

Pivot Partition

Quick Sort

Comparator Problems

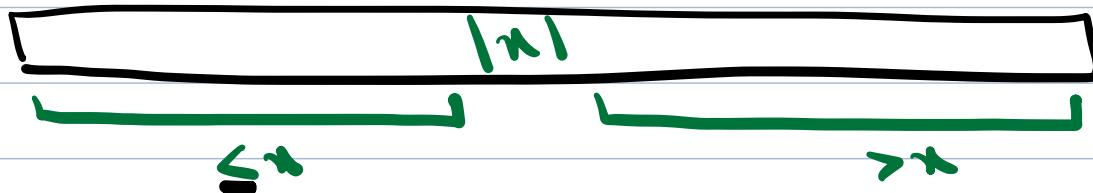
Contest 1 → Monday (25 Nov)

Arrays, Bit manipulation, Recursion, Math,
Hashing & Sorting

4 Q → 3/4 Passed

Given an integer array, consider 1st element as pivot
 rearrange the elements such that for all i:
 if $A[i] < p$ then it should be present on left side
 if $A[i] > p$ then it should be present on right side

Note: All elements are distinct



$a = [] : \underline{54}, 26, 93, 17, 77, 31, 44, 55, 20$

Ans : $\underline{26, 17, 31, 44, 20}, \underline{54, 55, 77, 93}$

$a = [] : \underline{10}, 13, 7, 8, 25, 20, 23, 5$

Ans : $\underline{7, 8, 5} \quad 10 \quad \underline{13, 25, 20, 23}$

① On partitioning the array based on pivot, pivot reaches its sorted place.



Soln 1 : Sort array

TC : $O(N \log N)$

54

26 93 17 77 31 44 55 20



17 20 26 31 44 54 55 77 93
[< 54] [> 54]

Sol 2 :

< 54

> 54

54

26 93 17 77 31 44 55 20 93
.....

$l \rightarrow$ smaller
 $r \rightarrow$ bigger

l crosses r
stop

54 26 20 17 44 31 77 55 93
[< 54] [> 54]

31
54 26 20 17 44 31 77 55 93
[< 54] [> 54]

swap ($a[\text{pivot}]$, $a[r]$)

54

26 ~~93~~
~~20~~ 17 ~~71~~
44 31 ~~44~~
~~71~~ 55 ~~20~~
~~93~~

8 8

If l is happy

$l++$

else if r is happy

$r--$

else

swap

$l++$ $r--$

$l \leftarrow$

54

~~102~~
~~22~~

100

~~22~~
~~102~~

\downarrow

100

22

54

102

O $N-1$

int partition (A, first, last) <

int ind = Math.random (first, last)
swap (A[ind], A[first])

pivot = A[first]

l = first + 1

r = last

while (l ≤ r) <

if (A[l] ≤ pivot) <

 l++
 ↓
 r

else if (A[r] > pivot) <

 r--
 ↓
 l

else <

 swap (A[l], A[r])

