An Introduction to Mathematics in LaTeX 2ε

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1 Writing Text

There are two "modes" in \LaTeX 2_{ε} , text-mode and math-mode. When you write a mathematics document in \LaTeX 2_{ε} , you mix these modes. By default, you are in text-mode.

Generally, writing text in \LaTeX Z_{ε} feels like writing in any basic text editor. There is a lot going on "behind the scenes" though. Because \LaTeX Z_{ε} is designed to do professional typesetting, it makes your document look professional in ways that you may never have cared to think about. One of the many examples is in \LaTeX automatic display of ligatures:

fire flower instead of fire flower

and optional display of the forgotten "long s", should you ever have the necessity to use it.

1.1 Special Text Characters in LATEX

The following characters will not appear as expected in \LaTeX 2ε as they do special things. If you wish for these characters to appear as themselves in your document, you must place a backslash before them (all \LaTeX 2ε commands start with a backslash), with the exception of the \ symbol itself which is written as \backslash\$.

Character	$ ext{ETEX } 2_{arepsilon} ext{ Meaning}$	How to Write
#	macro parameter symbol	\#
\$	starts/ends inline math-mode	\\$
%	comment character	\%
\sim	non-breaking space character	∞
\	command character	\$\backslash\$
-	math subscript character	\$_\$
{	begin argument delimiter	\$\{\$
}	end argument delimiter	\$\}\$

Other characters (mainly those not appearing on your keyboard) will have special commands that display them in LATEX. Much of the time learning LATEX is spent learning these commands. A good reference (or an editor with a nice collection of selectable characters) is always nice to have.

1.2 Font Faces

The following types of fonts are available in text-mode.

Command	Font	Example	Result
	Plain Text (for inside math mode)	<pre>\text{Example 1}</pre>	Example 1
	Sans Serif Font	<pre>\textsf{Example 2}</pre>	Example 2
	Typewriter Font	<pre>\texttt{Example 3}</pre>	Example 3
	Bold Face Font	<pre>\textbf{Example 4}</pre>	Example 4
	Italic Font	<pre>\textit{Example 5}</pre>	Example 5
	Small Caps Font	\textsc{Example 6}	Example 6

1.3 Font Sizes

You want to declare font sizes within an environment or IATEX will try to declare them globally since there is no terminating comand for a font size. Putting curly brackets around the text you want to size, or using font size declarations within other commands are ways of accomplishing this.

Command	Example	Result
\tiny	{\tiny Example 1}	Example 1
\scriptsize	{\scriptsize Example 2}	Example 2
\footnotesize	{\footnotesize Example 3}	Example 3
\small	{\small Example 4}	Example 4
\normalsize	{\normalsize Example 5}	Example 5
\large	{\large Example 6}	Example 6
\Large	{\Large Example 7}	Example 7
\huge	{\huge Example 8}	Example 8
\Huge	{\Huge Example 9}	Example 9

1.4 Horizontal Spacing

Forced spacing can be tricky in \LaTeX $2_{\mathcal{E}}$. Simply inserting spaces in your code where you want spaces to appear in the finished document won't generally work. Instead, there are commands to insert space. Horizontal space commands can be used in both text and math environments.

Command	Example	Result
	Used to insert four spaces	Used to insert four spaces
\qquad	Eight\qquad spaces	Eight spaces
\sim	These~spaces~won't~break~into a~new~line	These spaces won't break into a new line
١,	Half a space. E.g., Hold breath for 10s.	Hold breath for 10 s.
	<pre>Insert\hspace{0.5in}half an inch</pre>	Insert half an inch
\hfill	<pre>Insert as much\hfill space as possible</pre>	Insert as much space as possible

Some notes:

• Writing \setlength\parindent{0pt} in the header of your document will stop \LaTeX from indenting. When you want to indent in this situation, use a \quad at the beginning of your paragraph.

1.5 Vertical Spacing

Vertical spacing in \LaTeX 2 ε can also take some practice. Here are some guidelines.

• Writing a \\ results in a line break. For example: "This is a \\ line break" produces

This is a line break

• Writing \newline forces a new line. For example: "This is a \newline new line" produces

This is a new line

The difference between \newline and \\ is that \newline will attempt to justify text when possible, since it creates a new paragraph while \\ does not.

- Start a new paragraph by skipping a line in your L^ATEX document. Skipping more than one line will have no added effect.
- You may force vertical space with the \smallbreak, \medbreak, \bigbreak commands. Many LATEX authors will both skip a line and insert a \bigbreak at the beginning of a new paragraph.

