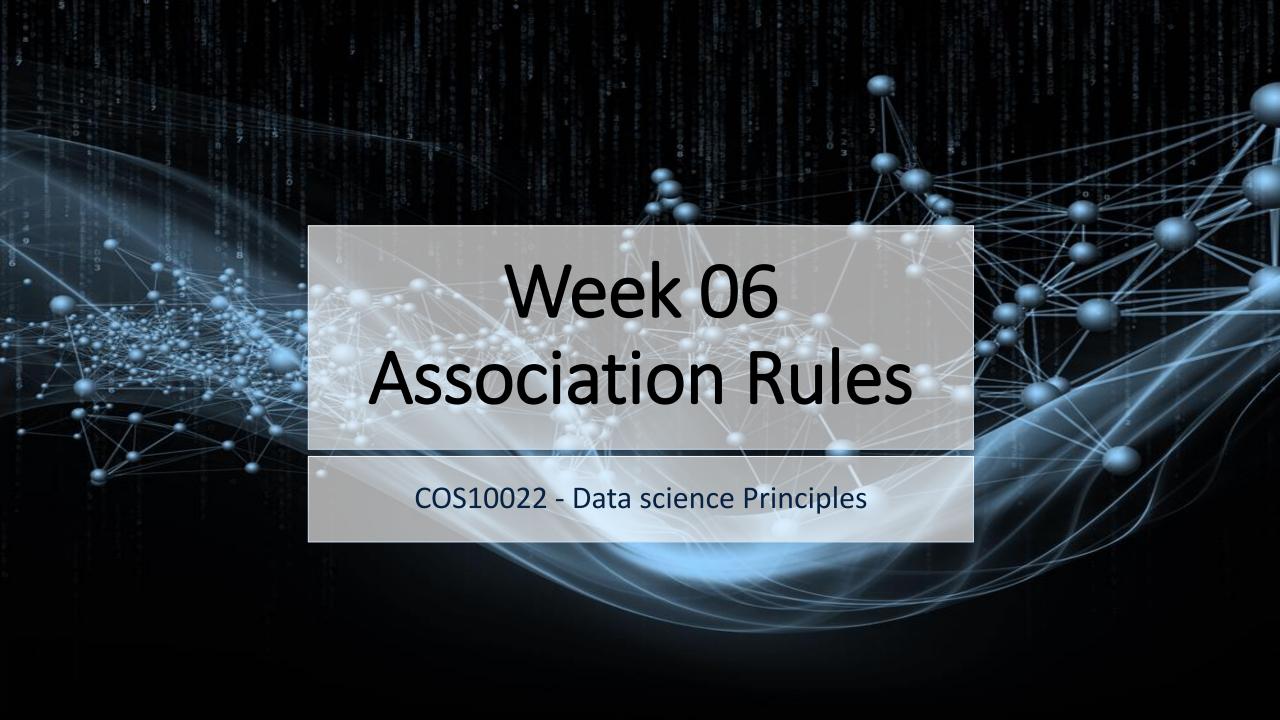


# COS10022 – DATA SCIENCE PRINCIPLES

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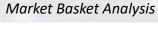


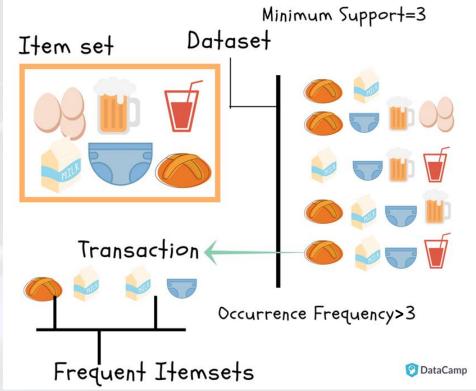


# Outline

- Overview
- Apriori Algorithm
- Evaluation of Candidate Rules
- Examples
- Application of Association Rules
- Validation and Testing
- Diagnostic

- Association rules
  - An unsupervised learning method.
  - A descriptive, not predictive, method.
  - Used to discover interesting hidden relationships in a large dataset.
  - The disclosed relationships are represented as rules or frequent itemsets.
  - Commonly used for mining transactions in database.





- Some questions that association rules can answer:
  - Which products tend to be purchased together?
  - Of those customers who are similar to this person, what products do they tend to buy?
  - Of those customers who have purchased this product, what other similar products do they tend to view or purchase?