 l++ r--
 ↓
 r

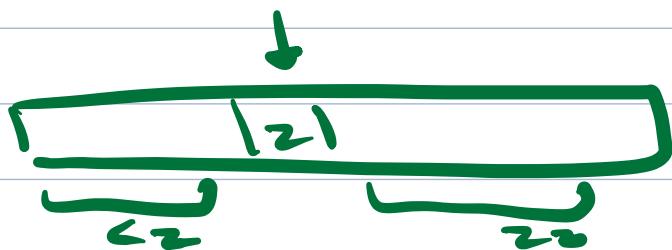
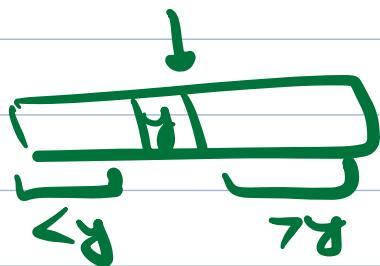
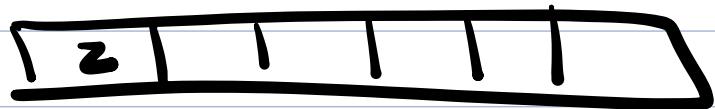
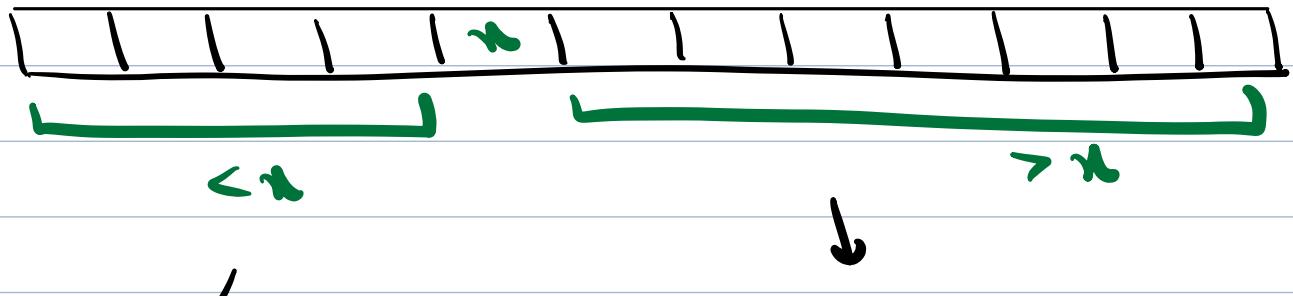
swap (A[first], A[r])

return r

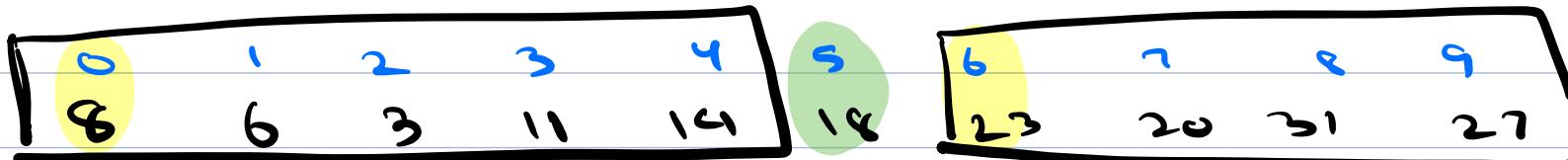
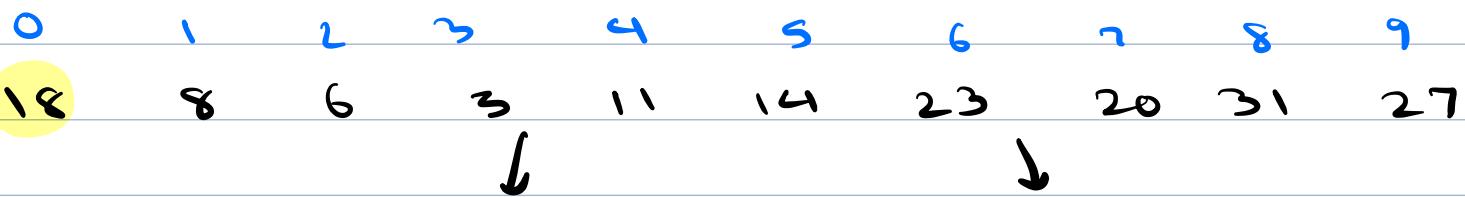
TC : O(N)

SC : O(1)

Quick Sort \rightarrow Divide and conquer strategy



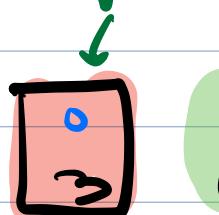
qs (0, 9)



qs (0, 4)



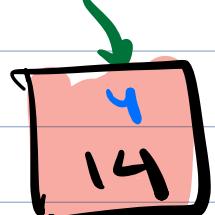
qs (0, 1)



