exploring word vectors 22 23

January 17, 2023

1 CS224N Assignment 1: Exploring Word Vectors (25 Points)

1.0.1 Due 4:30pm, Tue Jan 17

Welcome to CS224N!

Before you start, make sure you read the README.txt in the same directory as this notebook for important setup information. A lot of code is provided in this notebook, and we highly encourage you to read and understand it as part of the learning:)

If you aren't super familiar with Python, Numpy, or Matplotlib, we recommend you check out the review session on Friday. The session will be recorded and the material will be made available on our website. The CS231N Python/Numpy tutorial is also a great resource.

Assignment Notes: Please make sure to save the notebook as you go along. Submission Instructions are located at the bottom of the notebook.

```
[58]: # All Import Statements Defined Here
      # Note: Do not add to this list.
      # -----
      import sys
      assert sys.version_info[0]==3
      assert sys.version info[1] >= 5
      from platform import python_version
      assert int(python_version().split(".")[1]) >= 5, "Please upgrade your Python⊔
       \hookrightarrowversion following the instructions in \setminus
          the README.txt file found in the same directory as this notebook. Your ⊔
       →Python version is " + python_version()
      from gensim.models import KeyedVectors
      from gensim.test.utils import datapath
      import pprint
      import matplotlib.pyplot as plt
      plt.rcParams['figure.figsize'] = [10, 5]
      import nltk
      nltk.download('reuters') #to specify download location, optionally add the
       →argument: download_dir='/specify/desired/path/'
```

```
[nltk_data] Downloading package reuters to
[nltk_data] C:\Users\jason\AppData\Roaming\nltk_data...
[nltk_data] Package reuters is already up-to-date!
```

1.1 Word Vectors

Word Vectors are often used as a fundamental component for downstream NLP tasks, e.g. question answering, text generation, translation, etc., so it is important to build some intuitions as to their strengths and weaknesses. Here, you will explore two types of word vectors: those derived from co-occurrence matrices, and those derived via GloVe.

Note on Terminology: The terms "word vectors" and "word embeddings" are often used interchangeably. The term "embedding" refers to the fact that we are encoding aspects of a word's meaning in a lower dimensional space. As Wikipedia states, "conceptually it involves a mathematical embedding from a space with one dimension per word to a continuous vector space with a much lower dimension".

1.2 Part 1: Count-Based Word Vectors (10 points)

Most word vector models start from the following idea:

You shall know a word by the company it keeps (Firth, J. R. 1957:11)

Many word vector implementations are driven by the idea that similar words, i.e., (near) synonyms, will be used in similar contexts. As a result, similar words will often be spoken or written along with a shared subset of words, i.e., contexts. By examining these contexts, we can try to develop embeddings for our words. With this intuition in mind, many "old school" approaches to constructing word vectors relied on word counts. Here we elaborate upon one of those strategies, co-occurrence matrices (for more information, see here or here).

1.2.1 Co-Occurrence

A co-occurrence matrix counts how often things co-occur in some environment. Given some word w_i occurring in the document, we consider the *context window* surrounding w_i . Supposing our fixed window size is n, then this is the n preceding and n subsequent words in that document,

i.e. words $w_{i-n} \dots w_{i-1}$ and $w_{i+1} \dots w_{i+n}$. We build a co-occurrence matrix M, which is a symmetric word-by-word matrix in which M_{ij} is the number of times w_j appears inside w_i 's window among all documents.

Example: Co-Occurrence with Fixed Window of n=1:

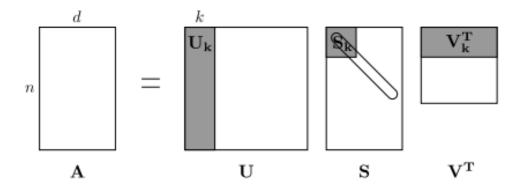
Document 1: "all that glitters is not gold"

Document 2: "all is well that ends well"

*	<start></start>	all	that	glitters	is	not	gold	well	ends	<end></end>
<start></start>	0	2	0	0	0	0	0	0	0	0
all	2	0	1	0	1	0	0	0	0	0
that	0	1	0	1	0	0	0	1	1	0
glitters	0	0	1	0	1	0	0	0	0	0
is	0	1	0	1	0	1	0	1	0	0
not	0	0	0	0	1	0	1	0	0	0
gold	0	0	0	0	0	1	0	0	0	1
well	0	0	1	0	1	0	0	0	1	1
ends	0	0	1	0	0	0	0	1	0	0
<end></end>	0	0	0	0	0	0	1	1	0	0

Note: In NLP, we often add <START> and <END> tokens to represent the beginning and end of sentences, paragraphs or documents. In this case we imagine <START> and <END> tokens encapsulating each document, e.g., "<START> All that glitters is not gold <END>", and include these tokens in our co-occurrence counts.

The rows (or columns) of this matrix provide one type of word vectors (those based on word-word co-occurrence), but the vectors will be large in general (linear in the number of distinct words in a corpus). Thus, our next step is to run dimensionality reduction. In particular, we will run SVD (Singular Value Decomposition), which is a kind of generalized PCA (Principal Components Analysis) to select the top k principal components. Here's a visualization of dimensionality reduction with SVD. In this picture our co-occurrence matrix is A with n rows corresponding to n words. We obtain a full matrix decomposition, with the singular values ordered in the diagonal S matrix, and our new, shorter length-k word vectors in U_k .



