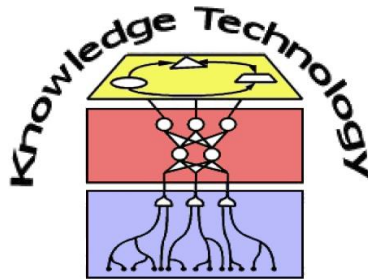


# Data Mining

## Lecture 8 Clustering and Selforganizing Networks



<http://www.informatik.uni-hamburg.de/WTM/>

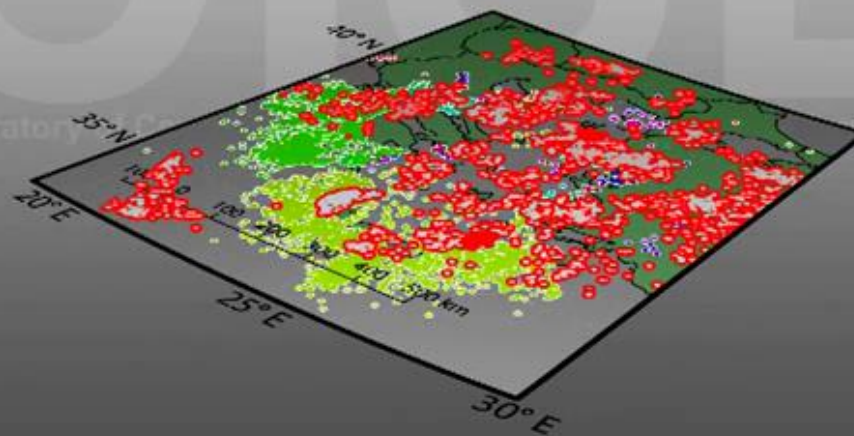
# What is Cluster Analysis?

- Cluster: A group of data objects
  - similar (or related) to one another within the same group
  - dissimilar (or unrelated) to the objects in other groups
- Cluster analysis
  - Finding similarities between data according to their characteristics and grouping similar data objects into clusters
- **Unsupervised learning**: no predefined classes
- Typical applications
  - As a **stand-alone tool** to get insight into data distribution
  - As a **preprocessing step** for other algorithms

# Clustering for Data Understanding and Applications

- Biology: taxonomy of living things: class, family, genus and species
- Information retrieval: document clustering
- Marketing: help marketers discover distinct customer groups, and develop targeted marketing programs
- Land use: similar land use in an earth observation database
- City-planning: identifying groups of houses according to their house type, value (and geographical location)
- Climate: understanding earth climate, find patterns of atmospheric similarities
- Earth-quake studies: observed earth quake epicenters should be clustered along continent faults

# Spatiotemporal Clustering of Earthquakes in Greece



# Quality: What Is Good Clustering?

- High quality clusters
  - high *intra-class* similarity: *cohesive* within clusters
  - low *inter-class* similarity: *distinctive* between clusters
- The **quality** of a clustering method depends on
  - the *similarity measure* used by the method
  - its implementation, and
  - its ability to discover the *hidden patterns*

# Measure the Quality of Clustering

- Dissimilarity/Similarity metric
  - **Similarity** is expressed in terms of a **distance function**, e.g. a **metric**  $d(i, j)$
  - The definitions of distance functions are usually different for interval-scaled, boolean, categorical, or vector variables
  - Different variables may be assigned different weights based on applications and data semantics
- Quality functions (“Clustering Indices”)
  - The “goodness” of a clustering process can be quantified, e.g. by relating intra-class vs. inter-class similarities
  - It is hard to set thresholds for “similar enough” for data points or “good enough” for the clustering

# Typical Requirements

- Scalability
- Incremental clustering and insensitivity to input order
- High dimensionality
- Ability to deal with different types of attributes
- Ability to deal with noisy data
- Discovery of clusters with arbitrary shape
- Constraint-based clustering
- Domain knowledge to determine input parameters
- Interpretability and usability

# Major Clustering Approaches (1)

## ■ ***Partitioning approach***

- Construct various partitions and then evaluate them by some criterion, e.g., minimizing the sum of squared errors
- Typical methods: k-means, k-medoids, CLARANS

## ■ ***Hierarchical approach***

- Create a hierarchical decomposition of the set of data (or objects) using some criterion
- Typical methods: Diana, Agnes, BIRCH, CAMELEON

## ■ ***Density-based approach***

- Based on connectivity and density functions above threshold
- Typical methods: DBSCAN, OPTICS, DenClue



# Major Clustering Approaches (2)

## ■ ***Grid-based approach***

- multiple-level granularity structure, finite number of cells
- Typical methods: STING, WaveCluster, CLIQUE

## ■ ***Model-based***

- A model is hypothesized for each of the clusters and tries to find the best fit of that model to each other
- Typical: Gaussian Mixture Models, EM, SOM, COBWEB

## ■ ***Frequent pattern-based***

- Based on the analysis of frequent patterns
- Typical methods: p-Cluster

## ■ ***Instance-based***

- Typical: K-nearest neighbors (kNN) — *classify* a data point by the majority vote of its K closest neighbour points

# Data Matrix and Dissimilarity Matrix

## ■ *Data matrix*

- n data points with p dimensions

$$\begin{bmatrix} x_{11} & \dots & x_{1f} & \dots & x_{1p} \\ \dots & \dots & \dots & \dots & \dots \\ x_{i1} & \dots & x_{if} & \dots & x_{ip} \\ \dots & \dots & \dots & \dots & \dots \\ x_{n1} & \dots & x_{nf} & \dots & x_{np} \end{bmatrix}$$

## ■ *Dissimilarity matrix*

- Registers the distances between the n data points
- A triangular matrix

$$\begin{bmatrix} 0 & & & & \\ d(2,1) & 0 & & & \\ d(3,1) & d(3,2) & 0 & & \\ \vdots & \vdots & \vdots & & \\ d(n,1) & d(n,2) & \dots & \dots & 0 \end{bmatrix}$$

# Reminder: Numeric Data: Minkowski Distance

- **Minkowski distance**: A popular distance measure

$$d(i, j) = \sqrt[h]{|x_{i1} - x_{j1}|^h + |x_{i2} - x_{j2}|^h + \dots + |x_{ip} - x_{jp}|^h}$$

where

$i = (x_{i1}, x_{i2}, \dots, x_{ip})$  and  $j = (x_{j1}, x_{j2}, \dots, x_{jp})$  are two  $p$ -dimensional data objects,

$h$  = order (the distance so defined is also called L- $h$  norm)

- Properties
  - $d(i, j) > 0$  if  $i \neq j$ , and  $d(i, i) = 0$  (Positive definiteness)
  - $d(i, j) = d(j, i)$  (Symmetry)
  - $d(i, j) \leq d(i, k) + d(k, j)$  (Triangle Inequality)
- A distance that satisfies these properties is a **metric**

# Reminder:

## Special Cases of Minkowski Distance

- $h = 1$ : ( $L_1$  norm) ***Manhattan distance***

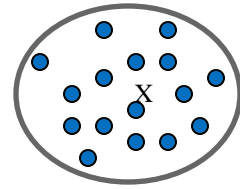
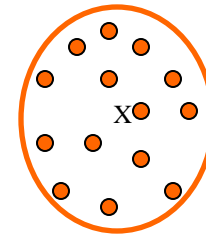
$$d(i, j) = |x_{i1} - x_{j1}| + |x_{i2} - x_{j2}| + \dots + |x_{ip} - x_{jp}|$$

- E.g., the ***Hamming distance*** between two ***binary vectors***: the number of bits that are different

- $h = 2$ : ( $L_2$  norm) ***Euclidean distance***

$$d(i, j) = \sqrt{|x_{i1} - x_{j1}|^2 + |x_{i2} - x_{j2}|^2 + \dots + |x_{ip} - x_{jp}|^2}$$

# Distance between Clusters



- Single link: **smallest distance** between any element ( $p$ ) in one cluster ( $i$ ) and any element ( $q$ ) in the other ( $j$ ), i.e.,  $dist(K_i, K_j) = \min_{p,q} d(x_{ip}, x_{jq})$
- Complete link: **largest distance** between any element in one cluster and any element in the other, i.e.,  $dist(K_i, K_j) = \max_{p,q} d(x_{ip}, x_{jq})$
- Average: **avg distance** between an element in one cluster and an element in the other, i.e.,  $dist(K_i, K_j) = avg_{p,q} d(x_{ip}, x_{jq})$
- Centroid: distance **between the centroids** of two clusters, i.e.,  $dist(K_i, K_j) = d(C_i, C_j)$
- Medoid: distance **between the medoids** of two clusters, i.e.,  $dist(K_i, K_j) = d(M_i, M_j)$ 
  - Medoid: a chosen, centrally located **object** in the cluster (whose dissimilarity to all other objects in the cluster is minimal)

# Centroid, Radius and Diameter of a Cluster (for numerical data sets)

- Centroid: the “center of mass” of a cluster  
( $N_i = \#$  points in the cluster  $i$ )  
← has minimal average Euclidean distance

$$C_i = \frac{\sum_{p=1}^{N_i} x_{ip}}{N_i}$$

- Radius: ~ average Euclidean distance  
from any point of the cluster to its  
centroid

$$R_i = \sqrt{\frac{\sum_{p=1}^{N_i} (x_{ip} - C_i)^2}{N_i}}$$

- Diameter: average Euclidean distance  
between all *pairs* of points in the cluster

$$D_i = \sqrt{\frac{\sum_{p=1}^{N_i} \sum_{q=1}^{N_i} (x_{ip} - x_{iq})^2}{N_i(N_i - 1)}}$$

# Partitioning Algorithms: Basic Concept

- **Partitioning method**: partition a database  $D$  of objects  $x_p$  into a set of  $k$  clusters, minimising sum of squared distances to means  $m_i$

$$E = \sum_{i=1}^k \sum_{p \in C_i}^{N_i} (x_p - m_i)^2$$

# points assigned to cluster  $i$

sum over clusters

each point  $p$  is assigned to exactly one cluster  $i$

- Given  $k$ , find a partition of  $k$  clusters that optimizes the chosen partitioning criterion
  - Find global optimum: exhaustively enumerate all possible partitions
  - Find a local optimum by heuristic methods:
    - ***k-means*** (MacQueen'67): Each cluster is represented by its center
    - ***k-medoids*** or Partition around medoids (PAM, Kaufman&Rousseeuw'87): Each cluster is represented by one of the objects in the cluster

# The *K-Means* Clustering Method

- Given  $k$ , the *k-means* algorithm is as:
  1. Partition objects into  $k$  non-empty subsets
  2. Compute the centroids (center of mass / mean) of the clusters of the current partitioning
  3. Assign each object to the cluster with the nearest centroid
  4. Go to Step 2; Stop when none of the assignments changed



# The $k$ -Means Algorithm

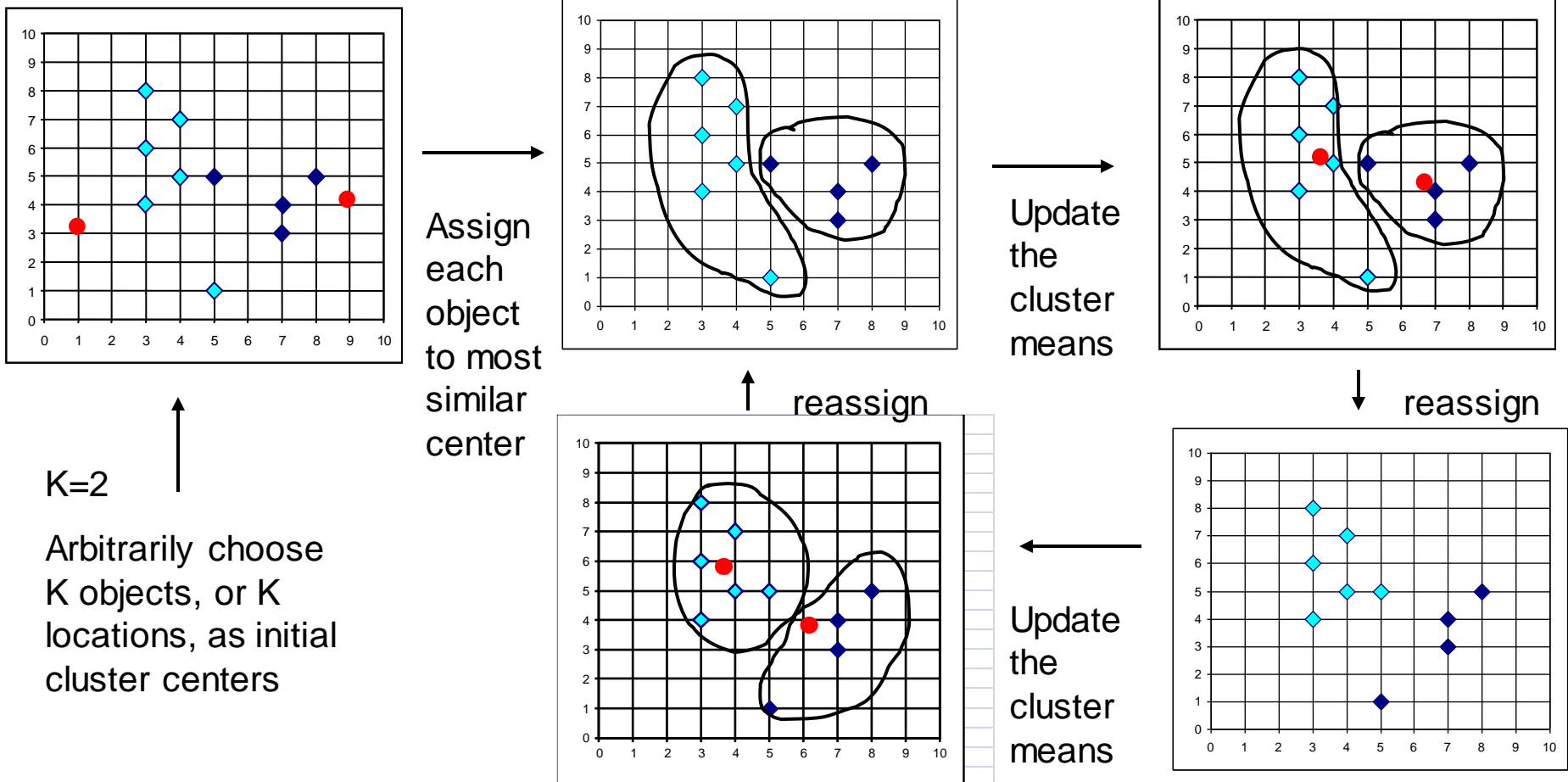
- Initialization
  - Set a value for  $k$
  - Place the  $k$  cluster centres  $\mu_j$  at random positions in input space
- Learning: Repeat ...
  - For each data point  $x_p$ 
    - Compute distance to each cluster centre
    - Assign data point to nearest cluster centre with distance
$$d_p = \min_j d(x_p, \mu_j)$$
  - For each cluster centre
    - Move position of centre to mean of points in cluster

$$\mu_j = \frac{1}{N_j} \sum_{i=1}^{N_j} x_i \quad N_j = \text{number of points in cluster } j$$

- ... until the assignments don't change (then, cluster centres stop moving)
- On-line version: move cluster center only a bit for each data point

