

i. the optimal cost of a subtree starting at node (i, j) is the sum of min cost of left and right subtrees plus the sum of frequencies i to j .

$$ii. \text{mincost}(i, j) = \sum_{x=i}^j P(x) + \min_{r=i}^j [\text{cost}(i, r-1) + \text{cost}(r+1, j)]$$

iii. pseudocode:

```
for  $i = 1 \rightarrow n$ 
   $c(i, i) = P(i)$ 
```

```
for  $L = 2 \rightarrow n$ 
```

```
  for  $i = 0 \rightarrow n - L + 1$ 
```

```
     $j = i + L - 1$ 
```

```
    for  $r = i \rightarrow j$ 
```

```
      left = if  $r > i$ 
              then  $c(i, r-1)$ 
              else 0
```

```
      right = if  $r < j$ 
               then  $c(r+1, j)$ 
               else 0
```

```
      cost = left + right +  $\sum_{x=i}^j P(x)$ 
```

```
      if cost <  $c(i, j)$ 
```

```
        cost( $i, j$ ) = cost
```