

AGENDA

- What is Tree?
- Terminology
- Traversal
- Inorder Traversal (Iterative)
- Equal Tree Partition

Revision Quiz 1

Queue example : People standing in line at ticket counter

Revision Quiz 2

Queue using LL :



Linear
Data structures

Access data in
sequential order

↓
Array, LL, stack, Queues etc.

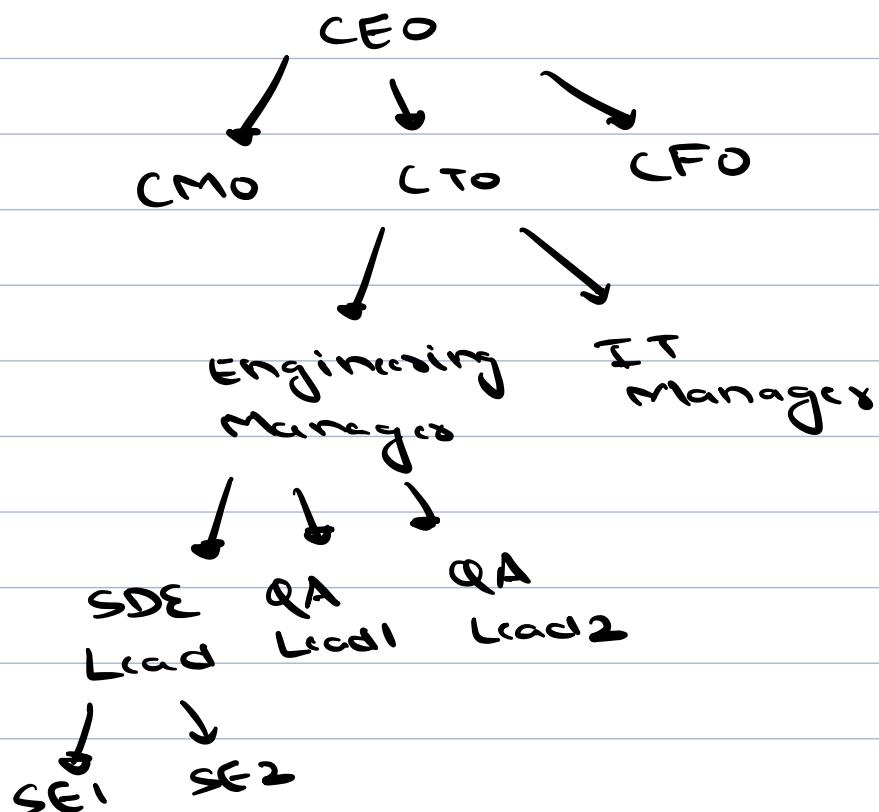
Tree : Fair topic among interviewers

Why ?

1. Requires solid recursion understanding
2. Ability to visualize concepts

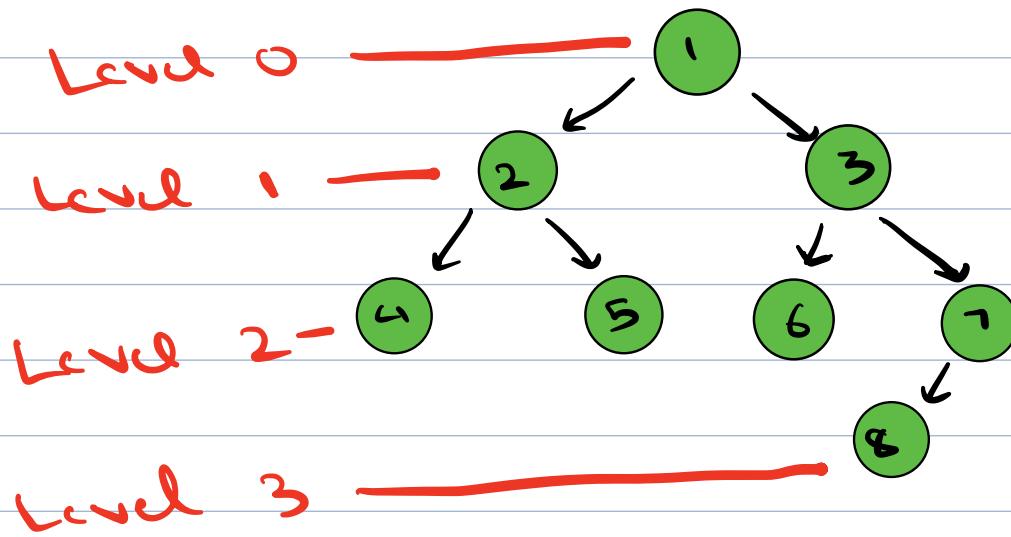
Tree is a non-linear data structure used to represent hierarchy in information.