# The *K-Means* Clustering Method

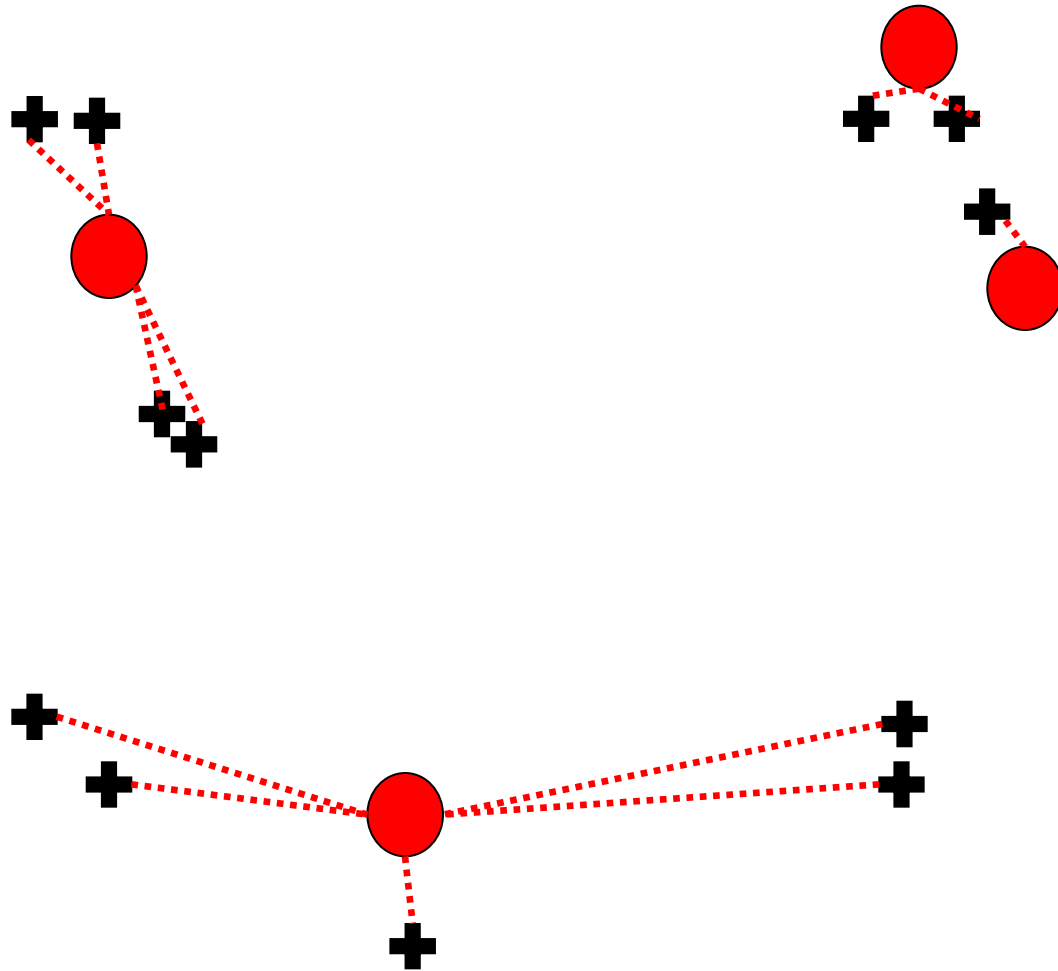
## ■ Example



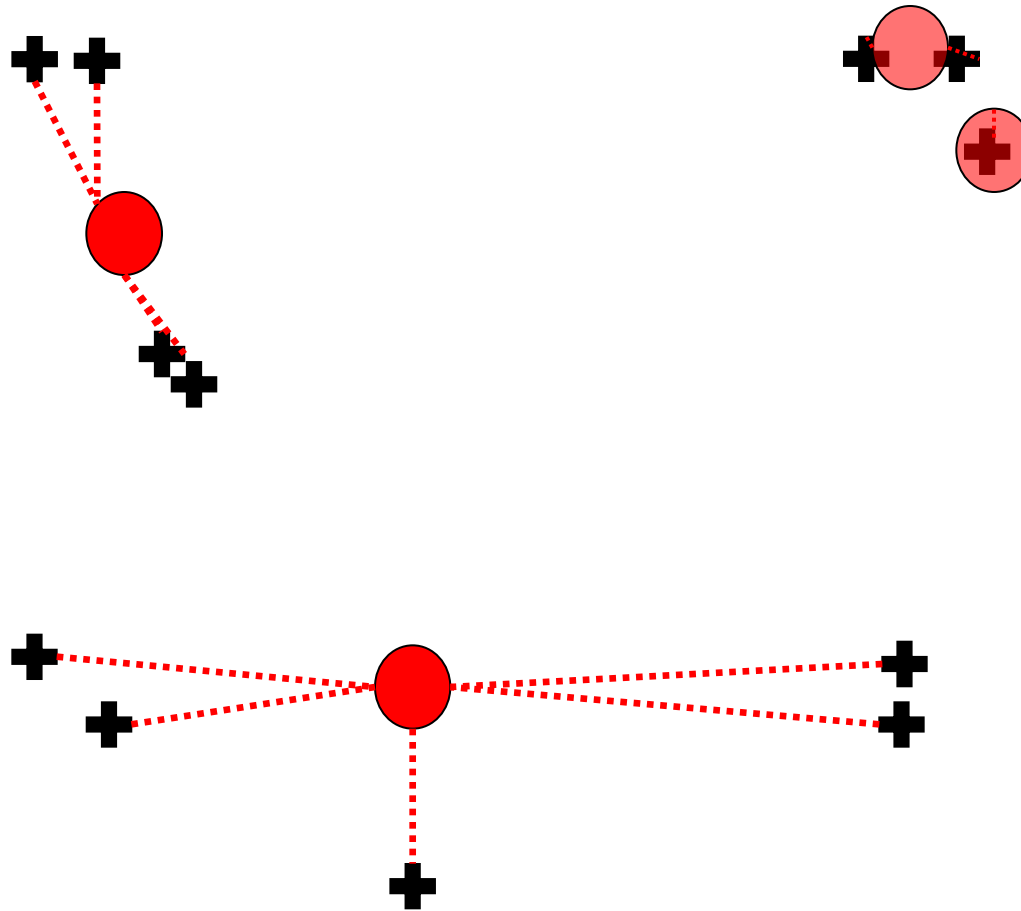
# Why k-Means Converges

- Change of **assignments** reduces the sum squared distances of the datapoints to their assigned cluster centers.
- Moving a **cluster center** reduces the sum squared distances of the datapoints to their assigned cluster centers.
- If the assignments do not change in the assignment step, we have converged.

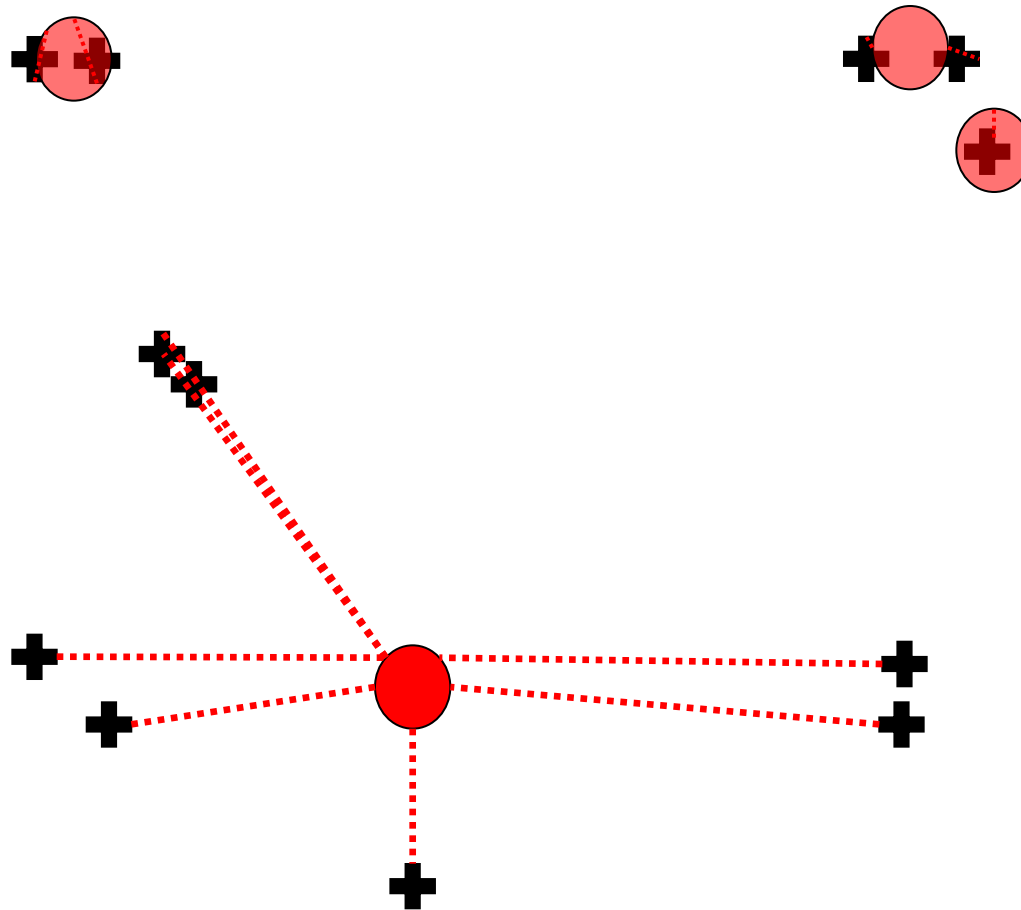
# Clustering: 4-means



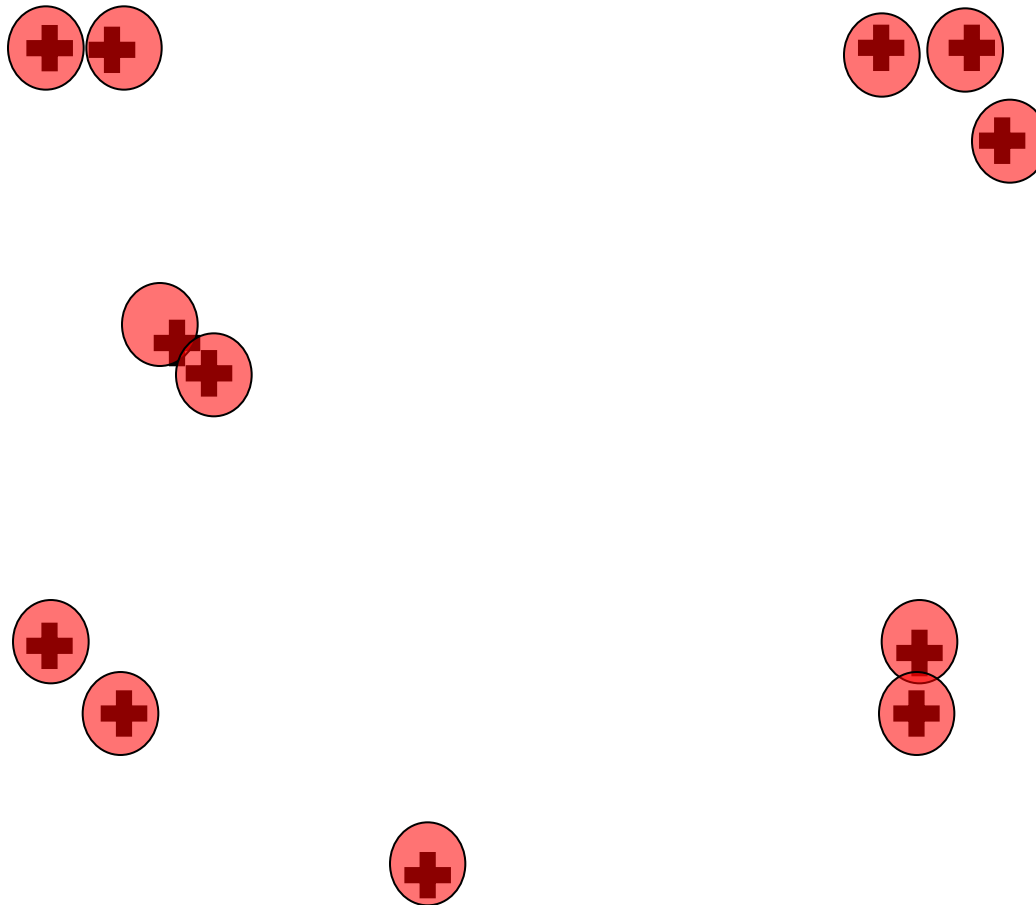
# Clustering: Local Minima (1)



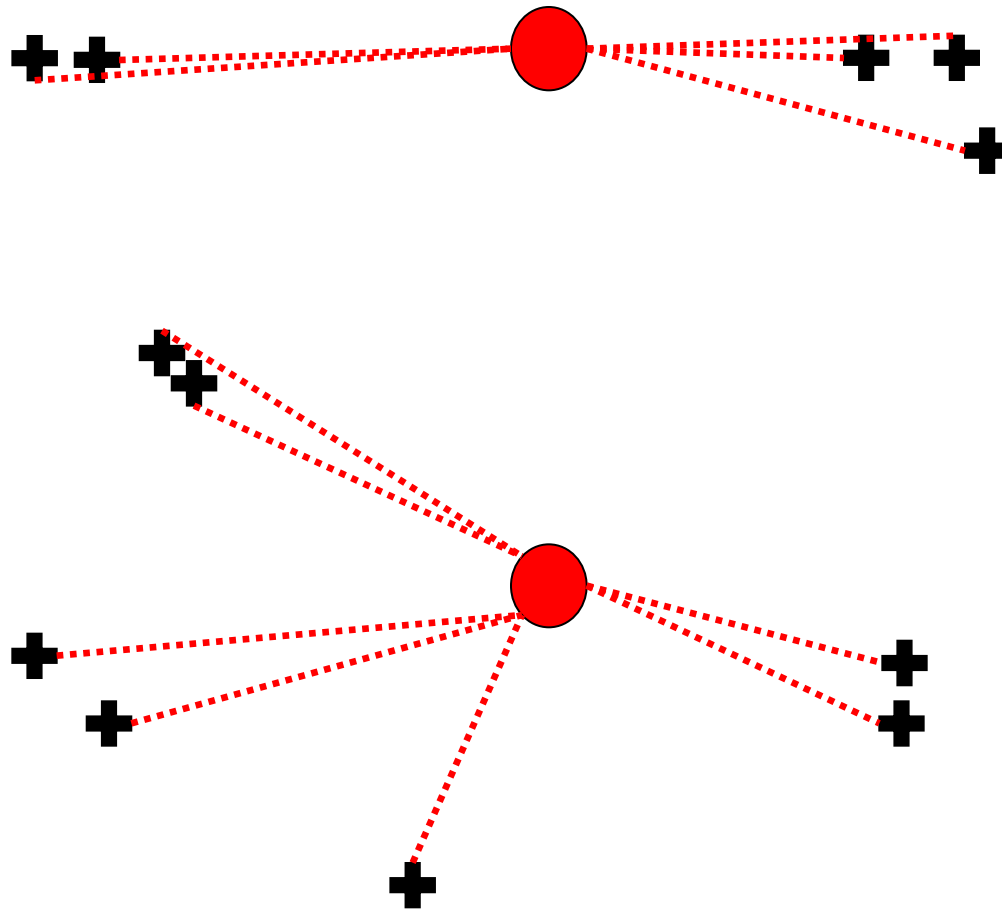
## Clustering: Local Minima (2)



# Clustering: Overfitting



# Clustering: Underfitting





# Comments on the *K-Means* Method

- **Strength:** *Relatively efficient:  $O(tkn)$ . Typically,  $k, t \ll n$ . ( $n = \text{\#objects}$ ,  $k = \text{\#clusters}$ ,  $t = \text{\#iterations}$ )*
- **Weaknesses**
  - Need to specify  $k$ , the *number* of clusters, in advance
  - Sensitive to noisy data and *outliers*
  - Terminates at a *local* optimum
  - Not suitable to discover clusters with *non-convex shapes*
  - Applicable only when *mean* is defined — not for categorical data

# Comments on the *K-Means* Method



k-means: choose the result that has minimal error  $E$

# Example: Object Hypotheses in Natural Scenes using k-Means

- In a stereo image pair of a scene, pixels can be clustered based on position, disparity, hue and saturation.
- For object segmentation, if two objects are in close proximity, they are likely to be encapsulated by the same segment.
- If we give the information that a segment covers two objects, k-means ( $k=2$ ) can find a likely split of that segment.
- Then the object modeling loop is resumed with the new hypotheses.

# Object Hypotheses Example

## Generating Object Hypotheses in Natural Scenes through Human-Robot Interaction

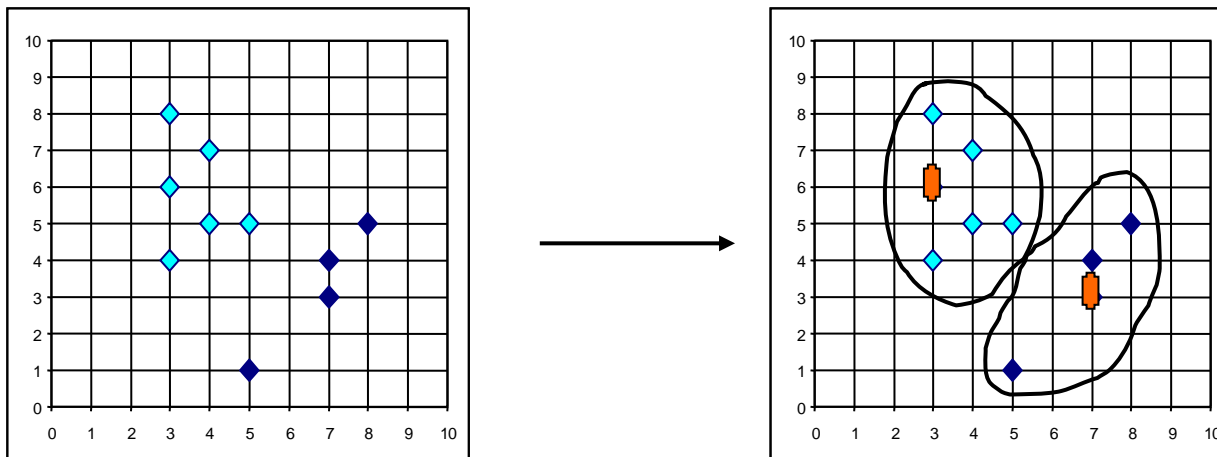
Niklas Bergström, Mårten Björkman, Danica Kragic

CSC/KTH Stockholm, Sweden

IROS '11

# Handling Outliers: the K-Medoids Method

- The k-means algorithm is sensitive to outliers!
  - Since an object with an extremely large value may substantially distort the distribution of the data.
- ***K-Medoids***: Instead of taking the *mean* value of the objects in a cluster as a reference point, *medoids* are used, which is the ***most centrally located object*** in a cluster.