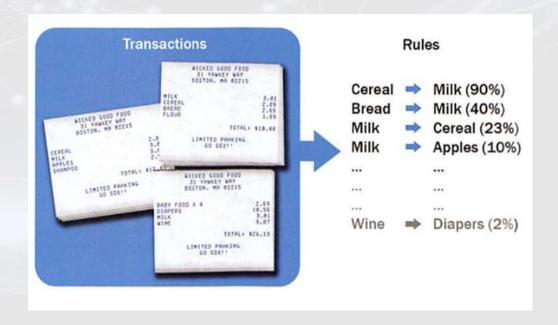




To analyze customer buying habits by finding associations and correlations between the different items that customers place in their shopping baskets.

#### The **general logic** behind association rules:

- A large collection of transactions (depicted as three stacks of receipts, in which each transaction consists of one or more items).
- 2. Association rules go through the **items** being purchased to see what items are **frequently** bought together and to discover a list of **rules** that describe the purchasing behavior.
- 3. The **rules** suggest that when *cereal* is purchased, 90% of the time *milk* is purchased; when *bread* is purchased, 40% of the time *milk* is purchased also; when *milk* is purchased, 23% of the time *cereal* is also purchased.

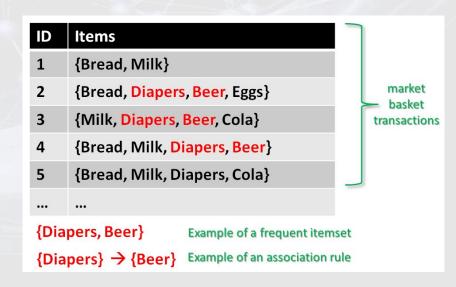


#### Rules

- Each rule is in the form  $X \rightarrow Y$ 
  - Means when Item X is observed, Item Y is also observed.

#### **Itemset**

- A collection of items or individual entities that contain some kind of relationship.
- An itemset containing k items is called a k-itemset.
  - *k*-itemset = {item 1, item 2,...,item *k*}
- Examples:
  - A set of retail items purchased together in one transaction.
  - A set of hyperlinks clicked on by one user in a single session.



## **Apriori Algorithm**

- The most fundamental algorithms for generating association rules.
- One major component of Apriori is support.
  - Given an Itemset L, the support of L is the percentage of transactions that contain L.
  - If 80% of all transactions contain itemset {bread}, then the support of {bread} is 0.8.
  - If 60% of all transactions contain itemset {bread, butter}, then the support of {bread, butter} is 0.6.

## **Frequent Itemset**

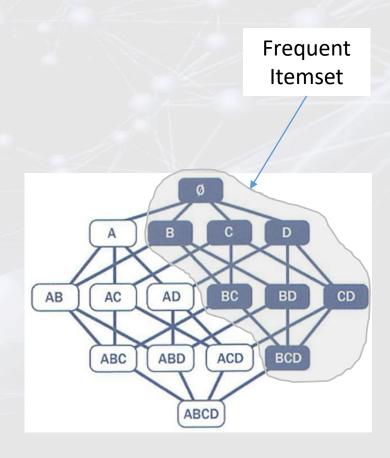
- Items that appear together "often enough" (i.e. meets the minimum support criterion).
  - If the minimum support is set at 0.7, {bread} is considered a frequent itemset; whereas {bread, butter} is not considered as a frequent itemset.

1-itemsets

2-itemsets

## **Apriori Property**

- Also called downward closure property.
- If an item is considered frequent, then any subset of the frequent itemset <u>must</u> also be frequent.
  - If 60% of the transactions contain {bread, jam}, then <u>at least</u> 60% of all the transactions will contain {bread} or {jam}.
  - If the support of {bread, jam} is 0.6, the support of {bread} or {jam} is at least 0.6.
- If itemset {B, C, D} is frequent, then all the subset of this itemset, **shaded in the figure**, must also be frequent itemsets.



#### **Association Rules**

- An implication expression of the form X
   → Y, where X and Y are non-overlapping itemsets.
  - E.g. {Milk, Diaper} → {Beer}
- Generating association rules:
  - Step 1: Find frequent itemsets whose occurrences exceed a predefined minimum support threshold.
  - Step 2: Derive association rules from those frequent itemsets (with the constrains of minimum confidence threshold).

#### **Rule evaluation Metrics**

- **Support** (s): No. of transactions that contain both X and Y out of total no. of transactions.
  - E.g. A support of 2% means that 2% of all the transactions under analysis show that {Milk, Diaper} and {Beer} are purchased together.
- Confidence (c): No. of transactions that contain both X and Y out of total no. of transactions that contains X.
  - E.g. A confidence of 60% means that 60% of customers who purchased {Milk, Diaper} also bought {Beer}

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#### **Creating Frequent Sets**

- Apriori employs an iterative approach known as a level-wise search, where *k-itemsets* are used to explore (*k*+1)-itemsets.
- First, the set of **frequent 1-itemsets** is found by scanning the database to accumulate the count for each item, and collecting those items that satisfy minimum support. The resulting set is denoted **L**<sub>1</sub>.
- Next,  $L_1$  is used to find  $L_2$ , the set of frequent 2-itemsets, which is used to find  $L_3$ , and so on, until no more frequent k-itemsets can be found.
- The finding of each  $L_k$  requires one full scan of the database.