For eg. Family Tree, Org Structure, Folder structure

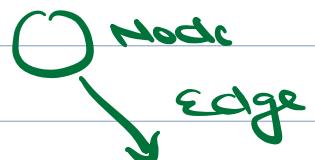


x parent of y
 y child of x

Tree Naming Convention



Node : element of tree with data and nodes are connected to it.



Root : Topmost node of a tree from which all other nodes descend . It has no parent.

1 is root node

Parent : A node that has child node connected to it. Parent Node → 1, 2, 3, 7

Child : A node that has a parent node connected to it. Every node except root

Leaf : Node with 0 children . It's a terminal node. Node 4, 5, 6 and 8

Depth / level : Distance from root node (in terms of edges)

Height : Length of longest path from a node to a leaf.

Height of tree = Height of root node

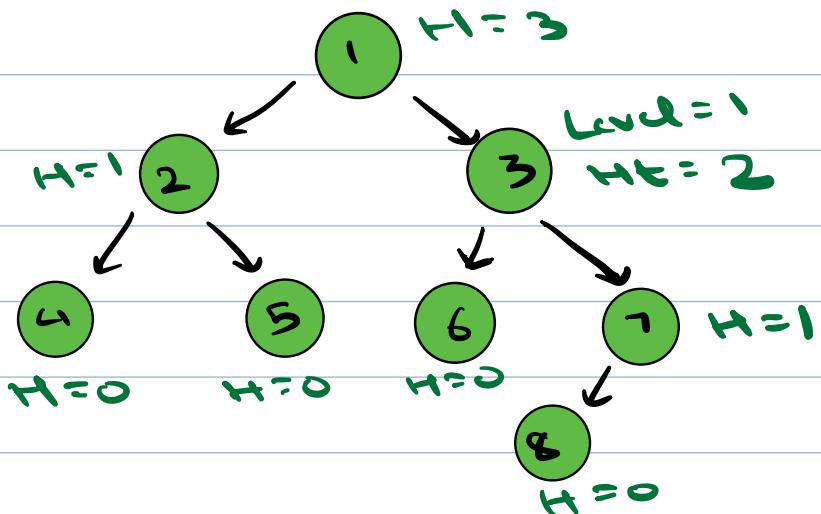
1 child



1 par

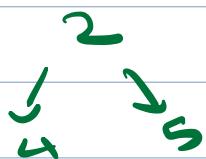
1 par

↓
Multiple
children

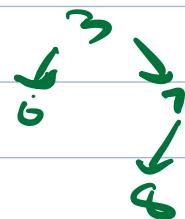


Subtree: A tree structure which is part of a larger tree

Subtree rooted at 2



Subtree rooted at 3



Siblings: Nodes that share same parent node.
 $P \rightarrow 2$; 4 and 5 are siblings.

Ancestor: All nodes from parent to root upwards are ancestors of a node.

8 : 1, 3, 7 are ancestors.

Descendant: All nodes from child to leaf node along all the paths.

Can a leaf node also be a subtree?

YES

Do all nodes have a parent node?