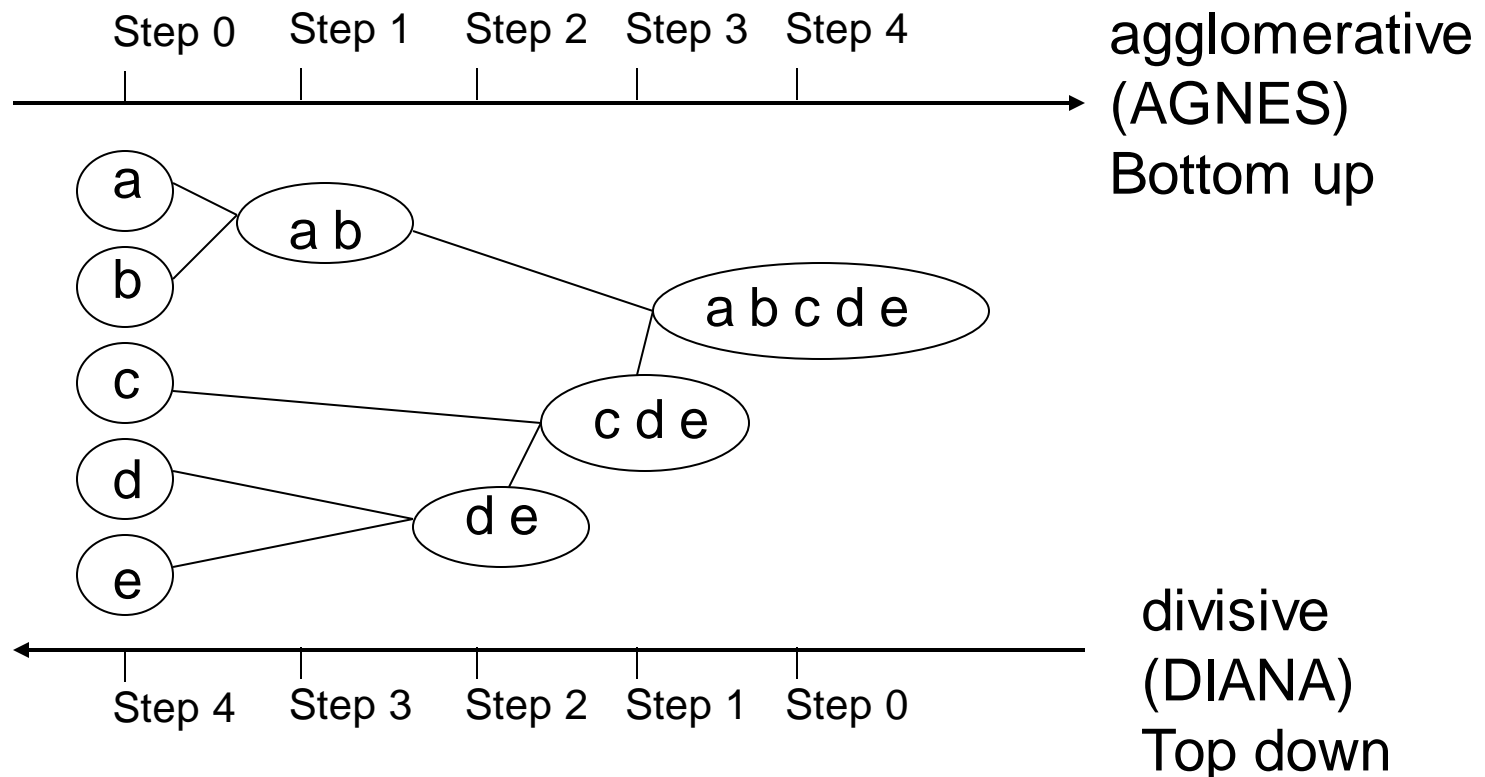


# Other Typical Partitioning Clustering Methods

- *K-Medoids* finds *representative* objects (*medoids*) in clusters
  - *PAM* (Partitioning Around Medoids, 1987)
    - starts from an initial set of medoids and iteratively replaces one of the medoids by one of the non-medoids if it improves the total distance of the resulting clustering
    - does not scale well for large data sets (computational complexity)
  - *CLARA* (Kaufmann & Rousseeuw, 1990): PAM on samples
  - *CLARANS* (Ng & Han, 1994): Randomized sampling

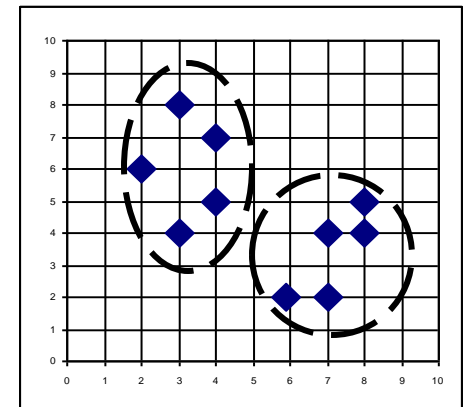
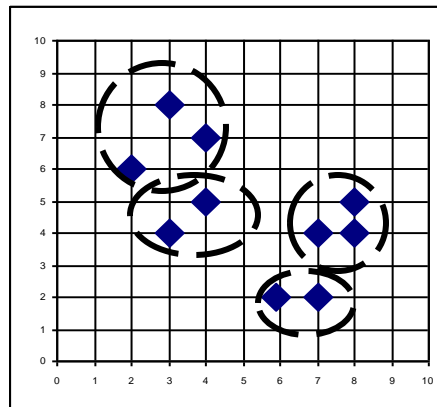
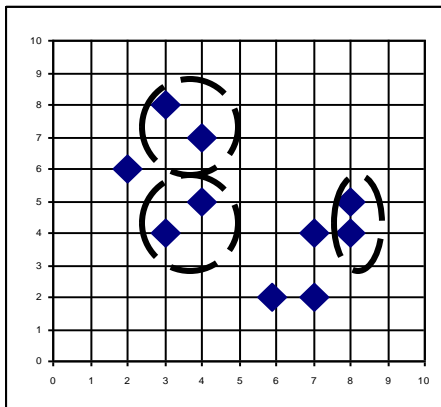
# Hierarchical Clustering

- Use distance matrix as clustering criteria. This method does not require the number of clusters  $k$  as an input, but needs a termination condition



# AGNES (Agglomerative Nesting)

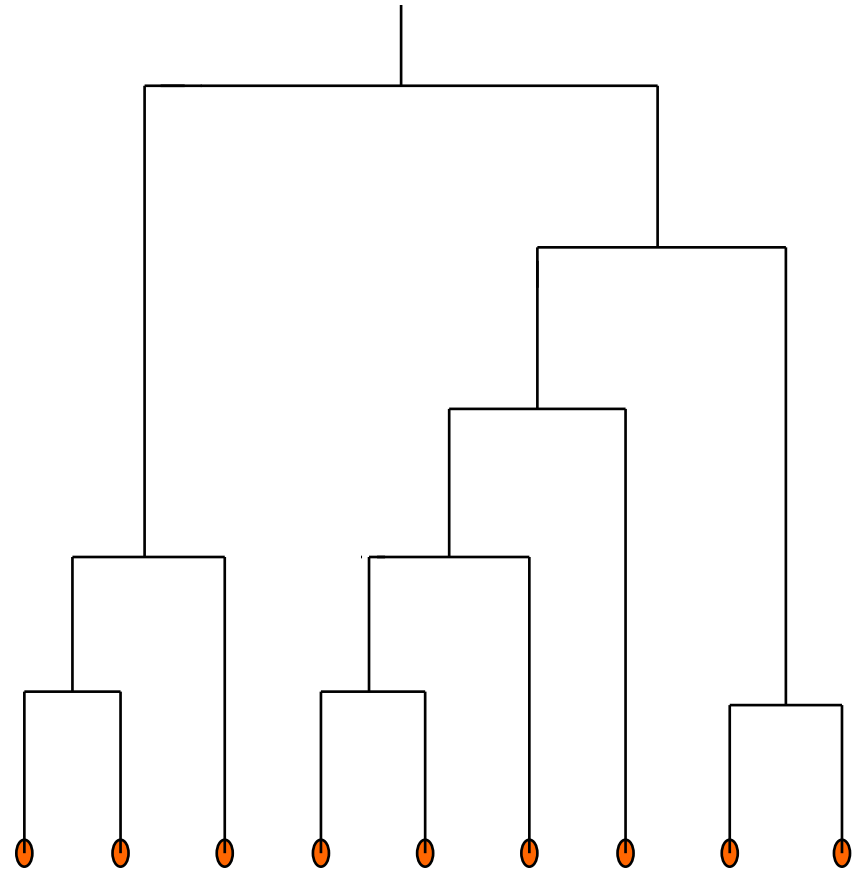
- Introduced in Kaufmann and Rousseeuw (1990)
- Implemented in statistical packages, e.g., Splus
- Use the *single-link* method and the dissimilarity matrix
- Merge nodes that have the least dissimilarity
- Go on in a non-descending fashion
- Eventually all nodes belong to the same cluster





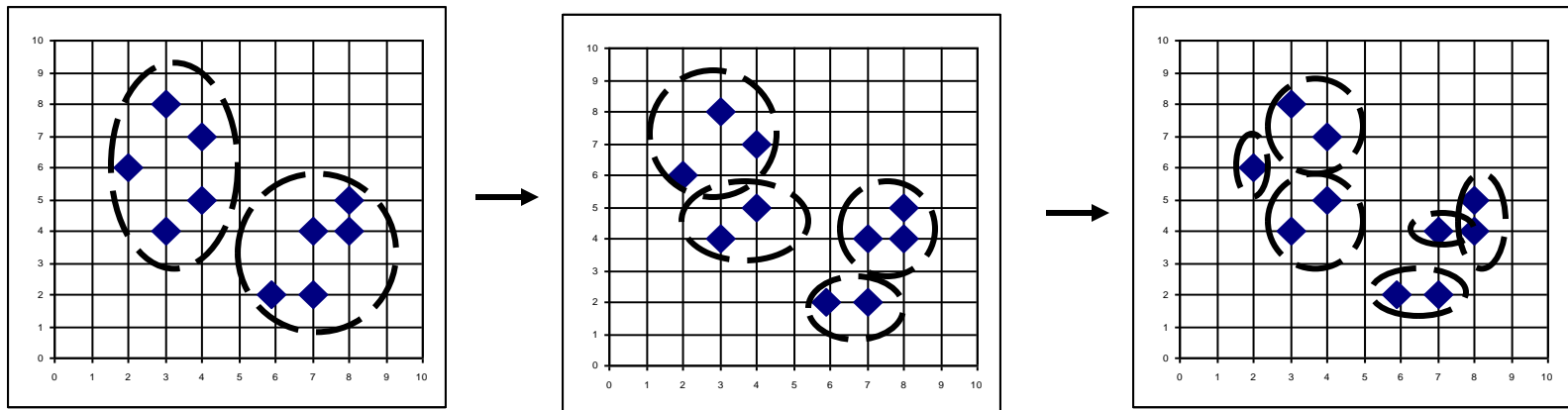
# Dendrogram Shows how Clusters are Merged

- Decompose data objects into several levels of nested partitioning (**tree** of clusters), called a **dendrogram**.
- A **clustering** of the data objects is obtained by **cutting** the dendrogram at the desired level, then each **connected component** forms a cluster.



# DIANA (Divisive Analysis)

- Introduced in Kaufmann and Rousseeuw (1990)
- Implemented in statistical analysis packages, e.g., Splus
- Inverse order of AGNES: **top down**
- Eventually each node forms a cluster on its own



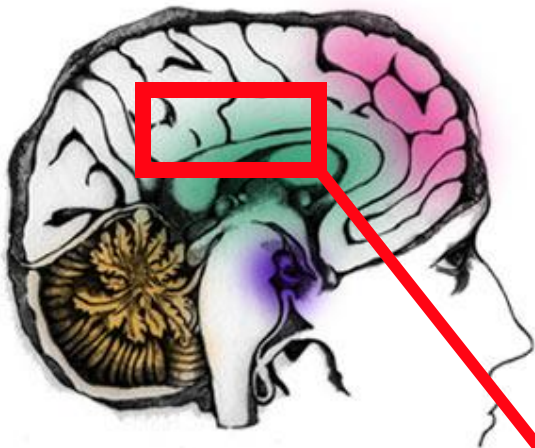
# Model-Based Clustering

- What is model-based clustering?
  - Assumption: a **cluster is generated by a model** such as a probability distribution
  - A model (e.g., Gaussian distribution) is determined by a set of parameters
  - Task: optimize the fit between the given data and some mathematical model by learning the parameters of the model
- Typical statistical methods
  - Gaussian Mixture Models, EM (Expectation maximization), AutoClass
- Typical neural network methods
  - SOM (Self-Organizing Feature Map)

# Neural Network Approaches

- Neural network approaches
  - Represent each cluster with an exemplar (a neuron), acting as a “**prototype**” of the cluster
  - New objects are assigned to the cluster whose exemplar is the **most similar** according to some distance measure
- Typical methods
  - **SOM (Self-Organizing feature Map)**
  - Competitive learning
    - Neurons compete in a “**winner-takes-all**” fashion for the object currently being presented

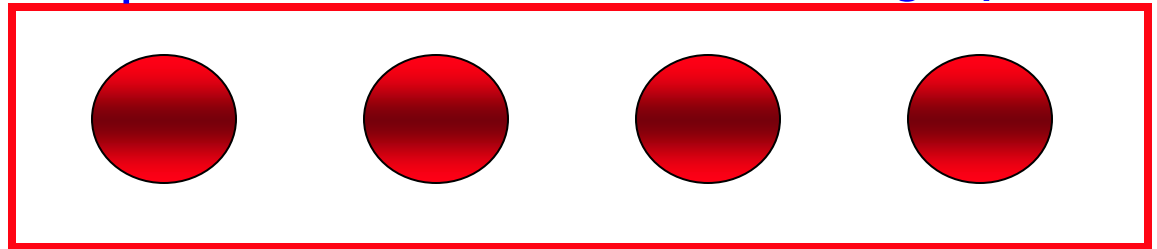
# Feature Maps



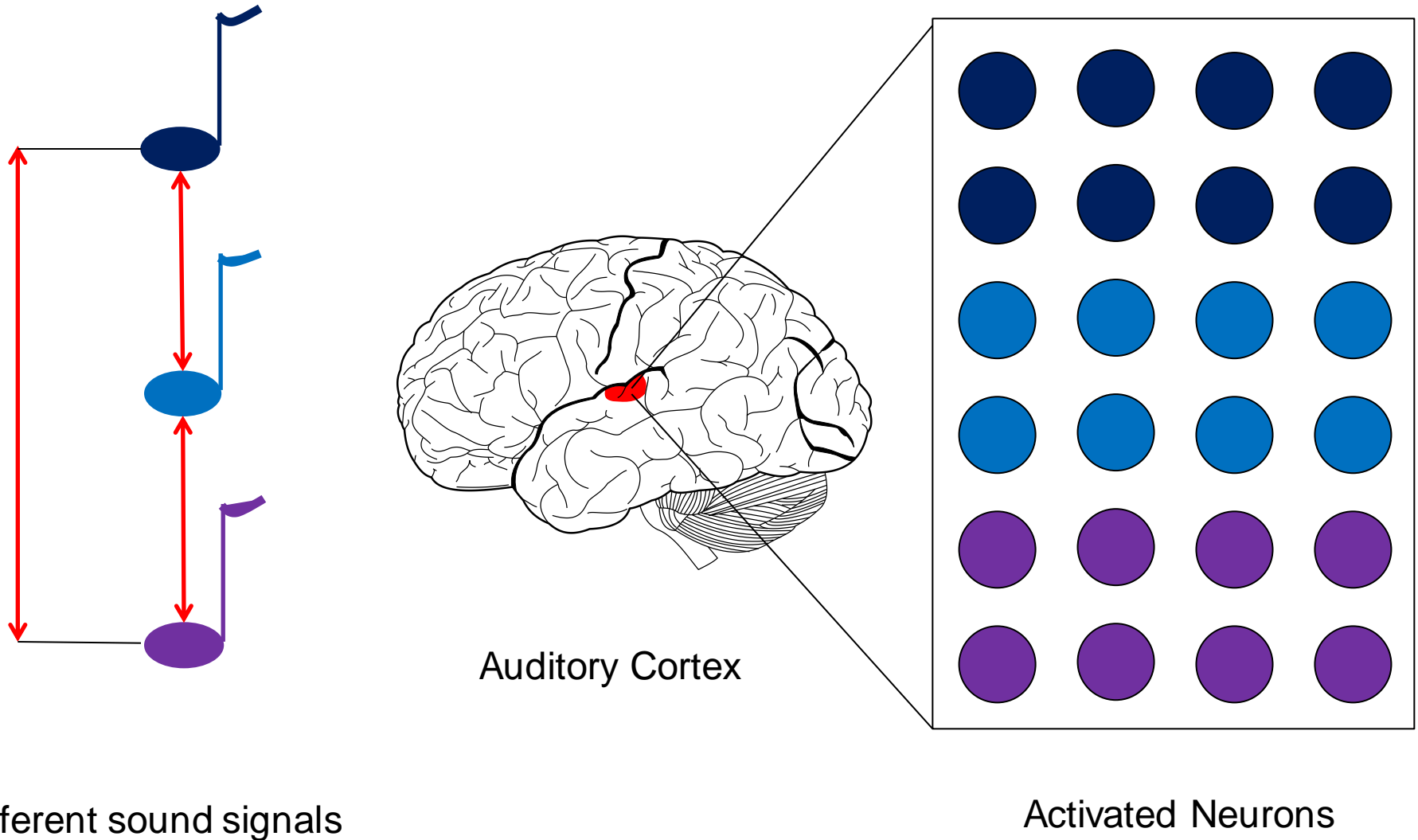
Low pitch

Higher pitch

High pitch



# Feature Maps: How are Signals Mapped into the Auditory Cortex?

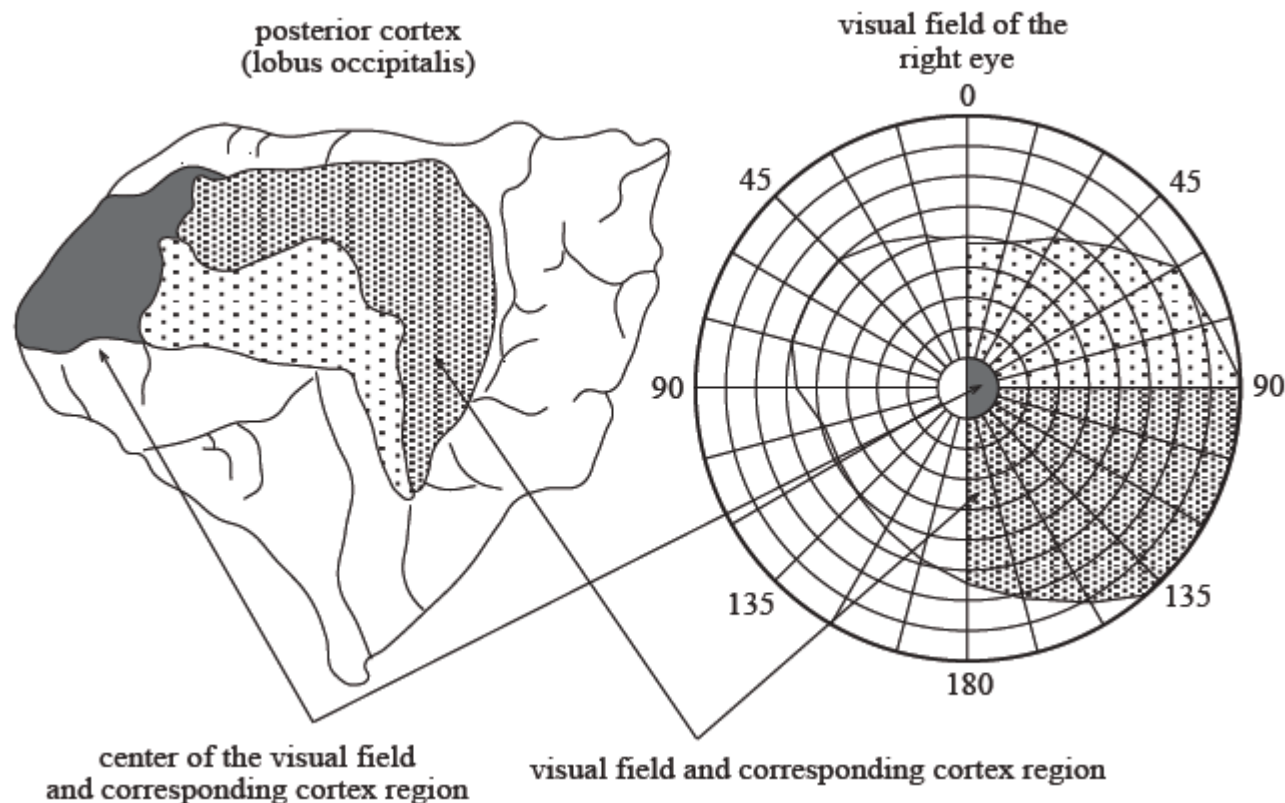


# Feature Maps

- Sounds that are similar ('nearby in input space') excite neurons that are near to each other (in 'output space')
- Sounds that are very different excite neurons that are a long way off
- This is known as *topology preservation*
- The ordering of the inputs is preserved
  - If possible (perfectly topology-preserving)