This reduced-dimensionality co-occurrence representation preserves semantic relationships between words, e.g. doctor and hospital will be closer than doctor and dog.

Notes: If you can barely remember what an eigenvalue is, here's a slow, friendly introduction to SVD. If you want to learn more thoroughly about PCA or SVD, feel free to check out lectures 7, 8, and 9 of CS168. These course notes provide a great high-level treatment of these general purpose algorithms. Though, for the purpose of this class, you only need to know how to extract the k-dimensional embeddings by utilizing pre-programmed implementations of these algorithms from the numpy, scipy, or sklearn python packages. In practice, it is challenging to apply full SVD to large corpora because of the memory needed to perform PCA or SVD. However, if you only want the top k vector components for relatively small k— known as Truncated SVD— then there are reasonably scalable techniques to compute those iteratively.

1.2.2 Plotting Co-Occurrence Word Embeddings

Here, we will be using the Reuters (business and financial news) corpus. If you haven't run the import cell at the top of this page, please run it now (click it and press SHIFT-RETURN). The corpus consists of 10,788 news documents totaling 1.3 million words. These documents span 90 categories and are split into train and test. For more details, please see https://www.nltk.org/book/ch02.html. We provide a read_corpus function below that pulls out only articles from the "gold" (i.e. news articles about gold, mining, etc.) category. The function also adds <START> and <END> tokens to each of the documents, and lowercases words. You do not have to perform any other kind of pre-processing.

```
[32]: def read_corpus(category="gold"):
    """ Read files from the specified Reuter's category.
    Params:
        category (string): category name
    Return:
        list of lists, with words from each of the processed files
    """
    files = reuters.fileids(category)
    return [[START_TOKEN] + [w.lower() for w in list(reuters.words(f))] +□
        ⇔[END_TOKEN] for f in files]
```

Let's have a look what these documents are like....

```
[33]: reuters_corpus = read_corpus()
    pprint.pprint(reuters_corpus[:3], compact=True, width=100)

[['<START>', 'western', 'mining', 'to', 'open', 'new', 'gold', 'mine', 'in',
    'australia', 'western',
    'mining', 'corp', 'holdings', 'ltd', '&', 'lt', ';', 'wmng', '.', 's', '>',
    '(', 'wmc', ')',
```

```
'mine', 'in', 'the',
  'northern', 'territory', 'at', 'a', 'cost', 'of', 'about', '21', 'mln',
'dlrs', '.', 'the',
  'mine', ',', 'to', 'be', 'known', 'as', 'the', 'goodall', 'project', ',',
```

'said', 'it', 'will', 'establish', 'a', 'new', 'joint', 'venture', 'gold',

```
'60', 'pct', 'by', 'wmc', 'and', '40', 'pct', 'by', 'a', 'local', 'w', '.',
'r', '.', 'grace',
 'and', 'co', '&', 'lt', ';', 'gra', '>', 'unit', '.', 'it', 'is', 'located',
'30', 'kms', 'east',
 'of', 'the', 'adelaide', 'river', 'at', 'mt', '.', 'bundey', ',', 'wmc',
'said', 'in', 'a',
  'statement', 'it', 'said', 'the', 'open', '-', 'pit', 'mine', ',', 'with',
'a', 'conventional',
 'leach', 'treatment', 'plant', ',', 'is', 'expected', 'to', 'produce',
'about', '50', ',', '000',
  'ounces', 'of', 'gold', 'in', 'its', 'first', 'year', 'of', 'production',
'from', 'mid', '-',
  '1988', '.', 'annual', 'ore', 'capacity', 'will', 'be', 'about', '750', ',',
'000', 'tonnes', '.',
 '<END>'],
['<START>', 'belgium', 'to', 'issue', 'gold', 'warrants', ',', 'sources',
'say', 'belgium',
  'plans', 'to', 'issue', 'swiss', 'franc', 'warrants', 'to', 'buy', 'gold',
',', 'with', 'credit',
 'suisse', 'as', 'lead', 'manager', ',', 'market', 'sources', 'said', '.',
'no', 'confirmation',
 'or', 'further', 'details', 'were', 'immediately', 'available', '.', '<END>'],
['<START>', 'belgium', 'launches', 'bonds', 'with', 'gold', 'warrants', 'the',
'kingdom', 'of',
  'belgium', 'is', 'launching', '100', 'mln', 'swiss', 'francs', 'of', 'seven',
'year', 'notes',
  'with', 'warrants', 'attached', 'to', 'buy', 'gold', ',', 'lead', 'mananger',
'credit', 'suisse',
  'said', '.', 'the', 'notes', 'themselves', 'have', 'a', '3', '-', '3', '/',
'8', 'pct', 'coupon',
 'and', 'are', 'priced', 'at', 'par', '.', 'payment', 'is', 'due', 'april',
'30', ',', '1987',
 'and', 'final', 'maturity', 'april', '30', ',', '1994', '.', 'each', '50',
',', '000', 'franc',
 'note', 'carries', '15', 'warrants', '.', 'two', 'warrants', 'are',
'required', 'to', 'allow',
 'the', 'holder', 'to', 'buy', '100', 'grammes', 'of', 'gold', 'at', 'a',
'price', 'of', '2', ',',
  '450', 'francs', ',', 'during', 'the', 'entire', 'life', 'of', 'the', 'bond'.
'.', 'the',
 'latest', 'gold', 'price', 'in', 'zurich', 'was', '2', ',', '045', '/', '2',
',', '070', 'francs',
  'per', '100', 'grammes', '.', '<END>']]
```

1.2.3 Question 1.1: Implement distinct words [code] (2 points)

Write a method to work out the distinct words (word types) that occur in the corpus. You can do this with for loops, but it's more efficient to do it with Python list comprehensions. In particular,

this may be useful to flatten a list of lists. If you're not familiar with Python list comprehensions in general, here's more information.

