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Master's Thesis

MASTERS OF ARTIFICIAL INTELLIGENCE AND COMPUTER SECURITY

Fuzzy-Genetic Hybrid Models for Large-Horizon Deterministic Planning

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Introduction

1.1 Motivation and Context

A deterministic planning problem for a stateful agent is one of the most generic formulations in artificial intelligence. The task can be summarized as selecting a sequence of actions which transforms the state of an agent into a desired goal state. This formulation naturally appears in a wide range of real-world domains: robotics (planning robot trajectories under resource and time constraints), industrial scheduling (allocating tasks to maximize production while minimizing downtime), and control systems (maintaining stability of dynamic processes under changing conditions).

The key difficulty in such problems is the combinatorial explosion. As soon as the number of available actions grows and the planning horizon becomes long, the search space of all possible trajectories expands exponentially. This phenomenon, commonly referred to as the curse of dimensionality, renders classical exhaustive approaches infeasible even for moderately sized problems.

Works like [4] cover both the real-world applications and a significance of the curse of dimensionality.

In this work, we use the Japanese computer game Princess Maker 2 (Gainax, 1993) as a motivating case study. While the game itself is narrative-driven and contains many mechanics that go beyond formal modeling, its core gameplay loop is a textbook instance of a deterministic planning problem. The player controls a stateful agent — the daughter character — by repeatedly selecting actions such as study, work, or leisure. Each action deterministically modifies a set of numerical attributes, and after a fixed horizon of ingame years, the outcome is evaluated against predefined conditions that determine the "ending."

Stripped of its narrative elements, Princess Maker 2 yields a highly formal planning problem: an agent with dozens of numeric attributes, several dozen possible actions, and a planning horizon of several thousand steps. This combination of a large state space, broad action set, and long horizon exemplifies the type of problem where classical planners and reinforcement learning approaches both struggle. At the same time, because the formulation is generic, any progress on this problem carries implications well beyond the original game context.

In the following section we will briefly review the most obvious approaches to this problem, namely, automatic planning theory and reinforcement learning, and discuss

1.2 Existing Approaches

1.2.1 Automatic Planning Theory

Automatic planning in artificial intelligence is historically grounded in the STRIPS [6] formalism, which defines planning as the composition of operators that transform an initial world model into one satisfying a goal condition. In principle, this description matches exactly the type of solver we are aiming for: we have a stateful agent, a set of deterministic actions, and a requirement to reach a specified goal state.

Modern planners, such as ENHSP [14] [13], extend this formalism to support numeric fluents and continuous effects. On small-scale problems they have been demonstrated to work effectively, often guaranteeing optimality of the resulting plan. For example, existing benchmarks ¹ include instances with up to forty numeric variables and around ten actions, which can be solved in practical time.

However, the core assumptions of classical planning diverge from the requirements of our case. Most planners are designed to minimize plan length, i.e., to find the shortest action sequence that satisfies the goal. In contrast, the Princess Maker 2 formulation requires executing a fixed number of steps before the final state can be evaluated. No-operation actions are not available, so every step transforms the agent's state irreversibly. This means that reaching the goal "too early" is not valid — it is only the state after the full horizon that determines success.

In addition, the problem of scale remains prohibitive. Even if the goal condition could be reformulated to suit the planner's semantics, the state space induced by 23 attributes, 27 actions, and thousands of steps is far outside the scope of tractable automatic planning. Research does exist on scaling planners with temporal logics [8] and heuristics, but these approaches are not focused on high-dimensional numeric fluents of the type present in our motivating case.

1.2.2 Reinforcement learning

Reinforcement learning [18] (RL) is another approach which seems, at first glance, to be a natural fit for the problem. In RL, we model an agent interacting with an environment: the agent observes a state, selects an action, and receives a reward. Over time, the agent is expected to learn a policy that maximizes cumulative reward. The analogy with our setting is straightforward — the state is the character's attributes, the actions are the available schedule choices, and the "reward" is the final outcome at the end of the planning horizon.

However, the practical obstacles are significant. The first is the dimensionality of the state space. With 23 attributes each taking values in the range of roughly 0 to 500, the number of possible states is astronomically large. A naive tabular representation of a Q-function would require a table of size 27×500^{23} , which is intractable to store or

¹https://github.com/hstairs/enhsp/tree/enhsp-20

update. While function approximation can reduce this requirement, it does not remove the exponential blowup inherent in such spaces.

The second issue is the length of the planning horizon. In the simplified gameplay setup, the player makes three choices per month for ten in-game years, which already leads to a search tree over 360 steps. In the full day-by-day formulation the horizon is an order of magnitude longer. Standard RL algorithms struggle when the reward is sparse and delayed, as in this case where only the terminal state matters. Exploration becomes ineffective because the probability of randomly reaching a good ending within thousands of steps is vanishingly small.

Finally, unlike in many RL benchmarks, our problem does not allow neutral or reversible actions. Every action irreversibly changes the state, which exacerbates the exploration problem. Taken together, these aspects make classical reinforcement learning algorithms impractical for the problem scale we consider.

1.3 Fuzzy Logic and Fuzzy Controllers

Fuzzy logic, introduced by L. Zadeh in 1965, extends classical set theory by allowing partial membership of elements in a set. Instead of a variable belonging to a set either completely or not at all, in fuzzy logic a variable may belong to a set with a degree between 0 and 1. This allows us to model linguistic terms such as "low," "medium," or "high" in a mathematically precise way.

A fuzzy controller applies this idea to decision-making. The system is defined through linguistic variables with associated membership functions, and a collection of symbolic rules. A typical example outside this work would be:

If temperature is high then fan speed is high.

Here, both "temperature" and "fan speed" are fuzzy variables, and the rule connects them in a way that corresponds directly to human reasoning. After applying fuzzification (mapping numeric input values into fuzzy terms), rule evaluation, and defuzzification (converting fuzzy outputs back into numeric values), the controller produces an actionable decision.

The benefit of this approach is the ability to capture domain knowledge without enumerating every possible combination of numeric parameters. Instead of constructing a complete reward table or transition map — which would be infeasible in large state spaces — we specify a relatively small set of symbolic rules which generalize across many states. This makes fuzzy controllers attractive for problems where expert intuition about the domain exists, but exhaustive specification is impossible.

In the context of this work, fuzzy controllers provide a mechanism to express priorities over actions in symbolic terms, forming a bridge between human-understandable heuristics and algorithmic decision-making.

1.4 Genetic Algorithms

Genetic algorithmss [16] [1] (GAs) are a class of optimization methods inspired by biological evolution. A population of candidate solutions is maintained, where each solution

is represented as a genome — a sequence of values encoding the parameters of interest. The algorithm proceeds iteratively through the following steps:

- 1. Evaluation: every genome is assigned a fitness score according to an objective function.
- 2. Selection: genomes with higher fitness are more likely to be chosen for reproduction.
- 3. Crossover: pairs of genomes exchange parts of their structure, creating new offspring that combine traits of both parents.
- 4. Mutation: with low probability, individual genes are randomly altered, introducing diversity.
- 5. Replacement: the new generation replaces the old, and the process repeats.

Over time, the population tends to evolve towards fitter solutions, even when the search space is large, non-linear, or poorly understood. The method does not guarantee a globally optimal solution, but it often finds good approximations in domains where exact methods are computationally infeasible.

The main advantage of GAs is that they treat the problem as a black box: only the ability to evaluate candidate solutions is required, while no assumptions about continuity, differentiability, or convexity are needed. This makes them well suited for combinatorial or highly non-convex problems.

In the context of this work, genetic algorithms will be used to optimize the inclinations — latent behavioral parameters that guide the fuzzy controller. This reduces the original planning problem from direct search over long sequences of actions to an evolutionary search in a much smaller parameter space.

1.5 Our Proposed Approach

The discussion above shows that classical approaches such as automatic planning or reinforcement learning are unable to scale to the requirements of our motivating problem. To address this, we propose a hybrid heuristic method which combines symbolic reasoning with evolutionary optimization.

The core idea is to replace direct search over complete action sequences with search over a smaller set of latent behavioral parameters, which we call inclinations. These inclinations represent tendencies toward particular groups of actions. A fuzzy controller then maps the inclinations together with the current state into a concrete choice of action.

This formulation has two benefits. First, it allows us to encode domain knowledge directly into the fuzzy rule base, reducing the effective dimensionality of the search. Second, it enables optimization to take place in the smaller inclination space, rather than in the exponentially large space of all possible trajectories. The resulting search problem becomes tractable for evolutionary algorithms such as genetic algorithms, which only require evaluation of candidate solutions, not explicit enumeration of the search space.

The hypothesis of this work is that such a hybrid fuzzy-genetic approach can find valid solutions in polynomial-like time in cases where reinforcement learning or automatic planners fail due to combinatorial explosion.

The overall process is illustrated in Figure 1.1.

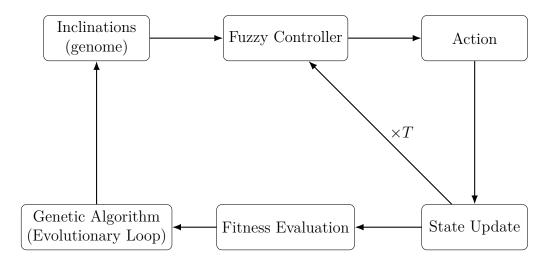


Figure 1.1: Schematic overview of the fuzzy-genetic approach.

1.6 Comparative assessment

To summarize the discussion above, in the Table 1.6 we compare the two obvious alternatives with the hybrid fuzzy-genetic approach proposed in this work.

Method	Strengths	Weaknesses in our context	
Automatic plan-	- Formal match to state-	- Focus on minimizing plan	
ning theory	action-goal formulation.	length, incompatible with fixed-	
	- Established solvers (e.g.,	horizon requirement.	
	ENHSP) exist.	- No-operation actions not avail-	
	- Optimality guarantees on	able, premature goal achievement	
	small problems.	invalidates plan.	
		- State space scaling beyond prac-	
		tical limits.	
Reinforcement	- Natural agent/action/re-	- Curse of dimensionality: 500 ²³	
learning	ward formalism.	states in the motivating case.	
	- Flexible and general	- Very long horizons with sparse	
	framework.	terminal rewards.	
	- Large body of research	- No reversible or neutral actions,	
	and practical algorithms.	exploration ineffective.	
Fuzzy-genetic	- Encodes domain knowl-	- Manual design of fuzzy rule base	
hybrid approach	edge symbolically via fuzzy	is non-trivial.	
(proposed)	rules.	- No global optimality guaran-	
	- Dimensionality reduction	tees.	
	through latent variables	- Performance depends on quality	
	("inclinations").	of rules and evolutionary hyper-	
	- Optimization operates on	parameters.	
	reduced space, not on raw		
	action sequences.		

Table 1.1: Comparison of alternative methods for solving large-horizon deterministic planning.

This comparison highlights why classical planners and reinforcement learning approaches are unsuitable for the case we focus on, and motivates the introduction of a fuzzy-genetic heuristic, which will be presented in detail in Chapter 3.