# Mapping of visual Field to Cortex

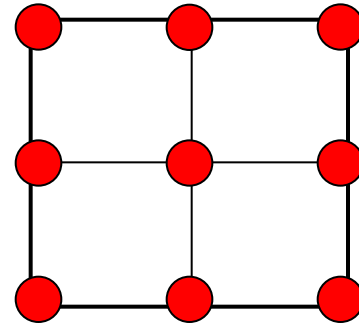
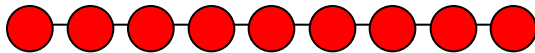
- Neighboring visual fields processed by neighboring cortex regions; fovea is large



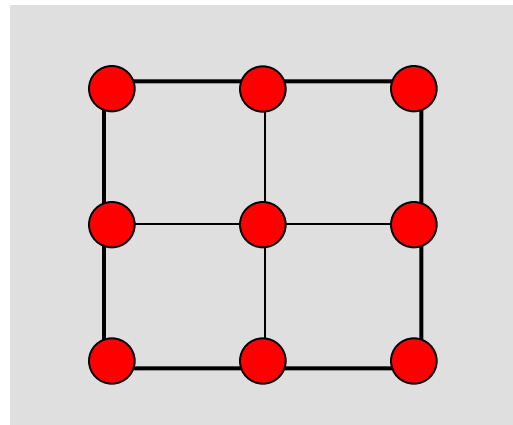
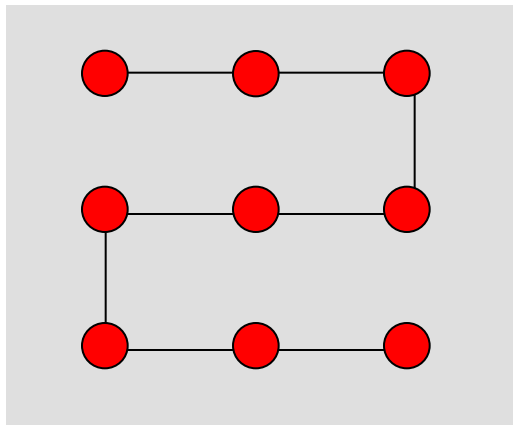


# Topology Preservation in 2D

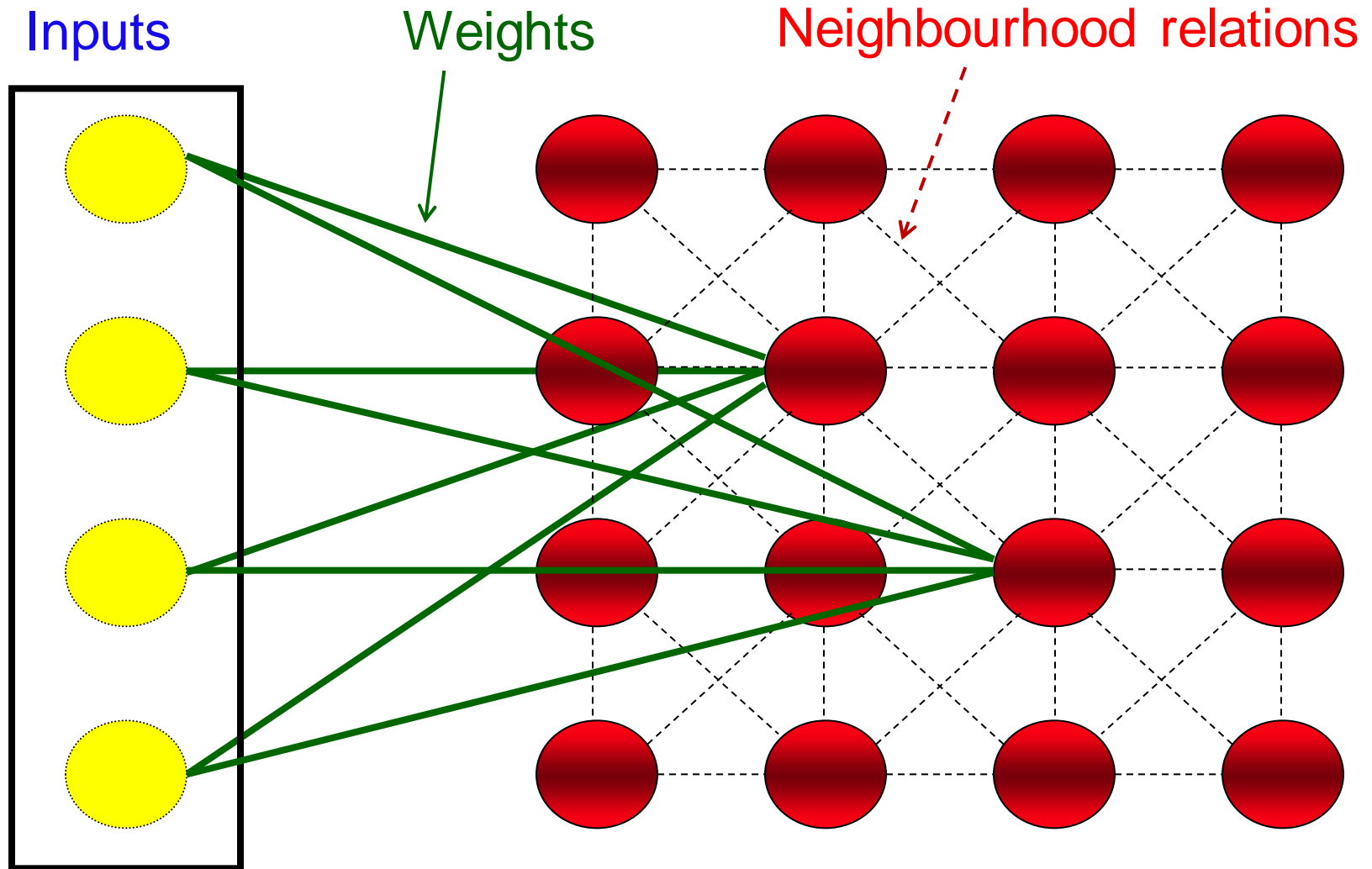
Network topology



Network representation of input space

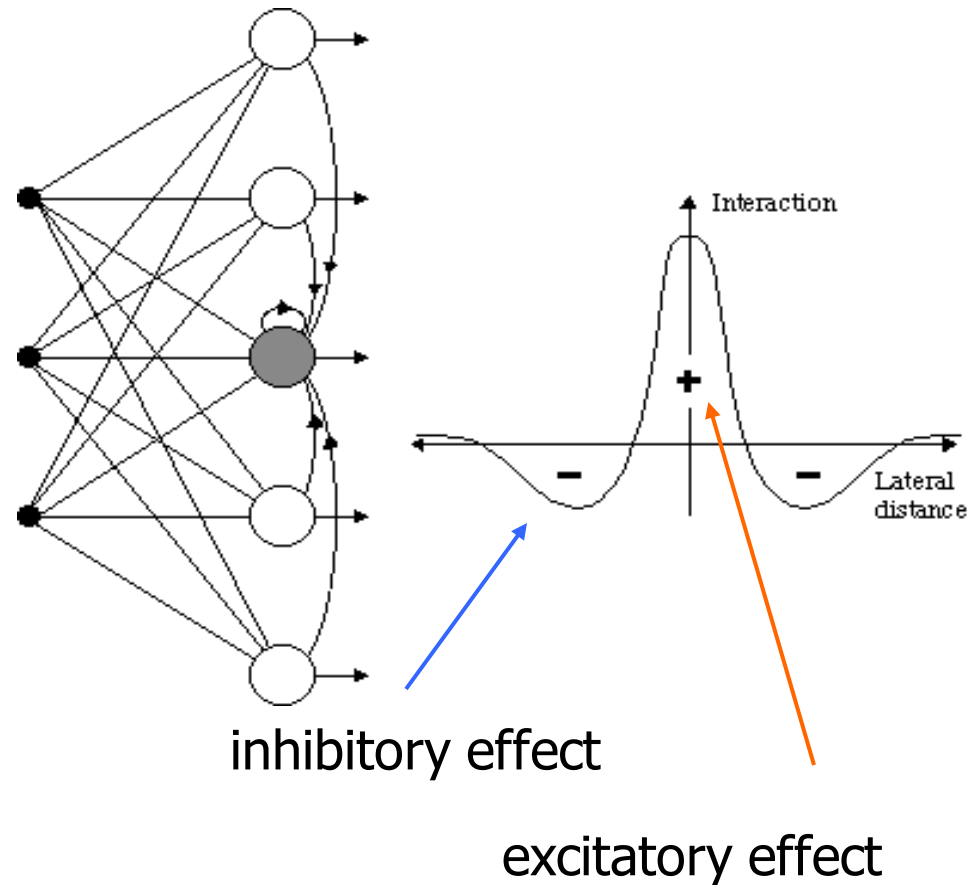


# The Self-Organising Map



# Mexican hat function

- The Mexican hat function represents the relationship between the distance from the winning neuron and the strength of “connections” within the Kohonen layer
- Near neighbourhood – short range lateral excitation area has strong positive effect
- Remote neighbourhood – has a weak negative inhibitory effect
- → WTA-like behaviour (competitive network!)



# Neuron Connections?

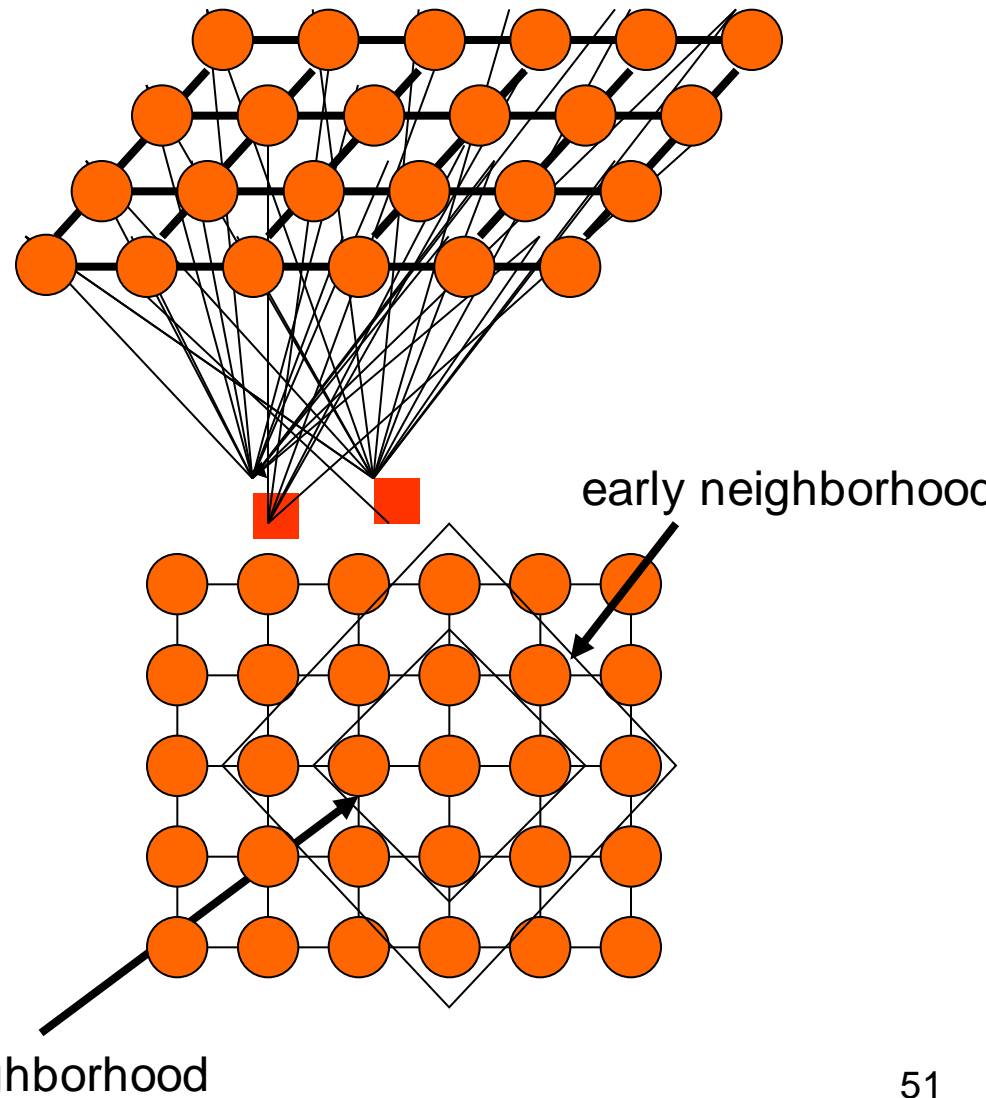
- We do not actually need the inhibitory connections
  - Just use a neighbourhood of positive connections
- How large should this neighbourhood be?
  - At the beginning of learning, the network is unordered
    - Large neighbourhood: each input vector excites many neurons
    - Nearby neurons will learn similarly
    - Their weights will be ordered in input space!
  - Later on, fine-tuning
    - Small neighbourhood: an input vector excites only neurons closeby
    - Neurons can specialize on small regions in input space

# Self-Organizing Map (SOM)

- SOMs, also called topological ordered maps, or Kohonen Self-Organizing Feature Map
- It maps the points in a **high-dimensional source space** into a **1D, 2D (most typical) or 3D target space**; distances and proximity relationships (i.e., topology) are preserved as much as possible
- Similar to k-means: cluster centers tend to lie in a low-dimensional manifold in the feature space
- Clustering is performed by having **several units competing** for the current object
  - The unit whose weight vector is closest to the current object wins
  - The winner **and its neighbors** learn by having their weights adjusted
- SOMs mimic some aspects of **competitive processing in the brain**
- Useful for visualizing high-dimensional data

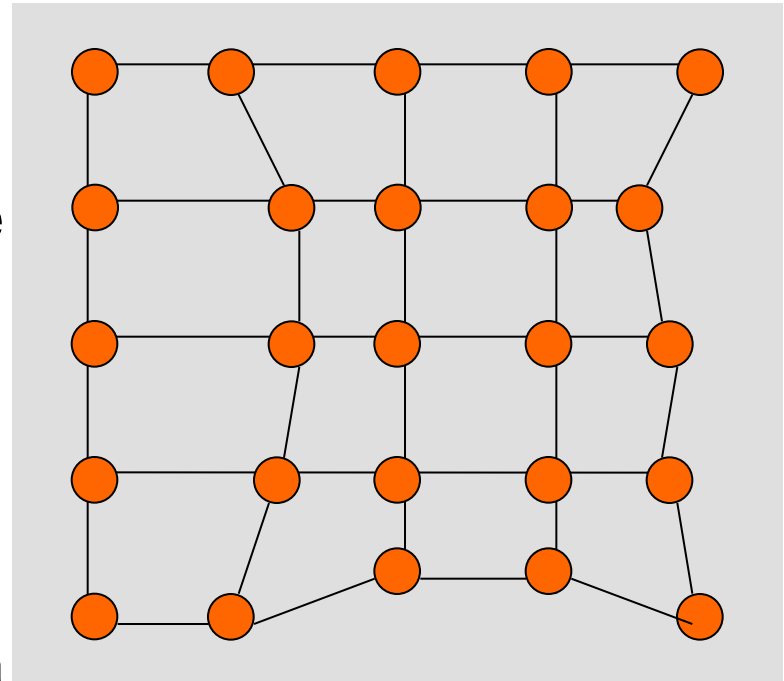
# Self organizing maps

- The activation of the neuron is spread in its direct neighborhood
  - neighbors become sensitive to the same input patterns
- The size of the neighborhood is initially large but reduced over time during training as the network neurons become more specialized