Your returned corpus_words should be sorted. You can use python's sorted function for this.

You may find it useful to use Python sets to remove duplicate words.

```
[34]: def distinct_words(corpus):
          """ Determine a list of distinct words for the corpus.
                  corpus (list of list of strings): corpus of documents
              Return:
                  corpus_words (list of strings): sorted list of distinct words⊔
       ⇔across the corpus
                  n_corpus_words (integer): number of distinct words across the corpus
          11 11 11
          corpus_words = []
          n_{corpus_{words}} = -1
          ### SOLUTION BEGIN
          flattened_corpus = [word for doc in corpus for word in doc]
          corpus_words = list(set(flattened_corpus))
          corpus_words.sort() # in place
          n_corpus_words = len(corpus_words)
          ### SOLUTION END
          return corpus_words, n_corpus_words
```

```
[35]: # -----
     # Run this sanity check
     # Note that this not an exhaustive check for correctness.
     # -----
     # Define toy corpus
     test_corpus = ["{} All that glitters isn't gold {}".format(START_TOKEN,_
      →END TOKEN).split(" "), "{} All's well that ends well {}".format(START TOKEN,
      →END_TOKEN).split(" ")]
     test_corpus_words, num_corpus_words = distinct_words(test_corpus)
     # Correct answers
     ans_test_corpus_words = sorted([START_TOKEN, "All", "ends", "that", "gold", "
      →"All's", "glitters", "isn't", "well", END_TOKEN])
     ans_num_corpus_words = len(ans_test_corpus_words)
     # Test correct number of words
     assert(num_corpus_words == ans_num_corpus_words), "Incorrect number of distinctu
       →words. Correct: {}. Yours: {}".format(ans_num_corpus_words, num_corpus_words)
```

Passed All Tests!

1.2.4 Question 1.2: Implement compute_co_occurrence_matrix [code] (3 points)

Write a method that constructs a co-occurrence matrix for a certain window-size n (with a default of 4), considering words n before and n after the word in the center of the window. Here, we start to use numpy (np) to represent vectors, matrices, and tensors. If you're not familiar with NumPy, there's a NumPy tutorial in the second half of this cs231n Python NumPy tutorial.

```
[36]: def clamp(n, minn, maxn):
          return max(min(maxn, n), minn)
      def compute_co_occurrence_matrix(corpus, window_size=4):
           """ Compute co-occurrence matrix for the given corpus and window size,
       \Leftrightarrow (default of 4).
              Note: Each word in a document should be at the center of a window. \Box
       →Words near edges will have a smaller
                     number of co-occurring words.
                     For example, if we take the document "<START> All that glitters_
       \hookrightarrow is not gold <END>" with window size of 4,
                     "All" will co-occur with "<START>", "that", "qlitters", "is", and
       \Rightarrow "not".
               Params:
                   corpus (list of list of strings): corpus of documents
                   window_size (int): size of context window
               Return:
                   M (a symmetric numpy matrix of shape (number of unique words in the \Box
       →corpus , number of unique words in the corpus)):
                       Co-occurence matrix of word counts.
                       The ordering of the words in the rows/columns should be the 
       ⇒same as the ordering of the words given by the distinct_words function.
```

```
word2ind (dict): dictionary that maps word to index (i.e. row/
⇔column number) for matrix M.
  words, n_words = distinct_words(corpus)
  M = None
  word2ind = {}
  ### SOLUTION BEGIN
  M = np.zeros(shape=(n_words, n_words))
  for idx, word in enumerate(words):
      word2ind[word] = idx
  for doc in corpus:
      max_word_idx = len(doc) - 1
      for i in range(len(doc)):
          centre_word_idx_in_M = word2ind[doc[i]]
          context_word_lwr_idx_lim = clamp(i-window_size, 0, max_word_idx)
          context word upp idx lim = clamp(i+window size, 0, max word idx)
          for j in range(context_word_lwr_idx_lim, i):
              ctx_word_idx_in_M = word2ind[doc[j]]
              M[centre_word_idx_in_M][ctx_word_idx_in_M] += 1
          for k in range(i+1, context_word_upp_idx_lim+1):
              ctx_word_idx_in_M = word2ind[doc[k]]
              M[centre_word_idx_in_M][ctx_word_idx_in_M] += 1
  ### SOLUTION END
  return M, word2ind
```

```
[[0., 0., 0., 0., 0., 0., 1., 0., 0., 1.,],
     [0., 0., 1., 1., 0., 0., 0., 0., 0., 0., ],
     [0., 1., 0., 0., 0., 0., 0., 0., 1., 0.,],
     [0., 1., 0., 0., 0., 0., 0., 0., 0., 1.,],
     [0., 0., 0., 0., 0., 0., 0., 0., 1., 1.,],
    [0., 0., 0., 0., 0., 0., 0., 1., 1., 0.,],
    [1., 0., 0., 0., 0., 0., 0., 1., 0., 0.,],
     [0., 0., 0., 0., 0., 1., 1., 0., 0., 0.,],
     [0., 0., 1., 0., 1., 1., 0., 0., 0., 1.,],
     [1., 0., 0., 1., 1., 0., 0., 0., 1., 0.,]]
ans_test_corpus_words = sorted([START_TOKEN, "All", "ends", "that", "gold", "
⇔"All's", "glitters", "isn't", "well", END_TOKEN])
word2ind_ans = dict(zip(ans_test_corpus_words,__
 →range(len(ans_test_corpus_words))))
# Test correct word2ind
assert (word2ind_ans == word2ind_test), "Your word2ind is incorrect:\nCorrect:\
 →{}\nYours: {}".format(word2ind_ans, word2ind_test)
# Test correct M shape
assert (M_test.shape == M_test_ans.shape), "M matrix has incorrect shape.
 # Test correct M values
for w1 in word2ind_ans.keys():
   idx1 = word2ind_ans[w1]
   for w2 in word2ind_ans.keys():
       idx2 = word2ind_ans[w2]
       student = M_test[idx1, idx2]
       correct = M_test_ans[idx1, idx2]
       if student != correct:
           print("Correct M:")
           print(M_test_ans)
           print("Your M: ")
           print(M_test)
           raise AssertionError("Incorrect count at index ({}, {})=({}, {}) in

∪
 →matrix M. Yours has {} but should have {}.".format(idx1, idx2, w1, w2, □
 ⇔student, correct))
# Print Success
print ("-" * 80)
print("Passed All Tests!")
print ("-" * 80)
```