1.7 Contributions and Objectives

- 1. Formalization of Princess Maker–style problems as deterministic planning with large horizons.
- 2. Introduction of inclinations + fuzzy rule base as a dimensionality reduction heuristic.
- 3. Implementation of a solver using fuzzylite (fuzzy logic) and pagmo (evolutionary algorithms).
- 4. Experimental evaluation on trivial and baseline control cases.

This work is foundational proof of concept, not yet a full game solver nor a generic ready-to use solver for a wide range of real-world problems.

In Chapter 2 we now give a precise problem formulation, and in Chapter 5 we develop the proposed fuzzy-genetic heuristic approach in detail.

Formal problem statement

As follows from the section ??, formally we have a choice of whether to treat this as a planning problem or a control problem. Despite Reinforcement learning not being fit for our cause, we will still approach our origin problem as a control problem, as it allows us to formally introduce our solution approach later in the chapter 3.

2.1 Actor behavior as a control problem

Assuming we have a character described as a set of numeric characteristics

$$\mathbf{x} \in \mathbb{Z}^n \tag{2.1}$$

we have a set of possible actions

$$A = \{a_1, a_2, \dots, a_m\} \tag{2.2}$$

which collectively form a transfer function

$$f(\mathbf{x}, a) = \mathbf{x}' \tag{2.3}$$

To describe the desired outcome, we first declare a fitness function mapping the state to a numerical value:

$$\Phi: \mathbf{x}' \to \mathbb{R} \tag{2.4}$$

a goal fitness value

$$\mathbf{G} \in \mathbb{R} \tag{2.5}$$

and a planning horizon

$$T \in \mathbb{Z}$$
 (2.6)

We want to get an ordered actions sequence of length T which will lead \mathbf{x} to some \mathbf{x}^* :

$$\mathbf{a} \in A^T, x_o = \mathbf{x} : \bigodot_{i=1}^T f(x, a_i) = \mathbf{x}^*$$
(2.7)

(where \bigcirc is a fold operator) such as:

$$\Phi(\mathbf{x}^*) > \mathbf{G} \tag{2.8}$$

The transfer function f is assumed to be completely determined, and the whole process being non-stochastic. This is a significant restriction which cannot be lifted for the proposed solution to work.

2.2 Dimensionality explosion stemming from the original context

We assume a fixed-length trajectory of actions, each of which transforms the state of the system according to a known deterministic transfer function (2.3).

This means two restrictions:

- 1. No-operation actions are prohibited, each step must result in a meaningful state transformation, reflecting the irreversible nature of time.
- 2. Goal state must still be in effect at the step T.

While the agent cannot avoid taking actions — and hence cannot avoid changes to the system — it is allowed to evaluate its progress toward the goal at every intermediate state. In this sense, the problem is not a pure planning task but an episode-based control problem with delayed evaluation.

In this work we'll focus specifically on the cases which lead to combinatorial explosion for classical solutions, that is, when we have sufficiently large amount of characteristics, actions to choose from and most importantly, very large planning horizon:

$$n > 25 \tag{2.9}$$

$$m > 24 \tag{2.10}$$

$$T > 360$$
 (2.11)

The origin *Princess Maker* problem is the lower edge of the cases we are interested in.

With these restrictions in place, a need in an heuristic arises to perform efficient search in the state space, as its size becomes unrealistically large.

Proposed solution approach

Classical reinforcement learning methods become intractable in this domain due to the high dimensionality of the state space, large action set, and long planning horizon. Moreover, the inability to halt or take neutral actions further exacerbates the combinatorial explosion of the trajectory space.

To address this, we introduce a heuristic dimensionality reduction via the concept of inclinations — latent behavioral parameters — and model the behavior policy as a fuzzy controller which maps the current state and inclinations to a concrete action.

This parametrization constrains the space of possible behaviors, making the optimization tractable. Instead of learning or searching over action sequences directly, we perform optimization in the significantly smaller space of inclinations, evaluating the final outcome after T steps. The resulting problem becomes an offline, black-box control task—suitable for evolutionary algorithms, rather than classical RL or automatic planning methods.

3.1 Using the domain knowledge to reduce dimensionality

In this work we evaluate an approach which is defined as follows.

Let's assume that we can segment the set of possible actions to clusters with the following particularities:

- 1. actions in the same cluster lead to "similar" changes in the character state \mathbf{x} .
- 2. the cluster as a whole can be described symbolically

In this case we can synthesize a set of numeric characteristics which we'll call "inclinations":

$$\mathbf{I} \in \mathbb{Z}^q \tag{3.1}$$

$$q \ll n$$
 (3.2)

From this, we can define a set of fuzzy rules[12] mapping the inclinations to action choices:

- 1. if an inclination I_i has a fuzzy value V_I ,
- 2. and the current state \mathbf{x} has fuzzy values V_i^x
- 3. then P_a , the priority of an action a, is a fuzzy set V_A .

After the defuzzification of all the inferred fuzzy values P_a we select an action with the highest priority.

The selection and design of fuzzy rules is a critical aspect of this approach. In this thesis, the fuzzy rule base is constructed manually, leveraging domain knowledge to define the mapping from inclinations to action priorities. Future research may investigate automated methods for generating fuzzy rules, such as clustering or machine learning techniques, to further improve scalability and reduce manual effort.

While it is theoretically possible to define fuzzy rules that map every possible inclination vector \mathbf{I} or even every state \mathbf{x} to action priorities, such exhaustive rule sets would quickly become infeasible due to combinatorial growth. This reinforces the importance of dimensionality reduction and clustering in making the fuzzy-genetic approach tractable for high-dimensional planning problems.

The assumption which we explore among others in this work is the practical possibility to write a coherent set of fuzzy rules which will be clustered around the clusters of actions, and each inclination will tend to map to its own cluster of actions.

Now, using such a fuzzy controller $\xi(I, \mathbf{x})$ we can construct the goal function:

$$g(I, \mathbf{x}) = \bigodot_{i=1}^{T} f(x, \xi(I, x_i))$$
(3.3)

the above formula being subject to improvements in expressiveness, the main point of which being the fuzzy controller $\xi(I, x_i)$ selecting the action to perform on the step i according to the inclinations and (ideally) the current state x_i .

The argument \mathbf{x} is essentially a constant for both (2.7) and (3.3). As the transfer function f is non-stochastic, \mathbf{I} uniquely maps to the actions sequence \mathbf{a} . Thus, given (3.2), we effectively performed dimensionality reduction on the original problem.

We can find $\arg \max(g)$ now using an appropriate optimization method. For this work, because of a strong biosocial analogies a genetic algorithm[10] was chosen, with the vector of inclinations **I** as a chromosome (every inclination value being a separate gene).

3.2 Hypothesis

The hypothesis explored in this work is that the combination of assumptions described above constructs an heuristic which allows finding a locally optimal solution for the problem defined in chapter 2 in a polynomial time.

3.3 Objectives

This is a foundational work which proves a concept.

That is, whether a fuzzy-genetic heuristic can effectively solve high-dimensional deterministic planning problems through dimensionality reduction and symbolic reasoning. In particular, we aim to:

- 1. Formalize the problem as an optimization task.
- 2. Implement a working solver.
- 3. Evaluate the performance of the solver on a set of test cases of increasing complexity.
- 4. Analyze the results to draw conclusions about the effectiveness of the approach.

An objective 1 has been reached in the chapter 2.

As soon as our solver will be able to produce solutions with the fitness representing reaching the goal state, an objective 2 will be considered reached.

An objective 3 is covered by the chapters 6 and 7. Finally, chapter 8 covers the analysis of the results and conclusions about its applicability.

Methodology

In this section we will discuss the theory which this work is build upon, namely, fuzzy logic [12] and evolutionary algorithms [10].

4.1 Encoding domain knowledge of actions as a fuzzy controller

Normally the Fuzzy logic is being explained from the fuzzy set theory by L. Zadeh [20], but for this particular work the most important part of the fuzzy logic is the fuzzy rules for the fuzzy controller so it's more beneficial to start with them.

In the scope of the FL it is possible to express the domain knowledge in the form of symbolic rules, with the general form as follows:

```
If (input variable A) has a (fuzzy value Fa) then (output variable B) has a (fuzzy value Fb)
```

For example, for our particular problem and solution method:

```
If InclinationAggressiveness is High then DuelingClassesPriority is High
```

This rules format depends on the concept of the **Fuzzy Variable**, which is a combination of four major parts:

- 1. Name
- 2. Range of "strict" values
- 3. "strict" value itself
- 4. Set of fuzzy sets describing the possible fuzzy values of this variable

The concept of Fuzzy Variable, in turn, depends on the concept of a **fuzzy value**, which is a combination of two major parts:

1. Name

2. Membership function

Where the **membership function** is a continuous function mapping the input "strict" values to real numbers between 0 and 1. The *membership function* of a fuzzy value describes the *measure of belonging* of the current "strict" value of the variable to the given symbolic **term**, for example, "high", "low" and such. Because of the *terms* being literally words from a natural language, fuzzy variable is also called a **linguistic variable**.

Let's give an example. Assume the following fuzzy variable:

$$S = (N, R, V, T) \tag{4.1}$$

$$N =$$
"Strength" (4.2)

$$R = \mathbb{Z} \in [0, 100] \tag{4.3}$$

$$V \in R \tag{4.4}$$

$$T = (("Low", f_l), ("Acceptable", f_a), ("High", f_h))$$
(4.5)

It specifies three *fuzzy terms* for the numeric property "Strength", which can have integer "strict" values from 0 to 100. Thus, when we measure this property and provide a strict value for "Strength", we can determine the values of *membership functions* of its three *fuzzy terms*. For example, if V = 72 then

$$T = (("Low", f_l(72)), ("Acceptable", f_a(72)), ("High", f_h(72)))$$
(4.6)

Which should be interpreted as "Strength" of 72 being at the same time $f_l(72)$ "Low", $f_a(72)$ "Acceptable" and $f_b(72)$ "High".

The process of calculating the values of membership functions for all the terms of a linguistic variable given its strict value is called **fuzzification** of this value.

The main point of the fuzzification, which we exploit in our method and which is at the core of the fuzzy control theory, is that we get the formal mechanism of transforming numeric values to domain-specific inexact vocabulary.

Fuzzy logic provides the reverse process as well. It is possible to specify the values of the membership functions of all the terms in T of the fuzzy variable, and from them calculate the "strict" value V. This process is called **defuzzification** of the linguistic variable.

Continuing the above example, we can start by specifying the fuzzy values of "Strength" first, possibly, if we measure it by some inexact vague means: $f_l = 0.4$, $f_a = 0.8$, $f_h = 0$.

Then, depending on the exact shape of the functions f_l , f_a and f_h defuzzification gives us a strict value of "Strength", say, 42.