NO (Everyone has parent except root)

Height of leaf node

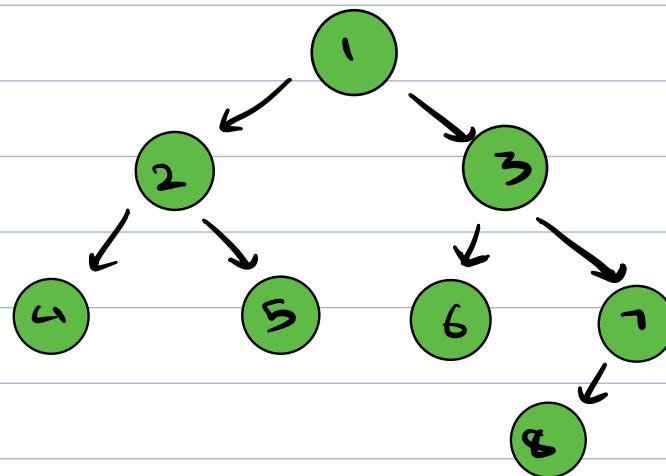
Length of path from leaf to leaf $\rightarrow 0$
 $\nwarrow \rightarrow 0$

Binary Tree

A type of tree in which each node can have atmost 2 children i.e. either 0,1,2.

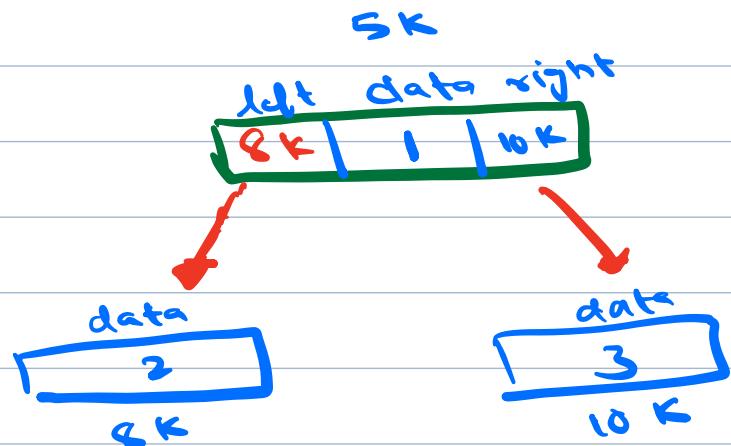
They are referred as left and right child

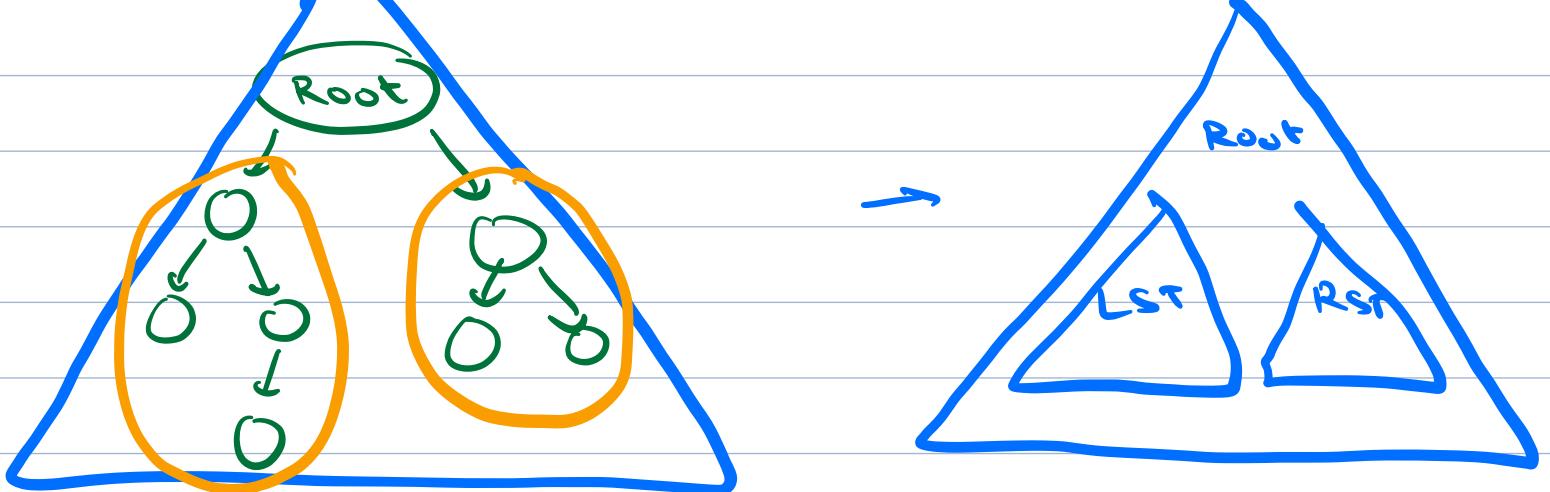
```
class TreeNode <  
    int data  
    TreeNode left  
    TreeNode right
```



```
TreeNode (int n) <
```

```
|  
| data = n  
| left = NULL  
| right = NULL
```