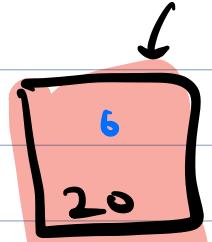
qs (0, 0)



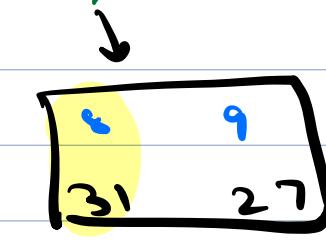
qs (3, 4)



qs (4, 4)



qs (6, 6)



qs (8, 9)

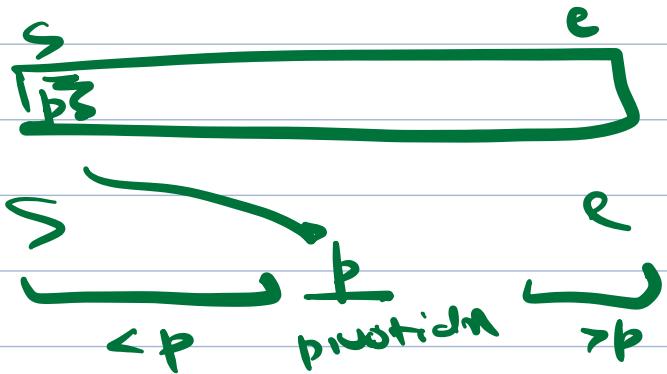
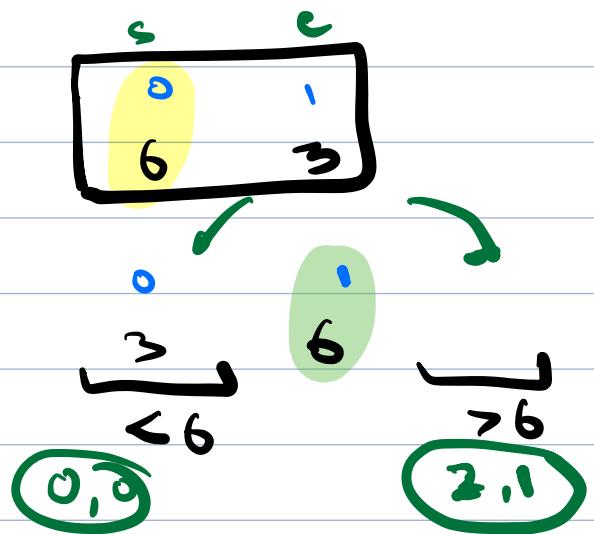
qs (8, 8)

3 6 8 11 14 18 20 23 27 31

// Given A, this fn will sort A from s to e
void quicksort (int A[], int s, int e)
if (s >= e) return