# Adaptation

- During training, the “winner” neuron and its neighborhood adapts to make their weight vector more similar to the input pattern that caused the activation
- The neurons are moved closer to the input pattern
- The magnitude of the adaptation is controlled via a learning parameter which decays over time



# SOM 'Cost Function'

- K-means:

$$E = \sum_{i=1}^k \sum_{p \in C_i} (x_p - m_i)^2$$

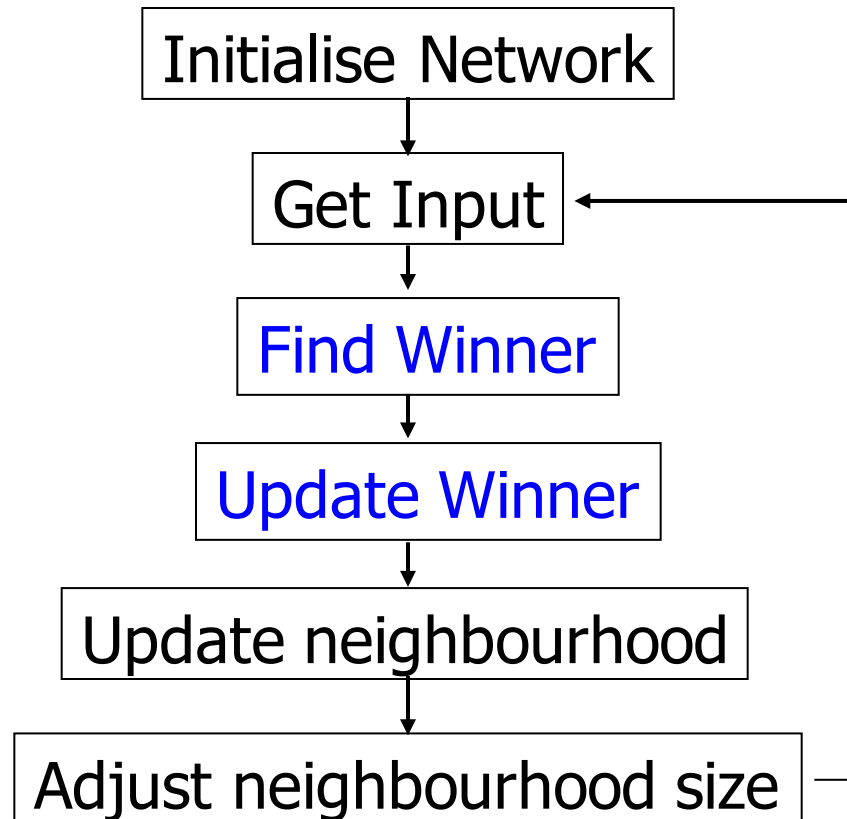
- SOM:

$$E = \sum_{i=1}^k \sum_{p \in C_i} \sum_j^k h(|i - j|) (x_p - m_j)^2$$

neighbourhood activation function  $h$



# SOM Algorithm



# The Self-Organising Map Algorithm

- The weight vectors are randomly initialised
- Input vectors are presented to the network
  - Determine **best matching neuron**  $n_b$  with the minimal Euclidean distance between input  $x$  and weight vector  $w$

$$n_b = \min_j \|x - w_j^T\|$$

- The winning node and neighbours have weight vector moved closer to the input (with learning rate  $\eta(t)$ )

$$w_j^T \leftarrow w_j^T + \eta(t) \cdot (x - w_j^T)$$

- Over time, the network *self-organises* so that the input topology is preserved

# The Self-Organising Map Algorithm

- The weight vectors are randomly initialised
- Input vectors are presented to the network
  - Determine **best matching neuron**  $n_b$  with the minimal Euclidean distance between input  $x$  and weight vector  $w$

$$n_b = \min_j \|x - w_j^T\|$$

- The winning node and neighbours have weight vector moved closer to the input (with learning rate  $\eta(t)$ )

$$w_j^T \leftarrow w_j^T + \eta(t) \cdot h(n_b, t) \cdot (x - w_j^T)$$

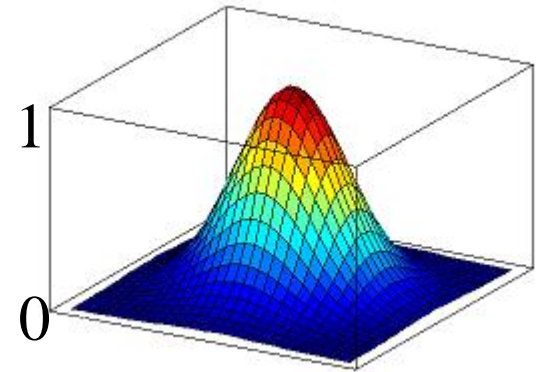
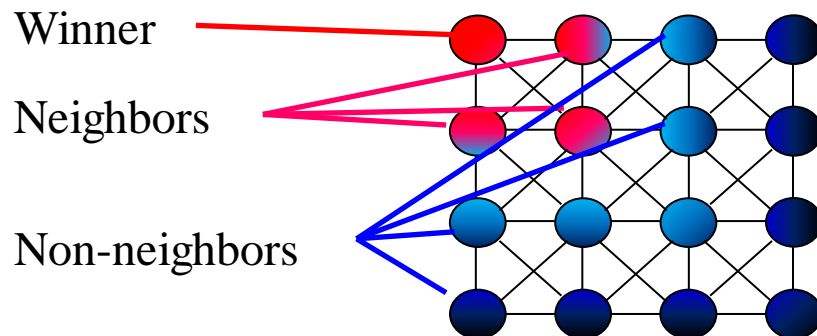
- Over time, the network *self-organises* so that the input topology is preserved

# Neighborhood Function Preserves Topology

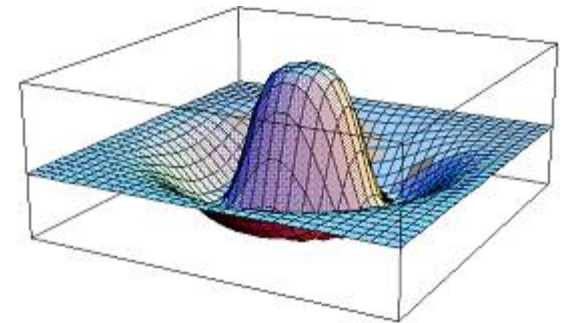
- The neighborhood function  $h(n_b, t)$  determines the degree of weight vector change of the neighbors

$$w_j^T \leftarrow w_j^T + \eta(t) \cdot h(n_b, t) \cdot (x - w_j^T)$$

- Mostly: Gaussian function;  
rarely: Mexican Hat function
- Width decreases during training  
( $\rightarrow$  implicit decrease of learning rate)
- *May* decrease to zero ( $\rightarrow$  k-means)



Gaussian  
(not normalized)



Mexican Hat  
(Difference of Gaussian)

# Self-Organization

- Global ordering from local interactions
  - Each neuron sees its neighbors
  - The whole network becomes ordered
- Understanding self-organization is part of ***complexity science***

# K-means

vs.

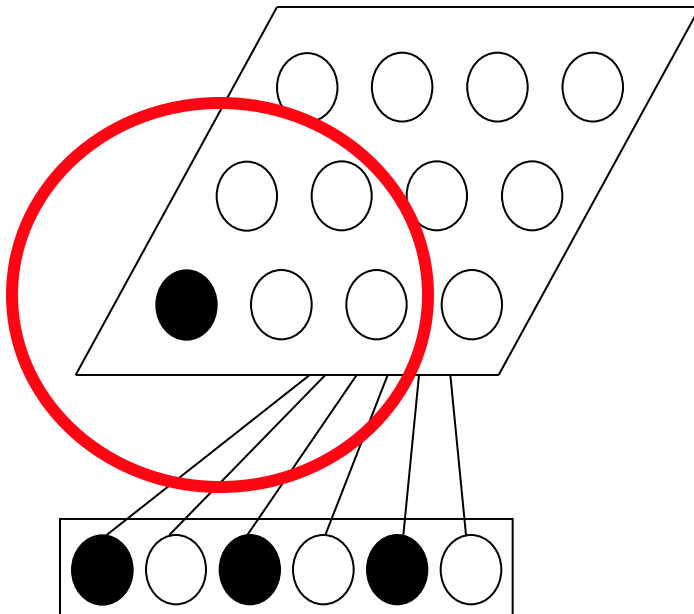
# SOM

- “Clusters”
- Clusters independent of each other
  - Clusters indices can be exchanged
- # clusters typically small
- Used for clustering

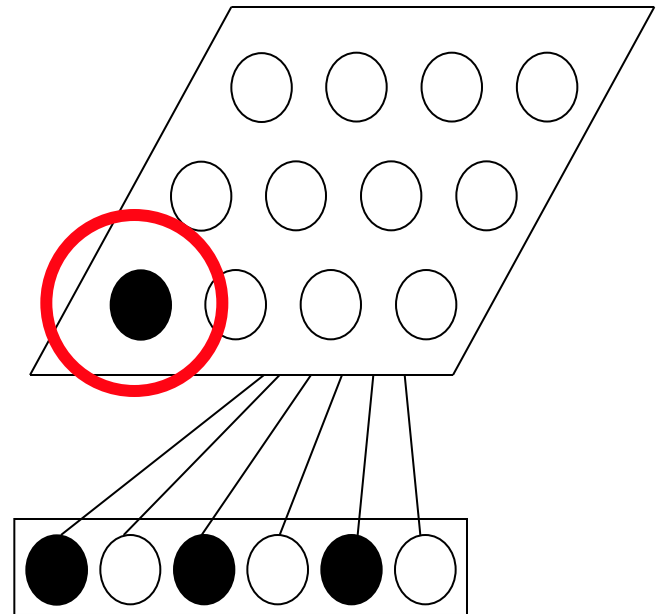
- “Neurons”
- Neurons co-excited by neighbourhood function
  - Neurons arranged on a map in 1D, 2D, ...
- # neurons typically large
- Used for mapping

# The Self-Organizing Map

Begin of training  
(large neighbourhood)

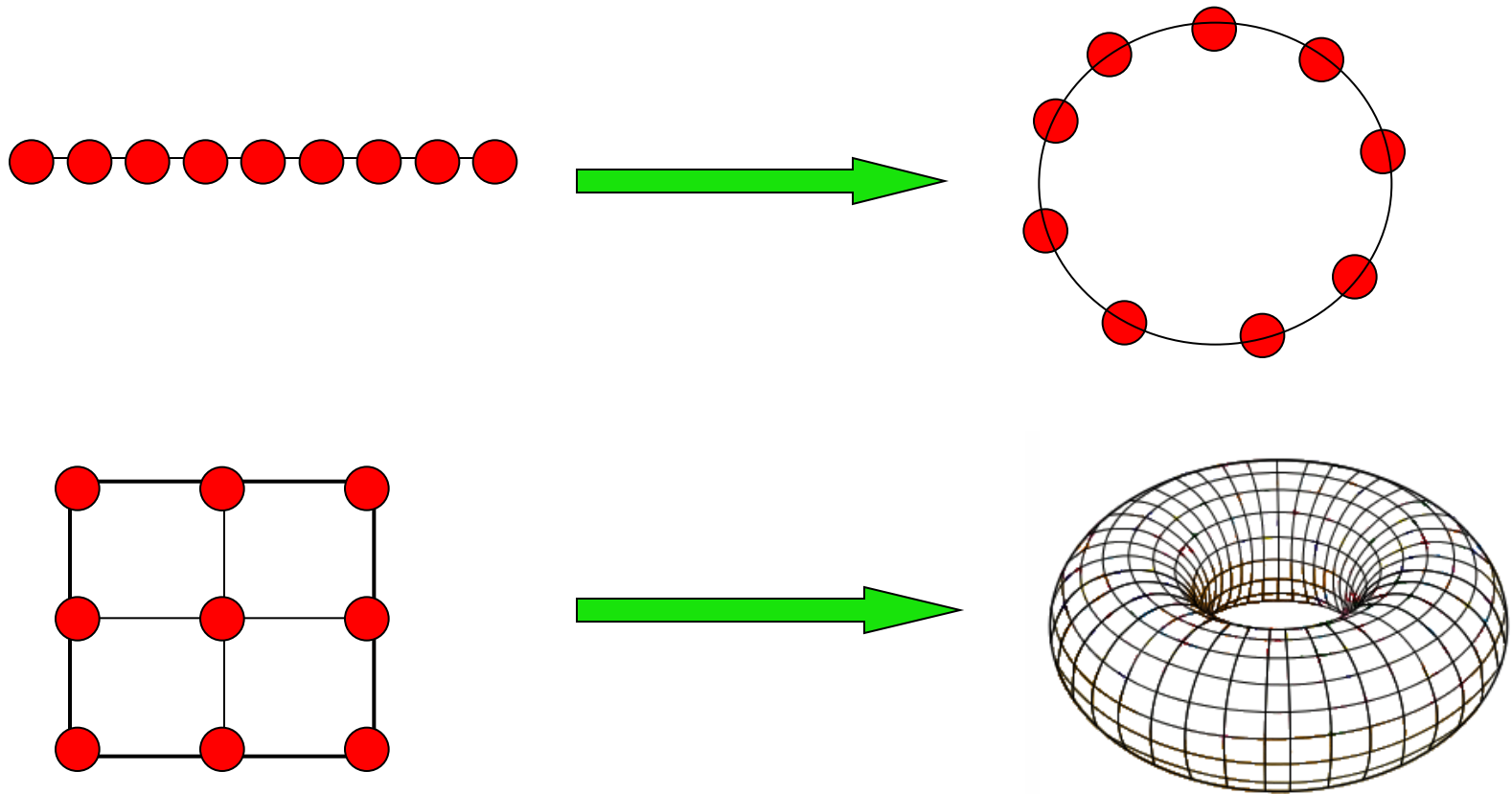


End of training  
(small neighbourhood)



If neighbourhood reduced to zero size:  $\rightarrow$  k-means

# Boundary Conditions: No Neurons at the End of the Map



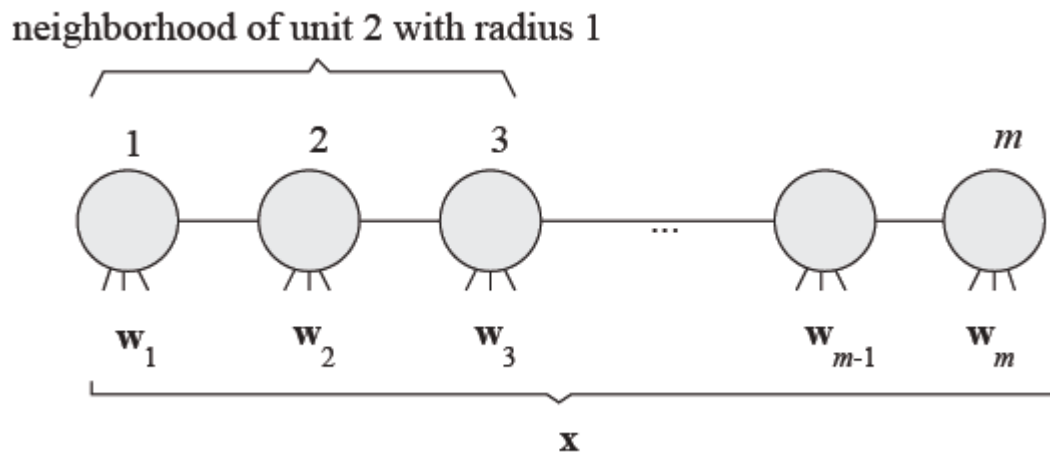


# Network Size

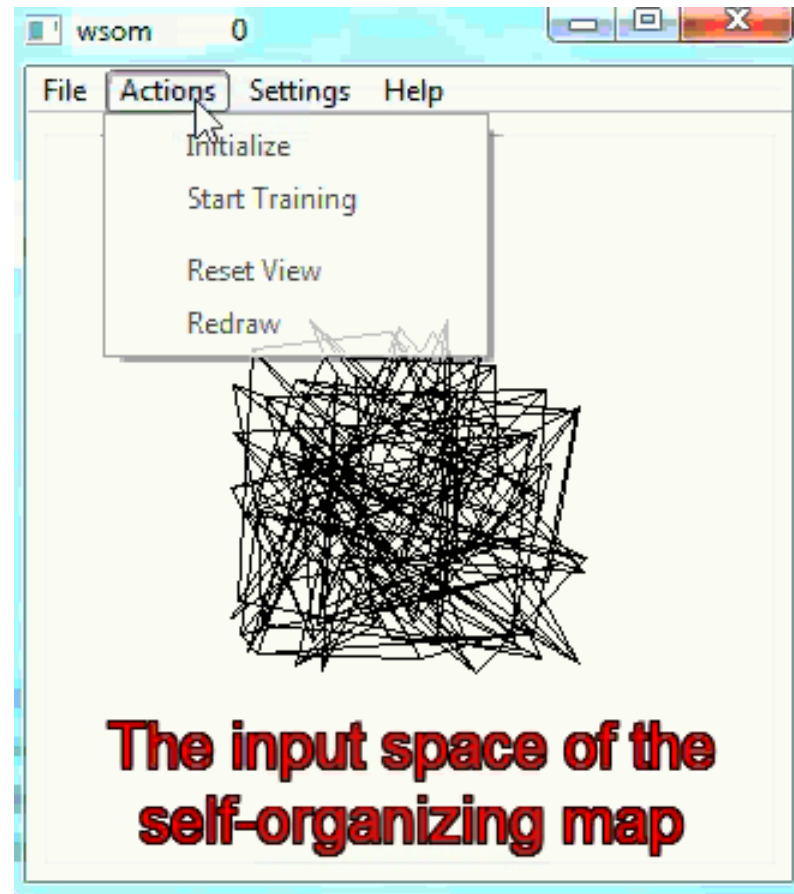
- We have to predetermine the network size
- Small network
  - Too much generalization  
→ no differentiation
- Large network
  - Each neuron can represent exact features  
→ little generalisation
  - Large neighbourhood interaction keeps network “small”, since the parameters are tied to each other  
→ this “regularization” allows SOMs to be kept large