Given all the above, a **fuzzy controller** is an algorithm which performs three large steps:

- 1. Applies fuzzification of the values of all the input variables (antecedents of the fuzzy rules)
- 2. Evaluate all the fuzzy rules, obtaining the fuzzy values of the output fuzzy variables

3. Applies defuzzification to the output fuzzy variables, obtaining their strict values.

The above algorithm is called a **Mamdani fuzzy controller** [9] and it's the one which we'll use in this work.

In our system, we're going to have the vector of inclinations and the current state of the specimen as input variables for the controller, and have the priorities of actions as the output variables. This will allow us to imitate the process of "decision making" of the specimen to choose the next action to perform.

The major benefit and the core reason for the fuzzy controller is the ability to encode the domain knowledge in a limited set of rules which will be formally processed.

Compared to, for example, some of the reinforcement learning methods, we don't need to specify the full table of rewards for every possible action-state combination. It is enough to specify one rule for every available action and the controller will already become fully functional. With some configuration of rules it's possible to write even less of them.

This allows to simplify the implementation of the solver, because one of the main weaknesses of the proposed solution is writing the fuzzy rules by hand.

The second benefit of using the fuzzy controller for decision making is that it can be applied without major changes to non-deterministic, stochastic environment, for example, if the actions would be allowed to make randomized changes to the specimen's state, that is, if the transfer function would not be pure. It opens up the possibilities to explore this topic further in the later works.

4.2 Control feedback loop as a fitness function

A single trajectory in the action space is explored using the following process.

- 1. We start with the initial state \mathbf{x}_0 and the given set of inclinations \mathbf{I}^k
- 2. We evaluate both \mathbf{x}_0 and \mathbf{I}^k with the preconfigured fuzzy controller
- 3. The defuzzified output of the controller is the set of priorities for all the actions. We pick the action with the highest priority. Tiebreaker is the position of the action in the list.
- 4. Action is executed and if we haven't made T actions yet we return to the step 2
- 5. After T executed actions we apply the goal conditions predicate $\Phi(\mathbf{x}^*)$ and calculate the fitness based on that.

It is important to understand that the state of a specimen is a transient value, used only for calculations of the final fitness after T iterations. The solution we seek is fully encoded in the inclinations vector \mathbf{I} , which stays unchanged for the entirety of the control loop.

4.3 Global optimization using an evolutionary algorithm

Strong biosocial analogies and the configuration of the control loop from 4.2 suggest us to use the evolutionary algorithms [16] [1] for optimization. This is what would be used in this work. However, in principle, any algorithm which is able to use the concept of a fitness function would be applicable here.

Evolutionary algorithms can be explained with an example of the so-called Simple Genetic Algorithm ¹.

SGA operates on the set of **specimens**, each one being a single option in the search space to explore. A specimen is classically a list of characters, which is called literally a **genome**. The whole set of specimens is called a **population**.

In our case, a specimen would be a list of inclination values.

Every specimen in a population is evaluated using the **fitness function**, producing a fitness value.

Then, a **selection operator** is applied, choosing a subset of the population. For example, our selection operator may be choosing the top 50% of the population by their fitness value.

After the selection, we apply the **crossover operator** to the pairs of selected specimens' genomes. The classical crossover operator picks a single place inside both of the genomes and then swaps the resulting halves between them. For example, a genome 'aaaa000' and a genome '1111bbb' after the crossover at point 5 become 'aaaabbb' and '1111000'.

After the crossover we apply the **mutation operator** to all of the selected genomes. The mutation changes (with some low probability) individual genes in the genomes at random. For example, we can have a mutation operator which has 0.01 probability of flipping a gene in the genome from 'a' to 'b' and *vice versa*. Then, we have 0.002 probability of a specimen with a genome 'aaabb' turning into 'ababb'.

After the crossover and mutation, we finally apply the **replacement** which forms the new population for the next generation and the next round of evolution. For example, we can use a so-called $(\mu + \lambda)$ -evolution strategy [15]: calculate the fitness for all the new genomes and then pick s ones with the best fitness from both the old genomes and new ones, where s is the target population size. The size of the population is being kept constant for the classical genetic algorithms, the role of the replacement operator is specifically to enforce that.

In the approach described in this work, the fitness function is the control loop described in the previous section 4.2. The genome of the specimen is the vector of inclinations. And due to the choice of the specific library for the implementation of the evolutionary algorithms we have a wide selection of them, which means, we can explore different options starting from the Simple Genetic Algorithm and continuing with more complicated options.

The library Pagmo [2] includes a lot of already implemented different evolutionary algorithms apart from the simple genetic algorithm so it enables us easier exploration of possibilities in optimizing the full solver.

¹https://esa.github.io/pagmo2/docs/cpp/algorithms/sga.html

Implementation

The technical implementation of the method is performed in C++ [17] using the libraries FuzzyLite [11] and Pagmo [2]

5.1 Choice of a C++ language as foundation

As the root problem of this work is the problem of scale, it has been decided that we trade comfort of experimentation for pure processing power.

Contemporary C++, starting with the standard version 20, allows for a very high-level code as readable as a natural language. It also has libraries for both the fuzzy logic [11] and evolutionary computations [2] for us to not implement any of them from scratch.

In talking on choice of the language for the implementation we cannot avoid comparisons with Python ¹, assumed leader and language of choice for scientific experiments. As has been stated above, it has been conscious decision to trade the ability to make rapid changes in the code, especially the ability to run convenient machinery like Jupyter notebooks ², for the raw processing power. This is because the C++20 and later is expressive enough to be as readable as Python sans some of the required syntax boilerplate, and in reality the most painful part of choosing C++ is building the program to be crossplatform, as Python programs are, and doing that with the code which uses third-party libraries is a nontrivial implementation problem.

5.2 Fuzzylite library for the fuzzy controller implementation

This work turned out to be more or less an assessment of usefulness of the fuzzylite [11] C++ library in addition to the main goal. While being fully open sourced with a non-restrictive license terms, actually adding it to an existing C++ program is a task certainly not feasible for an arbitrary computer scientist not being a seasoned software engineer

¹https://www.python.org/

²https://jupyter.org/

at the same time. Which is a shame, as it offers a straightforward idiomatic API which allows expressing the algorithms in a readable format.

fuzzylite also provides a domain-specific language for specifying the fuzzy controller, which allows us to describe this part of the algorithm in a language more expressive than the raw C++ function calls.

On the following code example is a description of a fuzzy variable in the DSL of fuzzylite.

```
InputVariable: PhysicalInclination
enabled: true
range: 0 1.000
lock—range: false
term: tiny Ramp 0.330 0.000
term: low Triangle 0.000 0.330 0.670
term: high Triangle 0.330 0.670 1.000
term: highest Ramp 0.670 1.000
```

Base syntax of this DSL is essentially YAML 3 .

At the first line we specify the name of the variable and whether it will be used as an input or an output for the fuzzy rules. Among the properties of the variable we have the numerical range of strict values for it, supplementary flags enabled and lock-range not interesting at this moment and several term declarations which are the concise descriptions of all the linguistic terms of the variable.

In the example only two membership functions are used: Ramp and Triangle, but fuzzylite has around 20 of them predefined at the time of writing this report.

The following line specifies a single term of a fuzzy variable:

```
term: tiny Ramp 0.330 0.000
```

In this line, the word tiny is the symbolic name of the term, which represents the vague description of the value directly from the domain knowledge.

The word Ramp is a keyword selecting the appropriate membership function from among the ones built-in in the fuzzylite library. Figure 5.1 displays the plot of this function.

The notation $0.330\,0.000$ is an internal trick of the library to indicate the downward slope of the ramp by convention instead of some other method. Writing the x values in ascending order would mean that the ramp is increasing instead of decreasing.

Given the definitions of all the fuzzy variables, the list of rules of the fuzzy controller is specified in almost the natural language ⁴:

```
RuleBlock: mamdani
enabled: true
conjunction: Minimum
disjunction: Maximum
implication: AlgebraicProduct
```

³https://yaml.org/

⁴"then" clauses has been moved to the next lines for the line to fit on the paper, in an actual code the rule is written on a single line without breaks

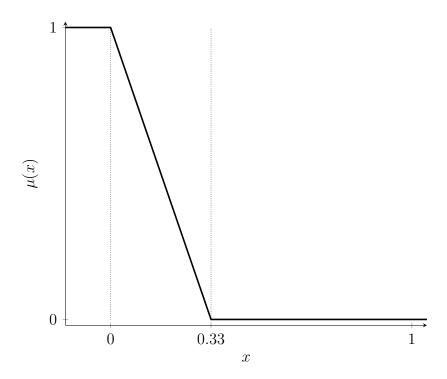


Figure 5.1: "Left ramp" membership function: $\mu(x) = 1$ when x < 0, linearly decreasing on [0, 0.33], and $\mu(x) = 0$ when x > 0.33.

```
activation: General
rule: if PhysicalInclination is low and MentalInclination is low
then MannersClass is high
rule: if PhysicalInclination is low and MentalInclination is low
then Hunting is low
```

RuleBlock declaration specifies what is the exact variant of fuzzy controller we are going to use, the Mamdani [9] one or Sugeno [19] one. In the scope of this work we will be using Mamdani controllers exclusively.

5.3 Pagmo library for evolutionary computations

Authors of the Pagmo library designed a very high-level API for the evolutionary computation, which can be completely summarized in the following code snippet:

```
// declare the problem to solve
pagmo::problem prob(pm_problem{});

// declare the algorithm to use
pagmo::algorithm algo(pagmo::sade(100));

// declare the population to use
pagmo::archipelago archi(16u, algo, prob, 20u);

// work
```

```
archi.evolve(10);
archi.wait_check();

for (const auto& isl : archi)

const auto& champion = isl.get_population().champion_x();

// for example, print the champion.

}
```

Pagmo library includes a large amount of already implemented algorithms which brings us two benefits:

- 1. there's no need to implement them from scratch
- 2. it's easy to experiment as we can change the algorithm just by changing the function name to use in the pagmo::algorithm object creation.

Pagmo uses a Generalized Island Model to perform computations in parallel [7], and because of that instead of the "population" the base terminology is "archipelago". An archipelago consists of "islands", each containing a separate population to evolve.

After we run an evolution, we can visit every island and check the final result of the population evolution, including getting the best specimen, called "champion" in Pagmo.

5.4 Implementing the method using fuzzylite and pagmo libraries

To implement our solver in this computational framework, first we need to declare our own "problem" class compatible with pagmo::problem class requirements.

For this, in the span of this work, it is enough for us to declare the following structure with two member functions:

```
struct pm_problem {
    std::pair<pagmo::vector_double, pagmo::vector_double> get_bounds() const
    {
        return { {0., 0.}, {1., 1.} };
    }

    // Implementation of the objective function.
    pagmo::vector_double fitness(const pagmo::vector_double& dv) const
    {
        // ...implementation of the fitness function...
    }
};
```

The function **get_bounds** describes the range of values from which the specimens would be generated.

In the example above, we declare that every specimen is a vector of two real values between 0 and 1 inclusive. This is the setup for the "Trivial case" experiment from the section 6. Every element of the vector would be used as an inclination value in the fuzzy inference stage. Depending on the amount of inclination values we require, we specify vectors of according length as return values of this function.

