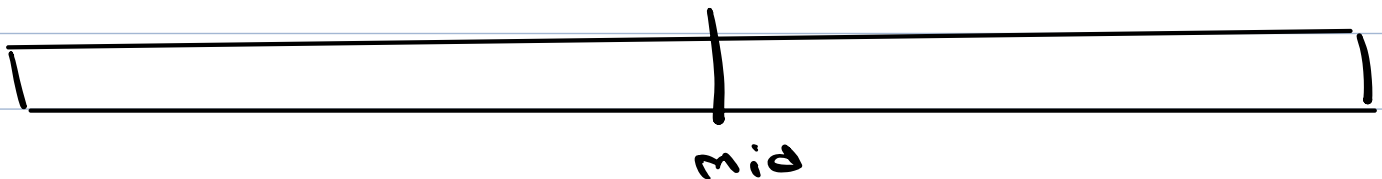


## Agenda

1. Painter Partitions Problem
2. Aggressive Cows Problem

Revision Quiz 1

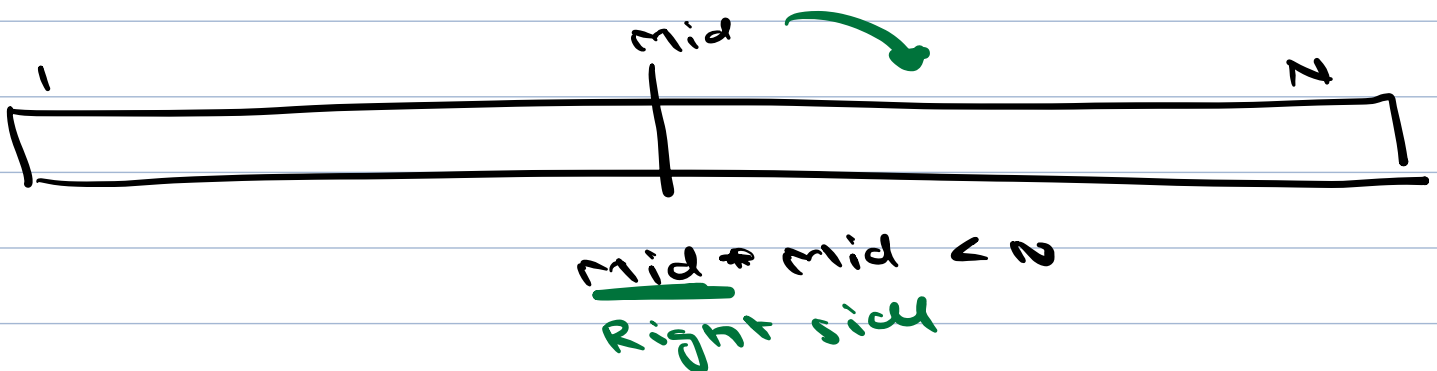


Revision Quiz 2

$$x \times x = N$$

$$N = 36 \quad \text{ans} = \sqrt{36} = 6$$

$$N = 38 \quad \text{ans} = \sqrt{38} = 6$$



Revision Quiz 3 : TC :  $O(\log_2 N)$

Revision Quiz 4 : SC of recursive Binary Search :  $O(\log_2 N)$

Q. Given an array representing board length (N boards). Paint all boards if T time is available with you. Find min no. of painters required to get job done.

- 1 unit of length takes 1 unit of time to paint.
- 1 board can't be divided in painters.
- Painters will paint consecutive boards only.

Ex:  $\langle 3 \quad 5 \quad 1 \quad 7 \quad 6 \quad 9 \quad 1 \quad 5 \rangle$   $T=9$   
 $P_1 \quad P_1 \quad P_1 \quad P_2 \quad P_3 \quad P_4 \quad P_5 \quad P_5$

ans = 5

$P_1 \rightarrow 9$        $P_5 \rightarrow 6$

$P_2 \rightarrow 7$

$P_3 \rightarrow 6$

$P_4 \rightarrow 9$

TC:  $O(N)$

SC:  $O(1)$

```
int minNoOfPainters (arr, T) {
```

```
    int cnt = 1
```

```
    int work = 0
```

```
    for (i = 0 ; i < N ; i++) {
```

```
        if (work + arr[i] > T) {
```

```
            cnt++
```

```
            work = arr[i]
```

```
        } else {
```

```
            work = work + arr[i]
```

```
        }  
    }  
    return cnt
```

Q. Given an array representing board length (N boards). Paint all boards if T time and P painters are available with you. Can these painters do the job within T time?