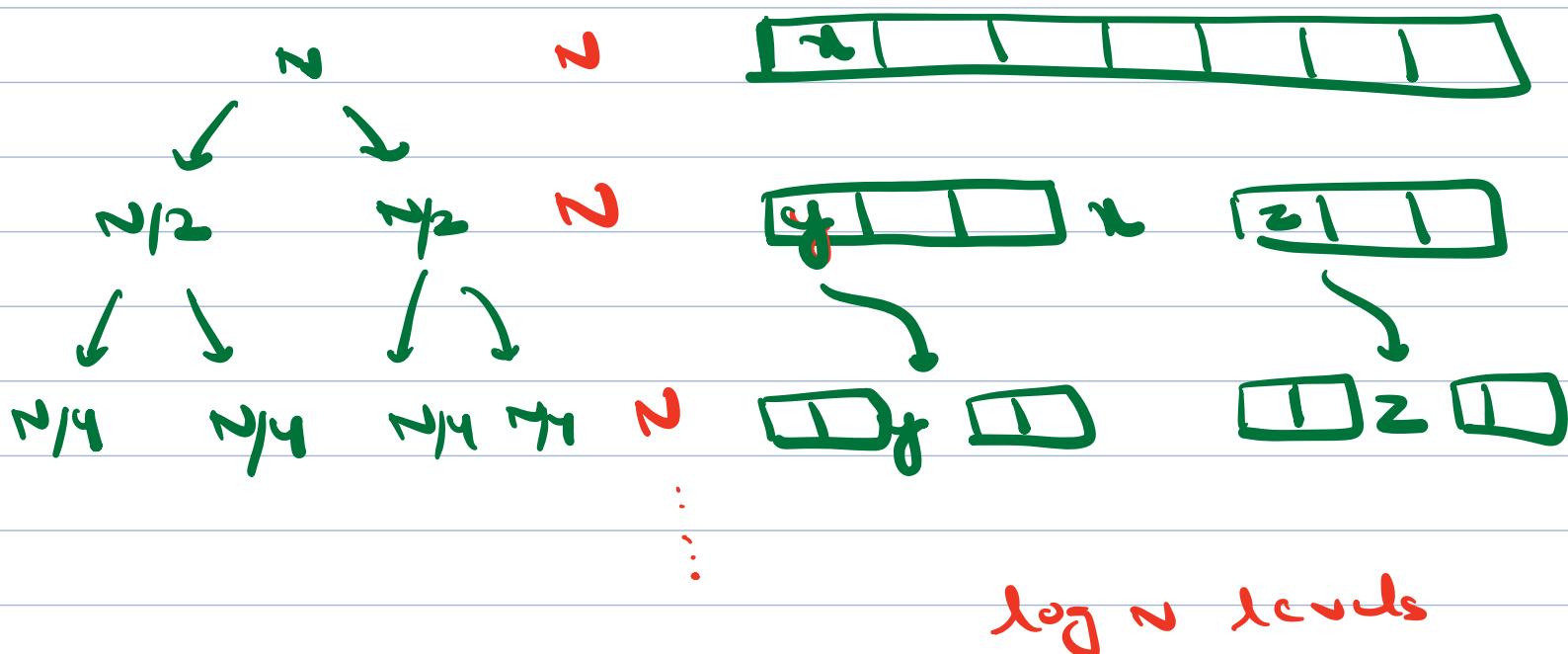
```
int partition = partition (A, s, e)
quicksort (A, s, pivotidx - 1)
quicksort (A, pivotidx + 1, e)
```