Passed All Tests!

1.2.5 Question 1.3: Implement reduce_to_k_dim [code] (1 point)

Construct a method that performs dimensionality reduction on the matrix to produce k-dimensional embeddings. Use SVD to take the top k components and produce a new matrix of k-dimensional embeddings.

Note: All of numpy, scipy, and scikit-learn (sklearn) provide *some* implementation of SVD, but only scipy and sklearn provide an implementation of Truncated SVD, and only sklearn provides an efficient randomized algorithm for calculating large-scale Truncated SVD. So please use sklearn.decomposition.TruncatedSVD.

```
[38]: def reduce to k dim(M, k=2):
           """ Reduce a co-occurence count matrix of dimensionality (num_corpus_words,_{\sqcup}
        →num_corpus_words)
               to a matrix of dimensionality (num_corpus words, k) using the following_
        \hookrightarrow SVD function from Scikit-Learn:
                   - http://scikit-learn.org/stable/modules/generated/sklearn.
       {\scriptsize \ominus decomposition.} TruncatedSVD.html
               Params:
                   M (numpy matrix of shape (number of unique words in the corpus, _{\sqcup}
        →number of unique words in the corpus)): co-occurence matrix of word counts
                   k (int): embedding size of each word after dimension reduction
               Return:
                   M reduced (numpy matrix of shape (number of corpus words, k)):
        \negmatrix of k-dimensioal word embeddings.
                            In terms of the SVD from math class, this actually returns.
        \hookrightarrow U * S
           11 11 11
          n_{iters} = 10
                             # Use this parameter in your call to `TruncatedSVD`
          M reduced = None
          print("Running Truncated SVD over %i words..." % (M.shape[0]))
          ### SOLUTION BEGIN
          M reduced = TruncatedSVD(n_components=k, n_iter=n_iters).fit_transform(M)
          ### SOLUTION END
          print("Done.")
          return M_reduced
```

Running Truncated SVD over 10 words...
Done.

Passed All Tests!

1.2.6 Question 1.4: Implement plot_embeddings [code] (1 point)

Here you will write a function to plot a set of 2D vectors in 2D space. For graphs, we will use Matplotlib (plt).

For this example, you may find it useful to adapt this code. In the future, a good way to make a plot is to look at the Matplotlib gallery, find a plot that looks somewhat like what you want, and adapt the code they give.

```
[40]: def plot_embeddings(M_reduced, word2ind, words):

""" Plot in a scatterplot the embeddings of the words specified in the list

""words".

NOTE: do not plot all the words listed in M_reduced / word2ind.

Include a label next to each point.

Params:

M_reduced (numpy matrix of shape (number of unique words in the

corpus , 2)): matrix of 2-dimensical word embeddings

word2ind (dict): dictionary that maps word to indices for matrix M

words (list of strings): words whose embeddings we want to visualize

"""

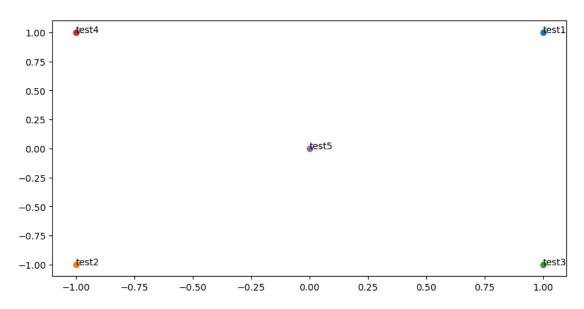
### SOLUTION BEGIN

for idx_in_words, word in enumerate(words):
```

```
idx_of_word_in_M = word2ind[word]
vector_of_word = M_reduced[idx_of_word_in_M]

plt.plot(vector_of_word[0], vector_of_word[1], 'o')
plt.text(vector_of_word[0], vector_of_word[1], word)
### SOLUTION END
```

Outputted Plot:

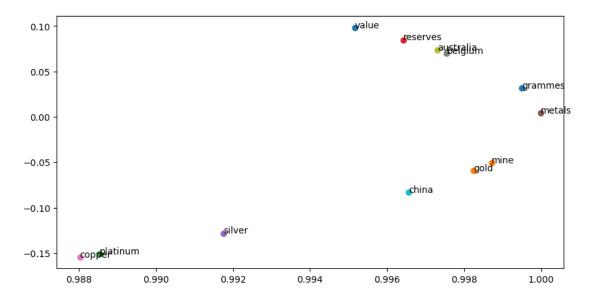


1.2.7 Question 1.5: Co-Occurrence Plot Analysis [written] (3 points)

Now we will put together all the parts you have written! We will compute the co-occurrence matrix with fixed window of 4 (the default window size), over the Reuters "gold" corpus. Then we will use TruncatedSVD to compute 2-dimensional embeddings of each word. TruncatedSVD returns U*S, so we need to normalize the returned vectors, so that all the vectors will appear around the unit circle (therefore closeness is directional closeness). **Note**: The line of code below that does the normalizing uses the NumPy concept of *broadcasting*. If you don't know about broadcasting, check out Computation on Arrays: Broadcasting by Jake VanderPlas.

Run the below cell to produce the plot. It'll probably take a few seconds to run.

Running Truncated SVD over 2830 words... Done.



Verify that your figure matches "question_1.5.png" in the assignment zip. If not, use that figure to answer the next two questions.

```
[43]: # My plot matches. Hooray.
```

a. Find at least two groups of words that cluster together in 2-dimensional embedding space. Give an explanation for each cluster you observe.

1.2.8 SOLUTION BEGIN

Group 1: copper, platinum, silver Group 2: australia, belgium

Group 1 are metals, while Group 2 are countries. ### SOLUTION END

b. What doesn't cluster together that you might think should have? Describe at least two examples.

1.2.9 SOLUTION BEGIN

China should cluster with Australia and Belgium since they are all countries. Gold should also cluster more closely with copper, platinum since they are metals.

It's possible that in higher dimensional space the expected clusters are more apparent. ### SOLUTION END

1.3 Part 2: Prediction-Based Word Vectors (15 points)

As discussed in class, more recently prediction-based word vectors have demonstrated better performance, such as word2vec and GloVe (which also utilizes the benefit of counts). Here, we shall explore the embeddings produced by GloVe. Please revisit the class notes and lecture slides for more details on the word2vec and GloVe algorithms. If you're feeling adventurous, challenge yourself and try reading GloVe's original paper.

Then run the following cells to load the GloVe vectors into memory. **Note**: If this is your first time to run these cells, i.e. download the embedding model, it will take a couple minutes to run. If you've run these cells before, rerunning them will load the model without redownloading it, which will take about 1 to 2 minutes.

```
[45]: # -------
# Run Cell to Load Word Vectors
# Note: This will take a couple minutes
# -------
wv_from_bin = load_embedding_model()
```

Loaded vocab size 400000

Note: If you are receiving a "reset by peer" error, rerun the cell to restart the download. If you run into an "attribute" error, you may need to update to the most recent version of gensim and numpy. You can upgrade them inline by uncommenting and running the below cell:

```
[46]: #!pip install gensim --upgrade
#!pip install numpy --upgrade
```

1.3.1 Reducing dimensionality of Word Embeddings

Let's directly compare the GloVe embeddings to those of the co-occurrence matrix. In order to avoid running out of memory, we will work with a sample of 10000 GloVe vectors instead. Run the following cells to:

- 1. Put 10000 Glove vectors into a matrix M
- 2. Run reduce_to_k_dim (your Truncated SVD function) to reduce the vectors from 200-dimensional to 2-dimensional.

```
[47]: def get_matrix_of_vectors(wv_from_bin, required_words):
          """ Put the GloVe vectors into a matrix M.
              Param:
                  wv_from_bin: KeyedVectors object; the 400000 GloVe vectors loaded ∪
       ⇔from file
              Return:
                  M: numpy matrix shape (num words, 200) containing the vectors
                  word2ind: dictionary mapping each word to its row number in M
          11 11 11
          import random
          words = list(wv_from_bin.index_to_key)
          print("Shuffling words ...")
          random.seed(225)
          random.shuffle(words)
          words = words[:10000]
          print("Putting %i words into word2ind and matrix M..." % len(words))
          word2ind = {}
          M = []
          curInd = 0
          for w in words:
              try:
                  M.append(wv_from_bin.get_vector(w))
                  word2ind[w] = curInd
```

```
curInd += 1
except KeyError:
    continue

for w in required_words:
    if w in words:
        continue

    try:
        M.append(wv_from_bin.get_vector(w))
        word2ind[w] = curInd
        curInd += 1
    except KeyError:
        continue

M = np.stack(M)
print("Done.")
return M, word2ind
```

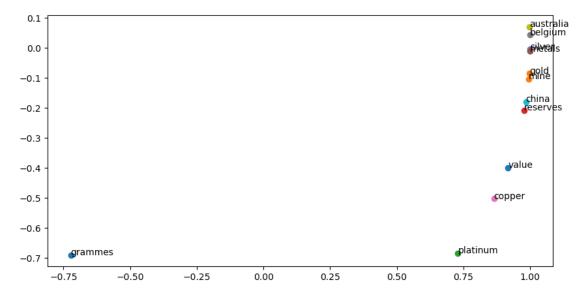
Shuffling words ...
Putting 10000 words into word2ind and matrix M...
Done.
Running Truncated SVD over 10012 words...
Done.