# Example 1

L<sub>1</sub>

Item	Count
Bread	4
Coke	2
Milk	4
Beer	3
Diaper	4
Eggs	1

Items (1-itemsets)

L<sub>2</sub>

Itemset	Count
{Bread,Milk}	3
{Bread,Beer}	2
{Bread,Diaper}	3
{Milk,Beer}	2
{Milk,Diaper}	3
{Beer,Diaper}	3

Pairs (2-itemsets)

(No need to generate candidates involving Coke or Eggs)

Lз

Itemset	Count
{Bread,Milk,Diaper}	2
{Bread,Milk,Beer}	1
{Bread,Diaper,Beer}	2

Triplets (3-itemsets)

Items

Bread, Milk

Bread, Diaper, Beer, Eggs

Milk, Diaper, Beer, Coke

Bread, Milk, Diaper, Beer

Bread, Milk, Diaper, Coke

(5 transactions; 6 types of items)

MinSupp = 3/5=0.6

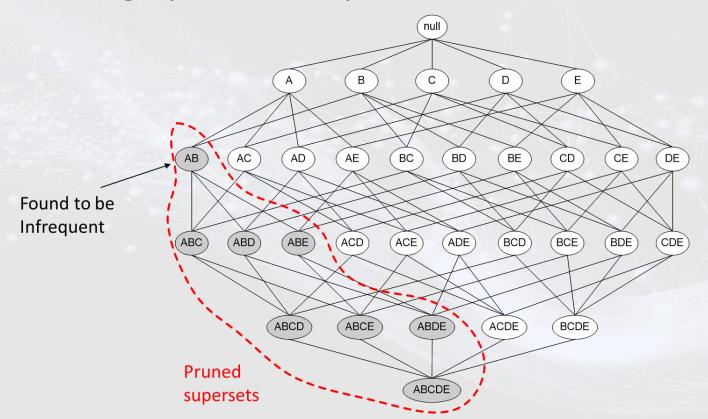
## **Creating Frequent Sets**

• Let's define:

```
C_k as a candidate itemset of size k L_k as a frequent itemset of size k
```

- Main steps of iteration are:
  - 1. Find frequent itemset  $L_{k-1}$  (starting from  $L_1$ )
  - 2. Join step:  $C_k$  is generated by joining  $L_{k-1}$  with itself (cartesian product  $L_{k-1} \times L_{k-1}$ )
  - 3. Prune step (Apriori Property): Any (k-1) size itemset that is not frequent cannot be a subset of a frequent k size itemset, hence should be removed from  $C_k$
  - 4. Frequent set  $L_k$  has been achieved

## Illustrating Apriori Principle



- Any subset of a frequent itemset must also be frequent.
- Itemsets that do not meet the minimum support threshold are pruned away.

#### **Pseudo Code**

```
L_1 = {frequent items};

for (k = 1; L_k != \varnothing; k++) do begin

C_{k+1} = candidates generated from L_k;

for each transaction t in database do

increment the count of all candidates in C_{k+1} that are contained in t

L_{k+1} = candidates in C_{k+1} with min_support

end

return \bigcup_k L_k;
```

# Example 2

 $Sup_{min} = 2$ 

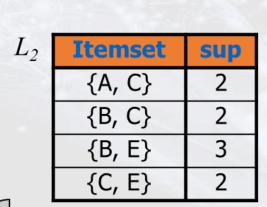
Database TDB

Tid	Items
10	A, C, D
20	В, С, Е
30	A, B, C, E
40	B, E

 $C_{I}$   $\xrightarrow{1^{\text{st}} \text{ scan}}$ 

Itemset	sup
{A}	2
{B}	3
{C}	3
{D}	1
{E}	3

	Itemset	sup
	{A}	2
	{B}	3
+	{C}	3
	{E}	3



2	Itemset	sup
	{A, B}	1
	{A, C}	2
	{A, E}	1
	{B, C}	2
	{B, E}	3
	{C, E}	2

 $C_2$   $2^{\mathrm{nd}}$  scan

Itemset
{A, B}
{A, C}
{A, E}
{B, C}
{B, E}
{C, E}



 $C_3$  **Itemset** {B, C, E}

 $3^{\text{rd}} \operatorname{scan} \xrightarrow{L_3}$ 

Itemset	sup	
{B, C, E}	2	

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The process of creating association rules is two-staged.

