

1. (1 pt) Consider the function  $f(x) = 7 - 3x^2$  on the interval  $[-3, 6]$ . Find the average or mean slope of the function on this interval, i.e.

$$\frac{f(6) - f(-3)}{6 - (-3)} =$$

By the Mean Value Theorem, we know there exists a  $c$  in the open interval  $(-3, 6)$  such that  $f'(c)$  is equal to this mean slope. For this problem, there is only one  $c$  that works. Find it.

Answer(s) submitted:

- -9
- 3/2

(correct)

Correct Answers:

- -9
- 1.5

2. (1 pt) Consider the function  $f(x) = \frac{1}{x}$  on the interval  $[4, 7]$ . Find the average or mean slope of the function on this interval.

By the Mean Value Theorem, we know there exists a  $c$  in the open interval  $(4, 7)$  such that  $f'(c)$  is equal to this mean slope. For this problem, there is only one  $c$  that works. Find it.

Answer(s) submitted:

- -1/28
- 2sqrt(7)

(correct)

Correct Answers:

- -0.0357142857142857
- 5.29150262212918

3. (1 pt) Consider the function

$$f(x) = -2x^3 + 3x^2 - x - 1$$

Find the average slope of this function on the interval  $(4, 7)$ .

By the Mean Value Theorem, we know there exists a  $c$  in the open interval  $(4, 7)$  such that  $f'(c)$  is equal to this mean slope. Find the value of  $c$  in the interval which works \_\_\_\_\_

Answer(s) submitted:

- -154
- (1/2) (1+sqrt(103))

(correct)

Correct Answers:

- -154

• 5.57444578254611

4. (1 pt) Consider the function  $f(x) = x^2 - 4x + 6$  on the interval  $[0, 4]$ . Verify that this function satisfies the three hypotheses of Rolle's Theorem on the interval.

$f(x)$  is \_\_\_\_\_ on  $[0, 4]$ ;

$f(x)$  is \_\_\_\_\_ on  $(0, 4)$ ;

and  $f(0) = f(4) =$  \_\_\_\_\_.

Then by Rolle's theorem, there exists a  $c$  such that  $f'(c) = 0$ . Find the value  $c$ .

$c =$  \_\_\_\_\_

Answer(s) submitted:

- continuous
- differentiable
- 6
- 2

(correct)

Correct Answers:

- CONTINUOUS
- DIFFERENTIABLE
- 6
- 2

5. (1 pt) Suppose  $f(x)$  is continuous on  $[4, 8]$  and  $-2 \leq f'(x) \leq 4$  for all  $x$  in  $(4, 8)$ . Use the Mean Value Theorem to estimate  $f(8) - f(4)$ .

Answer: \_\_\_\_\_  $\leq f(8) - f(4) \leq$  \_\_\_\_\_

Answer(s) submitted:

- -8
- 16

(correct)

Correct Answers:

- -2\*(8-(4))
- 4\*(8-(4))

6. (1 pt) Does there exist a continuous function  $f(x)$  such that  $f(0) = 3$ ,  $f(2) = 8$  and  $f'(x) \leq -3$  for all  $x$  in  $(0, 2)$ ?

Answer: (yes or no ) \_\_\_\_\_

**Note:** You only have one chance to input your answer.

Answer(s) submitted:

- no

(correct)

Correct Answers:

- NO