How can we traverse a tree? Depth First Search (DFS)

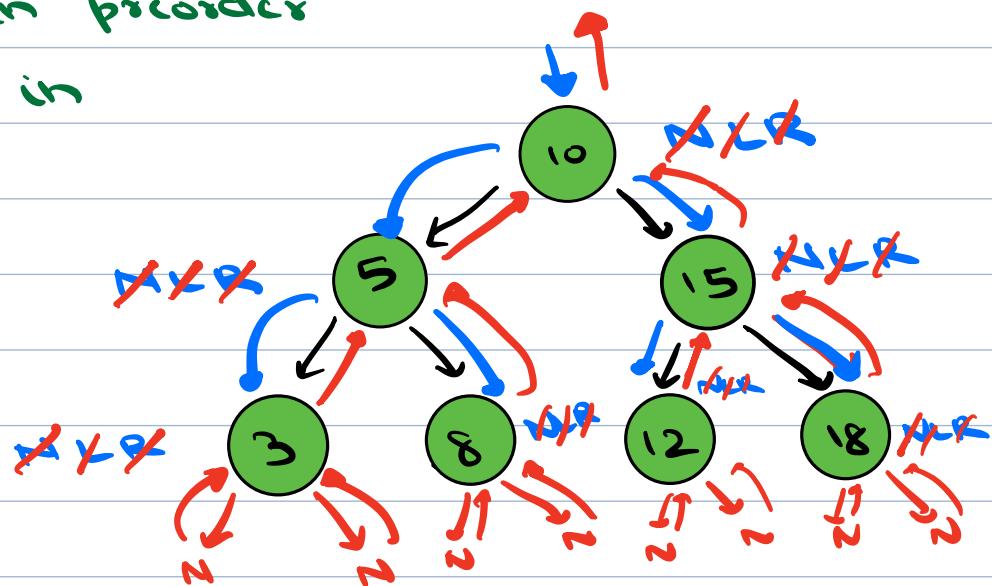
L → Left subtree

R → Right subtree

N → Node

Preorder → NLR

1. Visit the node
2. Left subtree in preorder
3. Right subtree in preorder



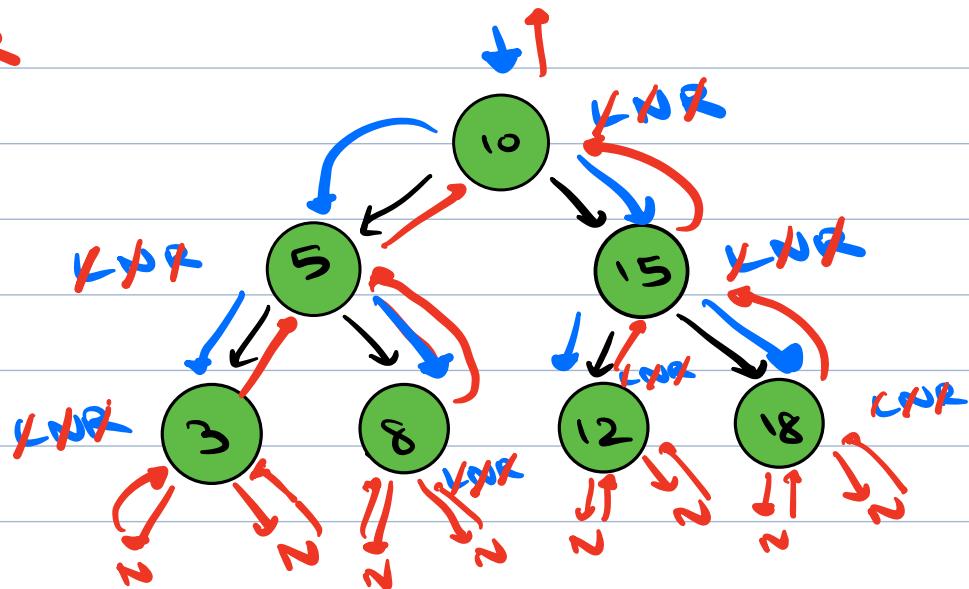
O/P: 10 5 3 8 15 12 18

// Given root node as IP, fn will visit nodes in preorder

```