The function **fitness** calculates the fitness value of the given specimen. In a classical evolutionary optimization problems, this fitness function is a pure mathematical function easy to calculate, so the algorithm itself presents the main computational challenge for the computing device. In our problem, however, this function contains the implementation of the control loop described in the section 4.2.

```
pagmo::vector_double fitness(const pagmo::vector_double& dv) const

// Inclinations is an alias for std::tuple < double, double >
const Inclinations specimen { dv[0], dv[1] };

auto engine = init();

return { simulate(specimen, engine.get())};

}
```

This function does three things:

- 1. converts the specimen from the raw data provided by Pagmo to the vector of inclinations we use in our fuzzy controller. For simplicity the mapping is direct: values of genes and values of inclinations both belong to $[0,1] \in \mathbb{R}$.
- 2. initializes the fuzzy controller ⁵
- 3. runs the full simulation

Fuzzy controller initialization is a by-the-book copy of the code from fuzzylite documentation.

```
std::unique_ptr<fl::Engine> init()
  {
2
    // Initialize the engine
3
    std::string path{ "C:\\projects\\pm_solver\\Trivial.fll" };
    std::unique_ptr<fl::Engine> engine{ fl::FllImporter().fromFile(path) };
5
    // Checking for errors in the engine loading.
    std::string status;
    if (not engine->isReady(&status))
9
10
      throw fl::Exception("[engine_error]engine_is_not_ready:_\n" + status);
11
12
13
    return engine;
14
  }
15
```

⁵In the final implementation of the solver, initialization of the engine is performed in a more optimized way, only once at the launch of the program. Instead of initializing the fuzzy controller every time for each instance of the problem in a highly parallel Pagmo run, we make an individual copy of the already prepared controller for each specimen to use.

The main point is that the specification of input and output variables and fuzzy rules is kept as a separate text file loaded at runtime.

The simulation is an implementation of the control loop from the section 2

```
double simulate (const Inclinations & inclinations, fl:: Engine * engine)
2
     // Initialize a character
3
     Stats stats { 0.0, 0.0, 0.0, 0.0 };
5
     // Set inclinations
6
     engine->getInputVariable("PhysicalInclination")
         ->setValue(std::get<0>(inclinations));
     engine->getInputVariable("MentalInclination")
           ->setValue(std::get<1>(inclinations));
10
11
     for (int i = 0; i < T; ++i)
12
13
       single_step(stats, engine);
14
15
16
     return fitness (stats);
17
  }
18
```

We prepare the character with the starting characteristics, load the fuzzy controller with the values of inclinations and then repeat the action choice and application T times.

```
void single_step(Stats& stats, fl::Engine* engine)

// Choose an action based on the current stats and inclinations
std::string chosen_action_name = choose_action(engine, stats);

// Apply the effects of the chosen action
Stats stats_diff = actions.at(chosen_action_name);
// sum_stats is just a helper for summing two std::tuple values
stats = sum_stats(stats, stats_diff);
}
```

This function for simplicity of implementation references the statically created global dictionary **actions** which maps action names to the changes in characteristics. With this approach once we know the name of the chosen action we can extract the characteristics changes vector and apply it to the current character state via summation.

Below is an example declaration of **actions** from the section 6. Four real values bound to each action name are changes in the four characteristics of the current character (changes in the current state of the agent).

```
const std::unordered_map<
std::string, // job name
stats // stat changes after taking this action
state // stat changes after taking this action
state // stat changes after taking this action
state // state stat
```

```
7  { "ScienceClass", { 0.0, 0.0, 0.02, 0.0 } },
8  { "MannersClass", { 0.0, 0.0, 0.0, 0.02 } },
9  };
```

An implementation of the **choose_action** is very technical but it boils down to just two things:

- 1. run the fuzzy controller loaded with the current values of stats and inclinations
- 2. figure out what output variable got the highest defuzzified value.

```
std::string choose_action(fl::Engine* engine, const Stats& stats)
2
     // Load the specimen into the engine
3
     // assume that inclinations are already set
4
     engine->getInputVariable("strength")->setValue(std::get<0>(stats));
     engine->getInputVariable("constitution")->setValue(std::get<1>(stats));
     engine->getInputVariable("intelligence")->setValue(std::get<2>(stats));
     engine->getInputVariable("refinement")->setValue(std::get<3>(stats));
10
     // Get action priorities
11
     engine->process();
12
13
     const auto& output_vars = engine->outputVariables();
14
     auto it = std::max_element(
15
     output_vars.begin(), output_vars.end(),
16
       [](const auto* a, const auto* b) {
17
         // defaulting to 0 if the value is NaN
         const auto left_priority = std::isnan(a->getValue())
19
           ? 0.0
20
           : a->getValue();
21
         const auto right_priority = std::isnan(b->getValue())
22
           ? 0.0
23
           : b->getValue();
25
         return left_priority < right_priority;
26
       }
27
     );
28
29
     // Either return the name of the action with the highest priority,
30
     // or the first action if no rules fired (i.e., all priorities are 0).
31
     std::string chosen_action_name = (it != output_vars.end())
32
       ? (*it)—>getName()
33
       : (*output_vars.begin())->getName();
34
35
     return chosen action name;
36
  }
37
```

In the listing, we are setting four characteristics — this is the setup for the trivial case from the section 6.

After we finish the simulation, we calculate the fitness. Below is an example from the trivial case, where the goal state is just for one of the characteristics to become higher than the threshold value 0.05.

```
/** the lower the better (conforming to pagmo2 conventions) */
double fitness (const Stats& stats)

{
// demo fitness: desirable refinement is 0.05+
return 0.05 - std::get<3>(stats);
}
```

This completes the full code for the solver.

5.5 Using the implemented solver

Internal beauty of the code and external configurability were not the goals of the implementation, so to prepare the solver for the given problem a set of changes has to be done to the code itself.

According to the definitions in 2, to specify the problem we need to specify the following parameters:

- 1. a list of n numerical characteristics
- 2. a list A of m possible actions
- 3. a list of changes for characteristics for each action
- 4. a fitness function Φ mapping the characteristics to a single real number, representing the goal state
- 5. a planning horizon T

All these items are hardcoded in the implementation, directly as types and constants in the C++ source code.

In addition to that, for the method explored in this work to work we need to specify the following:

- 1. a list of q inclinations
- 2. fuzzy variables for all the inclinations and characteristics, with all their fuzzy terms
- 3. fuzzy variables which represent the priorities of each action, with all their fuzzy terms
- 4. fuzzy rules binding the inclinations, characteristics and action priorities

The shape of the vector of inclinations is being specified as a type in the source code, but all the fuzzy variables and rules are expressed in a DSL of fuzzylite in a separate file.

The configuration for the fuzzy controller, specifically, the membership functions for the fuzzy terms, aggregation, defuzzification, conjuction, disjunction, implication operators, can be seen as hyperparameters for the solver itself detached from the particular problem instance to solve.

Finally, we have an option to choose from the built-in evolutionary algorithms in pagmo library and a configuration of the archipelago of populations, which are also part of the hyperparameters.

Having corrected the code to specify all the above settings, the code for solver just compiles and runs as an executable without any arguments.

Experiment 1: Trivial case

First case has been used solely for assessing the possibility of constructing the system at all. It is too small to be a useful example of problems solvable by the proposed solver.

We define 4 numerical attributes: Strength, Constitution, Intelligence and Refinement.

These 4 attributes are changed by 4 mutually exclusive actions, listed in the table 6.1.

Table 6.1: Trivial case actions

	Atrribute changes			
Action	Strength	Constitution	Intelligence	Refinement
Hunting	0.00	0.01	0.00	-0.01
Lumberjack	0.02	0.00	0.00	-0.02
ScienceClass	0.00	0.00	0.02	0.00
MannersClass	0.00	0.00	0.00	0.02

We will run this problem on a goal states reachable in 4 steps, meaning, our T is 4 for a trivial case.

This scenario represents a trivial case, with only 4^3 possible action sequences—a total of 64. The small state space allows for exhaustive enumeration and manual verification of results. This case serves to validate the correctness of the implementation and the fuzzy controller, as the system's behavior can be easily traced and analyzed by hand.

From the list of attributes and actions we synthesize two inclinations: Physical Inclination and Mental Inclination, which represent, correspondingly, "an inclination to perform actions related to physical attributes improvement" and "an inclination to perform actions related to mental attributes improvement".

The full text of the fuzzy controller for the trivial case, which binds two inclinations and four actions, looks as follows:

Engine: Trivial

Inclinations

InputVariable: PhysicalInclination enabled: true range: 0 1.000

```
lock-range: false
     term: tiny Ramp 0.330 0.000
9
     term: low Triangle 0.000 0.330 0.670
10
     term: high Triangle 0.330 0.670 1.000
11
     term: highest Ramp 0.670 1.000
12
13
  Input Variable: MentalInclination
14
     enabled: true
15
     range: 0 1.000
16
     lock-range: false
17
     term: tiny Ramp 0.330 0.000
18
     term: low Triangle 0.000 0.330 0.670
19
     term: high Triangle 0.330 0.670 1.000
20
     term: highest Ramp 0.670 1.000
21
22
  # Action Priorities
23
24
  Output Variable: Hunting
25
     enabled: true
26
     range: 0.000 1.000
27
     lock-range: false
28
     aggregation: Maximum
29
     defuzzifier: Centroid 100
30
     default: nan
31
     lock-previous: false
32
     term: low Ramp 1.000 0.000
33
     term: high Ramp 0.000 1.000
35
  Output Variable: Lumberjack
36
     enabled: true
37
     range: 0.000 1.000
38
     lock-range: false
39
     aggregation: Maximum
40
     defuzzifier: Centroid 100
41
     default: nan
42
     lock-previous: false
43
     term: low Ramp 1.000 0.000
44
     term: high Ramp 0.000 1.000
45
46
  OutputVariable: ScienceClass
47
     enabled: true
48
     range: 0.000 1.000
49
     lock-range: false
50
     aggregation: Maximum
51
     defuzzifier: Centroid 100
52
     default: nan
53
```

```
lock-previous: false
54
    term: low Ramp 1.000 0.000
55
    term: high Ramp 0.000 1.000
56
57
  OutputVariable: MannersClass
58
     enabled: true
59
    range: 0.000 1.000
60
    lock-range: false
61
     aggregation: Maximum
62
     defuzzifier: Centroid 100
63
     default: nan
64
    lock-previous: false
65
    term: low Ramp 1.000 0.000
    term: high Ramp 0.000 1.000
67
68
69
  # Rules
70
71
  RuleBlock: mamdani
72
     enabled: true
73
     conjunction: Minimum
74
     disjunction: Maximum
75
    implication: AlgebraicProduct
76
     activation: General
77
     rule: if PhysicalInclination is low
                                             and MentalInclination is low
78
            then MannersClass is high
    rule: if PhysicalInclination is low
                                             and MentalInclination is low
          then Hunting is low
81
     rule: if MentalInclination is high
                                             and PhysicalInclination is low
82
          then ScienceClass is high
83
     rule: if MentalInclination is high
                                             and PhysicalInclination is low
84
          then Lumberjack is low
85
     rule: if PhysicalInclination is high and MentalInclination is low
          then Lumberjack is high
87
     rule: if PhysicalInclination is high and MentalInclination is low
88
          then ScienceClass is low
89
     rule: if MentalInclination is high
                                             and PhysicalInclination is high
90
          then Hunting is high
91
     rule: if MentalInclination is high
                                             and PhysicalInclination is high
92
            then MannersClass is low
93
```

Correspondingly, the goal state is expressed as the following fitness function:

```
double fitness(const Stats& stats)
{
    // Stat of index 3 is refinement
    return 0.07 - std::get<3>(stats);
```

In the 4-tuple Stats the element at index 3 (zero-based) is a Refinement attribute, so this fitness function expresses the goal "Refinement must be more than 0.07".