• You may force a certain amount of vertical space with the \vspace{} command. In text mode, this command must have a line break before it (cannot be written inline). To skip a large amount of space, write something like \vspace{5in} or \vspace{10pc}

1.6 List Environments

The first example of a list environment is a bulletted list. Such a list starts with the command \begin{itemize} and ends with \end{itemize}, with each bullet created by the command \item.

```
\begin{itemize}
  \item Here is a bullet.
  \item And another bullet.
  \begin{itemize}
    \item Some subbullet.
    \item And another.
  \end{itemize}
  \item And a final bullet.
\end{itemize}
```

• Here is a bullet.

• And another bullet.

- Some subbullet.

- And another.

• And a final bullet.

Another popular kind of list is an enumeration.

```
\begin{enumerate}
   \item Here is the first thing.
   \item Here is the second thing.
   \begin{enumerate}
     \item First subthing.
     \item Second subthing.
   \end{enumerate}
   \item Third thing.
\end{enumerate}
```

- 1. Here is the first thing.
- 2. Here is the second thing.
 - (a) First subthing.
 - (b) Second subthing.
- 3. Third thing.
- 1. Here is the first thing.
- 2. Here is the second thing.
 - (a) First subthing.
 - (b) Second subthing.
- 3. Third thing.

If you wish to change the numbering, or have it display in a specific way, you can use the following sort of option when declaring an item:

```
\item[\textbf{13:}]
```

Notice the difference.

```
\begin{enumerate}
  \item[\textbf{1.}] Here is the first thing.
  \item[\textbf{2.}] Here is the second thing.
  \begin{enumerate}
    \item[\textbf{2a.}] First subthing.
    \item[\textbf{2b.}] Second subthing.
  \end{enumerate}
  \item[\textbf{3.}] Third thing.
\end{enumerate}
```

- 1. Here is the first thing.
- 2. Here is the second thing.
 - **2a.** First subthing.
 - **2b.** Second subthing.
- **3.** Third thing.

1.7 Tabular Environments

Tables can also take some practice in LATEX. If you want something other than the basic table, look online as there are entire pages that are devoted to table structures in LATEX. But keep this in mind: Tabular environments are for text and arrays are for math.

```
\begin{center}
    \begin{tabular}{|r|c|1|}
                                                                  Col 1
                                                                           Col 2
                                                                                   Col 3
    \hline
    \hline
                                                                                   r1c3
                                                                    r1c1
                                                                            r1c2
    \textbf{Col 1} & \textbf{Col 2} & \textbf{Col 3}\\
                                                                    r2c1
                                                                            r2c2
                                                                                   r2c3
    \hline
   r1c1 & r1c2 & r1c3 \\
   r2c1 & r2c2 & r2c3 \\
    \hline
    \end{tabular}
\end{center}
```

One of the main things to notice in the tabular environment is the $\{|r|c|l|\}$ option. This tells LATEX to use three table columns, with text aligned right, center and left respectively. The | just says to draw a vertical line. The command \\ (which is usually a new line command) tells LATEX that the current row is finished, where rows are separated by the & symbol.

2 Math Mode

There are two modes in which $\LaTeX 2_{\varepsilon}$ will write mathematics.

2.1 Generic Notes on Math Modes

- To make subscripts, use $_$. For instance, x_α produces x_α .
- To make superscripts, use \hat{x} . For instance, x^{β} .
- You can use the two together: x_α or x^β or x^β .
- If you want to include more than one "thing" as a sub/superscript use curly brackets:

$$\mathcal{A}_{\alpha+\beta}$$

2.2 Inline Math Mode

Inline Math Mode enables you to write math inline so things like $f(x) = x^2 + 2x - 8$ appear within the regular flow of text.

To write inline math, put a \$ on either side of your math. For example, writing $h(x)=e^x$ produces the inline math text $h(x)=e^x$.

- Many mathematical notations will display in a compact version when written in inline mode. For instance, writing $\int_0^1 \sin x \, dx$. You may attempt to get around this in certain cases by using $\int_0^1 \sin x \, dx$. In this case, writing that displays the following: $\int_0^1 \sin x \, dx$.
- You may use text within math mode with the \text{} command.

2.3 Block Math Modes

There are several options here. If you just want to include math in a block (centered on the page, not compact like inline math mode) then the most common option is to write something like the following.

