

1.

a. $R(A,B,C,D)$ with FD's $AB \rightarrow C, C \rightarrow D, D \rightarrow A, B \rightarrow D$

i. Find BCNF violations

1. $AB^+ = \{A,B,C,D\}$, Superkey!
2. $C^+ = \{C,D,A\}$ BCNF violation
3. $D^+ = \{D,A\}$ BCNF violation
4. $B^+ = \{B,D,A\}$ BCNF violation

ii. Decompose!

1. $C^+ = \{C,D,A\}$ BCNF violation
2. Decompose into $R1 = \{C,D,A\}$ and $R2 = \{C,B\}$
3. Find FDs in $R1 \{ C \rightarrow D, C \rightarrow A, D \rightarrow A \}$, $R2 \{ \}$
4. $R2$ is in BCNF
5. $C^+ = \{C,D,A\}$ BCNF violation, $D^+ = \{D,A\}$ BCNF violation
decompose $R1$ into $\{D,A\}, \{D,C\}$
6. Decomposition: $\{D,A\}, \{D,C\} \{C,B\}$

b. $R(A,B,C,D)$ with FD's $B \rightarrow C, B \rightarrow D, A \rightarrow B$

i. Find BCNF violations

1. $B^+ = \{B,C,D\}$ BCNF violation
2. $A^+ = \{A,B,C,D\}$ Superkey!

ii. Decompose!

1. $B^+ = \{B,C,D\}$ BCNF violation
2. Decompose into $R1 = \{B,C,D\}$ and $R2 = \{B,A\}$
3. Find FDs in $R1 \{ B \rightarrow C, B \rightarrow D \}$, $R2 \{ \}$
4. $R2$ is in BCNF
5. $B^+ = \{B,C,D\}$, left sides of FDs are superkeys
6. Decomposition: $\{B,C,D\}, \{B,A\}$

2. $R(A,B,C,D,E)$ is decomposed into $R1(A,B,C), R2(B,C,D), R3(A,C,E)$

	a	b	c	d	e
r1	a	b	c	d1	e1
r2	a2	b	c	d	e2
r3	a	b3	c	d3	e

a. $B \rightarrow E$ and $CE \rightarrow A$

1. Apply $CE \rightarrow A$ and $B \rightarrow$ to table

2.

	a	b	c	d	e
r1	a	b	c	d1	e1
r2	a2	b	c	d	e1
r3	a	b3	c	d3	e

3. Not lossless because there is no row without a subscript

b. $AC \rightarrow E$ and $BC \rightarrow D$

1. Apply $AC \rightarrow E$, and $BC \rightarrow D$

2.

	a	b	c	d	e
r1	a	b	c	d	e
r2	a2	b	c	d	e1
r3	a	b3	c	d3	e

3. Lossless because r1 has no subscripts

3. $R(A,B,C)$

Given MVD $A \twoheadrightarrow B$ and tuples $(a1,b1,c1),(a, b2, b2),(a,b3,c3)$

Other tuples in R include $(a,b1,c2), (a,b1,c2),(a,b1,c3), (a,b2,c1),(a,b2,c3),$

$(a,b3,c1),(a,b3,c2)$. We know they are in the current instance of R because they are the remaining combinations that can be made with the given tuples.

4. Imagine you are tasked with coming up with a new Virtual Reality Movie Website. VR movies can be 180, 360 with or without 3D. People might want to have accounts to comment on Movies. Make an E/R diagram that might be suitable for the database of such a site and include it in your Hw3.pdf.