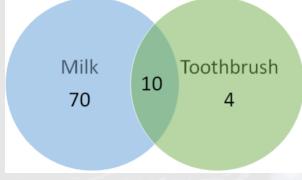
- First, a set of candidate rule based on frequent itemsets is generated.
  - If {Bread, Egg, Milk, Butter} is the frequent itemset, candidate rules will look like:
    - {Egg, Milk, Butter} → {Bread}
    - {Bread, Milk, Butter} → {Egg}
    - {Bread, Egg} → {Milk, Butter}
    - Etc.
- Second, the appropriateness of these candidate rules are evaluated using:
  - Confidence
  - Lift
  - Leverage

#### Confidence

- The measures of certainty or trustworthiness associated with each discovered rule.
- Mathematically, the percentage of transactions that contain both X and Y out of all transactions that contain X.

Confidence(
$$X \rightarrow Y$$
) =  $\frac{Support(X + Y)}{support(X)}$ 

- E.g. if {bread, eggs, milk} has support of 0.15 and {bread, eggs} also has a support of 0.15, the confidence of rule {bread, eggs} → {milk} is 1.
  - This means 100% of the time a customer buys bread and eggs, milk is brought as well. The rule is therefore correct for 100% of the transactions containing bread and eggs.



 $\{Toothbrush\} \rightarrow \{Milk\}:$ Confidence = 10/(10+4) = 0.7

#### Confidence

 A relationship may be thought of as interesting when the algorithm identifies the relationship with a measure of confidence greater than or equal to the predefined threshold (i.e. the minimum confidence).

- Problem with Confidence:
  - Given a rule  $X \rightarrow Y$ , confidence considers only the antecedent (X) and the cooccurrence of X and Y.
  - Cannot tell if a rule contains true implication of the relationship or if the rule is purely coincidental.

#### Lift

- Measures how many times more often X and Y occur together than expected if they are statistically independent of each other.
- A measure of how X and Y are really related rather than coincidentally happening together.

Lift( X 
$$\Rightarrow$$
 Y ) =  $\frac{\text{support}(X + Y)}{\text{support}(X) \times \text{support}(Y)}$ 

- Lift = 1 if X and Y are statistically independent
- Lift > 1 indicates the degree of usefulness of the rule
  - A larger value of lift suggests a greater strength of the association between X and Y.

#### Lift

- E.g. Assuming 1000 transactions,
  - If {milk, eggs} appears in 300, {milk} in 500, and {eggs} in 400 of the transactions, then Lift(milk  $\rightarrow$  eggs) = 0.3 / (0.5 \* 0.4) = 1.5
  - If {milk, bread} appears in 400, {milk} in 500, and {bread} in 400 of the transactions, then Lift(milk  $\rightarrow$  bread) = 0.4/(0.5\*0.4) = 2.0
- Therefore it can be concluded that milk and bread have a stronger association than milk and eggs.

#### Leverage

 Measure the difference in the probability of X and Y appearing together in the dataset compared to what would be expected if X and Y were statistically independent of each other.

Leverage(
$$X \rightarrow Y$$
) = Support( $X + Y$ ) – Support( $X$ ) × Support( $Y$ )

- Leverage = 0 if X and Y are statistically independent
- Leverage > 0 indicates the degree of relationship between X and Y,
  - A larger leverage value indicates a stronger relationship between X and Y.

## Leverage

- E.g. Assuming 1000 transactions,
  - If {milk, eggs} appears in 300, {milk} in 500, and {eggs} in 400 of the transactions, then Leverage(milk → eggs) = 0.3 0.5\*0.4 = 0.1
  - If {milk, bread} appears in 400, {milk} in 500, and {bread} in 400 of the transactions, then Leverage (milk → bread) = 0.4 0.5\*0.4 = 0.2

 It again confirms that milk and bread have a stronger association than milk and eggs.

# Summary

- Assuming 1000 transactions,
  - If {milk, eggs} appears in 300, {milk} in 500, and {eggs} in 400 of the transactions.
  - If {milk, bread} appears in 400, {milk} in 500, and {bread} in 400 of the transactions.

	{Milk} → {Egg}	{Milk} → {Bread}
Confidence	$0.3/_{0.5} = 0.6$	$0.4/_{0.5} = 0.8$
Lift	$0.3/_{(0.5 \times 0.4)} = 1.5$	$0.4/_{(0.5 \times 0.4)} = 2$
Leverage	$0.3 - (0.5 \times 0.4) = 0.1$	$0.4 - (0.5 \times 0.4) = 0.2$
	Smaller	Greater

 Confidence is able to identify trustworthy rules, but it cannot tell whether a rule is coincidental.