Given the table of action effects and the goal, it's obvious that the only correct sequence of actions which can reach this goal is an action "MannersClass" repeated 4 times in a row, as this action is the only way to get an increase in the "Refinement" attribute.

The archipelago has been configured in the following manner:

```
pagmo::algorithm algo(pagmo::sade(100));
pagmo::archipelago archi(16u, algo, prob, 20u);
```

Four arguments to the pagmo::archipelago constructor are number of islands, algorithm to use, problem to solve and size of the population on each island. These are the slice of the hyperparameters which are related to evolutionary optimizations.

The algorithm that has been chosen (pagmo::sade) is an instance of Self-adaptive Differential Evolution algorithm, jDE variant [3] [5], for no reason other than being mentioned the first in the Pagmo documentation examples.

Running this system with the above setup results in 16 islands all evolving to the specimen which successfully reach the goal.

The following listing is an example listing of champions across the archipelago — due to stochastic nature of evolutionary optimization, every run will provide different specimen.

```
{0.292813, 0.31037} fitness -0.03
{0.223563, 0.274446} fitness -0.03
{0.667839, 0.0552651} fitness -0.03
... 12 more ...
{0.036359, 0.0444171} fitness -0.03
```

Due to the deterministic nature of the problem, we can get the exact list of actions from the specimen by simply calling the simulate function (explained in the section 5.4) with the inclination values gotten from the archipelago champions.

In this case, the list of actions is correctly inferred as 4 instances of "MannersClass". If we change the goal to check the "Constitution", then the system converges to an action sequence of 4 instances of a "Hunting" action, with the following specimen examples:

```
{0.379914, 0.929484} fitness 0.01
{0.334496, 0.832509} fitness 0.01
{0.96071, 0.470057} fitness 0.01
... 12 more ...
{0.516274, 0.708208} fitness 0.01
```

6.1 Discussion of the results

This basic trivial case confirms that we are indeed able to construct the hybrid fuzzy-genetic system which is able to produce optimal sequences of actions which lead to the goal state.

Using the fuzzy controller came out more complicated than it could be seen from the theory alone. While the target of the work was reducing the search state space, the amount of parameters in the fuzzy controller exploded the hyperparameters space instead, as by different configuration of the fuzzy rules and fuzzy variables we can change the behavior of the specimen.

It can be seen that if we exclude the current state of the specimen from the fuzzy rules, we trivialize the trajectories, reducing them to repetition of the same action T times. While this does not simplify the optimization step, as it is assumed that though (3.2), q is still large enough for the bruteforce enumeration to be intractable, it leaves us with action sequences intuitively unfit as solutions for any realistic nontrivial goal states.

If we setup the fuzzy action-prioritizing rules in such a way that they would indeed use the current state of the specimen, we do turn the problem into the control one with non-trivial solutions, but at the same time we end up having to specify not only at least one rule per each action priority, but also at least one rule per each term per each input variable, which starts competing with the complexity of the problem we are trying to solve by this method in the first place.

In the discussion of reducing the dimensionality of the problem, one should not forget the actual issue which explodes the dimensionality of the problem. While on the surface the method explored in this work is based on the inequality (3.2) and the amount of inclinations seems to be the target of discussions, the actual solution to the origin problem is a *list of actions*, and the true reason for dimensionality explosion is the length T of the list of actions to find and the amount of actions to be considered at each step.

It also can be seen that the configuration of the fuzzy controller and a tiebreaking rule is paramount for getting the solution. Intuitively by construction it can be expected that, if we set some "Physical" attribute as a goal, we expect that the specimen with high "Physical Inclination" and low "Mental Inclination" will be the only possible solution, but it's not the case.

In the example results for the "Strength must be higher than 0.07" case above, we can see a winning specimen with "Physical Inclination" being as low as 0.379914 and "Mental Inclination" being as high as 0.929484, which is a situation completely opposite to the expectations. If we single-step the evolution process for this specimen, we can see that on the step of choosing an action it gets actions with identical priorities, but opposite effects.

For a visual example, this is how the text report looks like if we introduce it in the program appropriately:

```
island champion: {0.379914, 0.929484} Step 1:
```

Comparing Hunting with value 0.66665 and Lumberjack with value 0.33335 Comparing Hunting with value 0.66665 and ScienceClass with value 0.66665 Comparing Hunting with value 0.66665 and MannersClass with value 0.33335 Chosen action: Hunting

Three following steps are not shown because they are identical to this one. We can see that priorities of the "Hunting" and "ScienceClass" actions were inferred as identical, and the "Hunting" action has been chosen solely by the reason of being the first in the list of actions compared to "ScienceClass".

From one perspective we can see it as a deficiency in an algorithm and implement a more robust tiebreaker, but on the other hand we should not forget that the solution we seek is the list of actions leading to the goal state, not the inclination values which are essentially transient intermediaries representing paths in the actions space.

Experiment 2: Base control case

24 characteristics, 25 actions with varied amount of steps.

This case is the base case, as it introduces enough complexity to test the proposed approach and at the same time compare it with classical approaches.

A decision tree of the size 25^{100} is already too large to be completely enumerated, and as we show later in this section, we go twelve times deeper than that.

In this case we copy all the numerical attributes of the character sans one from the original *Princess Maker 2* problem, and all the actions with their effects on these attributes.

The attributes are represented as the following tuple:

```
using Stats = std::tuple <
     int, //0 strength
2
     int, // constitution
     int, // intelligence
     int, // refinement
     int, //4 charisma
     int , // morality
     int , // faith
     int , // sin
9
     int , // sensitivity
10
11
     int, //9 combat skill
12
     int, // combat attack
13
     int, // combat defense
14
     int, // magic skill
15
     int, // magic attack
16
     int, //14 magic defense
17
     int, // decorum
     int, // artistry skill
19
     int, // eloquence
20
     int, // cooking skill
21
     int, //19 cleaning skill
22
     int // temperament
23
```

The effects of actions are listed in the table 7.2 for reference.

Applying the methodology explored in this work, we synthesize the 5 inclinations out of all the attributes and actions:

```
using Inclinations = std::tuple <
double, // fighting
double, // magic
double, // housekeeping
double, // artistry
double // sinfulness
>;
```

Each inclination represents literally an inclination towards performing a particular set of actions, which we express as a fuzzy rules in a fuzzy controller.

Compared to the trivial case from the chapter 6, now we will use the rules which include both inclination values and the current attribute values of the character. This allows the agent to actually "choose" actions to perform depending on the "actual needs".

The full code for the fuzzy controller is in the appendix A.

This is a case representing the full complexity we want to explore in the scope of this work, as it was never intended to replicate the original gameplay. The other way around, we wanted to strip away all the unnecessary things from the game to leave only the essential generic problem.

With such an elaborate set of attributes we can formulate complicated fitness rules, for example, the "High General" ending ¹:

- 1. Intelligence attribute > 500 and > than Sensitivity attribute
- 2. Morality attribute > 30
- 3. Faith attribute > 300 and > than Sensitivity attribute
- 4. "Fighting reputation" which is a sum of all fighting-related stats and skills, > 421

The following piece of code is an example of encoding this ending into a fitness function:

```
double fitness (const Stats& stats)
2
      const int fighter_reputation = std::get<0>(stats) + std::get<1>(stats)
3
      + \text{ std} :: \text{get} < 9 > (\text{stats}) + \text{std} :: \text{get} < 10 > (\text{stats}) + \text{std} :: \text{get} < 11 > (\text{stats});
4
5
      // if sensitivity is higher than intelligence or faith,
      // return an absolute instant loss
      if (std::get < 8 > (stats) >= std::get < 2 > (stats)
         \parallel \text{std} :: \text{get} < 8 > (\text{stats}) > = \text{std} :: \text{get} < 6 > (\text{stats})) 
9
         return std::numeric_limits<double>::max();
10
11
12
      double fitness_value = 0.0;
13
14
```

¹https://princessmaker.fandom.com/wiki/High_General_Ending_(PM2)

```
// add penalty for intelligence below 500
15
     if (std::get < 2 > (stats) < 500) {
16
        fitness\_value += (500 - std :: get < 2 > (stats));
17
     }
18
19
     // add penalty for morality below 30
20
     if (std::get < 5 > (stats) < 30) {
21
        fitness\_value += (30 - std :: get < 5 > (stats));
23
24
     // add penalty for faith below 300
25
     if (std::get < 6 > (stats) < 300) {
26
        fitness\_value += (300 - std::get < 6 > (stats));
27
28
29
     // add penalty for fighter reputation below 421
30
     if (fighter_reputation < 421) {
31
        fitness_value += (421 - fighter_reputation);
32
33
     return fitness_value;
35
36
   }
```

When we run it on T=1200 which is already far outside of any classical algorithms, we get the following result (an output verbatim from the reference implementation of the solver):

```
Stats changes:

str: +0, con: +0, int: +507,

ref: +0, cha: +0, mor: +102,

fai: +612, sin: -204, sen: -588

cs: +330, ca: +165, cd: +165,

ms: +0, ma: +0, md: +408,

dec: +0, art: +0, elo: +0,

coo: +294, cle: +294, tem: +294

Simulation Result:
```

With the runtime of 12 minutes 30 seconds on the standard home PC machine ². To decode the raw output above, we received a specimen with the:

- 1. "Intelligence" of 507,
- 2. "Morality" of 102,
- 3. "Faith" of 612,

Fitness: 0

 $^{^2 \}rm{Intel}(R)$ Core(TM) i7-9700 CPU @ 3.00 GHz with 32 GB DDR4 RAM, NVIDIA(R) GeForce(TM) RTX 2060

- 4. "Sensitivity" of -588 which is guaranteed to be less than both intelligence and faith
- 5. "Combat skill" 330, "Combat attack" 165 and "Combat defense" 165 summing up to more than 421.

These are exactly the stats we asked for in the goal function, which the fitness score of 0 represents.