# Examples: One-dimensional Lattice of Kohonen Elements

- Units are arranged in sequence
- Each unit learns to specialize for a different region in input space



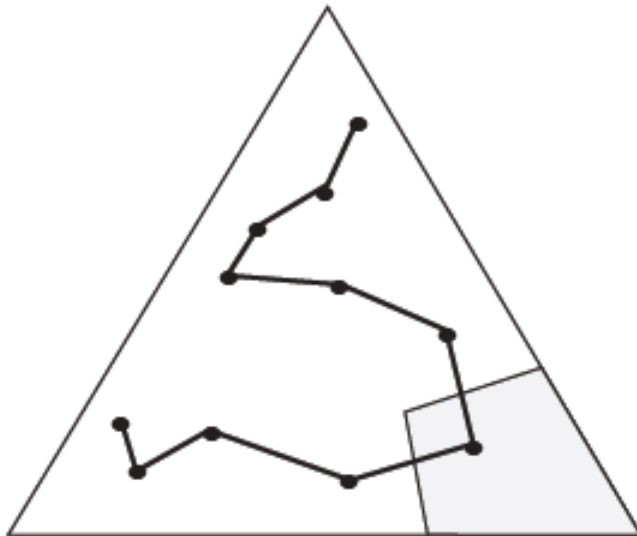
# SOM Demo – 2D lattice in 2D / 3D input space



[<http://www.borgelt.net/somd.html>]

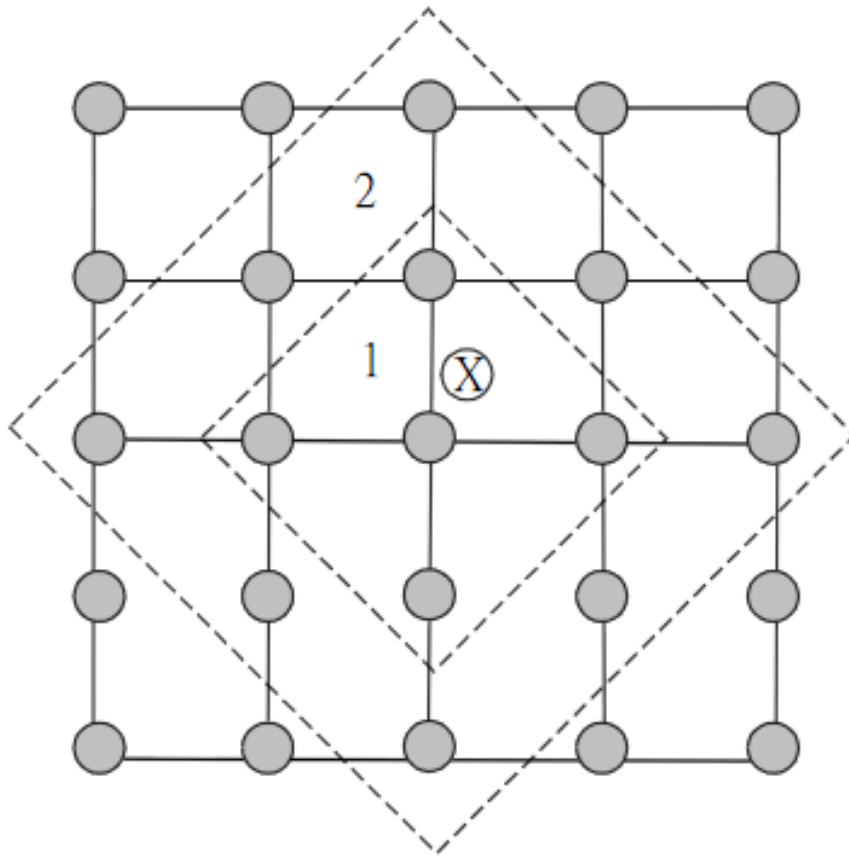
# 1D Lattice Mapping a 2D Triangular Region

- Triangular input domain is mapped to a small number of one-dimensional representative units



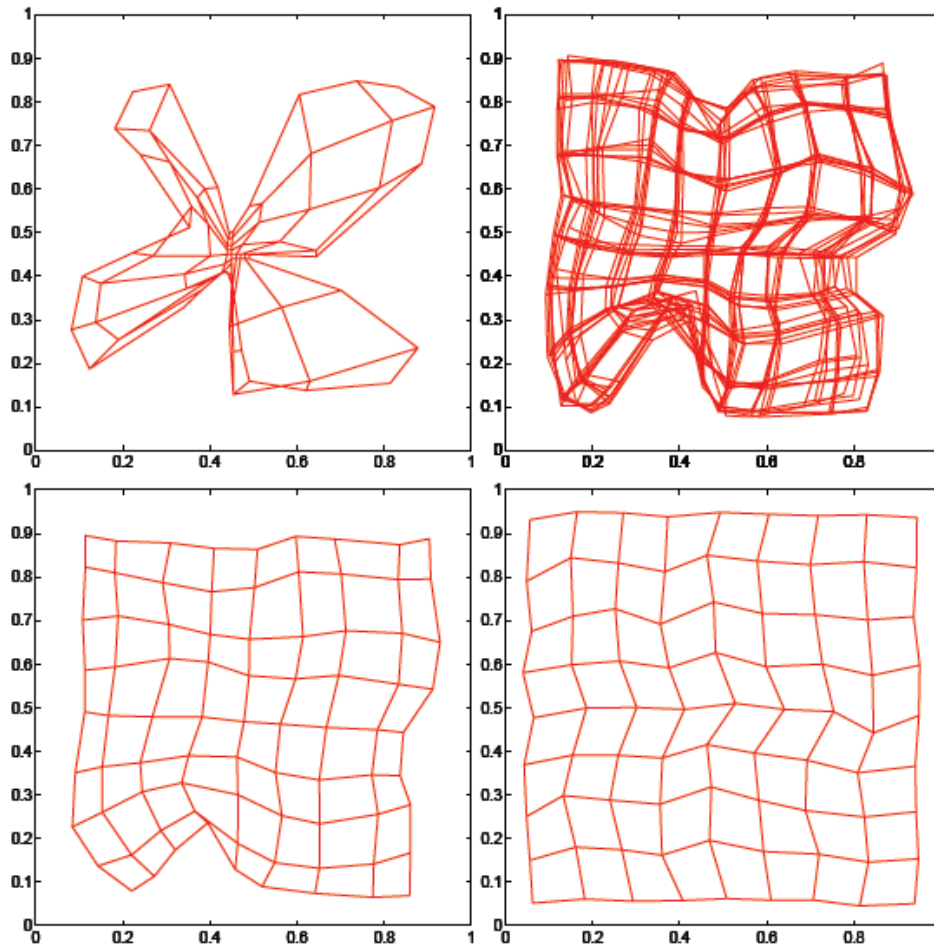
Unit with strongest  
excitation for shaded region

# Example of SOM Neighborhood



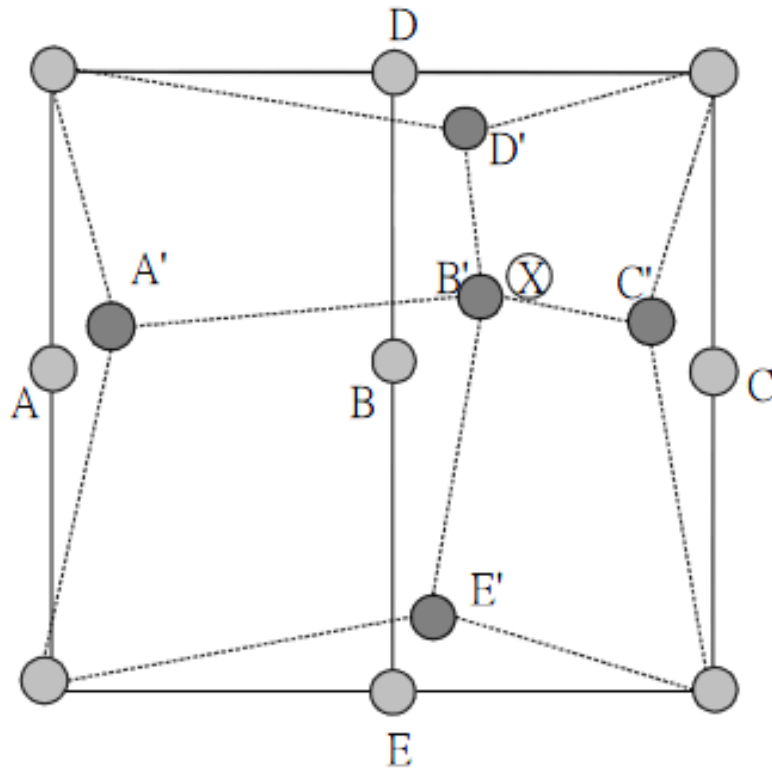
The input vector is represented as X. Units in neighbourhood 1 are more active than those in neighbourhood 2.

# Good Fit of dimensions: Mapping a Square with a 2-dimensional Lattice



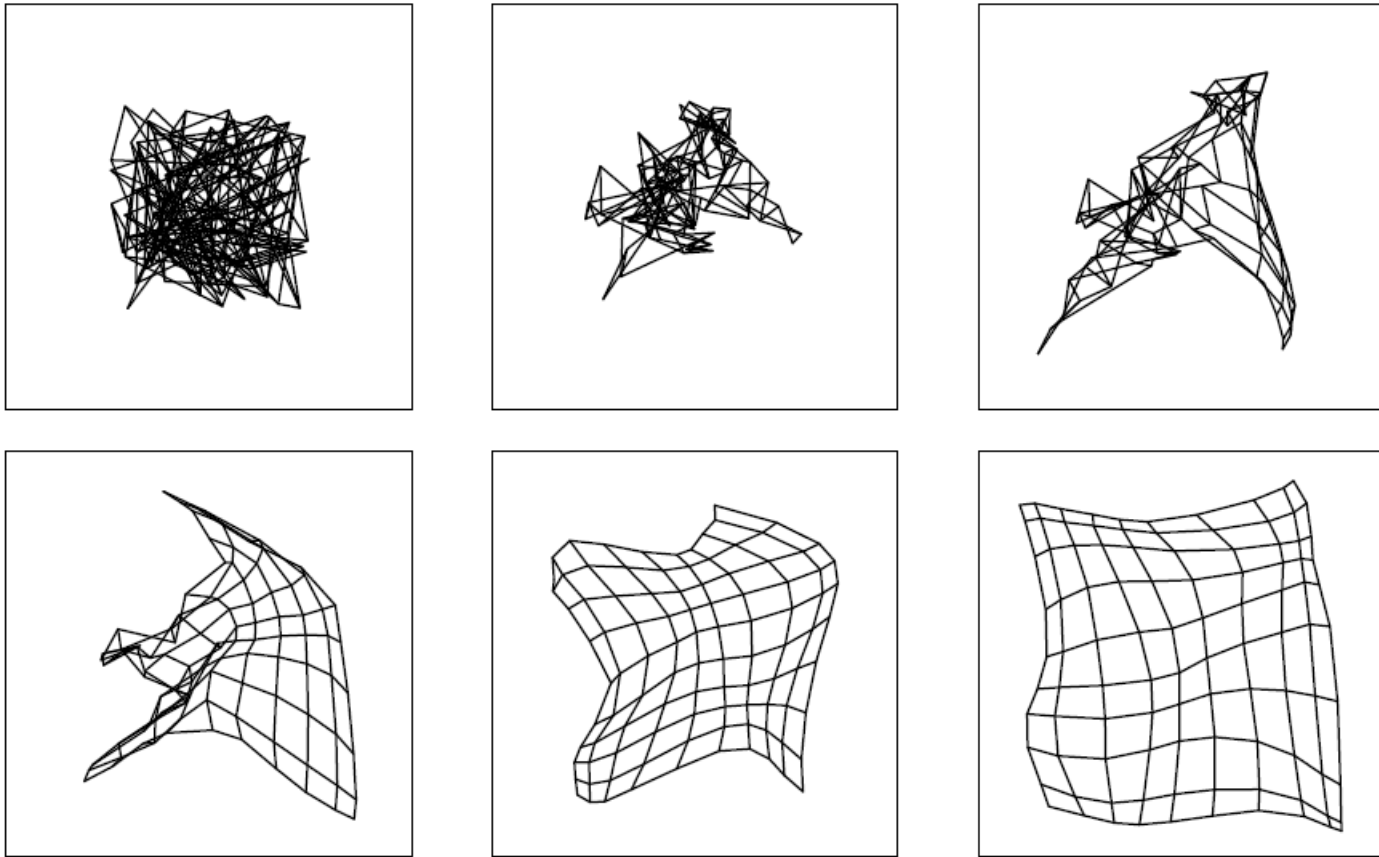
- Upper right with some overlapped learning iterations
- Results for 100, 1000, 5000, 10000 iterations (Kohonen 1984)

# Influence by Pre-Defined Topology



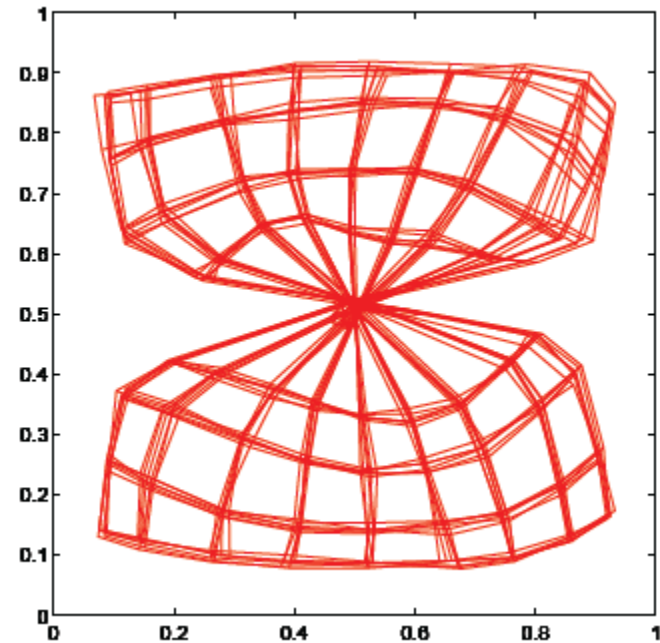
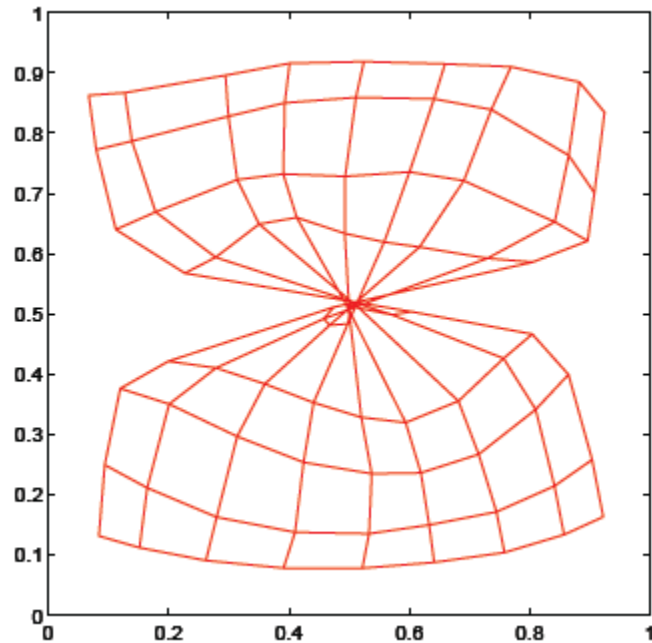
- The winner B and its neighbors such as A, C, D and E move towards the input vector X
- Modified units are shown as dark circles