• Measures such as lift and leverage not only ensure interesting rules are identified but also filter out the coincidental rules.

 Support, confidence, lift and leverage ensures the discovery of interesting and strong rules from sample dataset.

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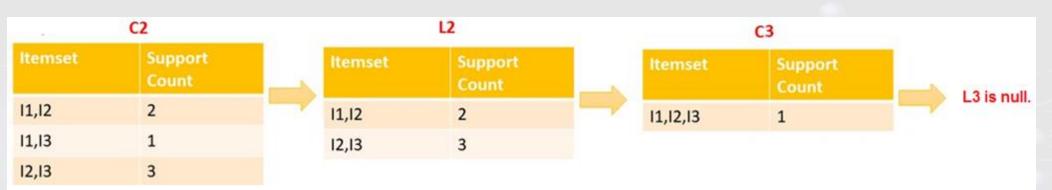
# Example 3

Min\_Supp Count = 2 Min\_Conf = 50%

ransaction	Items	C1	Itemset	Support Count	L1	Itemset	Support Count
D			11	3		11	3
.00	11,12		12	4		12	4
00	12,13,14,15				-		*
300	12,13	-	13	3	Par.	13	3
100	11		14	1			
500	11,12,13		15	1			

Five Market Basket transactions with items labelled as I1, I2, I3 and so on.

- 1. Candidate list generation, C1:
  Start by creating all individual items called candidates and calculate their support counts.
- 2. Create frequent 1-itemsets, L1:
  Remove candidates that fail
  min\_sup count (i.e. I4 and I5).
  No supersets of infrequent
  itemset must be generated and
  tested.



Min\_Supp Count = 2 Min\_Conf = 50%

- Generate second candidate list, C2:C2 is generated by L1 cross join L1.
- Transaction Items
  ID

  100 I1,I2
  200 I2,I3,I4,I5
  300 I2,I3
  400 I1

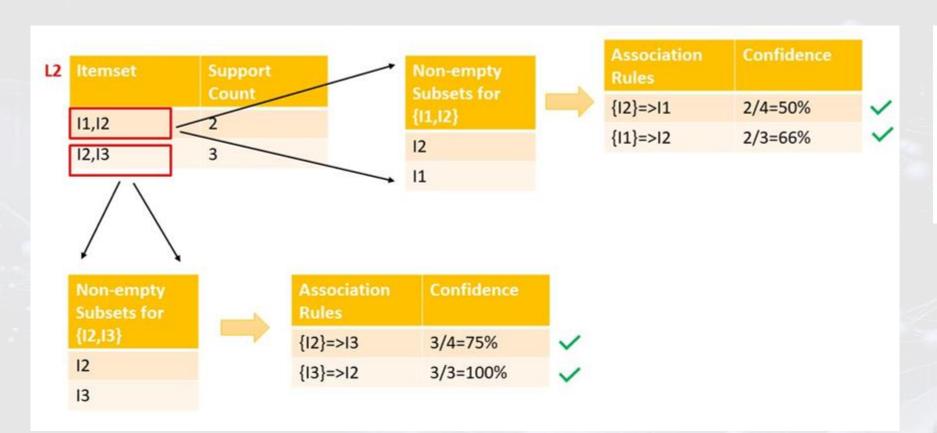
11,12,13

500

- 4. Create Frequent 2itemsets, L2: Remove candidates that fail min sup count.
- {L1, L2} appears in 2 transactions together.
  {L2, L3} appears in 3 transactions together.

{L1, L2, I3} appears in only 1 transaction together.

- 5. Generate thirdcandidate list, C3:C3 is generated by L2cross join L2.
- 6. Support count for {I1, I2, I3} fails min\_supp.
  Association rule mining is completed and there will be no C4 candidate list.



<b>7.</b>	Generate candidate rules: Take the
	last non-empty frequent itemset (i.e.
	L2 = {I1, I2}, {I2, I3}) and Use all the
	non-empty subsets of the frequent
	itemset to generate association rules.

8. Calculate confidence of each candidate rule:

Confidence(
$$X \rightarrow Y$$
) =  $\frac{Support(X + Y)}{support(X)}$ 

L1		
Itemset	Support Count	
11	3	
12	4	
13	3	

9. Strong association rules:

Green ticked are all strong rules satisfying min\_conf >=50% and min\_supp count =2.

