (3+6) = 2/9$$

$$P(\text{Tokyo}|j) = (1+1) / (3+6) = 2/9$$

$$P(\text{Japan}|j) = (1+1) / (3+6) = 2/9$$

$$P(j|d5) \propto \frac{1}{4} * \left(\frac{2}{9}\right)^3 * \frac{2}{9} * \frac{2}{9} \approx 0.0001$$



Naïve Bayes in Spam Filtering

- SpamAssassin Features:
 - Mentions Generic Viagra
 - Online Pharmacy
 - Mentions millions of (dollar) ((dollar) NN,NNN,NNN.NN)
 - Phrase: impress ... girl
 - From: starts with many numbers
 - Subject is all capitals
 - HTML has a low ratio of text to image area
 - One hundred percent guaranteed
 - Claims you can be removed from the list
 - 'Prestigious Non-Accredited Universities'
 - http://spamassassin.apache.org/tests_3_3_x.html



Summary: Naive Bayes is Not So Naive

- Very Fast, low storage requirements
- Robust to Irrelevant Features
 - Irrelevant Features cancel each other without affecting results
- Very good in domains with many equally important features
 - Decision Trees suffer from *fragmentation* in such cases – especially if little data
- Optimal if the independence assumptions hold: If assumed independence is correct, then it is the Bayes Optimal Classifier for problem
- A good dependable baseline for text classification
 - **But we will see other classifiers that give better accuracy**



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