This produces:

$$\int_0^1 \sin x \, dx$$

2.3.1 Equations

Notice the difference between

which produces

$$\cos(x) = \cos(-x),\tag{1}$$

and

```
\begin{equation*}
\cos(x)=\cos(-x),
\end{equation*}
```

which produces

$$\cos(x) = \cos(-x).$$

The difference is that LATEX automatically numbers equations in the equation environment, while it doesn't number those in the equation* environment.

2.3.2 Aligns

Some LATEX authors will recommend the equarray environment here. Use of that environment is not recommended (it was removed from the LATEX standard many years ago) as it displays different in various compilers and there is no protection for spacing (equation numbers may be overrun). If you submit your code to a journal, for instance, using the equarray environment, there is no sure bet that their compiled result will appear as the result on your personal computer.

An example of the align environment is as follows:

This produces the output:

$$\sum_{k=1}^{5} (k^2 + 2) = (1^2 + 2) + (2^2 + 2) + (3^2 + 2) + (4^2 + 2) + (5^2 + 2)$$

$$= 3 + 6 + 11 + 18 + 27$$

$$= 65$$

We can make multiple equation aligns per row as follows:

$$a_{11} = b_{11}$$
 $a_{12} = b_{12}$ $a_{21} = b_{21}$ $a_{22} = b_{22} + c_{22}$.

2.3.3 Misc. Block Math Environments

Here, the left will correspond to what we write in LATEX and the right will be the corresponding displayed result.

2.4 More, Largely Random Examples

Again, the input is on the left. The output is on the right, except where this would create spacing problems, in which cases the input is displayed above the output.

Fractions

\frac{2}{3}
$$\frac{2}{3}$$

We can force $\LaTeX 2_{\varepsilon}$ to not compress fractions. (The numerator and denominator of a fraction are displayed with inline math-mode.) Use tfrac in text mode and dfrac in math modes. (You may also use the command displaystyle as in text mode, use it in the numerator and in the denominator.)

This outputs:

$$\Re z = \frac{n\pi \frac{\theta + \psi}{2}}{\left(\frac{\theta + \psi}{2}\right)^2 + \left(\frac{1}{2}\log\left|\frac{B}{A}\right|\right)^2}.$$

Binomial Expressions

IATEX 2ε uses the \binom command. See the following examples.

$$\binom{n}{r}$$

$$\binom{n}{r}$$

$$2^k-\frac{k}{1}2^{k-1}+\frac{k}{2}2^{k-2}$$

$$2^k-\binom{k}{1}2^{k-1}+\binom{k}{2}2^{k-2}$$

Continued Fractions

$$\frac{1}{\sqrt{2} + \frac{1}{\sqrt{2} + \frac{1}{\sqrt{2} + \cdots}}}$$

Limits and Such

There are several ways to do this.

\lim_{x\rightarrow+\infty}f(x)=\infty

$$\lim_{x \to +\infty} f(x) = \infty$$

 $\lim_{x \to \infty} x + \inf_{x \to s} \text{ and } \sup_{x \to s}$

$$\lim_{x \to +\infty}, \inf_{x > s} \text{ and } \sup_{K}$$

Sums

$$\sum_{k=1}^n k^2 = \frac{1}{2} n (n+1).$$

$$\sum_{k=1}^{n} k^2 = \frac{1}{2}n(n+1).$$

Integrals

$$\int_0^4 x^2 + 2x - \frac{1}{2}x \, dx$$

Here is a more complicated example. The limits are moved under the integral instead of beside it.

$$\label{eq:limits_{x^2 + y^2 \leq R^2} f(x,y),dx,dy} = \inf_{\text{theta=0}^{2\neq i} \int_{r=0}^R f(r\cos\theta,r\sin\theta) r,dr,d\theta}$$

$$\int\limits_{x^2+y^2\leq R^2} f(x,y)\,dx\,dy = \int_{\theta=0}^{2\pi} \int_{r=0}^R f(r\cos\theta,r\sin\theta)r\,dr\,d\theta$$

Matrices

$$\left(\begin{array}{ccc}
a & b & c \\
d & e & f \\
g & h & i
\end{array}\right)$$

Certain Characters

Don't ever use the keyboard keys < or > when you mean to use one of the following