And we decode the full plan from the inclination values which is the solution bringing us to these attribute values:

- 1. TheologyClass x 383
- 2. FencingClass x 106
- 3. FightingClass x 106
- 4. TheologyClass FencingClass FightingClass x 24
- 5. TheologyClass
- 6. FencingClass FightingClass x 2
- 7. TheologyClass FencingClass FightingClass x 33
- 8. Housework x 294
- 9. Church x 63
- 10. Church ScienceClass x 3
- 11. Church
- 12. Church ScienceClass x 6
- 13. Church
- 14. Church ScienceClass x 7
- 15. Church
- 16. Church ScienceClass x 6
- 17. Church
- 18. Church ScienceClass x 7
- 19. Church
- 20. Church ScienceClass x 4
- 21. Church

The runtime is dependent on the complexity of the fitness function.

If we remove the check for the fighter reputation, lines 28-31 from the listing 7, it cuts the runtime to 6 minutes 30 seconds to reach the fitness 0.

If we remove two checks, lines 23-31 from the same listing, we get the runtime of 5 minutes 50 seconds.

Then, removing additionally the check for morality, lines 18-21, we get the runtime of 6 minutes 10 seconds.

And, finally, if we reduce the fitness function to only the check for sensitivity being lower than intelligence and faith, that is, keep only the lines 6-11 and 33 of the listing 7, the runtime becomes 3 minutes 20 seconds.

We can summarize the dependency of the runtime on the complexity of the fitness function calculation in the table 7.1

Table 1.1. Runtime versus intress function complexity, baseline case experiment	
Requirements clauses amount	Runtime on a reference machine
full "General" ending goal	12 m 30 s
no reputation check	$6~\mathrm{m}~30~\mathrm{s}$
no reputation, no faith checks	$5~\mathrm{m}~50~\mathrm{s}$
no reputation, no faith, no morality checks	6 m 10 s
no attribute checks, only the predicate	3 m 20 s

Table 7.1: Runtime versus fitness function complexity, baseline case experiment

7.1 Discussion of the results

First note we must make immediately is that the T is actually dependent on the goal. When we have a real goal we want to evaluate, it has less significance, but when experimenting, it's possible to set the goal which is completely unreachable by the solver — for example, if we demand a value of an attribute to be 100 after 10 steps (T=10), but every action increasing this attribute increases it by 1.

Pagmo is a highly optimized library so it detects when the chosen evolutionary algorithm converges and stops the evolution returning the fitness reached. This prevents us from naively benchmarking the performance of the solver because when we change the goal, runtime can change arbitrarily. Essentially, adding more conditions — making the fitness calculation depending on more attributes — tend to increase the runtime, as the evolution starts to converge slower.

Then, we received a result for T=1200 which is already outside of all the initial expectations in 12 minutes, a time minuscule compared to modern demands in scientific computations. It is clear that we successfully reduced the combinatorically hard problem to something with at least a polynomial time. More than that, given the nature of a fuzzy controller, on every step it performs the same amount of calculations, which means that each simulation for an individual specimen is O(T), and the computational complexity completely shifts to the evolutionary algorithm, which is reflected in our observations over the dependence of a runtime on a complexity of the goal function.

When writing the inference rules of the fuzzy controller, there is a choice of two ways.

TEM7 77 CLE $\ddot{+}$ 7 7 7 7 ELO Table 7.2: Action effects per day in Princess Maker 2 (nonzero shown; + indicates increase) 7 MD DEC ART $^{+}_{1}^{+}_{2}$ 7 \pm 7 17 - 17 MS MA +7 CD \mp CA7 CS7 7 \mp \pm 77 SEN \mp \mp 7777 $\frac{-2}{1}$ SIN $^{+2}_{11}$ $\frac{1}{2}$ CHA MOR FAI +5က္ 77 7 $\frac{1}{2}$ $\begin{array}{c} -1 \\ +2 \\ +3 \end{array}$ Η $\vec{\ } \vec{\ } \vec{\ } \vec{\ } \vec{\ } \vec{\ } \vec{\ }$ REF 7 7 -1 ⊣ 7 INI $\begin{array}{c} + & + & + & + \\ + & + & + & + \\ \end{array}$ 5 CON \mp +27 \mp STR7 7 StrategyClass ScienceClass TheologyClass MagicClass PaintingClass PoetryClass Fencing Class Fighting Class MannersClass Cabaret DanceClass Hunting Lumberjack Babysitting Church Farming Innkeeping Masonry Graveyard Bar Housework Restaurant SleazyBar Tutoring Action Salon

First way, we can express the domain knowledge by writing rules "from the inclinations to actions", that is, for each term of every inclination (input variable) describe what impact it should have on the priority of the actions. This option has two drawbacks:

- 1. it scales with the amount of inclinations times amount of their terms
- 2. we risk missing out some of the actions if we made a mistake in synthesizing the list of inclinations

This problem becomes much more significant once we start using the attributes in the rules, as the number of attributes is larger than the number of inclinations due to (3.2).

Second way, we can express the domain knowledge by writing rules "from the actions back to inclinations", that is, for every term of every action (output variable) we describe what combination of inclination and attribute values can lead to it. This option has its drawbacks, too:

- 1. it scales with the amount of actions times amount of their terms
- 2. we risk missing out some of the combinations of inclinations and attributes

If we go this way and start adding more rules than the absolute minimum we still risk getting into the combinatorial explosion.

Still, the drawbacks listed here do not mean that there are absolute requirements on the amount of rules we have to write. The more specific we would be in writing the rules, the more correct the action selection is expected to be.

One of the observed situation was skipping the input variables because of overspecification of terms.

Let's say we specify our "artistry" and "housekeeping" inclinations as follows, with four terms tiny, low, high, highest:

```
InputVariable: InclinationArtistry
enabled: true
range: 0 1.000
lock—range: false
term: tiny Ramp 0.330 0.000
term: low Triangle 0.000 0.330 0.670
term: high Triangle 0.330 0.670 1.000
term: highest Ramp 0.670 1.000

# (identical definition for InclinationHousekeeping)
```

And we also have a block of rules like following:

```
    rule: if InclinationArtistry is high then MannersClass is high
    rule: if InclinationHousekeeping is high then MannersClass is low
```

If we have a specimen with InclinationArtistry =0.9 and InclinationHousekeeping =0.6, then, unexpectedly to us, priority of MannersClass would be low, not high. Because the membership function for the term "high" will emit higher value for "housekeeping" inclination than for the "artistry". As we don't have a rule for InclinationArtistry

is highest the values higher than specified in the rule, despite being "obviously" fitting the rule, are actually ignored instead.

To resolve this problem it's more beneficial to actually reduce the amount of terms, removing the ones not used in the rules.

Chapter 8

Conclusions and Future Work

To sum it up, we achieved the following results:

- 1. a reference solver implementing the method described in this work is actually able to produce the solutions with fitness 0, meaning, the ones which fully satisfy the predefined goal predicate;
- 2. performance-wise, the solver depends on T linearly, effectively completely eliminating the computational complexity dependent on the amount of actions to execute;
- 3. discoveries has been done related to the actual complexity of encoding the domain knowledge as a fuzzy controller;
- 4. it has been determined that the speed of convergence is actually dependent on the complexity of the fitness function calculation;

All objectives defined in Section 3.3 have been met: we formalized the problem, implemented a solver, tested it on different scales, and analyzed the results.

The codebase of the reference solver is located at the GitHub repository in the Internet accessible by the URL https://github.com/hijarian/urv-mesiia-2025-tfm-code.

With this, all objectives defined in section 3.3 have been met: we formalized the problem, implemented a solver, tested it on different scales, and analyzed the results.

We can give now a brief summary on the further research spanning outside the scope of this particular work.

A game so mechanically interdependent as *Princess Maker 2* is too complex to solve using such a straightforward model. A lot of simplifications were needed to arrive at a coherent model of the deterministic planning problem with a stateful agent. Nevertheless, the hybrid solver built in the scope of this work have shown that it successfully determines a solution given that all the domain knowledge is accurately encoded in the fuzzy controller, and as such, it can be used to solve any high-dimensional deterministic planning problem which can be modeled according to our definitions from the section 2. This constitutes the core value of this work.

We have shown that the hybrid fuzzy-genetic system described in this work has a linear complexity in relation to the amount of planning steps T assuming that executing T steps is a requirement. Computing T=1200 steps in 12 minutes is effectively instantaneous nowadays so there's a little benefit in a further research of the computational complexity

in relation to T. However, a research on how the computational complexity of this solver depends on amount of attributes n (2.1) and amount of actions m (2.2) is still needed to be done.

A useful comparison is with reinforcement learning. In our case, if we try to set up a tabular RL agent with 23 attributes ranging up to 500 and 27 actions, the Q-table would be 27×500^{23} , which is clearly infeasible to store or explore. Even with function approximation, RL still faces the horizon problem: with $\gamma = 0.99$ and T = 1200, the learning signal from the final reward is around 6×10^{-6} , practically zero. Raising γ makes the effective horizon too long and increases sample complexity. Our method avoids this by using the known deterministic model to directly simulate trajectories, and by searching in the much smaller space of inclinations $q \ll n$. The trade-off is that we have to supply a fuzzy rule base by hand. In short: we pay in design effort, but in return we get a tractable solver that actually reaches the goal.

In the span of this work, only two cases distinct in the number of actions m were explored, and the more thorough exploration of the parameter space is left for a dissertation-level research.

An additional path of exploration is researching how well this method can be applied to problems where the effects of actions are non-deterministic. While lifting the restriction of determinism does not affect the fuzzy inference at all, it presents challenges in decoding the solution sequence of actions from the vector of inclination values.

While the fuzzy controller can indeed be seen as a tool to formalize the decision making using the expert knowledge in the given domain, it is too complicated mechanism by itself to help reducing the complexity of the problem it's solving. One should treat it not as a tool which helps make complicated problems simpler but which, hopefully, makes unsolvable ones solvable at all, as proper configuration of the fuzzy controller is already a problem in itself.

One of the possible areas to explore is automation of the fuzzy rule base generation with clustering or learning, to reduce the manual workload.

The proof-of-concept solver implemented and discussed in this work is obviously an instance of an automated planner, for which an extensive framework of both machinery and benchmarking exists. The logical next step would be to determine a correct place of this method in the existing body of knowledge about the automated planners and perform formal comparisons of performance with some other state-of-the-art methods.

Another work which exploits the idea of using the domain knowledge in the solution process exists, but it uses the Linear Temporal Logic instead, and utilizes the existing PDDL automatic planning machinery [8].

The paper [16] briefly mentioned in the section 4.3, is an possible alternative hybrid system, where the target of evolution is a reinforcement learning process.

Both these are examples of possible further research in the area of hybrid systems solving the high-dimensional planning problems of large horizon using the domain knowledge.