void preorder (TreeNode root) {  
    if (root == NULL) return;  
    print (root.data)  
    preorder (root.left)  
    preorder (root.right)}
```



Inorder : L N R

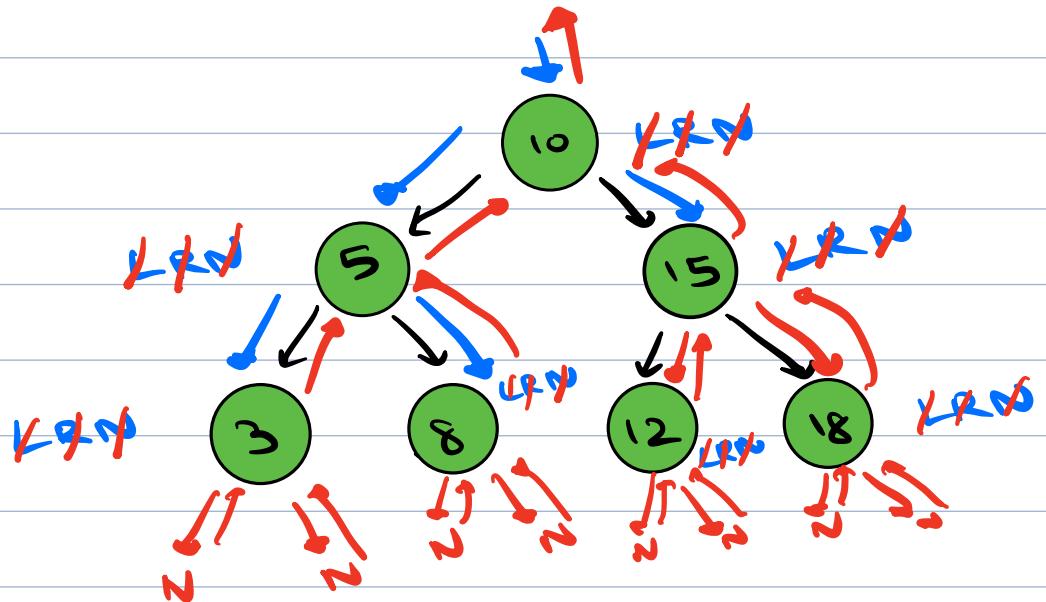


OP: 3 5 8 10 12 15 18

```
void inorder (TreeNode root) {  
    if (root == NULL) return;  
    inorder (root.left)  
    print (root.data)  
    inorder (root.right)}
```