# Unfolding of a 2-D Map in a 2-D Data Space



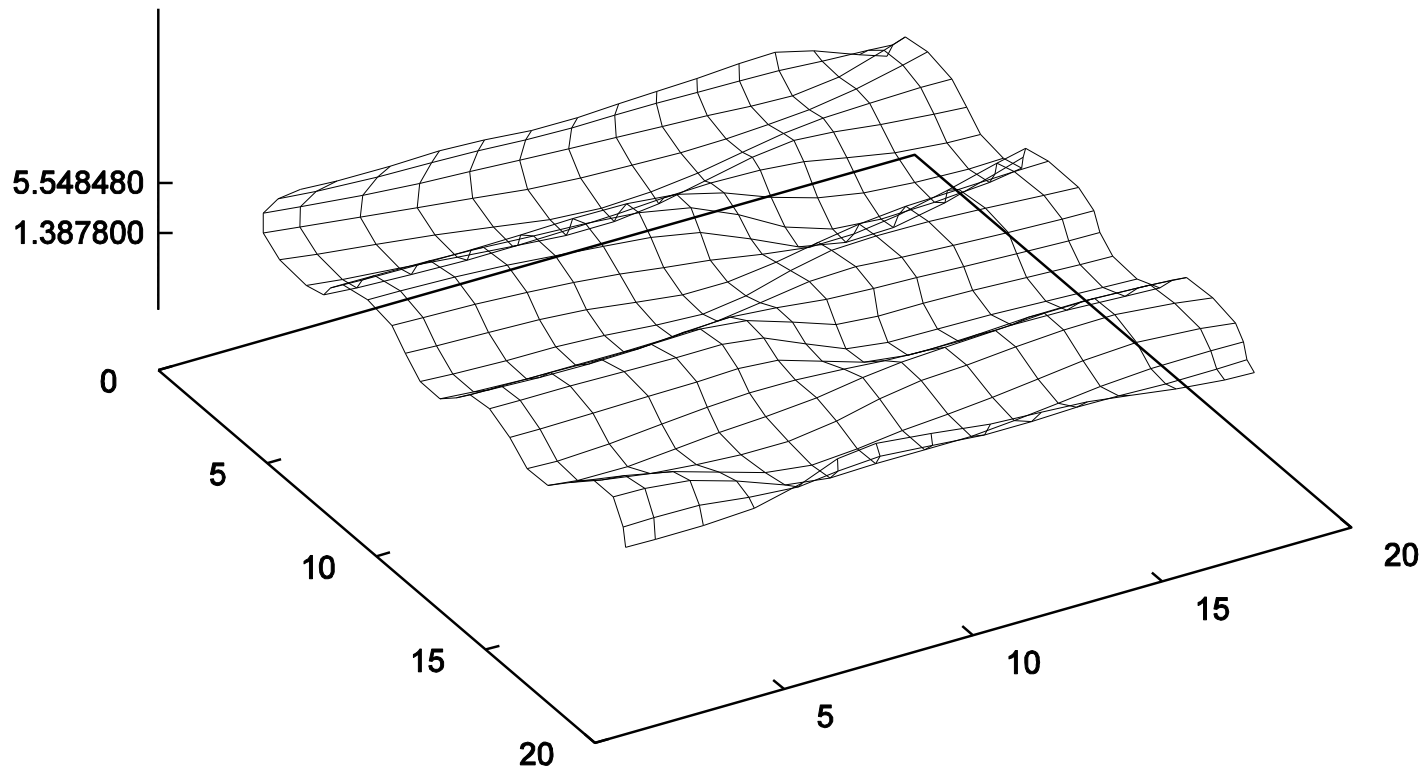


# Planar Network with a Knot



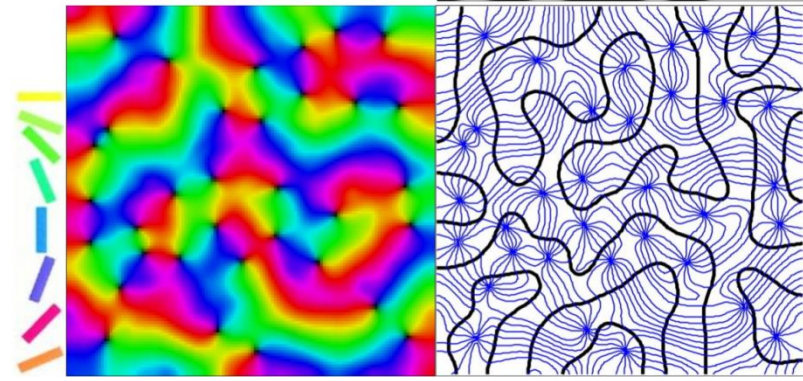
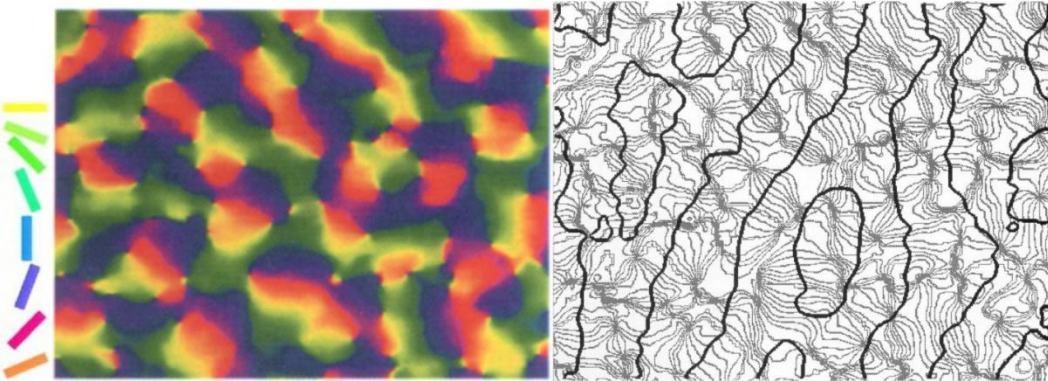
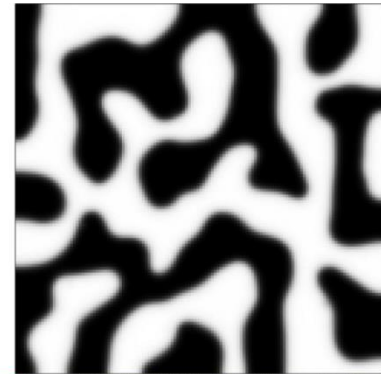
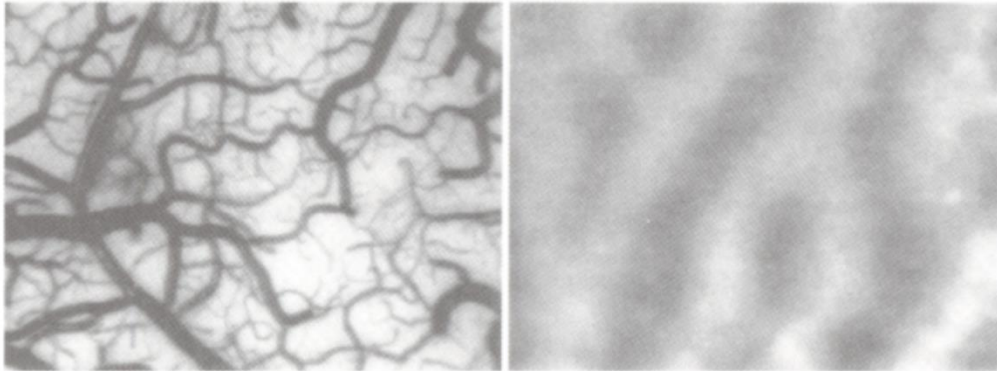
State difficult to correct

# Unfolding of a 2-D Map in a 3-D Data Space



# Example Application: V1 Maps

ocular dominance



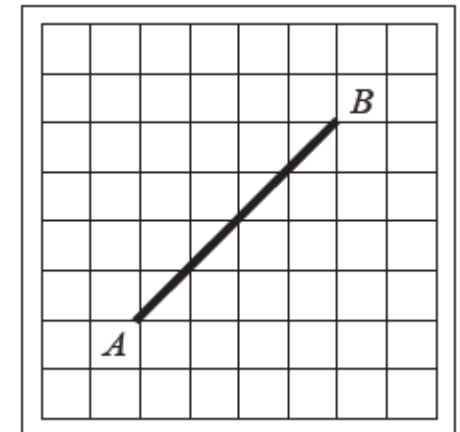
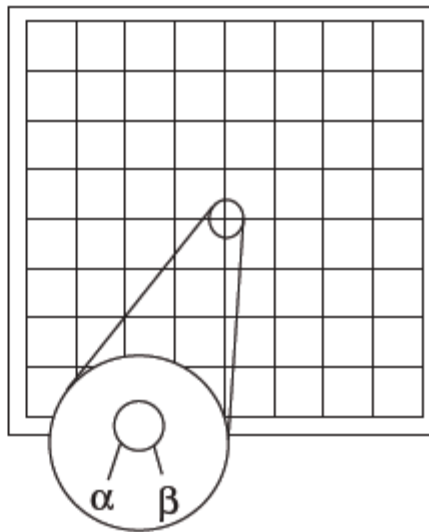
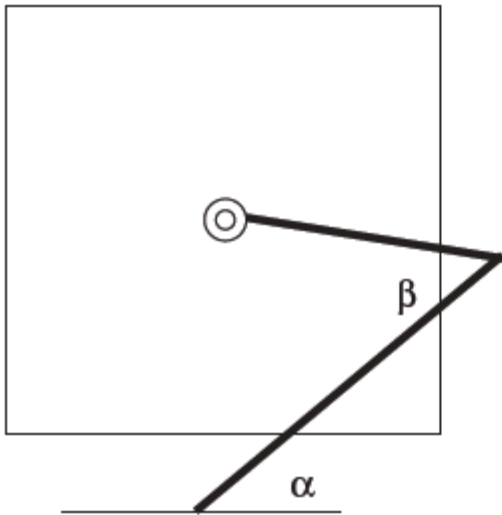
orientation preference

Obermayer, Blasdel. .. Orientation and Ocular Dominance Columns in Monkey .. Jneurosci, 1993

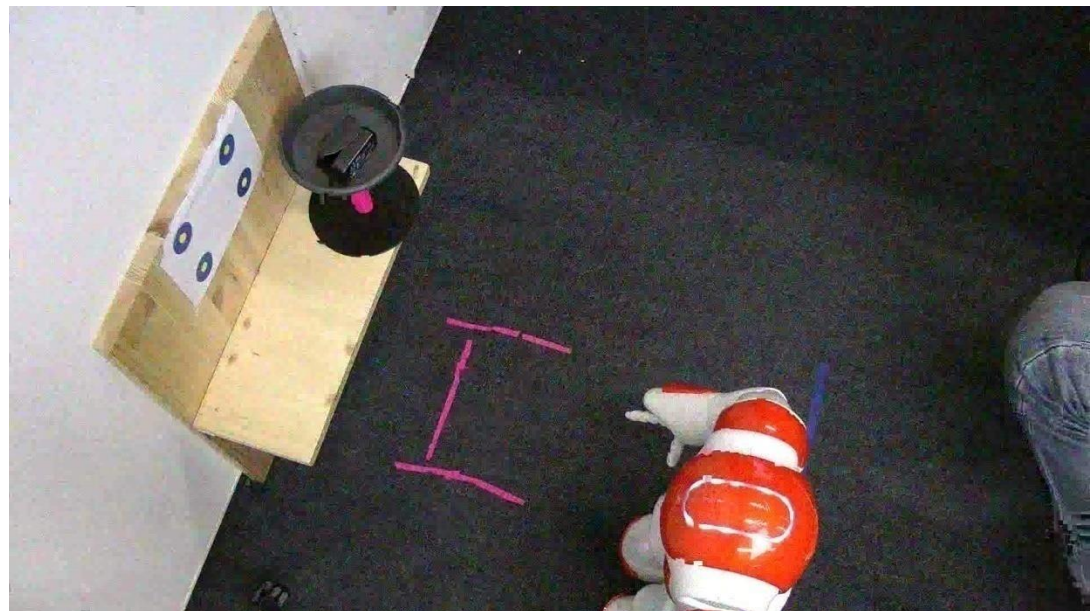
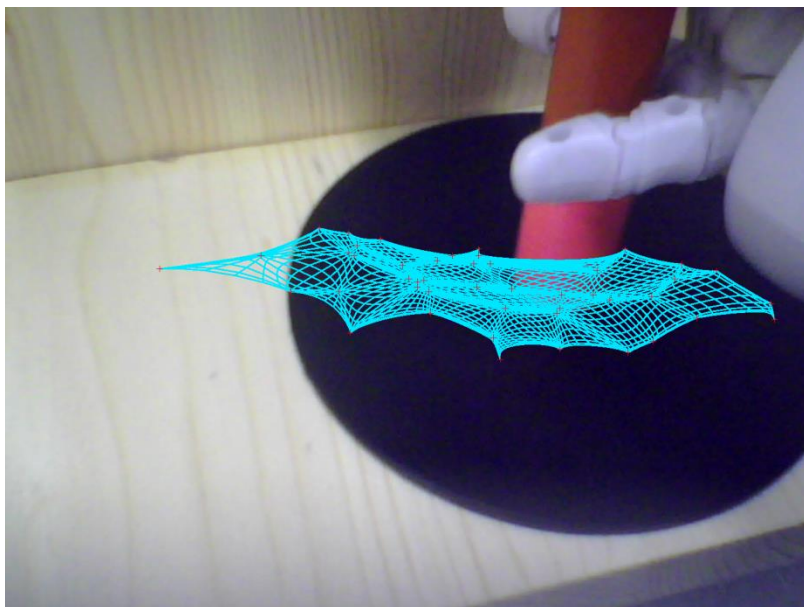
Goodhill . Theoretical Modelling to .. Neural Map Development. Neuron, 2007

# Learning Simple Inverse Kinematics

- Mapping the configuration space of a robot arm using 2-dimensional network
- For one point only one parameter combination; many paths from A to B



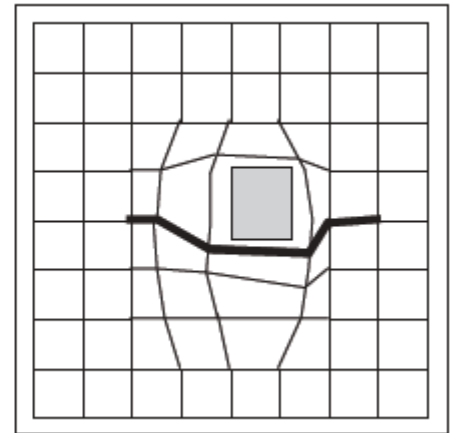
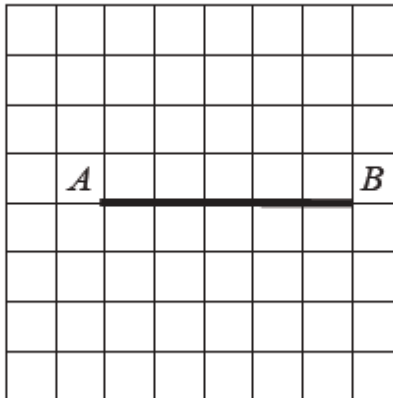
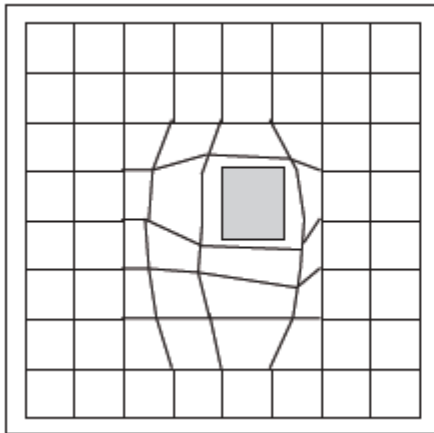
# Learning Simple Inverse Kinematics





# Learning Obstacles in Work Area

- Kohonen network charts configuration space avoiding the obstacles
- Moving the arm from A to B avoids the obstacle

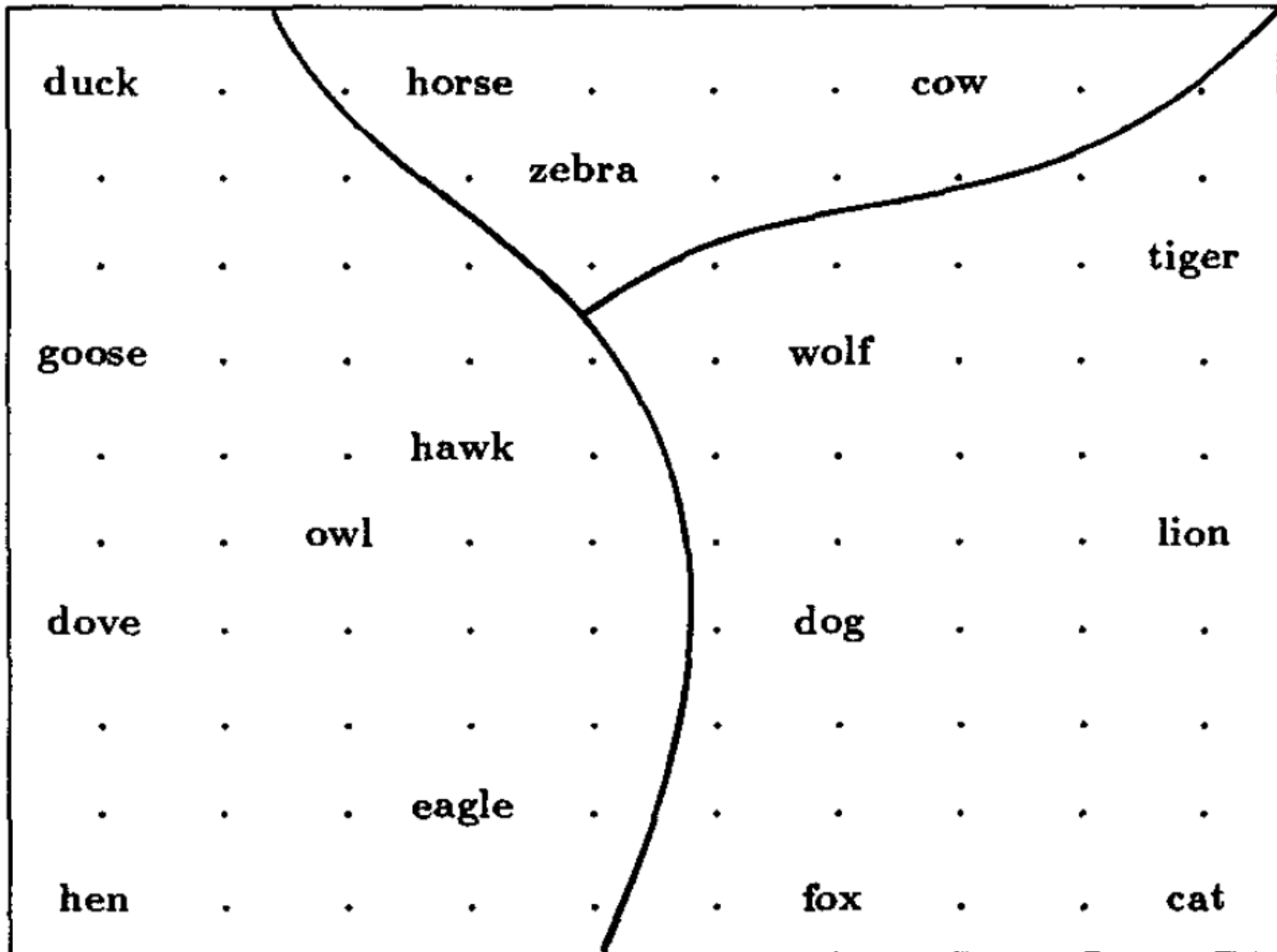


# Semantic Map – Input data

attributes of  
the inputs

[illegible]

