

1. (1 pt) Find two numbers  $A$  and  $B$  (with  $A \leq B$ ) whose difference is 38 and whose product is minimized.

$A =$  \_\_\_\_\_

$B =$  \_\_\_\_\_

Answer(s) submitted:

- -19
- 19

(correct)

Correct Answers:

- -19
- 19

2. (1 pt) Find two positive numbers whose product is 196 and whose sum is a minimum.

Answer: \_\_\_\_\_, \_\_\_\_\_

Answer(s) submitted:

- 14
- 14

(correct)

Correct Answers:

- 14
- 14

3. (1 pt) Find the length  $L$  and width  $W$  (with  $W \leq L$ ) of the rectangle with perimeter 80 that has maximum area, and then find the maximum area.

$L =$  \_\_\_\_\_

$W =$  \_\_\_\_\_

Maximum area = \_\_\_\_\_

Answer(s) submitted:

- 20
- 20
- 400

(correct)

Correct Answers:

- 20
- 20
- 400

4. (1 pt) A fence is to be built to enclose a rectangular area of 290 square feet. The fence along three sides is to be made of material that costs 5 dollars per foot, and the material for the fourth side costs 14 dollars per foot. Find the length  $L$  and width  $W$  (with  $W \leq L$ ) of the enclosure that is most economical to construct.

$L =$  \_\_\_\_\_

$W =$  \_\_\_\_\_

Answer(s) submitted:

- 23.47
- 12.35

(correct)

Correct Answers:

- 23.473389188611
- 12.3544153624268

5. (1 pt) A box is to be made out of a 10 cm by 16 cm piece of cardboard. Squares of side length  $x$  cm will be cut out of each corner, and then the ends and sides will be folded up to form a box with an open top.

(a) Express the volume  $V$  of the box as a function of  $x$ .

$V =$  \_\_\_\_\_  $\text{cm}^3$

(b) Give the domain of  $V$  in interval notation. (Use the fact that length and volume must be positive.)

(c) Find the length  $L$ , width  $W$ , and height  $H$  of the resulting box that maximizes the volume. (Assume that  $W \leq L$ ).

$L =$  \_\_\_\_\_ cm

$W =$  \_\_\_\_\_ cm

$H =$  \_\_\_\_\_ cm

(d) The maximum volume of the box is \_\_\_\_\_  $\text{cm}^3$ .

Answer(s) submitted:

- $(4x^3) - (52x^2) + (160x)$
- (0, 5)
- 12
- 6
- 2
- 144

(correct)

Correct Answers:

- $(10 - 2 * x)(16 - 2 * x)x$
- $(0, 5)$
- 12
- 6
- 2
- 144

6. (1 pt) A rectangular storage container with an open top is to have a volume of 12 cubic meters. The length of its base is twice the width. Material for the base costs 13 dollars per square meter. Material for the sides costs 7 dollars per square meter. Find the cost of materials for the cheapest such container.

Total cost = \_\_\_\_\_ (Round to the nearest penny and include monetary units. For example, if your answer is 1.095, enter \$1.10 including the dollar sign and second decimal place.)

Answer(s) submitted:

- \$223.37

(correct)

Correct Answers:

- \ \$223.37

7. (1 pt) Find the minimum distance from the parabola

$$x + y^2 = 0$$

to the point  $(0, -3)$ .

Minimum distance = \_\_\_\_\_

Answer(s) submitted:

- $\sqrt{5}$

(correct)

Correct Answers:

- 2.23606797749979

8. (1 pt) A rectangle is inscribed with its base on the x-axis and its upper corners on the parabola  $y = 11 - x^2$ . What are the dimensions of such a rectangle with the greatest possible area?

Width = \_\_\_\_\_ Height = \_\_\_\_\_

Answer(s) submitted:

- $2\sqrt{11/3}$
- $11 - (11/3)$

(correct)

Correct Answers:

- 3.82970843102535
- 7.33333333333333