Transaction ID	Items
100	11,12
200	12,13,14,15
300	12,13
400	11
500	<b>I1,I2,I3</b> 32

# Example 4

TID	List of Items		
T100	11, 12, 15		
T101	12, 14		
T102	12, 13		
T103	11, 12, 14		
T104	11, 13		
T105	12, 13		
T106	I1, I3		
T107	11, 12 ,13, 15		
T108	11, 12, 13		

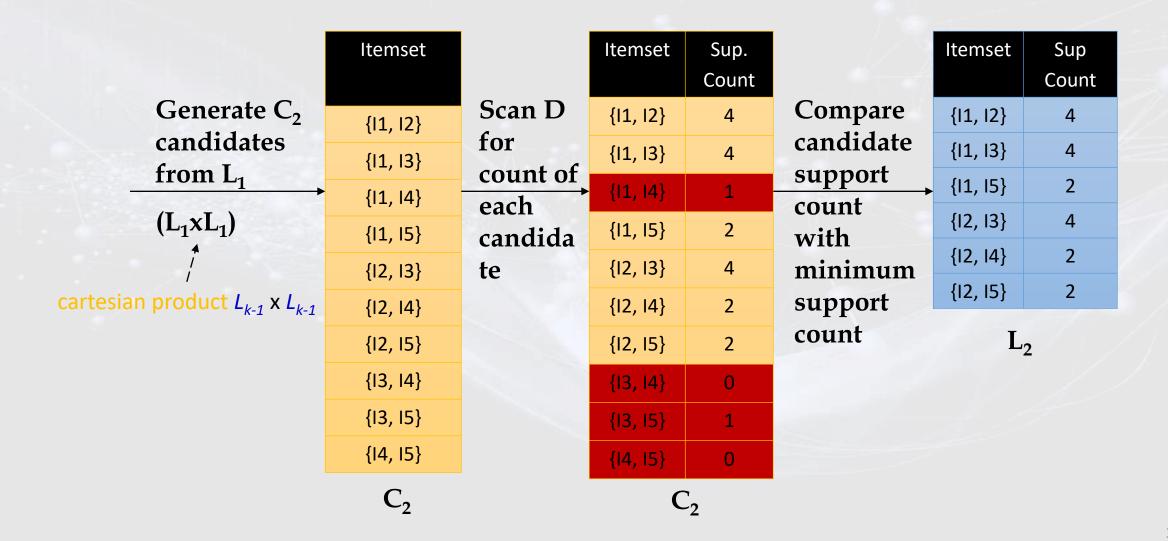
- Consider a database, D, consisting of 9 transactions.
- Suppose minimum support count required is 2 (i.e. min\_sup = 2/9 = 22 %)
- Let minimum confidence required be 70%.
- We have first to find out the frequent itemsets using Apriori algorithm.
- Then, Association rules will be generated using min. support & min. confidence.

## **Step 1**: Generating 1-itemset Frequent Pattern

	Itemset	Sup.Count		Itemset	Sup.Count
Scan D to	{11}	6	Compare	{I1}	6
count of	{12}	7	candidate	{12}	7
each	{13}	6	support count	{13}	6
candidate	{14}	2	with minimum	{14}	2
	{15}	2	support count (2)	{15}	2
$C_1$				$L_1$	

- In the first iteration of the algorithm, each item is a member of the set of candidate.
- The set of frequent 1-itemsets, L<sub>1</sub>, consists of the candidate 1-itemsets satisfying minimum support.

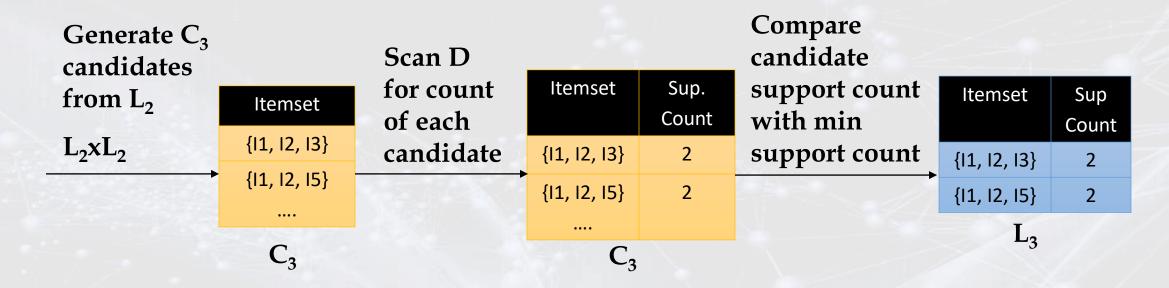
## Step 2: Generating 2-itemset Frequent Pattern



## Step 2: Generating 2-itemset Frequent Pattern [Cont.]

- To discover the set of frequent 2-itemsets,  $L_2$ , the algorithm uses  $L_1$  Join  $L_1$  to generate a candidate set of 2-itemsets,  $C_2$ .
- Next, the transactions in D are scanned and the support count for each candidate itemset in C<sub>2</sub> is accumulated (as shown in the middle table).
- The set of frequent 2-itemsets, L<sub>2</sub>, is then determined, consisting of those candidate 2-itemsets in C<sub>2</sub> having minimum support.
- Note: We haven't used Apriori Property yet.