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Appendix A

Baseline case fuzzy controller

```
Engine: Baseline
  # Inclinations
  InputVariable: InclinationFighting
     enabled: true
     range: 0 1.000
     lock-range: false
     term: low Ramp 1.0 0.0
     term: high Ramp 0.0 1.0
10
  InputVariable: InclinationMagic
11
     enabled: true
12
     range: 0 1.000
13
     lock-range: false
14
     term: low Ramp 1.0 0.0
15
     term: high Ramp 0.0 1.0
16
  InputVariable: InclinationHousekeeping
17
     enabled: true
18
     range: 0 1.000
19
     lock-range: false
20
     term: low Ramp 1.0 0.0
^{21}
     term: high Ramp 0.0 1.0
22
  InputVariable: InclinationArtistry
     enabled: true
24
     range: 0 1.000
25
     lock-range: false
26
     term: low Ramp 1.0 0.0
27
     term: high Ramp 0.0 1.0
28
  InputVariable: InclinationSinfulness
     enabled: true
30
     range: 0 1.000
31
     lock-range: false
32
     term: low Ramp 1.0 0.0
33
```

```
term: high Ramp 0.0 1.0
34
35
    Attributes
36
37
  InputVariable: strength
38
     enabled: true
39
     range: 0 810
40
     lock-range: false
41
     term: low Ramp 810 0
42
     term: high Ramp 0 810
43
  InputVariable: constitution
44
     enabled: true
45
     range: 0 810
46
     lock-range: false
47
     term: low Ramp 810 0
48
     term: high Ramp 0 810
49
  InputVariable: intelligence
50
     enabled: true
51
     range: 0 810
52
     lock-range: false
     term: low Ramp 810 0
54
     term: high Ramp 0 810
55
  InputVariable: refinement
56
     enabled: true
57
     range: 0 810
58
     lock-range: false
59
     term: low Ramp 810 0
     term: high Ramp 0 810
61
   InputVariable: charisma
62
     enabled: true
63
     range: 0 810
64
     lock-range: false
65
     term: low Ramp 810 0
66
     term: high Ramp 0 810
67
  InputVariable: morality
68
     enabled: true
69
     range: 0 810
70
     lock-range: false
71
     term: low Ramp 810 0
72
     term: high Ramp 0 810
73
  InputVariable: faith
74
     enabled: true
75
     range: 0 810
76
     lock-range: false
77
     term: low Ramp 810 0
78
     term: high Ramp 0 810
79
```

```
InputVariable: sinfulness
     enabled: true
81
     range: 0 810
82
     lock-range: false
83
     term: low Ramp 810 0
84
     term: high Ramp 0 810
   InputVariable: sensitivity
86
     enabled: true
87
     range: 0 810
88
     lock-range: false
89
     term: low Ramp 810 0
90
     term: high Ramp 0 810
91
   # Skills (same as attributes but range is 0-540 instead of 0-810)
93
   InputVariable: CombatSkill
94
     enabled: true
95
     range: 0 540
96
     lock-range: false
97
     term: low Ramp 540 0
98
     term: high Ramp 0 540
   InputVariable: CombatAttack
100
     enabled: true
101
     range: 0 540
102
     lock-range: false
103
     term: low Ramp 540 0
104
     term: high Ramp 0 540
105
   InputVariable: CombatDefense
106
     enabled: true
107
     range: 0 540
108
     lock-range: false
109
     term: low Ramp 540 0
110
     term: high Ramp 0 540
111
   InputVariable: MagicSkill
112
     enabled: true
113
     range: 0 540
114
     lock-range: false
115
     term: low Ramp 540 0
116
     term: high Ramp 0 540
117
   InputVariable: MagicAttack
118
     enabled: true
     range: 0 540
120
     lock-range: false
121
     term: low Ramp 540 0
122
     term: high Ramp 0 540
123
   InputVariable: MagicDefense
124
     enabled: true
125
```

```
range: 0.540
126
      lock-range: false
127
     term: low Ramp 540 0
128
     term: high Ramp 0 540
129
   InputVariable: Decorum
130
      enabled: true
131
     range: 0 540
132
     lock-range: false
133
     term: low Ramp 540 0
134
     term: high Ramp 0 540
135
   InputVariable: Artistry
136
     enabled: true
137
     range: 0 540
138
     lock-range: false
139
     term: low Ramp 540 0
140
     term: high Ramp 0 540
141
   Input Variable: Eloquence
142
     enabled: true
143
     range: 0 540
144
     lock-range: false
145
     term: low Ramp 540 0
146
     term: high Ramp 0 540
147
   InputVariable: CookingSkill
148
     enabled: true
149
     range: 0 540
150
     lock-range: false
151
     term: low Ramp 540 0
152
     term: high Ramp 0 540
153
   InputVariable: CleaningSkill
154
     enabled: true
155
     range: 0 540
156
      lock-range: false
157
     term: low Ramp 540 0
158
     term: high Ramp 0 540
159
   InputVariable: Temperament
160
      enabled: true
161
     range: 0 540
162
     lock-range: false
163
     term: low Ramp 540 0
164
     term: high Ramp 0 540
165
166
   # Action Priorities
167
168
   ## Jobs
169
170
171
```

Output Variable: Hunting

```
enabled: true
172
     range: 0.000 1.000
173
     lock-range: false
174
     aggregation: Maximum
175
     defuzzifier: Centroid 100
176
     default: nan
     lock-previous: false
178
     term: low Ramp 0.500 0.000
179
     term: medium Triangle 0.000 0.500 1.000
180
     term: high Ramp 0.500 1.000
181
182
   OutputVariable: Lumberjack
183
     enabled: true
184
     range: 0.000 1.000
185
     lock-range: false
186
     aggregation: Maximum
187
     defuzzifier: Centroid 100
188
     default: nan
189
     lock-previous: false
190
     term: low Ramp 0.500 0.000
191
     term: medium Triangle 0.000 0.500 1.000
192
     term: high Ramp 0.500 1.000
193
194
   OutputVariable: Housework
195
     enabled: true
196
     range: 0.000 1.000
197
     lock-range: false
198
     aggregation: Maximum
199
     defuzzifier: Centroid 100
200
     default: nan
201
     lock-previous: false
202
     term: low Ramp 0.500 0.000
203
     term: medium Triangle 0.000 0.500 1.000
204
     term: high Ramp 0.500 1.000
205
206
   Output Variable: Babysitting
207
     enabled: true
208
     range: 0.000 1.000
209
     lock-range: false
210
     aggregation: Maximum
211
     defuzzifier: Centroid 100
212
     default: nan
213
     lock-previous: false
214
     term: low Ramp 0.500 0.000
215
     term: medium Triangle 0.000 0.500 1.000
216
     term: high Ramp 0.500 1.000
217
```

```
218
   Output Variable: Church
219
     enabled: true
220
     range: 0.000 1.000
221
     lock-range: false
222
      aggregation: Maximum
223
      defuzzifier: Centroid 100
224
      default: nan
225
     lock-previous: false
226
     term: low Ramp 0.500 0.000
227
     term: medium Triangle 0.000 0.500 1.000
228
     term: high Ramp 0.500 1.000
229
230
   Output Variable: Farming
231
     enabled: true
232
     range: 0.000 1.000
233
     lock-range: false
234
      aggregation: Maximum
235
      defuzzifier: Centroid 100
236
      default: nan
237
     lock-previous: false
238
     term: low Ramp 0.500 0.000
239
     term: medium Triangle 0.000 0.500 1.000
240
     term: high Ramp 0.500 1.000
241
242
   Output Variable: Innkeeping
243
     enabled: true
244
     range: 0.000 1.000
245
     lock—range: false
246
      aggregation: Maximum
247
      defuzzifier: Centroid 100
248
      default: nan
249
     lock-previous: false
250
     term: low Ramp 0.500 0.000
251
     term: medium Triangle 0.000 0.500 1.000
252
     term: high Ramp 0.500 1.000
253
254
   OutputVariable: Restaurant
255
     enabled: true
256
     range: 0.000 1.000
257
     lock-range: false
258
      aggregation: Maximum
259
      defuzzifier: Centroid 100
260
      default: nan
261
     lock-previous: false
262
     term: low Ramp 0.500 0.000
263
```

```
term: medium Triangle 0.000 0.500 1.000
264
     term: high Ramp 0.500 1.000
265
266
   Output Variable: Salon
267
     enabled: true
268
     range: 0.000 1.000
269
     lock-range: false
      aggregation: Maximum
271
      defuzzifier: Centroid 100
272
      default: nan
273
     lock-previous: false
274
     term: low Ramp 0.500 0.000
275
     term: medium Triangle 0.000 0.500 1.000
276
     term: high Ramp 0.500 1.000
277
278
   Output Variable: Masonry
279
     enabled: true
280
     range: 0.000 1.000
281
     lock-range: false
282
     aggregation: Maximum
      defuzzifier: Centroid 100
284
      default: nan
285
     lock-previous: false
286
     term: low Ramp 0.500 0.000
287
     term: medium Triangle 0.000 0.500 1.000
288
     term: high Ramp 0.500 1.000
289
290
   Output Variable: Graveyard
291
     enabled: true
292
     range: 0.000 1.000
293
     lock-range: false
294
      aggregation: Maximum
295
      defuzzifier: Centroid 100
296
      default: nan
297
     lock-previous: false
298
     term: low Ramp 0.500 0.000
299
     term: medium Triangle 0.000 0.500 1.000
300
     term: high Ramp 0.500 1.000
301
302
   Output Variable: Bar
303
      enabled: true
304
     range: 0.000 1.000
305
     lock-range: false
306
      aggregation: Maximum
307
      defuzzifier: Centroid 100
308
      default: nan
309
```

```
lock-previous: false
310
     term: low Ramp 0.500 0.000
311
     term: medium Triangle 0.000 0.500 1.000
312
     term: high Ramp 0.500 1.000
313
314
   Output Variable: Tutoring
      enabled: true
316
     range: 0.000 1.000
317
      lock-range: false
318
      aggregation: Maximum
319
      defuzzifier: Centroid 100
320
      default: nan
321
     lock-previous: false
322
     term: low Ramp 0.500 0.000
323
     term: medium Triangle 0.000 0.500 1.000
324
     term: high Ramp 0.500 1.000
325
326
   OutputVariable: SleazyBar
327
      enabled: true
328
     range: 0.000 1.000
329
      lock-range: false
330
      aggregation: Maximum
331
      defuzzifier: Centroid 100
332
      default: nan
333
      lock-previous: false
334
     term: low Ramp 0.500 0.000
335
     term: medium Triangle 0.000 0.500 1.000
336
     term: high Ramp 0.500 1.000
337
338
   OutputVariable: Cabaret
339
      enabled: true
340
     range: 0.000 1.000
341
      lock-range: false
342
      aggregation: Maximum
343
      defuzzifier: Centroid 100
344
      default: nan
345
      lock-previous: false
346
     term: low Ramp 0.500 0.000
347
     term: medium Triangle 0.000 0.500 1.000
348
     term: high Ramp 0.500 1.000
349
350
   ## Classes
351
352
   OutputVariable: DanceClass
353
     enabled: true
354
     range: 0.000 1.000
355
```

```
lock-range: false
356
      aggregation: Maximum
357
      defuzzifier: Centroid 100
358
      default: nan
359
     lock-previous: false
360
     term: low Ramp 0.500 0.000
361
     term: medium Triangle 0.000 0.500 1.000
362
     term: high Ramp 0.500 1.000
363
364
   OutputVariable: FencingClass
365
     enabled: true
366
     range: 0.000 1.000
367
     lock-range: false
368
      aggregation: Maximum
369
      defuzzifier: Centroid 100
370
      default: nan
371
     lock-previous: false
372
     term: low Ramp 0.500 0.000
373
     term: medium Triangle 0.000 0.500 1.000
374
     term: high Ramp 0.500 1.000
376
   OutputVariable: FightingClass
377
     enabled: true
378
     range: 0.000 1.000
379
     lock-range: false
380
      aggregation: Maximum
381
      defuzzifier: Centroid 100
382
      default: nan
383
     lock-previous: false
384
     term: low Ramp 0.500 0.000
385
     term: medium Triangle 0.000 0.500 1.000
386
     term: high Ramp 0.500 1.000
387
   OutputVariable: MagicClass
389
     enabled: true
390
     range: 0.000 1.000
391
      lock-range: false
392
      aggregation: Maximum
393
      defuzzifier: Centroid 100
394
      default: nan
395
     lock-previous: false
396
     term: low Ramp 0.500 0.000
397
     term: medium Triangle 0.000 0.500 1.000
398
     term: high Ramp 0.500 1.000
399
400
   OutputVariable: PaintingClass
```

