Long Maturity Overflowing 192e18

The Hifi AMM relies heavily on the <u>pow</u> function part of PRBMath. This is an exponential function that accepts fractional values for both the base and the exponent. The implementation is based on the following mathematical identity:

$$x^y = 2^{log_2(x) * y}$$

One limitation of the $\underline{\text{exp2}}$ function in PRBMath is that it doesn't accepts exponents greater than 192 ($192*10^{18}$ in the PRBMath format). In most cases, this is not a problem:

- 1. The Yield Space exponent is sub-unitary (smaller than 1), and most computations use this exponent directly, not its inverse.
- 2. There is a natural limit to how large the token amounts can be. E.g. <u>Circle</u> can't increase the total supply of USDC to one quadrillion without help from the FED (fingers-crossed we won't get there anytime soon).

However, there is one computation where the upper bound of the exp2 function could pose a problem. That is the <u>inversion</u> of the Yield Space exponent:

$$\frac{1}{1-g*t}$$

Combined with a long-dated bond expiration time (used as a base to pow), a contract call could revert due to the exponent being greater than 192.

Possible solutions to explore:

- 1. Reimplement pow such that it accepts exponents greater than 192.
- 2. Renormalize the time to maturity such that 1 unit = 10 years.
- 3. Write a custom pow function that introduces a normalization factor (see how Yield does it) to skirt around the upper bounds of PRBMath.

We're open to other ideas as well.