Ex :  $\langle 3 \quad 5 \quad 1 \quad 7 \quad 6 \quad 9 \quad 1 \quad 5 \rangle$   $T=9, P=4$   
 $P_1 \quad P_1 \quad P_1 \quad P_2 \quad P_3 \quad P_4 \quad P_5 \quad P_5$

Min of 5 painters  $> P \Rightarrow \text{False}$

Ex :  $\langle 3 \quad 5 \quad 1 \quad 7 \quad 6 \quad 9 \quad 1 \quad 5 \rangle$   $T=9, P=6$

Min of 5 painters  $\leq P \Rightarrow \text{True}$

boolean isPossibleToPaintBoard (arr, T, P)

```
int cnt = 1
int work = 0
for (i=0 ; i < N ; i++) {
    if (work + A[i] > T) {
        cnt++
        work = A[i]
    }
    else {
        work = work + A[i]
    }
}
```

```
if (cnt ≤ P)
    return true
else
    return false
```

TC :  $O(N)$   
SC :  $O(1)$

2. Given an array representing board length (N boards). Paint all boards if P painters are available with you. Find min. time required to get job done by the painters.

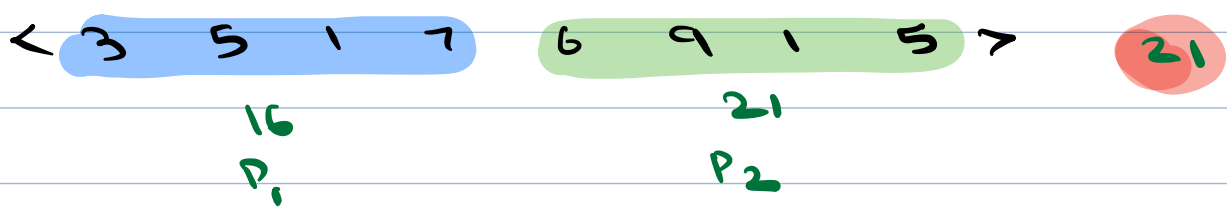
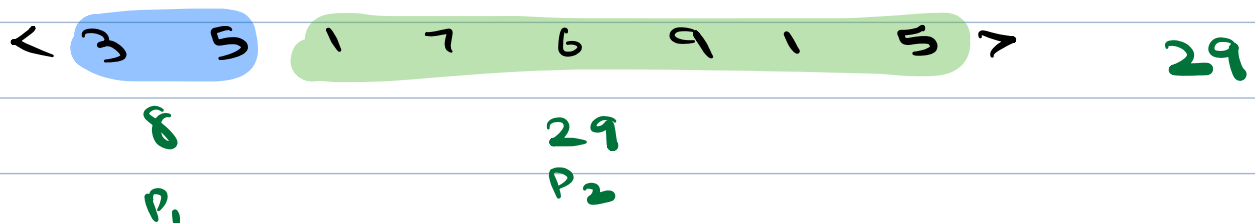
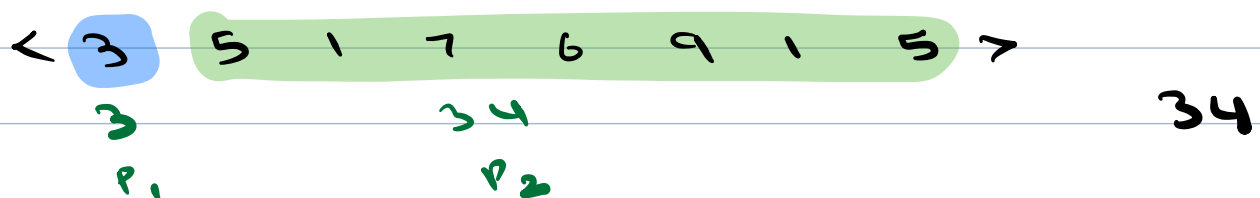
- 1 unit of length takes 1 unit of time to paint.
- 1 board can't be divided in painters.
- Painters will paint consecutive boards only.

Ex :  $\langle 3 \ 5 \ 1 \ 7 \ 6 \ 9 \ 1 \ 5 \rangle \quad P=1$

$$\text{ans} = 3 + 5 + 1 + 7 + 6 + 9 + 1 + 5 \\ = 37$$

Ex :  $\langle 3 \ 5 \ 1 \ 7 \ 6 \ 9 \ 1 \ 5 \rangle \quad P=2$

$$\text{ans} = 21$$



$$\langle \underbrace{3 \ 5 \ 1 \ 7 \ 6}_{22 \ P_1} \ \underbrace{9 \ 1 \ 5}_{15 \ P_2} \rangle \quad 22$$