$\sqrt{5} \in (0, 1)$



pivot - idx = 1

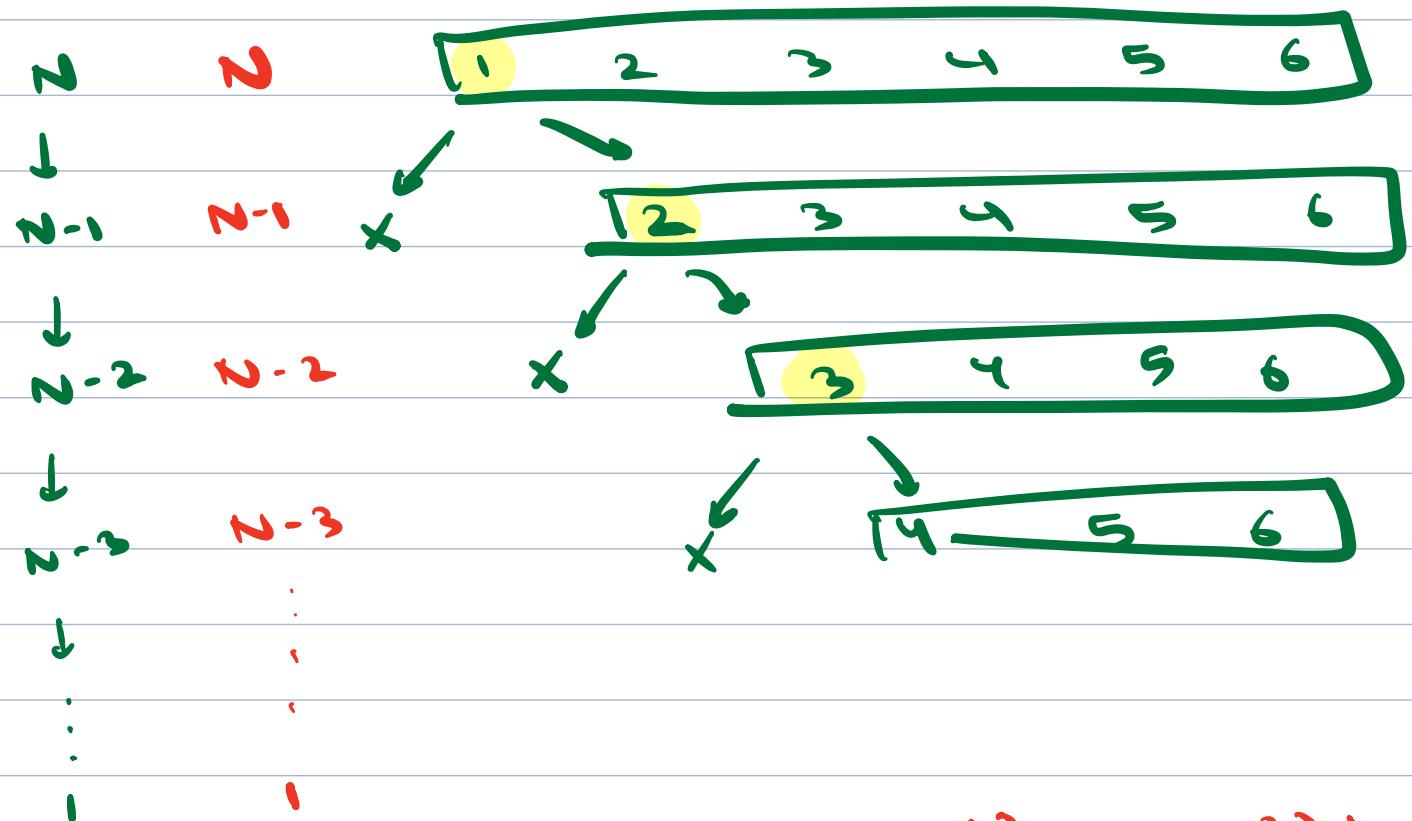
Best Case TC



TC: O(N log N)

$SC : O(C \log N)$

Worst case T_C (corrected data ↑ or ↓)



$$\begin{aligned}
 T_C &: N + (N-1) + (N-2) + \dots \\
 &= \frac{N(N+1)}{2} = O(N^2)
 \end{aligned}$$

$S_C: O(N)$

→ function calls

Pivot → min / Max (worst case)

Quick Sort $T_C: N \log N / \log N$ Best case: $N \log N / \log N$ Worst case: N^2 / N	Merge Sort $T_C: N \log N / N \log N$ $S_C: N \log N / N \log N$
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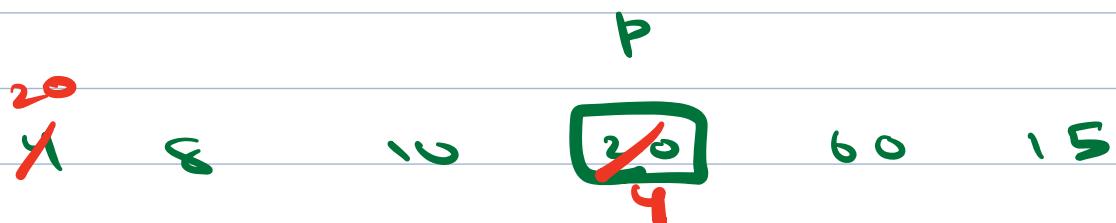
Randomised quick sort \rightarrow

Rather than always choosing first / last element as pivot, a random element as pivot.

