

# Pre-midterm Section

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Today in section, we reviewed the bootstrap. First, conceptually; then in R code.

This code contains two ways to go about bootstrapping: We can define a function or use a `for` loop. The first may be more helpful for the near future.

## Bootstrapping: Concepts

- Plug-in principle
- ECDF
- “Pull yourself up by your bootstraps”

Remember that we are trying to characterize the uncertainty of our estimator.

## Bootstrapping: 4 steps

First, let us walk through the steps of bootstrapping.

We will talk through each step and figure out the code for **one** resampling iteration first.

We will start with one variable. Remember Pset 2? What was the setting then? Remember to keep population and sample straight.

### Data

Now let's assume that this example data `df_eg1` is our sample data ( $n = 100$ ):

```
# Let's say this is our sample data
df_eg1 <- sample(x = c(56:59), size = 100, replace = TRUE)
head(df_eg1)
```

```
## [1] 59 57 56 58 59 58
```

### 4 steps

1. From your sample, take a *with replacement* sample of size  $n$ .

```
# Define the number of samples you want to draw
n_data <- length(df_eg1)

# Sample
samp <- sample(x = df_eg1, size = n_data, replace = TRUE)
samp
```

```
## [1] 58 56 58 58 59 57 59 56 56 56 58 58 56 56 59 59 56 56 59 56 56 56 59
## [24] 56 57 59 59 56 59 57 56 59 57 59 59 58 57 59 58 57 56 56 58 57 56 57
## [47] 56 57 58 58 59 59 57 59 57 58 56 58 56 56 58 56 56 57 58 57 57 57 57
## [70] 56 58 59 59 58 57 58 57 59 59 58 56 56 57 59 58 59 58 56 56 58 58 58
## [93] 56 56 57 57 58 56 57 59
```

2. Calculate what your estimate would be using the bootstrap sample from step 1.

If the test statistic of interest was the mean, we would run:

```
mean(samp)
```

```
## [1] 57.39
```

3. Repeat step 1 and step 2 many times.

We now have a collection of bootstrap estimates.

4. Calculate the standard deviation of the bootstrap distribution of our estimator.

We take the bootstrap estimates obtained in step 3 and run the `sd()` function.

## Example 2: Full example

Now suppose there are multiple variables,  $X$ ,  $Y$ , and  $Z$ .

Suppose that our sample statistic of interest is the sum of the mean of  $X$ , mean of  $Y$ , and mean of  $Z$ . Now we will try the whole bootstrapping procedure, including the iteration part.

### Data

Let's use this toy data.

```
set.seed(503)

data_sample <- data.frame(
  x = rnorm(n = 1000, mean = 3, sd = 1),
  y = rnorm(n = 1000, mean = 4, sd = 2),
  z = rnorm(n = 1000, mean = 6, sd = 3)
)
```

### Define the function

Let's define our function estimator:

```
estimator <- function(sample) {mean(sample$x) + mean(sample$y) + mean(sample$z)}
estimator(sample = data_sample)
```

```
## [1] 13.02346
```

### Bootstrapping using a user-defined function

1. From your sample, take a *with replacement* sample of size  $n$ . This time, let's define this as a function. Notice how we sample different variables. *discussion*

```
draw_bootstrap_sample <- function() {
  data_sample[sample(nrow(data_sample), replace = TRUE), ]
}
```

Addendum: `samp.int` is a bare interface version of `sample`. *discussion*

2. Calculate what your estimate would be using the bootstrap sample from step 1.
3. Repeat step 1 and step 2 many times.

```
n_iter <- 1000
bootstrap_est <- replicate(n_iter, estimator(draw_bootstrap_sample()))
```

We now have a collection of bootstrap estimates.

4. Calculate the standard deviation of the bootstrap distribution of our estimator (standard error)

```
est_se_est <- sd(bootstrap_est)
est_se_est
```

```
## [1] 0.1141754
```

## Example using for loop

Suppose we have a function that will give us three values for each of the three variables.

### Define function

Don't worry about what this is, we just want to illustrate how we may do this with three outputs (as discussed in class).

```
estimator2 <- function(sample) {
  c(mean(sample$x), mean(sample$y)/mean(sample$x), mean(sample$z)/mean(sample$x))
}
estimator2(sample = data_sample)
```

```
## [1] 2.987772 1.327488 2.031432
```

### Using a for loop

```
# Number of sample data rows
nrow_samp <- nrow(data_sample)

# Number of iterations
n_iter = 1000

# Store the three coefficients from each iteration in a row of this matrix.
boot <- matrix(NA, nrow = n_iter, ncol = 3)

# For loop
for(i in 1:n_iter){
  samp_data <- data_sample[sample(nrow_samp, replace = T),]
  boot[i,] <- estimator2(samp_data)
}
```

```
# Take sd() of each column to return a bootstrapped SE on each estimate.  
apply(boot, MARGIN = 2, FUN = sd)
```

```
## [1] 0.03052673 0.02578081 0.03783804
```