L N R

Postorder : L R N



O/P: 3 8 5 12 18 15 10

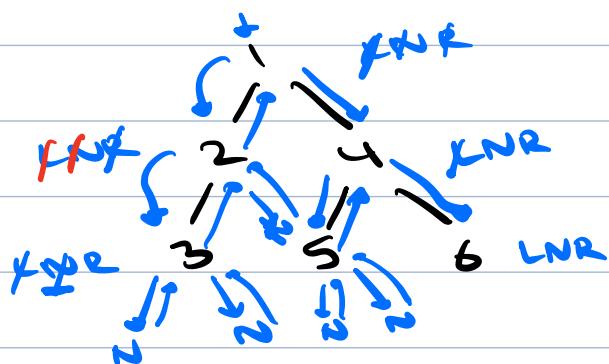
```
void postorder (TreeNode *root) { LRN
    if (root == NULL) return
    postorder (root.left)
    postorder (root.right)
    print (root.data)
```

Inorder : LNR

Preorder : N L R

Postorder : L R N N

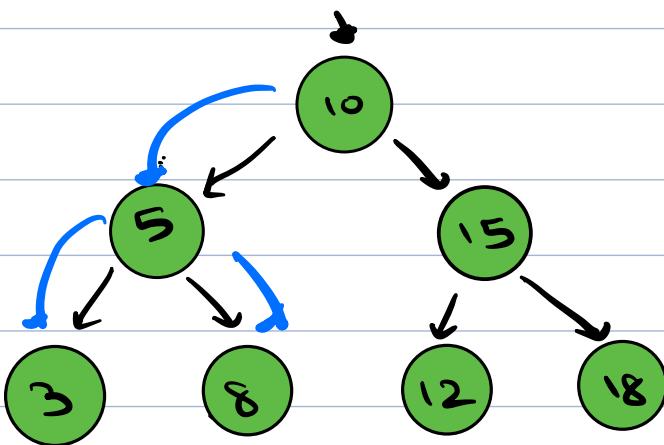
Inorder : L N R



O/P: 3 2 1 5 4 6

10:39

Preorder : NLR



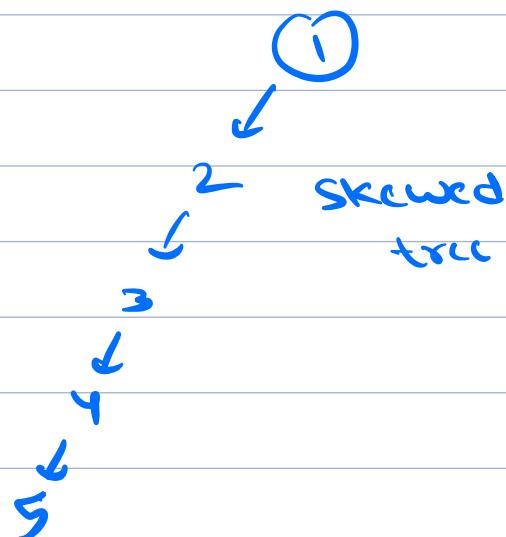
pre(8)
pre(3)
pre(5)
pre(10)

TC : O(N)

At any point, nodes of 1 path are on the stack. We are exploring nodes path by path.