Note: If you are receiving out of memory issues on your local machine, try closing other applications to free more memory on your device. You may want to try restarting your machine so that you can free up extra memory. Then immediately run the jupyter notebook and see if you can load the word vectors properly. If you still have problems with loading the embeddings onto your local machine after this, please go to office hours or contact course staff.

1.3.2 Question 2.1: GloVe Plot Analysis [written] (3 points)

```
Run the cell below to plot the 2D GloVe embeddings for ['value', 'gold', 'platinum', 'reserves', 'silver', 'metals', 'copper', 'belgium', 'australia', 'china', 'grammes', "mine"].
```

```
[49]:
```



a. What is one way the plot is different from the one generated earlier from the co-occurrence matrix? What is one way it's similar?

1.3.3 SOLUTION BEGIN

One difference is that 'grammes' and 'metals' has significantly diverged. The co-occurence matrix had them clustered together. One similarity is that 'Gold' and 'mine' are still clustered together. ### SOLUTION END

b. What is a possible cause for the difference?

1.3.4 SOLUTION BEGIN

One possible cause for the difference is that the Glove embeddings are 'better' trained'. Firstly, unlike the co-occurence matrix which is a naive count of word frequencies in a given window size, GloVe evaluates semantic relationships 'consisiting of the aggregated global word-word co-occurence statistics' by '[computing] the ratio of probabilities between any two pairs of words'. GloVe also evaluates the embeddings based on solving a loss function subject to those evaluated probabilities, whereas the co-occurence matrix technique does not do this.

Source: https://analyticsindiamag.com/word2vec-vs-glove-a-comparative-guide-to-word-embedding-techniques/

1.3.5 SOLUTION END

1.3.6 Cosine Similarity

Now that we have word vectors, we need a way to quantify the similarity between individual words, according to these vectors. One such metric is cosine-similarity. We will be using this to find words that are "close" and "far" from one another.

We can think of n-dimensional vectors as points in n-dimensional space. If we take this perspective L1 and L2 Distances help quantify the amount of space "we must travel" to get between these two points. Another approach is to examine the angle between two vectors. From trigonometry we know that:

Instead of computing the actual angle, we can leave the similarity in terms of $similarity = cos(\Theta)$. Formally the Cosine Similarity s between two vectors p and q is defined as:

$$s = \frac{p \cdot q}{||p|| ||q||}, \text{ where } s \in [-1, 1]$$

1.3.7 Question 2.2: Words with Multiple Meanings (1.5 points) [code + written]

Polysemes and homonyms are words that have more than one meaning (see this wiki page to learn more about the difference between polysemes and homonyms). Find a word with at least two different meanings such that the top-10 most similar words (according to cosine similarity) contain related words from both meanings. For example, "leaves" has both "go_away" and "a_structure_of_a_plant" meaning in the top 10, and "scoop" has both "handed_waffle_cone" and "lowdown". You will probably need to try several polysemous or homonymic words before you find one.

Please state the word you discover and the multiple meanings that occur in the top 10. Why do you think many of the polysemous or homonymic words you tried didn't work (i.e. the top-10 most similar words only contain **one** of the meanings of the words)?

Note: You should use the wv_from_bin.most_similar(word) function to get the top 10 similar words. This function ranks all other words in the vocabulary with respect to their cosine similarity to the given word. For further assistance, please check the **GenSim documentation**.

```
[50]: ### SOLUTION BEGIN
wv_from_bin.most_similar('dull')
### SOLUTION END
```

1.3.8 SOLUTION BEGIN

I tried web, cool, jaguar, fan, bright, which didn't seems to yield words with different meanings in the top 10 similar words result.

But 'dull' yields different meanings. The results decscribe dull in the 'visual' sense and dull as a synonym for uninspiring.

I think many of the polysems and homonyms I tried didn't work because the GloVe corpus may be so large that there are more than 10 similar words for each candidate polysem or homonymn tried. In the case of Jaguar, for example, the corpus might have many more tokens of jaguar as vehicle models than as animals. ### SOLUTION END

1.3.9 Question 2.3: Synonyms & Antonyms (2 points) [code + written]

When considering Cosine Similarity, it's often more convenient to think of Cosine Distance, which is simply 1 - Cosine Similarity.

Find three words (w_1, w_2, w_3) where w_1 and w_2 are synonyms and w_1 and w_3 are antonyms, but Cosine Distance $(w_1, w_3) <$ Cosine Distance (w_1, w_2) .

As an example, w_1 ="happy" is closer to w_3 ="sad" than to w_2 ="cheerful". Please find a different example that satisfies the above. Once you have found your example, please give a possible explanation for why this counter-intuitive result may have happened.