Greedy Approach: X

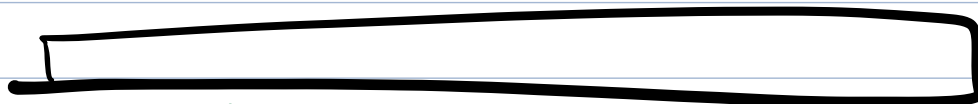
Divide total work by total no. of painters

$$A = [10, 20, 30, 40] \quad \text{ans} = 60 \quad P = 2$$

$$\frac{\text{Total work}}{\text{Painters}} = \frac{100}{2} = 50$$

$$A = [\underbrace{10, 20}_{30 \ P_1}, \underbrace{30, 40}_{70 \ P_2}] \quad P = 2 \quad 70$$

$$A = [\underbrace{10, 20, 30}_{60 \ P_1}, \underbrace{40}_{40 \ P_2}] \quad 60$$



✓  
P<sub>1</sub>  
x

✓  
P<sub>2</sub>  
y

✓  
P<sub>3</sub>  
z

→ max(x, y, z)

$A = [1, 2, 3, 4, 100]$

$\begin{matrix} 10 \\ P_1 \end{matrix}$ 
 $\begin{matrix} 100 \\ P_2 \end{matrix}$

$P = 2$

ans = 100

100

Approach 2 : Binary Search on Time

Search space :  $l = \max(arr[i])$  |  $r = \sum(arr[i])$

Lower limit  
time

Best case time  
to paint all  
boards

$P = N$

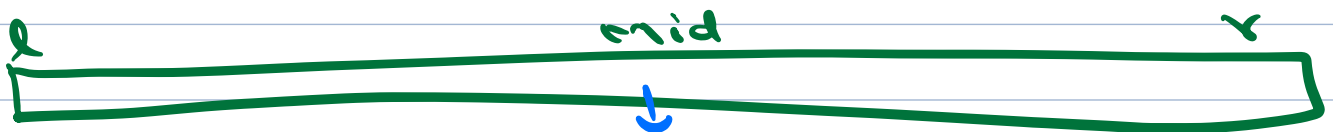
Upper limit

Worst case  
time to  
paint all  
boards

$P = 1$

Target : Min time to complete the job

Condition



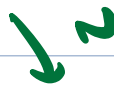
Is my mid the answer?

Can we paint all boards in  
 $\leq$  mid time (given  $k$  painters)

$l$

mid

$r$



2 10 5 X

no to right

$$N=15 \quad P=3$$

l    r    mid    Can we paint boards in  $\leq$  mid time?    where ans to go?



No  
weight  
 $N=15$   $K=2$

25      39      32

3 = 3

update ans 32  
no left

$$N=15 \quad K=3$$

$A[] = \begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 & 13 & 14 \\ 3 & 5 & 1 & 7 & 8 & 2 & 5 & 3 & 10 & 1 & 4 & 7 & 5 & 4 & 6 \end{matrix}$

$P_1$   $P_2$   $P_3$

l	r	mid		update ans	28
25	31	28	3 = 3	no left	
					n=15 k=3

$A[] = \begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 & 13 & 14 \\ 3 & 5 & 1 & 7 & 8 & 2 & 5 & 3 & 10 & 1 & 4 & 7 & 5 & 4 & 6 \end{matrix}$

$P_1$   $P_2$   $P_3$

$\lambda$        $r$       mid  
25    27      26                  3 = 3                  Update ans 26  
No left                   $N=15$        $K=3$

$A[i] =$ 

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
3	5	1	7	8	2	5	3	10	1	4	7	5	4	6
<u>                    </u>						<u>                    </u>					<u>                    </u>			
$P_1$						$P_2$					$P_3$			

l      r      mid

25    25    25

$3 = 3$

update ans    25  
no left

$N = 15$      $K = 3$

$A[] = \begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 & 13 & 14 \\ 3 & 5 & 1 & 7 & 8 & 2 & 5 & 3 & 10 & 1 & 4 & 7 & 5 & 4 & 6 \end{matrix}$

$P_1$   $P_2$   $P_3$

$l = 8$       End of BS      **STOP**

ans = 25



int minTimeToPaint (arr[], N, P) <

l = max (arr[]) > Iterate arr[]

r = sum (arr[]) >

int ansTime

while (l <= r) <

mid = l + (r - l) / 2

// Is mid answer? Can we paint  
all boards ≤ mid time?

bool  
canPaint = isPossibleToPaintBoard (arr, mid, P)

if (canPaint == true) <

ansTime = mid

r = mid - 1

// left

else <

l = mid + 1

// right

return ansTime

Formula for TC:

$\log(\text{range}) \times \text{TC of feasibility check}$

$\log(\text{sum}(\text{arr}) - \text{min}(\text{arr})) \times N$

$\times N$

$O(\log(\text{sum}(\text{arr}) - \text{min}(\text{arr})) \times N)$

10:45