\rightarrow First / Mid / Last

\rightarrow Median of first, mid, last

\rightarrow Randomly choose pivot



Prob of picking min de as pivot = $\frac{1}{n}$

Prob of picking 2nd min de as pivot = $\frac{1}{n-1}$

Prob of picking 3rd min de as pivot = $\frac{1}{n-2}$

⋮

Prob. of always picking min =

$$\frac{1}{n} \times \frac{1}{n-1} \times \frac{1}{n-2} \times \frac{1}{n-3} \times \dots \times \frac{1}{1} = \frac{1}{n!}$$

Blst / Avg TC \rightarrow TC: $O(n \log n)$
SC: $O(\log n)$

10:45

C++ \rightarrow Intro sort (Quick Sort + Heap Sort)

Java \rightarrow Algo based on Quick Sort

Python \rightarrow Tim Sort (Merge + Insertion sort)

JS \rightarrow Quick + Insertion sort

1, 3, 5, 7, 9, 2, 4, 6, 8

Sorting : arrangement in data in asc/desc order based on some parameter

Arrays.sort (A) \rightarrow asc order based on value

Collections.sort (A)

Collections.sort (A, new Comparator())

compClass implements Comparator<int> <

@Override

int compare (int a, int b) {

}

Comparator

- In programming, a **comparator** is a function that compares two values and returns a result indicating whether the values are equal, less than, or greater than each other.
- The **comparator** is typically used in sorting algorithms to compare elements in a data structure and arrange them in a specified order.

Comparator is a function that takes two arguments.

For languages - Java, Python, JS, C#, Ruby, the following logic is followed.

1. In sorted form, if first argument should come before second, -ve value is returned.
2. In sorted form, if second argument should come before first, +ve value is returned.
3. If both are same, 0 is returned.

For C++, following logic is followed.

1. In sorted form, if first argument should come before second, true is returned.
2. Otherwise, false is returned.

Given an array of size N , sort data in ascending order of count of factors. If count of factors are equal, sort based on magnitude.

A \rightarrow 9, 3, 10, 6, 4

$$\begin{array}{c} 3 \quad 4 \quad 9 \\ \hline 2 \end{array} \quad \begin{array}{c} 6 \quad 10 \\ \hline 4 \end{array}$$

A \rightarrow 10, 4, 5, 13, 1

1, 5, 13, 4, 10

- ③ 9 \rightarrow 1, 3, 9
- ② 3 \rightarrow 1, 3
- ④ 10 \rightarrow 1, 2, 5, 10
- ⑤ 6 \rightarrow 1, 2, 3, 6
- ③ 4 \rightarrow 1, 2, 4

10 \rightarrow 1, 2, 5, 10
4 \rightarrow 1, 2, 4

5 \rightarrow 1, 5
1 \rightarrow 1
13 \rightarrow 1, 13

CompClass implements Comparator<int>

@Override

```
int compare (int a, int b) {  
    int cnta = countFactors(a)  
    int cntb = countFactors(b)  
    if (cnta < cntb) {  
        return -1  
    }  
    else if (cntb < cnta) {  
        return 1  
    }  
    else {  
        if (a < b) return -1  
        else if (b < a) return 1  
        else return 0  
    }  
}
```

Solution

```
void main() {
```

```
    // A
```

```
    Collections.sort(A, new CompClass())
```

TC: $O(N \log N \times \text{TC of compare function})$

TC: $O(N \log N \times \sqrt{\text{max num in array}})$

9, 3, 10, 6, 4

3 4 9 10 6
3 < 9 10 > 9

9 → 1, 3, 9

3 → 1, 3

10 → 1, 2, 5, 10

6 → 1, 2, 3, 6

4 → 1, 2, 4

```
import functools

//please write the code for finding factors by yourself

def compare(v1, v2):
    if(factors(v1) == factors(v2)):
        if(v1<v2):
            return -1;
        if(v2<v1):
            return 1;
        else
            return 0;
    elif (factors(v1)<factors(v2)):
        return -1;
    else
        return 1;

class Solution:
    def solve(self, A):
        A = sorted(A, key = functools.cmp_to_key(compare))
        return A
```