\langle A \rangle
$$\langle A \rangle$$

3 Document Headers

The document header for this file looks like the following:

```
\documentclass[letterpaper,twoside,10pt]{article}
\usepackage{amsfonts,amsmath,amssymb,amsthm,multicol,color}

\usepackage[hmargin=2.5cm,vmargin=2.5cm]{geometry}

\setlength\parindent{0pt}

\newtheorem{thm}{Theorem}[section]
\newtheorem{cor}[thm]{Corollary}
\newtheorem{lem}[thm]{Lemma}

\author{\textsc{Jason B. Hill}\\\textsc{\small University of Colorado -- Boulder}}
\title{\textsc{An Introduction to Mathematics in {\LaTeXe}}}
\date{\textsc{\today}}
```

3.1 Document Classes

The first line of a LATEX file is typically the \documentclass[options]{class} argument. This document uses the article class. Almost everything commonly written in mathematics will use this class. Documents written in the article class may contain sections, subsections, subsubsections, paragraphs and subparagraphs. They may not contain parts or chapters. (See Section 4.)

If you intent to print your LATEX document duplex style (front and back) and bind it, then using the class book will alternate margin sizes left and right to accommodate the extra spacing needed by the binding.

3.2 Document Class Options

It's generally a good idea to specify your paper type and font size in the header. Doing this ensures that your audience will view the results of your LATEX code as you intend. These options are in square brackets, such as [letterpaper,10pt] within the document class declaration.

For documents beind viewed/printed in North America: [letterpaper]
For documents beind viewed/printed outside North America: [a4paper]

The option [letterpaper, 10pt] then makes a US letter sized paper with the standard font being 10pt.

3.3 Packages

LATEX is mostly a giant collection of packages on top of old-school TEX. These packages are really what make LATEX work. The packages typically used for math are:

amsfonts Makes certain math symbols/fonts possible. E.g., \mathbb{R} amsmath Makes most math notation possible. E.g., $\int_1^x \frac{1}{x^2} dx$ amssymb Make some symbols possible. E.g.,

The fullpage package will make sure the margins of your page are 1 inch on all sides. The geometry package allows you to define margins at will. Without these options, you'll see that the article class in particular gives much bigger margins. More packages are discussed in this document as they are needed.

3.4 Document Length Declarations

You'll notice that the header for this file contains setlength\parindent{0pt}. By default, LaTeX indents new paragraphs, which can actually be quite annoying when writing mathematics. The parindent setting in the header in this case resets that length to zero. (You could make it bigger if you wanted to.) Other length declarations that may be useful are as follows.

\parindent normal paragraph indentation
\baselineskip vertical distance between lines in a paragraph
\parskip extra vertical space between paragraphs

3.5 New Commands and Renew Commands

Defining new commands and renewing standard commands can make your code writing more efficient. For instance, typically to write a \mathbb{R} symbol in LaTeX one would write \mathbb{R} in math mode (more on math mode later). We can make this more efficient.

```
\newcommand{\mbr}{\mathbb{R}}
```

With the above line in the document (preferably in the header, but almost anywhere will do, just keep in mind that the command can only be used below where it is defined in the code), we would only need to type \mbr in math mode to achieve the same symbol. The idea is as follows: whenever an instance of the content inside the first brackets is found in your LATEX document, it is replaced with the content in the second set of brackets and then compiled. The following example takes this a step further.

```
\newcommand{\mbr}[1]{\mathbb{#1}}
```

Here, [1] is an argument that we send to the command \mbr and in turn we get the output \mathbb{1}. For example, if we type \mbr{Q} in math mode, it will display Q. It is also possible to renew commands so that they do something different than their current definition. For example, writing

```
\renewcommand{\mathbb}[1]{\mathf[thm]rak{#1}}
```

will force \mathbf{C} to display as \mathfrak{C} (a fraktur letter) instead of \mathbb{C} (a blackboard letter).

4 Document Organization

\section{Document Organization}\label{divisions}

This is Section \ref{divisions}, although the number "\ref{divisions}" doesn't appear... results in the beginning of the following paragraph.

This is Section 4, although the number "4" doesn't appear anywhere in the code for this sentence. If T_EX automatically numbers many constructs (pages, sections, subsections, chapters, theorems, lemmas, etc.) and has a special environment for labelling and referencing such constructs. This is very convenient, since you can move constructs around (e.g., change the order of theorems) and If $T_EX 2_{\varepsilon}$ will automatically change any references. First, we will look at some of these constructs. Then, we will see how to assign labels and references.