You should use the the wv_from_bin.distance(w1, w2) function here in order to compute the cosine distance between two words. Please see the GenSim documentation for further assistance.

```
[51]: ### SOLUTION BEGIN

w1 = 'poor'
w2 = 'broke'
w3 = 'rich'
w1_w2_dist = wv_from_bin.distance(w1, w2)
w1_w3_dist = wv_from_bin.distance(w1, w3)

print("Synonyms {}, {} have cosine distance: {}".format(w1, w2, w1_w2_dist))
print("Antonyms {}, {} have cosine distance: {}".format(w1, w3, w1_w3_dist))

### SOLUTION END
```

Synonyms poor, broke have cosine distance: 0.7683512419462204 Antonyms poor, rich have cosine distance: 0.5232119858264923

1.3.10 SOLUTION BEGIN

One possible reason for that the cosine distance of the synonym is greater than the cosine distance of the antonym is due to the corpus on which the GloVe algorithm was trained. The corpus likely has more instances where 'rich' and 'poor' are employed in phrases close to each other unlike 'poor' and 'broke' ### SOLUTION END

1.3.11 Question 2.4: Analogies with Word Vectors [written] (1.5 points)

Word vectors have been shown to *sometimes* exhibit the ability to solve analogies.

As an example, for the analogy "man: grandfather: woman: x" (read: man is to grandfather as woman is to x), what is x?

In the cell below, we show you how to use word vectors to find x using the most_similar function from the **GenSim documentation**. The function finds words that are most similar to the words in the positive list and most dissimilar from the words in the negative list (while omitting the input words, which are often the most similar; see this paper). The answer to the analogy will have the highest cosine similarity (largest returned numerical value).

```
[52]: # Run this cell to answer the analogy -- man : grandfather :: woman : x

pprint.pprint(wv_from_bin.most_similar(positive=['woman', 'grandfather'],___
negative=['man']))

[('grandmother', 0.7608445286750793),
    ('granddaughter', 0.7200808525085449),
    ('daughter', 0.7168302536010742),
    ('mother', 0.7151536345481873),
    ('niece', 0.7005682587623596),
    ('father', 0.6659888029098511),
    ('aunt', 0.6623408794403076),
    ('grandson', 0.6618767380714417),
    ('grandparents', 0.6446609497070312),
    ('wife', 0.6445354223251343)]
```

Let m, g, w, and x denote the word vectors for man, grandfather, woman, and the answer, respectively. Using **only** vectors m, g, w, and the vector arithmetic operators + and - in your answer, to what expression are we maximizing x's cosine similarity?

Hint: Recall that word vectors are simply multi-dimensional vectors that represent a word. It might help to draw out a 2D example using arbitrary locations of each vector. Where would man and woman lie in the coordinate plane relative to grandfather and the answer?

1.3.12 SOLUTION BEGIN

g - m + w ### SOLUTION END

1.3.13 Question 2.5: Finding Analogies [code + written] (1.5 points)

a. For the previous example, it's clear that "grandmother" completes the analogy. But give an intuitive explanation as to why the most_similar function gives us words like "granddaughter", "daughter", or "mother?

1.3.14 SOLUTION BEGIN

One possible reason is that granddaughter, daughter and mother are very tightly clustered together. Thus, when we evaluate 'grandfather' - 'man' + 'woman', the resulting vector is approximate to many words that describe female family roles such that we can't discern the expected meaning we seek. ### SOLUTION END

b. Find an example of analogy that holds according to these vectors (i.e. the intended word is ranked top). In your solution please state the full analogy in the form x:y:: a:b. If you believe the analogy is complicated, explain why the analogy holds in one or two sentences.

Note: You may have to try many analogies to find one that works!

```
[59]: ### SOLUTION BEGIN

x, y, a, b = 'serve', 'tennis', 'fight', 'boxing'
assert wv_from_bin.most_similar(positive=[a, y], negative=[x])[0][0] == b

### SOLUTION END
```

1.3.15 SOLUTION BEGIN

serve:tennis:: fight:boxing ### SOLUTION END

1.3.16 Question 2.6: Incorrect Analogy [code + written] (1.5 points)

a. Below, we expect to see the intended analogy "hand : glove :: foot : **sock**", but we see an unexpected result instead. Give a potential reason as to why this particular analogy turned out the way it did?

1.3.17 SOLUTION BEGIN

It's possible that the training data underpinning the corpus is derived from sources that use imperial units rather than metric, suggesting origins in the U.S. or U.K. Thus there are likely significantly more instances in the corpus of foot being associated to measurement units, in this case, area. ### SOLUTION END

b. Find another example of analogy that does *not* hold according to these vectors. In your solution, state the intended analogy in the form x:y :: a:b, and state the **incorrect** value of b according to the word vectors (in the previous example, this would be '45,000-square').

```
[55]: ### SOLUTION BEGIN
```

```
x, y, a, b = 'recruit', 'military', 'freshman', 'university'
pprint.pprint(wv_from_bin.most_similar(positive=[a, y], negative=[x]))
### SOLUTION END
```

```
[('sophomore', 0.46105578541755676),
  ('came', 0.46030867099761963),
  (',', 0.4584762156009674),
  ('army', 0.4517575204372406),
  ('after', 0.4469948709011078),
  ('guard', 0.4414523243904114),
  ('during', 0.4395792782306671),
  ('took', 0.43703970313072205),
  ('led', 0.43583187460899353),
  ('earlier', 0.43098458647727966)]
```

1.3.18 SOLUTION BEGIN

recruit:military :: freshman:university The incorrect value returned is sophomore ### SOLUTION END

1.3.19 Question 2.7: Guided Analysis of Bias in Word Vectors [written] (1 point)

It's important to be cognizant of the biases (gender, race, sexual orientation etc.) implicit in our word embeddings. Bias can be dangerous because it can reinforce stereotypes through applications that employ these models.