Python

```
bool compare(int val1, int val2)
{
    int cnt_x = count_factors(x);
    int cnt_y = count_factors(y);

    if(factors(val1) == factors(val2))
    {
        if(val1<val2)
        {
            return true;
        }
        return false;
    }
    else if(factors(val1)<factors(val2))
    {
        return true;
    }
    return false;
}

vector<int> solve(vector<int> A) {
    sort(A.begin(), A.end(), compare);
    return A;
}
```

C++

Given a list of non-negative integers nums, arrange them such that they form the largest number and return it.

Since the result may be very large, so you need to return a string instead of an integer.

Ex. $[10, 2] \rightarrow "102"$

$[2, 10] \rightarrow "210"$

$\text{ans} = "210"$

Ex. $[3, 30] \rightarrow "330"$

$[30, 3] \rightarrow "303"$

$\text{ans} = "330"$

Ex. $[3, 30, 34, 5, 9]$

$\text{ans} \rightarrow 9534330 \checkmark$

$[9, 5, 34, 3, 30]$

Idea: Largest no. \rightarrow sort arr in desc order

$[34, 30, 9, 5, 3]$

\downarrow

"3430953" \times

Quiz : $[10, 5, 2, 8, 200]$

\downarrow

$[8, 5, 2, 200, 10] \rightarrow "85220010"$

x, y

if ($xy > yx$)

x should come first

else

y should come first

$x = 2$
 $y = 200$

$xy = 2200$
 $yx = 2002$

2 should come first

compClass implements Comparator<int> {

@Override

int compare (int a, int b) {

String a' = String.valueOf(a)

String b' = String.valueOf(b)

String ab = a' + b'

String ba = b' + a'

if (ab.compareTo(ba) > 0)

 return -1

 else if (ab.compareTo(ba) < 0)

 return 1

 else return 0

$T_C : O(n \log n) + T_C$ of your
comparator fn

```
public class Solution {  
    public String largestNumber(ArrayList<Integer> A) {  
        Collections.sort(A, new Comparator<Integer>() {  
            public int compare(Integer a, Integer b) {  
                String XY = String.valueOf(a) + String.valueOf(b);  
                String YX = String.valueOf(b) + String.valueOf(a);  
                return XY.compareTo(YX) > 0 ? -1 : 1;  
            }  
        });  
        StringBuilder ans = new StringBuilder();  
        for (int x : A) {  
            ans.append(String.valueOf(x));  
        }  
        if (ans.charAt(0) == '0')  
            return "0";  
        return ans.toString();  
    }  
}
```

Java

s1. compareTo(s2)

$s1 > s2 \rightarrow +ve$

$s1 < s2 \rightarrow -ve$

$s1 == s2 \rightarrow 0$

To Do

Recording : Inversion Count

Solve : Max Chunks

$$A \oplus B = (A \wedge B) + 2^k (A \wedge B)$$

$$x = x + 0$$

$$A \wedge B = 0$$

2^{s+1} —

$$\begin{array}{r} A \rightarrow 00111010 \\ 2^s x \quad 00000101 \\ \hline \end{array}$$

$$\begin{array}{r} A \rightarrow 0001010 \\ 2^s x \rightarrow 0000101 \\ \hline \end{array}$$

for ($i = 31$; $i \geq 0$; $i--$) {

 if ($\text{setBit}(A, i)$)
 break;

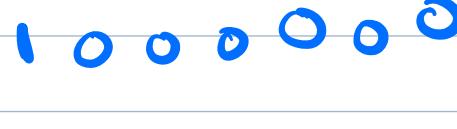
}

int $x = 0$

while ($i \geq 0$) {

 if ($\text{unsetBit}(A, i)$)
 $x = x | (1 << i)$

$y > A$

$A \rightarrow$ 
 $\underline{y} = \underline{\underline{0}}$ 

Last set bit $\rightarrow x$

$y = 1 \ll (x+1)$