401

```
enabled: true
402
     range: 0.000 1.000
403
     lock-range: false
404
     aggregation: Maximum
405
     defuzzifier: Centroid 100
406
     default: nan
407
     lock-previous: false
408
     term: low Ramp 0.500 0.000
409
     term: medium Triangle 0.000 0.500 1.000
410
     term: high Ramp 0.500 1.000
411
412
   OutputVariable: PoetryClass
413
     enabled: true
414
     range: 0.000 1.000
415
     lock-range: false
416
     aggregation: Maximum
417
     defuzzifier: Centroid 100
418
     default: nan
419
     lock-previous: false
420
     term: low Ramp 0.500 0.000
421
     term: medium Triangle 0.000 0.500 1.000
422
     term: high Ramp 0.500 1.000
423
424
   OutputVariable: StrategyClass
425
     enabled: true
426
     range: 0.000 1.000
427
     lock-range: false
428
     aggregation: Maximum
429
     defuzzifier: Centroid 100
430
     default: nan
431
     lock-previous: false
432
     term: low Ramp 0.500 0.000
433
     term: medium Triangle 0.000 0.500 1.000
434
     term: high Ramp 0.500 1.000
435
436
   OutputVariable: ScienceClass
437
     enabled: true
438
     range: 0.000 1.000
439
     lock-range: false
440
     aggregation: Maximum
     defuzzifier: Centroid 100
442
     default: nan
443
     lock-previous: false
444
     term: low Ramp 0.500 0.000
445
     term: medium Triangle 0.000 0.500 1.000
446
     term: high Ramp 0.500 1.000
447
```

```
448
   Output Variable: Theology Class
449
     enabled: true
450
     range: 0.000 1.000
451
     lock-range: false
452
     aggregation: Maximum
453
     defuzzifier: Centroid 100
454
     default: nan
455
     lock-previous: false
456
     term: low Ramp 0.500 0.000
457
     term: medium Triangle 0.000 0.500 1.000
458
     term: high Ramp 0.500 1.000
459
460
   OutputVariable: MannersClass
461
     enabled: true
462
     range: 0.000 1.000
463
     lock-range: false
464
     aggregation: Maximum
465
     defuzzifier: Centroid 100
466
     default: nan
467
     lock-previous: false
468
     term: low Ramp 0.500 0.000
469
     term: medium Triangle 0.000 0.500 1.000
470
     term: high Ramp 0.500 1.000
471
472
473
   # Rules
475
   RuleBlock: mamdani
476
     enabled: true
477
     conjunction: Minimum
478
     disjunction: Maximum
479
     implication: AlgebraicProduct
480
     activation: General
481
482
     # at least one rule for each action priority
483
     # We will follow a pattern where high inclination + low attribute/skill
484
     # and opposite inclination high and the penalized attribute/skill low -
485
     # Jobs
486
     rule: if InclinationFighting is high and strength is low
                                                                      then Lumberjac
     rule: if InclinationArtistry is high and refinement is low
488
   then Lumberjack is low
489
                                                and constitution is low then Hun
     rule: if InclinationFighting is high
490
     rule: if InclinationArtistry is high and refinement is low
491
   then Hunting is low
```

```
492
     rule: if InclinationHousekeeping is high and CookingSkill is low then H
493
     rule: if InclinationHousekeeping is high and CleaningSkill is low then I
494
     rule: if InclinationHousekeeping is high and Temperament is low then Ho
495
     rule: if InclinationSinfulness is high and sensitivity is low then House
496
     rule: if InclinationHousekeeping is high and sensitivity is low then Ba
498
     rule: if InclinationArtistry is high and charisma is low then Babysittin
499
500
     rule: if Inclination Housekeeping is high and morality is low then Church
501
     rule: if InclinationHousekeeping is high and faith
                                                              is low then Church
502
     rule: if InclinationSinfulness is high and sinfulness is low then Church
503
     rule: if InclinationFighting is high and strength
                                                              is low then Farmin
505
     rule: if InclinationFighting is high and constitution is low then Farmin
506
     rule: if InclinationArtistry is high and refinement
                                                              is low then Farmin
507
508
     rule: if InclinationHousekeeping is high and CleaningSkill is low
509
   then Innkeeping is high
                                   is high
                                               and CombatSkill is low then Innl
     rule: if InclinationFighting
511
     rule: if InclinationHousekeeping is high and CookingSkill is low
512
   then Restaurant is high
     rule: if InclinationFighting
                                    is high
                                               and CombatSkill is low then Res
513
514
     rule: if InclinationArtistry is high
                                              and sensitivity is low
   then Salon is low
     rule: if InclinationFighting
                                   is high
                                               and strength is low then Salon
516
517
     rule: if InclinationFighting is high
                                              and constitution is low then Mas
518
     rule: if InclinationArtistry is high
                                             and charisma is low
                                                                     then Mason:
519
520
     rule: if InclinationMagic is high and MagicDefense is low then Graveys
521
     rule: if InclinationArtistry is high
                                            and sensitivity is low
522
   then Graveyard is high
     rule: if InclinationArtistry is high
                                            and charisma is low then Graveyan
523
524
     rule: if InclinationArtistry is high and Eloquence is low
525
   then Bar is high
     rule: if InclinationHousekeeping is high
                                                  and CookingSkill is low then
526
     rule: if InclinationMagic is high
                                          and intelligence is low then Bar is
527
528
     rule: if InclinationHousekeeping is high
                                                  and morality is low
529
   then Tutoring is high
     rule: if InclinationArtistry is high and charisma is low
                                                                    then Tutorin
530
531
```

```
and sinfulness is low then Slea
     rule: if InclinationSinfulness is high
532
     rule: if InclinationArtistry is high
                                              and charisma is low then SleazyBa
533
     rule: if InclinationHousekeeping is high
                                                  and morality is low
534
   then SleazyBar is low
     rule: if InclinationHousekeeping is high
                                                  and faith is low then Sleazy
535
     rule: if InclinationHousekeeping is high
                                                  and Temperament is low
536
   then SleazyBar is low
537
     rule: if InclinationSinfulness is high
                                               and sinfulness is low
538
   then Cabaret is high
     rule: if InclinationArtistry is high
                                              and charisma is low then Cabaret
539
     rule: if InclinationMagic is high
                                           and intelligence is low then Cabaret
540
     rule: if InclinationHousekeeping is high
                                                  and Temperament is low
   then Cabaret is low
     rule: if InclinationArtistry is high
                                              and refinement is low
542
   then Cabaret is low
     # Classes
543
                                             and constitution is low
     rule: if InclinationFighting is high
544
   then DanceClass is high
     rule: if InclinationArtistry is high
                                             and charisma is low
                                                                     then Dance
     rule: if InclinationArtistry is high
                                                                      then Dance
                                             and Artistry is low
546
     rule: if Inclination Magic is high
                                        then DanceClass is low
547
548
     rule: if InclinationFighting is high
                                             and CombatSkill is low
549
   then FencingClass is high
     rule: if InclinationFighting is high
                                            and CombatAttack is low
550
   then FencingClass is high
     rule: if InclinationHousekeeping is high then FencingClass is low
551
552
     rule: if InclinationFighting is high
                                             and CombatSkill is low
553
   then FightingClass is high
     rule: if InclinationFighting is high
                                             and CombatDefense is low
554
   then FightingClass is high
     rule: if InclinationHousekeeping is high then FightingClass is low
555
556
                                        and MagicSkill is low
     rule: if InclinationMagic is high
                                                                     then MagicC
557
     rule: if Inclination Magic is high
                                        and MagicAttack is low
                                                                     then Magic
558
     rule: if InclinationFighting is high then MagicClass is low
559
560
     rule: if InclinationArtistry is high
                                             and sensitivity is low then Paint:
561
     rule: if InclinationArtistry is high
                                            and refinement is low then Painting
562
     rule: if Inclination Magic is high and intelligence is low then Painting
563
     rule: if InclinationArtistry is high
                                            and Artistry is low then Painting
564
     rule: if InclinationFighting is high then PaintingClass is low
565
```

#

566

```
rule: if InclinationArtistry is high
                                            and refinement is low
567
   then PoetryClass is high
     rule: if InclinationArtistry is high
                                            and sensitivity is low
568
   then PoetryClass is high
     rule: if InclinationArtistry is high
                                           and Artistry is low
                                                                     then Poetry
569
     rule: if Inclination Magic is high and intelligence is low then Poetry C
     rule: if InclinationFighting is high then PoetryClass is low
571
572
     rule: if InclinationMagic is high
                                                                    then Strateg
                                        and intelligence is low
573
     rule: if InclinationFighting is high
                                            and CombatSkill is low
574
   then StrategyClass is high
     rule: if InclinationArtistry is high
                                             and sensitivity is low then Strat
575
576
                                         and intelligence is low
     rule: if InclinationMagic is high
577
   then TheologyClass is high
     rule: if InclinationMagic is high
                                         and MagicDefense is low
578
   then TheologyClass is high
     rule: if InclinationHousekeeping is high
                                                  and faith is low then Theolog
579
     rule: if InclinationSinfulness is high then TheologyClass is low
581
     rule: if InclinationArtistry is high
                                             and Decorum is low
                                                                    then Manner
582
                                             and refinement is low then Manne
     rule: if InclinationArtistry is high
583
     rule: if InclinationHousekeeping is high then MannersClass is low
584
585
     rule: if InclinationMagic is high and intelligence is low
                                                                   then Science
586
     rule: if InclinationMagic is high and MagicDefense is low
                                                                   then Science
587
     rule: if InclinationHousekeeping is high and faith is low
                                                                     then Science
```