## Step 3: Generating 3-itemset Frequent Pattern



- The generation of the set of candidate 3-itemsets, C<sub>3</sub>, involves the use of the Apriori Property.
- In order to find  $C_3$ , we compute  $L_2$  Join  $L_2$ .
- $C_3 = L2 \ Join \ L2 = \{\{11, 12, 13\}, \{11, 12, 15\}, \{11, 13, 15\}, \{12, 13, 14\}, \{12, 13, 15\}, \{12, 14, 15\}\}.$
- Now, Join step is complete and Prune step will be used to reduce the size of  $C_3$ . Prune step helps to avoid heavy computation due to large  $C_k$ .

### **Step 3**: Generating 3-itemset Frequent Pattern [Cont.]

 $C_3 = \{\{I1, I2, I3\}, \{I1, I2, I5\}, \{I1, I3, I5\}, \{I2, I3, I4\}, \{I2, I3, I5\}, \{I2, I4, I5\}\}.$ 

- Based on the **Apriori property** that all subsets of a frequent itemset must also be frequent, we can determine that four latter candidates cannot possibly be frequent. How?
- For example, let's take {I1, I2, I3}. The 2-item subsets of it are {I1, I2}, {I1, I3} & {I2, I3}. Since all 2-item subsets of {I1, I2, I3} are members of  $L_2$ , we will keep {I1, I2, I3} in  $C_3$ .
- Let's take another example of {I2, I3, I5} which shows how the pruning is performed. The 2-item subsets are {I2, I3}, {I2, I5} & {I3,I5}.
- BUT,  $\{13, 15\}$  is not a member of  $L_2$  and hence it is not frequent violating Apriori Property. Thus we will have to remove  $\{12, 13, 15\}$  from  $C_3$ .
- Therefore,  $C_3 = \{\{11, 12, 13\}, \{11, 12, 15\}\}$  after checking for all members of **result of Join operation** for **Pruning**.
- Now, the transactions in D are scanned in order to determine  $L_3$ , consisting of those candidates 3-itemsets in  $C_3$  having minimum support.

### Step 4: Generating 4-itemset Frequent Pattern

- The algorithm uses  $L_3$  Join  $L_3$  to generate a candidate set of 4-itemsets,  $C_4$ . Although the join results in  $\{\{11, 12, 13, 15\}\}$ , this itemset is pruned since its subset  $\{\{12, 13, 15\}\}$  is not frequent.
- Thus,  $C_4 = \phi$ , and algorithm terminates, having found all the frequent items. This completes our Apriori Algorithm.

#### • What's Next?

These frequent itemsets will be used to generate **strong association rules** ( where strong association rules satisfy both minimum support & minimum confidence).

### Step 5: Generating Association Rules from Frequent Itemsets

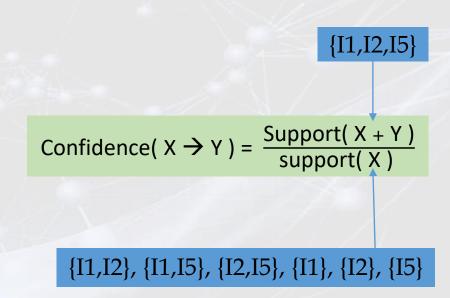
#### Back To Example:

List all frequent itemsets,  $L = \{\{11\}, \{12\}, \{13\}, \{14\}, \{15\}, \{11,12\}, \{11,13\}, \{11,15\}, \{12,13\}, \{12,14\}, \{12,15\}, \{11,12,13\}, \{11,12,15\}\}.$ 

- Lets take the 3-itemsets: {I1,I2,I5}.
- Its all nonempty subsets are {I1,I2}, {I1,I5}, {I2,I5}, {I1}, {I2}, {I5}.
- The resulting candidates rules are:
  - {I1,I2} → {I5}
  - {I1,I5} → {I2}
  - {I2,I5} → {I1}
  - {I5} → {I1,I2}
  - {I2} → {I1,I5}
  - {I1} → {I2,I5}

### **Step 5:** Generating Association Rules from Frequent Itemsets [Cont.]

- Let minimum confidence threshold is , say 70%.
- The resulting association rules are shown below, each listed with its confidence.
  - R1:  $|1 ^ |2 \rightarrow |5$ 
    - Confidence =  $sc{11,12,15}/sc{11,12} = 2/4 = 50\%$
    - R1 is Rejected.
  - R2: I1 ^ I5 → I2
    - Confidence = sc{I1,I2,I5}/sc{I1,I5} = 2/2 = 100%
    - R2 is Selected.
  - R3: I2 ^ I5 → I1
    - Confidence =  $sc{11,12,15}/sc{12,15} = 2/2 = 100\%$
    - R3 is Selected.