4.1 Parts, Chapters and Sections

A part may include several chapters, a chapter may include several sections, each section may include several subsections, and so on. We can begin a new section (or whatever) by writing

```
\section{Put Section Title Here}
```

The constructs available in \LaTeX 2ε for this sort of organization are as follows. (We will discuss them in a little more detail in the coming subsections.)

```
\part{title} Can only be used in certain document classes. (Not in article.)
\chapter{title} Can only be used in certain document classes. (Not in article.)
\section{title} Automatically numbered 1, 2, 3, ...
\subsubsection{title} When in Section 3, automatically numbered 3.1, 3.2, 3.3, ...
\where \text{When in Subsection 4.3, automatically numbered 4.3.1, 4.3.2, ...}
```

4.2 Table of Contents

Once you have defined sections and subsections, using the following command (preferably at the beginning of your document) will result in a table of contents where \LaTeX will insert the document structures, substructures and page numbers automatically.

\tableofcontents

You can force part/chapter/section/subsection/subsubsection names to appear differently in the Table of Contents than they appear in headings by using the following modification:

```
\subsection[Parts, Chapters \& Sections] {Parts, Chapters and Sections}
```

Notice that in the current document, Subsection 4.1 has the title Parts, Chapters & Sections in the Table of Contents, yet has the title Parts, Chapters and Sections in the subsection heading. (The backslash is placed in front of the & because & is a special character in IATEX and placing a backslash in front of it tells IATEX to actually display a &.)

4.3 Theorems, Corollaries and Lemmas

Like Sections and other constructs, IATEX can automatically number Theorems and such. We need to do a little work first to tell IATEX explicitly how to number the theorems and how to display the content of the theorems. IATEX thinks of five constructs here: theorems, corollaries, lemmas, definitions and remarks. Mathematical texts typically write the first three of these in italics, and the latter two in a regular font. Following that convention, the following should be placed in the document header.

```
\newtheorem{thm}{Theorem}[section]
\newtheorem{cor}[thm]{Corollary}
\newtheorem{lem}[thm]{Lemma}
```

This is somewhat complex, but it tells LATEX to order theorems by Section (so the third theorem in Section 2 will be Theorem 2.3) and to order corollaries and lemmas with the same ordering as theorems (so the first corollary in Section 5 will be Corollary 5.7 if it comes after Theorem 5.6). Removing the [section] declaration will order all theorems, corollaries and lemmas linearly throughout the entire document (the third such theorem/corollary/lemma in the document will be numbered 3 regardless of which section in which it appears). The [thm] declaration in the Corollary and Lemma definitions just tell LATEX to tie the numbering of Corollaries and Lemmas to the numbering of Theorems. If you remove this declaration, it would be possible to have Lemma 1 appear after Theorem 32, for instance.

For proofs, use the \begin{proof} and \end{proof} environments (these require the amsthm package). Late X will automatically place a square at the end of the proof. If you want to use a different symbol, renew (Section 3.5) the command \qedsymbol.

The following is an example that demonstrates this. Notice that we are currently in Section 4 of the current document, and so we expect the first theorem/corollary/lemma to be numbered 2.1. Here is what we type:

```
\begin{thm}
This is a theorem.
\end{thm}

\begin{proof}
This is the proof. Notice the box thing at the end.
\end{proof}

\begin{cor}
Here is a corollary.
\end{cor}

\begin{lem}
And a lemma.
\end{lem}

\begin{thm}[Some Famous Name]
And another theorem.
\end{thm}
```

That will display the following.

Theorem 4.1. This is a theorem.

Proof. This is the proof. Notice the box thing at the end.

Corollary 4.2. Here is a corollary.

Lemma 4.3. And a lemma.

Theorem 4.4 (Some Famous Name). And another theorem.

4.4 Labels and References

For items in LATEX which contain some sort of number, we can assign a label to that number and reference it throughout the document. To place a label, use the \label{labelname} command. To reference the labelled item, use the \ref{labelname} command. For example, if we wish to reference a theorem through the text of a document, the following will accomplish that.

```
\begin{thm}\label{importanttheorem}
This is a very important theorem.
\end{thm}
```

We can reference Theorem \ref{importanttheorem} like so.

That will display the following:

Theorem 4.5. This is a very important theorem.

We can reference Theorem 4.5 like so.

IATEX will automatically number many equations and other items as well. Since there are so many things that may be numbered, it is generally a standard practice to label things so that the label gives some information about the item it labels. For instance, a label of \label{thm:HeineBorel} would be used on a theorem (thm) named Heine Borel and a label of \label{eqn:myequation} could be used on an equation (eqn).