# Semantic Map - Results





# Semantic Map - Results

duck	duck	horse	horse	zebra	zebra	cow	cow	cow	cow
duck	duck	horse	zebra	zebra	zebra	cow	cow	tiger	tiger
goose	goose	goose	zebra	zebra	zebra	wolf	wolf	tiger	tiger
goose	goose	hawk	hawk	hawk	wolf	wolf	wolf	tiger	tiger
goose	owl	hawk	hawk	hawk	wolf	wolf	wolf	lion	lion
dove	owl	owl	hawk	hawk	dog	dog	dog	lion	lion
dove	dove	owl	owl	owl	dog	dog	dog	dog	lion
dove	dove	eagle	eagle	eagle	dog	dog	dog	dog	cat
hen	hen	eagle	eagle	eagle	fox	fox	fox	cat	cat
hen	hen	eagle	eagle	eagle	fox	fox	fox	cat	cat

# Existing Neural Clustering models

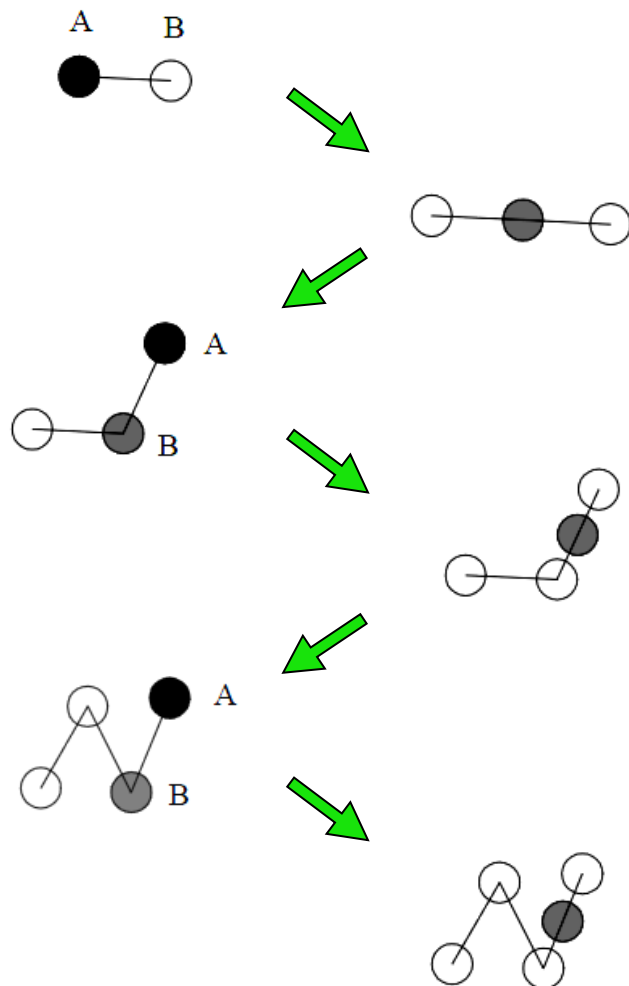
- **Static Models** (fixed number of units): Competitive Learning (CL), Self-Organizing Map (SOM), Neural Gas (NG), ....
  - *Hierarchical*: Multilayered Self-Organising Feature Maps (M-SOM), etc.

There are shortcomings for static models in a non-stationary environment.

- **Dynamic Models** (variable number of units): Growing Grid (GG), Growing Cell Structure (GCS), Growing Neural Gas (GNG), Grow When Required (GWR), etc.
  - *Hierarchical*: Growing Hierarchical Self-Organizing Map (GHSOM), etc.

# Growing Neural Gas – GNG

(Fritzke)

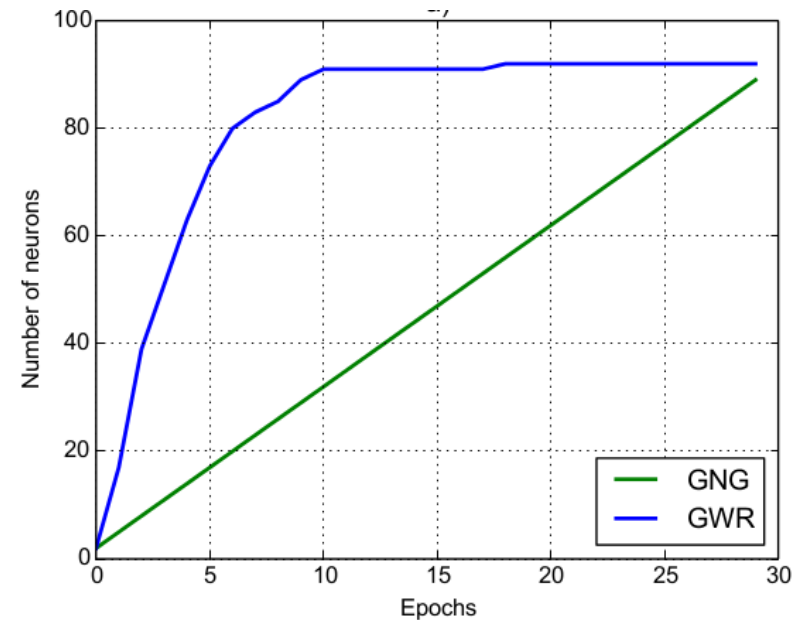


- GNG adds unit after every pre-defined period.
- Units are represented as circles.
- Circle A indicates *unit with biggest error*
- Circle B indicates *neighbor with biggest error* for Circle A.
- The grey circle is the *new unit* at each stage.

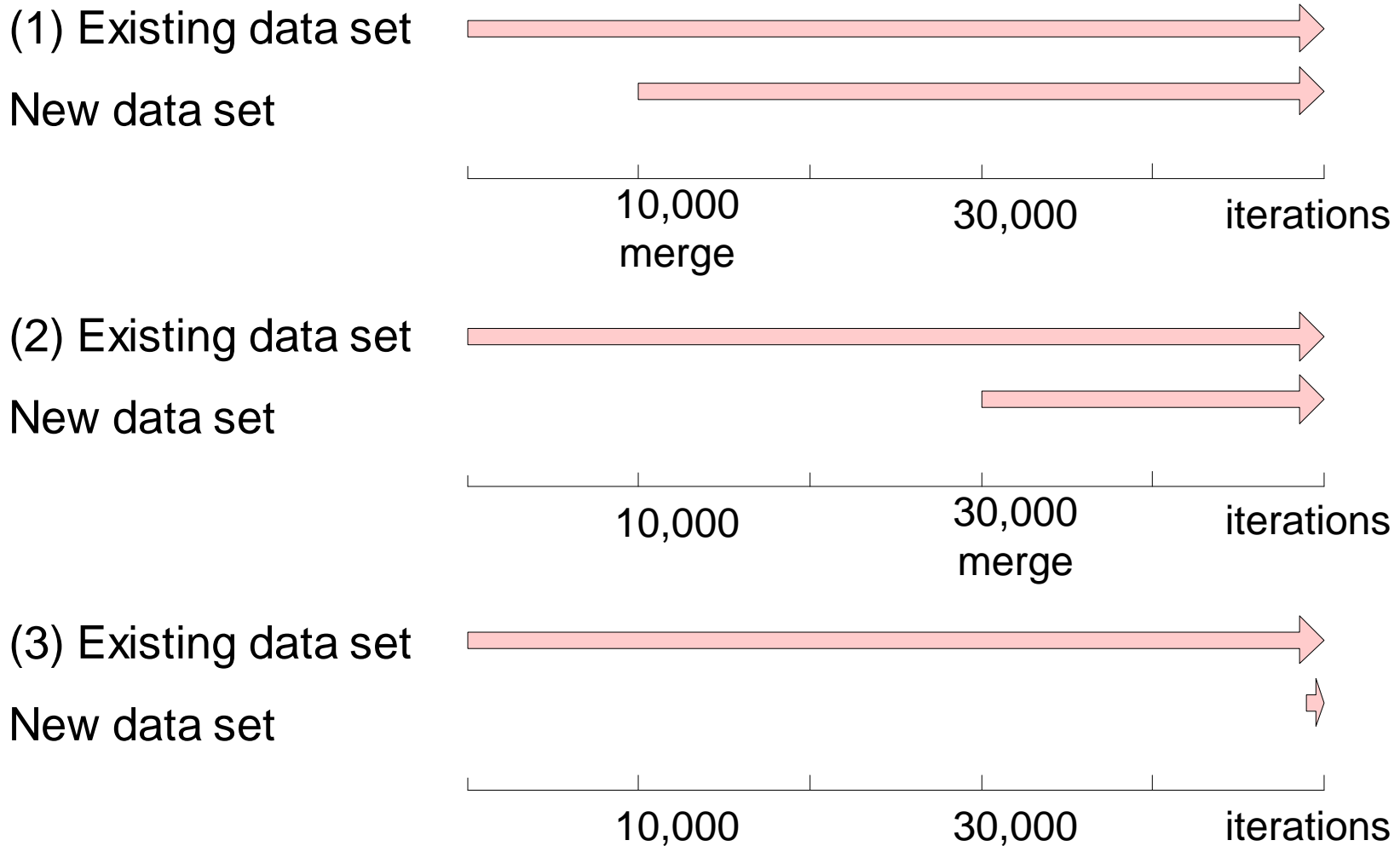
# Growing When Required – GWR

(Marsland et al., 2002)

- **GNG**: network grows with *time*
- **GWR**: network grows *when required*  
→ strong neurogenesis at early stages
- Each neuron has a *firing counter* (how often is it the winner)
  - Many counts → lower learning rate to help convergence
  - Few counts → novelty detected
- Each edge has an *age* (refreshed when linking winner and 2<sup>nd</sup> winner)
  - Old edge → cut it (and remove units when isolated)



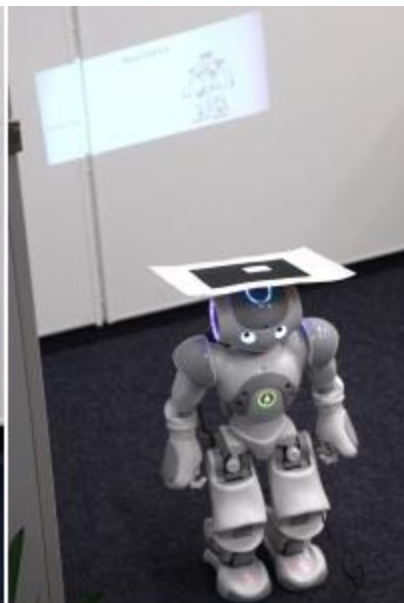
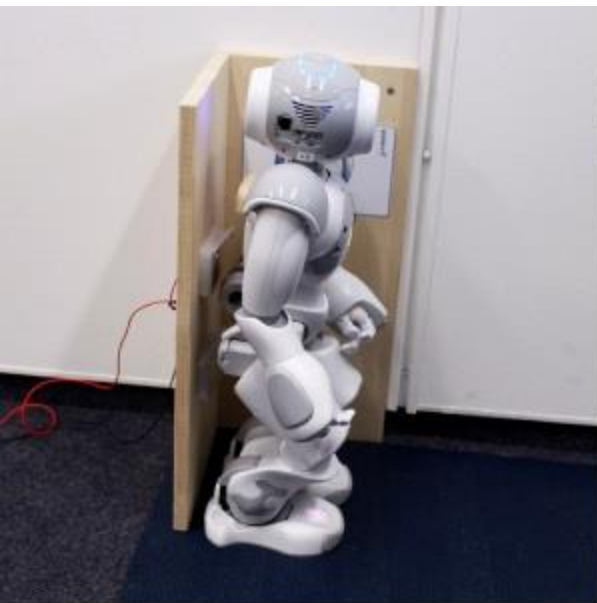
# Dynamical SOM for Dynamical Knowledge Acquisition Over Time



# Shortcomings of Static Models in a Non-stationary Environment

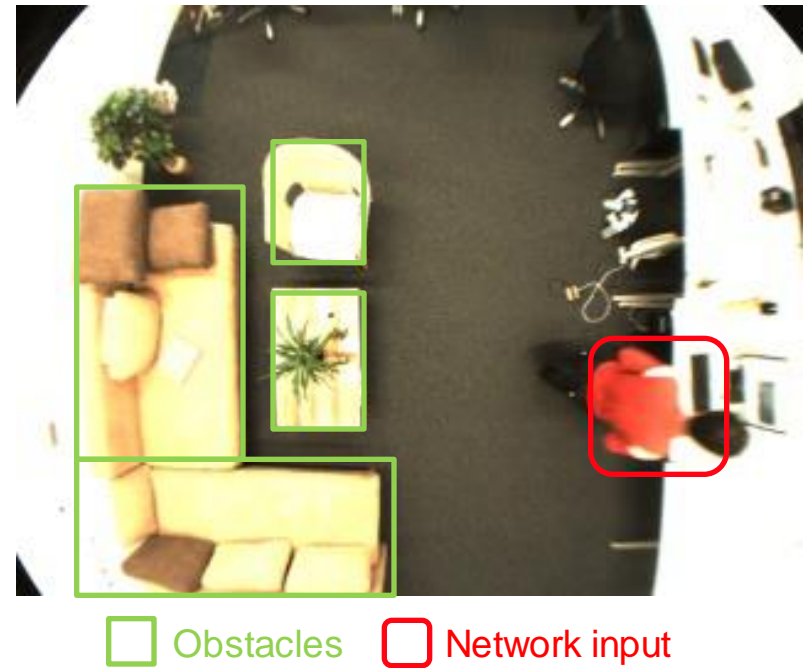
- Pre-defined number of units
- Pre-defined topology (mostly a grid)
- Pre-defined training length
- A decaying learning rate (e.g. SOM, CL, NG, GG, GSOM, Snet-SOM, M-SOM, GHSOM)

# Room Mapping via GNG (KT Lab)



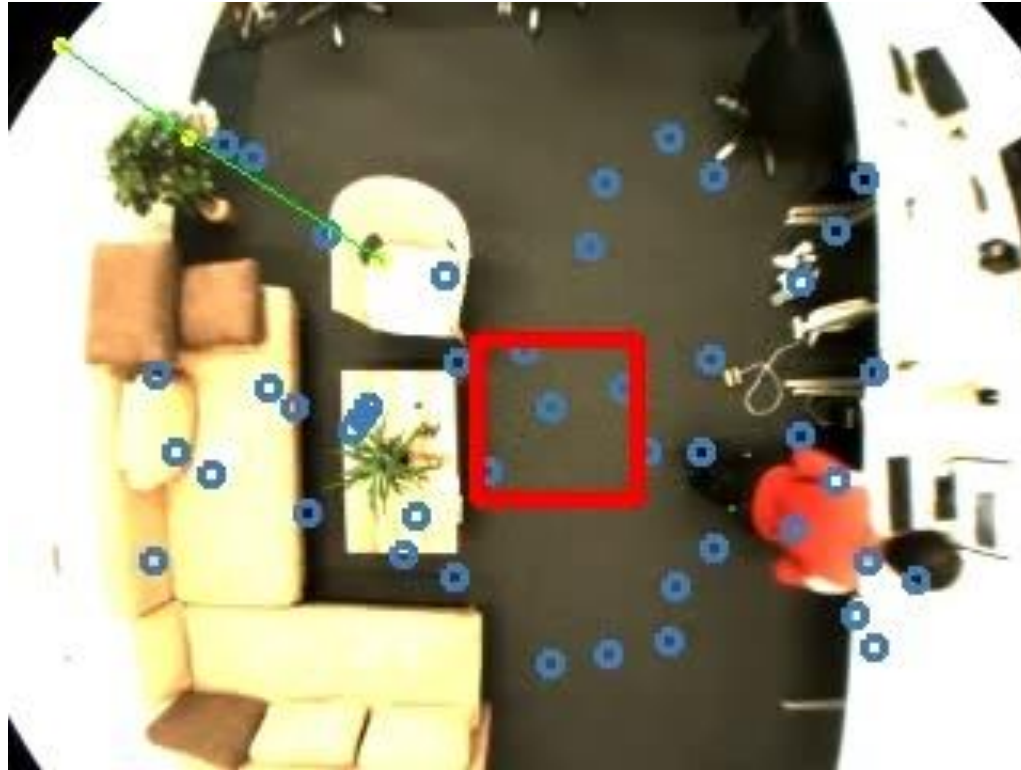
# Room Mapping via GNG (KT Lab)

- Map the topological structure of a room using growing neural gas for robot navigation
- Since the person's movement can show the free space in the room, we use the detected position of a person as the network input





# Room Mapping via GNG (KT Lab)



- Blue dots are particles for person detection
- Red bounding box shows the estimated position of the target person
- Yellow dots are the neurons of the growing neural gas and the green lines are the connections

# Summary

- **Cluster analysis** groups objects based on their **similarity** and has wide applications
- Measure of similarity can be computed for **various types of data**
- Clustering algorithms can be **categorized** into partitioning methods, hierarchical methods, density-based methods, grid-based methods, and model-based methods
- **Outlier detection** and analysis are very useful for fraud detection, etc. and can be performed by statistical, distance-based or deviation-based approaches
- There are still lots of research issues on cluster analysis