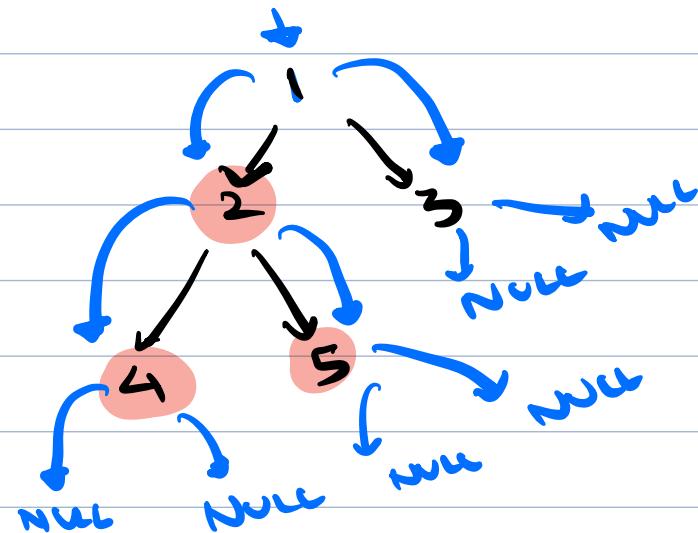
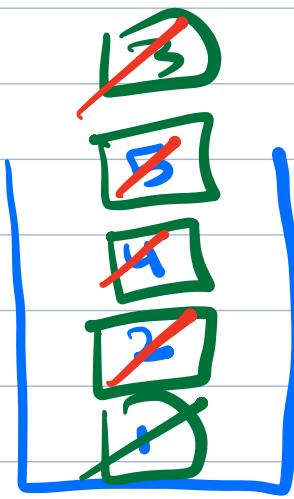
SC : O(H) \rightarrow height of tree

$\log_2 N$ N



Iterative Inorder Traversal

LNR



NULL : Take out a node from stack

1st : Push in stack , go to left

O/P : 4 2 5 1 3

STOP : cur == NULL and st.size() == 0

stack <Node> st

Node cur = root

while (cur != NULL || !st.isEmpty()) <

if (cur != NULL) {
 st.push (cur)
 cur = cur.left
}

else <

 Node t = st.top() st.pop()
 print (t.data)
 cur = t.right
}

return

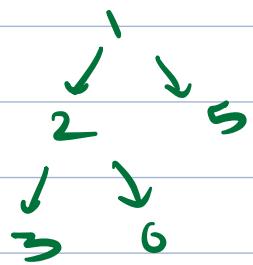
TC: O(N)

SC: O(H)

↓
stack

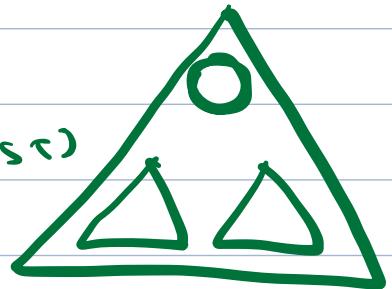
Iterative Preorder and Postorder

Q. Given a tree, find sum of tree



ans = 17

$$\text{sum(tree)} = \text{sum(LST)} + \text{sum(RST)} + \text{root.data}$$



// Given a root node, this fn will sum up all the nodes in tree rooted at 'root'

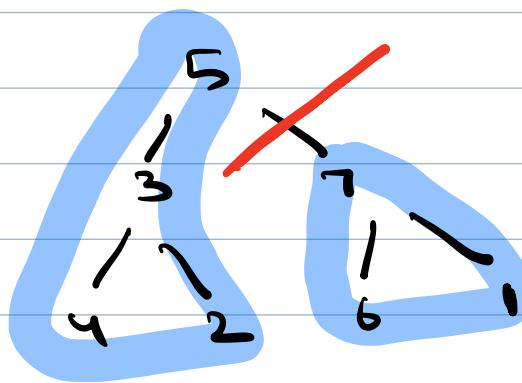
```
int Sum (TreeNode root) {  
    if (root == NULL) return 0;  
    return sum (root.left) + sum (root.right)  
        + root.data  
}
```

TC: O(N)

SC: O(H)

