

## Problem Set 4: Q: 4.1

- a) 1) Yes. The sum operation will space strings out by length.
  - 2) Yes. The sum operation will space strings out by contained characters.
  - 3) No as words' reordering in a string does not produce a different hash function.
  - 4) No, because it violates the independence condition of the simple uniform hashing assumption.
- b) Statement 4 is correct. The dynamic resizing and collision are both necessary for hash table. Without collision resolution, it could produce an actual hash function; however, no amount of resizing will be let into

the hash table. Without dynamic resizing, the load factor will get large, turning everything into a linear-time look up.

c)  $O(m' + n)$ .

- Take  $O(m')$  time to create a new hash table
- $\Theta(m + n)$  time to go through each slot in the old table and copy each item

→ Take  $\Theta(m' + m + n)$  } → Take  $\Theta(m' + n)$

We have  $m < m'$

d)

4.2) a) Statement 1 is correct

b) Because highly sparse hash table

is beneficial for unit test  $\rightarrow$  growth factor = 4

Also, lots of things will be inserted front

$\rightarrow$  Larger minimum size is better

$\rightarrow$  I choose statement 4.