Run the cell below, to examine (a) which terms are most similar to "woman" and "profession" and most dissimilar to "man", and (b) which terms are most similar to "man" and "profession" and most dissimilar to "woman". Point out the difference between the list of female-associated words and the list of male-associated words, and explain how it is reflecting gender bias.

```
[('reputation', 0.5250177383422852),
  ('professions', 0.5178037881851196),
  ('skill', 0.49046966433525085),
  ('skills', 0.4900550842285156),
  ('ethic', 0.4897659420967102),
  ('business', 0.4875851273536682),
```

```
('respected', 0.485920250415802),
('practice', 0.482104629278183),
('regarded', 0.4778572618961334),
('life', 0.4760662019252777)]

[('professions', 0.5957458019256592),
('practitioner', 0.4988412857055664),
('teaching', 0.48292145133018494),
('nursing', 0.48211807012557983),
('vocation', 0.4788965880870819),
('teacher', 0.47160351276397705),
('practicing', 0.46937811374664307),
('educator', 0.46524322032928467),
('physicians', 0.4628995656967163),
('professionals', 0.4601393938064575)]
```

1.3.20 SOLUTION BEGIN

('even', 0.5398813486099243), ('brown', 0.5203480124473572), ('those', 0.5113789439201355),

In case a) the terms most similar to 'woman' and 'profession' and most dissimilar to 'man' are: 'reputation', 'professions', 'skill/s', 'ethics', ... These words describe professional conduct rather than the duties of a specific profession.

In case b) the terms most similar to 'man' and 'profession' and most dissimilar to 'woman' are 'professions', 'practitioner', 'teaching', 'nursing'... These words describe specific professions.

This suggests that the corpus has more documents that associate women to how they conduct themselves in any professional setting whereas men are more associated with the duties of their profession. ### SOLUTION END

1.3.21 Question 2.8: Independent Analysis of Bias in Word Vectors [code + written] (1 point)

Use the most_similar function to find another pair of analogies that demonstrates some bias is exhibited by the vectors. Please briefly explain the example of bias that you discover.

```
[60]: ### SOLUTION BEGIN

A = 'poor'
B = 'neighbourhood'
word = 'white'
pprint.pprint(wv_from_bin.most_similar(positive=[A, word], negative=[B]))
print()
pprint.pprint(wv_from_bin.most_similar(positive=[B, word], negative=[A]))

### SOLUTION END

[('black', 0.6006960868835449),
```

```
('or', 0.5104084610939026),
('for', 0.507294774055481),
('because', 0.5060834884643555),
('made', 0.49783584475517273),
('fact', 0.49733829498291016),
('while', 0.49245014786720276)]
[('neighborhood', 0.47155851125717163),
('flanked', 0.3984229266643524),
('suburb', 0.39282652735710144),
('downtown', 0.3882233500480652),
('house', 0.37897351384162903),
('black', 0.37190479040145874),
('mosque', 0.37186577916145325),
('neighbourhoods', 0.3705892860889435),
('residential', 0.36877232789993286),
('surrounded', 0.36684638261795044)]
```

1.3.22 SOLUTION BEGIN

In case a) the terms most similar to 'white' and 'neighbourhood' and most dissimlar to 'poor' reveal words such as 'black' and 'brown'.

In case b) the terms most similar to 'poor' and 'white' and most dissimilar to 'neighbourhood' reveal words such as 'downtown, 'black', and 'mosque'.

This suggests some bias that associates race and religion to socio-economic status. ### SOLUTION END

1.3.23 Question 2.9: Thinking About Bias [written] (2 points)

a. Give one explanation of how bias gets into the word vectors. Briefly describe a real-world example that demonstrates this source of bias.

1.3.24 SOLUTION BEGIN

Bias gets into word vectors largely because of data introduced into the corpus. The data may be gathered from sources that have inherent bias. One real world example is youtuber Yannic Kilcher, who trained a language model on 4-chan forum content. The model 'perfectly encapsulated the mix of nihilism, offensiveness, trolling and deep mistrust of any information'.

Source: https://www.youtube.com/watch?v=efPrtcLdcdM ### SOLUTION END

b. What is one method you can use to mitigate bias exhibited by word vectors? Briefly describe a real-world example that demonstrates this method.

1.3.25 SOLUTION BEGIN

One technique to mitigate bias is to de-tune the effects of the bias in co-occurrence probabilities. Another technique to mitigate bias is to add a 'regularization' term in the cost function that penalises biased terms. For example, we could penalize words associated with professions that

have high values in dimensions associated with gender. This would help create words related to professions that are more gender neutral.

Source: https://cs229.stanford.edu/proj2016/report/BadieChakrabortyRudder-ReducingGenderBiasInWordEmbeddings-report.pdf ### SOLUTION END

2 Submission Instructions

- 1. Click the Save button at the top of the Jupyter Notebook.
- 2. Select Cell -> All Output -> Clear. This will clear all the outputs from all cells (but will keep the content of all cells).
- 3. Select Cell -> Run All. This will run all the cells in order, and will take several minutes.
- 4. Once you've rerun everything, select File -> Download as -> PDF via LaTeX (If you have trouble using "PDF via LaTex", you can also save the webpage as pdf. Make sure all your solutions especially the coding parts are displayed in the pdf, it's okay if the provided codes get cut off because lines are not wrapped in code cells).
- 5. Look at the PDF file and make sure all your solutions are there, displayed correctly. The PDF is the only thing your graders will see!
- 6. Submit your PDF on Gradescope.