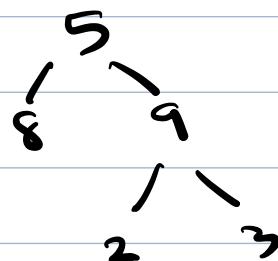
Equal Tree Partition

Q. Given a binary tree, check if you can partition the tree into 2 trees of equal sum.



total = 28

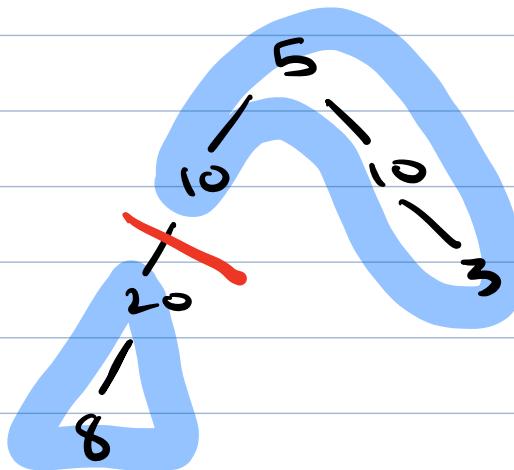
ans = true



total = 27

ans = false

If totalsum is odd, ans = false



total sum = 56

ans = true

1. calculate totalsum
2. If ($\text{totalsum} \% 2 == 1$) return false
3. look for a piece of tree \rightarrow



$$\text{sum} = \frac{\text{totalsum}}{2}$$

Look for any subtree with

$$\text{sum} = \frac{\text{totalsum}}{2}$$

```
int desiredSum = INT_MIN
```

```
bool ans = false
```

```
int sum(TreeNode root) <
```

```
| if (root == NULL) return 0
```

```
| int subtreeSum = sum(root.left)
| + sum(root.right) + root.data
```

```
| if (subtreeSum == desiredSum) <
```

```
| | ans = true
```

```
> return subtreeSum
```

main() <

```
int totalsum = sum(xroot)
if (totalsum % 2 == 1)
    return false
```

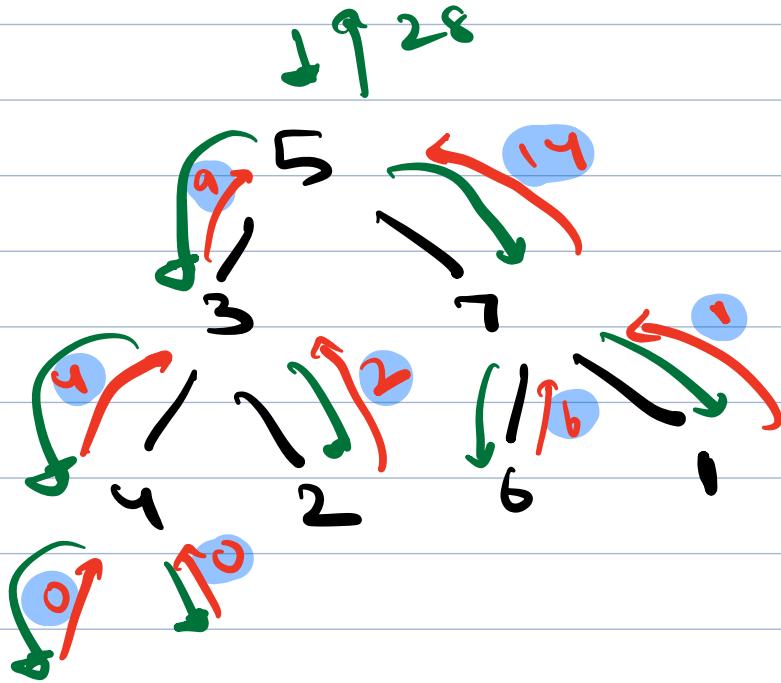
```
desiredsum = totalsum / 2
sum(xroot)
return ans
```

>

TC : O(N)

SC : O(H)

↓
height
of tree



$$\text{desiredsum} = -\cancel{\frac{14}{2}}$$

ans = ~~FT~~

$$\text{totalsum} = 28$$