# **Step 5:** Generating Association Rules from Frequent Itemsets [Cont.]

- R4: I1  $\rightarrow$  I2 ^ I5
  - Confidence =  $sc{I1,I2,I5}/sc{I1} = 2/6 = 33\%$
  - R4 is Rejected.
- R5: I2 → I1 ^ I5
  - Confidence =  $sc{I1,I2,I5}/{I2} = 2/7 = 29\%$
  - R5 is Rejected.
- R6: I5  $\rightarrow$  I1 ^ I2
  - Confidence =  $sc{I1,I2,I5}/{I5} = 2/2 = 100\%$
  - R6 is Selected.

    In this way, we have found three strong association rules.

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## **Applications of Association Rules**

The term market basket analysis refers to a specific implementation of association rules.

- For better merchandising products to include/exclude from inventory each month
- Placement of products
- Cross-selling
- Promotional programs—multiple product purchase incentives managed through a loyalty card program

## **Applications of Association Rules**

- Input: the simple point-of-sale transaction data
- Output: Most frequent affinities among items
- Example: according to the transaction data...

"Customer who bought a laptop computer and a virus protection software, also bought extended service plan 70 percent of the time."

- How do you use such a pattern/knowledge?
  - Put the items next to each other for ease of finding
  - Promote the items as a package (do not put one on sale if the other(s) are on sale)
  - Place items far apart from each other so that the customer must walk the aisles to search for it, and by doing so potentially seeing and buying other items

# **Applications of Association Rules**

#### **Recommender systems** – Amazon, Netflix:

- Clickstream analysis from web usage log files
- Website visitors to page X click on links A,B,C more than on links D,E,F

#### In medicine:

- relationships between symptoms and illnesses;
- diagnosis and patient characteristics and treatments (to be used in medical DSS);
- genes and their functions (to be used in genomics projects)..

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# Validation and Testing

- The frequent and high confidence itemsets are found by pre-specified minimum support and minimum confidence levels
- Measures like lift and/or leverage then ensure that interesting rules are identified rather than coincidental ones
- However, some of the remaining rules may be considered subjectively uninteresting because they don't yield unexpected profitable actions
  - E.g., rules like {paper} → {pencil} are not interesting/meaningful
- Incorporating subjective knowledge requires domain experts
- Good rules provide valuable insights for institutions to improve their business operations

### Outline

- Overview
- Apriori Algorithm
- Evaluation of Candidate Rules
- Examples
- Application of Association Rules
- Validation and Testing
- Diagnostic

# Diagnostics

- Although the Apriori algorithm is easy to understand and implement, some
  of the rules generated are uninteresting or practically useless.
- Additionally, some of the rules may be generated due to coincidental relationships between the variables.
- Measures like confidence, lift, and leverage should be used along with human insights to address this problem.

# Diagnostics

- Another problem with association rules is that, in Phase 3 and 4 of the Data Analytics Lifecycle, the team **must specify the minimum support** prior to the model execution, which may lead to **too many or too few rules**.
- In related research, a variant of the algorithm can use a predefined target range for the number of rules so that the algorithm can adjust the minimum support accordingly.
- Algorithm requires a scan of the entire database to obtain the result.
   Accordingly, as the database grows, it takes more time to compute in each run.

## Diagnostics

#### **Approaches to improve Apriori's efficiency:**

#### Partitioning:

• Any itemset that is potentially frequent in a transaction database must be frequent in at least one of the partitions of the transaction database.

#### Sampling:

• This extracts a subset of the data with a lower support threshold and uses the subset to perform association rule mining.

#### Transaction reduction:

• A transaction that does not contain frequent k-itemsets is useless in subsequent scans and therefore can be ignored.

#### Hash-based itemset counting:

• If the corresponding hashing bucket count of a k-itemset is below a certain threshold, the k-itemset cannot be frequent.

#### Dynamic itemset counting:

• Only add new candidate itemsets when all of their subsets are estimated to be frequent.

### References

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